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The Variable-Rate Decision for Multiple Inputs with Multiple Management Zones

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*Selected Paper Prepared for Presentation at the
Southern Agricultural Economics Association Annual Meeting
Little Rock, Arkansas, February 5-9, 2005*

Abstract: Research has evaluated the relative profitability of variable-rate versus uniform-rate application of a single input in fields with multiple management zones. This paper addresses the variable-rate decision for multiple inputs. The decision-making framework is evaluated for nitrogen and water applied to irrigated cotton in fields with three management zones.

Keywords: Breakeven analysis, cotton, economic feasibility, multiple inputs, precision farming, variable-rate technology

JEL Classifications: Q12

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The Variable-Rate Decision for Multiple Inputs with Multiple Management Zones

Introduction

Economic analyses of the decision to use variable-rate technology (VRT) versus uniform-rate technology (URT) to apply inputs within a farm field have concentrated on application of a single input (eg., Lambert and Lowenberg-DeBoer; Swinton and Lowenberg-DeBoer; English, Roberts, and Mahajanashetti). Unless inputs are independent of one another, a change in the quantity of one input affects the marginal product of the other inputs as they interact in producing output. Thus, for the multiple input VRT decision, the optimal quantities of the inputs for each management zone must be determined by the simultaneous solution of the first order conditions for profit maximization. This paper considers the profit-maximizing decision about whether to use VRT or URT to apply multiple inputs within a field and evaluates this decision for cases where nitrogen and water are applied to cotton fields with different proportions of their acreage in three management zones.

Farmers are interested in knowing whether VRT is economically viable for their fields. Profitability of VRT varies across fields with differences in spatial variability, where spatial variability is defined as the distribution across a field of management zones with different crop yield responses to inputs (Roberts, English, and Mahajanashetti). Within-field variability in soil physical and chemical characteristics is a necessary condition for the economic viability of using VRT (English, Roberts, and Mahajanashetti; Forcella; Hayes, Overton, and Price; Roberts, English, and Mahajanashetti; Snyder). Relationships among crop yields, input levels, and soil characteristics determine spatial variability within a field. These relationships also determine yield response variability, where yield response variability is defined as the differences in magnitudes of yield response among management zones (English, Roberts, and Mahajanashetti;

Forcella; Roberts, English, and Mahajanashetti). Spatial and yield response variability, along with the crop price, the input prices, and the additional cost of using VRT versus URT, in concert with farmer and farm characteristics, factor into the decision to adopt VRT (Roberts et al., 2004). In the end, no general formula exists for determining whether VRT or URT should be used on a particular field because each field presents a different case (Roberts et al., 2002).

The objectives of this paper are to 1) present an analytical framework for the VRT versus URT decision for applying multiple inputs in fields with multiple management zones and 2) illustrate the decision-making framework for irrigated cotton fields with nitrogen and water applied to three management zones.

Analytical Framework

Assume farmers are profit maximizers who can classify their fields into m management zones and have knowledge of the management-zone-specific yield response functions for a given crop and set of n inputs. Suppose further that yield responses can be represented by concave functions and fields can include any of these m management zones in any proportions. Let the response functions be represented by equations (1).

$$(1) \quad Y_i = Y_i(X_{i1}, \dots, X_{in}) \quad i = 1, 2, \dots, m$$

where Y_i is crop yield/acre for management zone i and X_{ij} is the amount of input j ($j=1, \dots, n$) applied per acre to management zone i .

Economically optimal quantities of the n inputs are determined for a particular management zone by equating the marginal physical products of the yield response function for that management zone with the input-to-crop price ratios and solving these equations simultaneously for input quantities. These n equations are the first order conditions for profit maximization for that management zone. Optimal quantities of inputs are different for each

management zone. Optimal return above input costs per acre for the field under VRT (R_{VRT}^*) is then calculated from the following profit function (Nicholson):

$$(2) \quad R_{VRT}^* = \sum_{i=1}^m \lambda_i [P_Y Y_i (X_{i1}^*, \dots, X_{in}^*) - \sum_{j=1}^n P_j X_{ij}^*]$$

$$= R_{VRT}^* (\lambda_1, \lambda_2, \dots, \lambda_{m-1}, P_Y, P_1, \dots, P_n)$$

where P_Y is the crop price; P_j is the price of input j ($j=1, \dots, n$); X_{ij}^* is the optimal input

($j=1, \dots, n$) application rate for the i^{th} management zone; π_i^* is optimal net return above input costs

for the i^{th} management zone; and λ_i is the proportion of the field in the i^{th} management zone

such that $\sum_{i=1}^m \lambda_i = 1$. Thus, R_{VRT}^* is the weighted average over λ_i of the optimal returns above

input costs per acre obtained for each management zone. The proportion of the field in

management zone m (λ_m) is not included as an argument in the R_{VRT}^* function because $\lambda_m = 1$

$$- \sum_{i=1}^{m-1} \lambda_i .$$

Numerous decision rules could be assumed for URT application of the inputs (English, Roberts, Majajanashetti). In this paper, farmers are assumed to base URT decisions on the profit-maximizing input levels obtained from a field-average yield response function, with the proportions of the field in each management zone (λ_i s) serving as weights. Determining the optimal uniform rate based on the weighted average response function is analogous to some methods used to develop fertilizer recommendations. For example, receiving a recommendation from a soil-test laboratory based on a soil sample that mixes soil cores drawn at random across a field (VanEck and Collier) is similar to weighting the recommendations for the management zones by the proportions of the field in each management zone. In addition, soil-test laboratories

and the Extension Service often base their fertilizer recommendations on yield goals developed by farmers (Savoy and Joines). These yield goals can be formed in a variety of ways (O'Neal et al.). If the farmer forms the field yield goal by implicitly averaging yield goals across management zones, the field yield goal and the fertilizer recommendation would be weighted by the proportions of the field in each management zone.

Assume the farmer determines optimal uniform application rates based on the field-average response function expressed as:

$$(3) \quad Y_u = Y_u (X_{u1}, \dots, X_{un}) = \sum_{i=1}^m \lambda_i Y_i (X_{u1}, \dots, X_{un})$$

where Y_u is the weighted average crop yield response function for the field and X_{uj} is the uniform application rate for input j ($j=1, \dots, n$). The optimal return above input cost per acre for URT (R_{URT}^*) is calculated from the following profit function:

$$(4) \quad R_{URT}^* = P_Y \sum_{i=1}^m \lambda_i Y_i (X_{u1}^*, \dots, X_{un}^*) - \sum_{j=1}^n P_j X_{uj}^* \\ = R_{URT}^* (\lambda_1, \lambda_2, \dots, \lambda_{m-1}, P_Y, P_1, \dots, P_n)$$

where X_{uj}^* is the optimal uniform application rate for input j obtained from the field-average yield response function through the simultaneous solution of the n first order conditions for profit maximization, which equate the marginal products of the inputs with their respective input-to-crop price ratios. Again λ_m is excluded as an argument because the sum of the λ_i s equals 1.

The difference between R_{VRT}^* and R_{URT}^* , which is the optimal return to VRT ($RVRT^*$), can be specified as:

$$(5) \quad RVRT^* = R_{VRT}^* - R_{URT}^* = RVRT^* (\lambda_1, \lambda_2, \dots, \lambda_{m-1}, P_Y, P_1, \dots, P_n)$$

where all variables have been previously defined.

VRT is more profitable than URT if $RVRT^* - V_1 - V_2 > 0$, where V_1 is the application cost for VRT minus the application cost for URT and V_2 is the cost of gathering spatial information and using it to identify management zones and their yield response functions. If the management zones and their response functions have already been identified, V_2 is known and the farmer will undertake VRT if $RVRT^* > V_1$, because V_2 is a sunk cost in making the VRT versus URT decision. If, on the other hand, V_2 is not known, the farmer can use conservative, educated guesses about the λ_i s, the corresponding yield response functions, and V_1 to estimate $RVRT^* - V_1$, which can be thought of as an education guess about the maximum amount a farmer can invest in gathering spatial information and identifying the field's management zones and their yield response functions.

Equation (5) is concave in λ_1 . Its concavity can easily be understood by considering fields with three management zones; management zones 1, 2, and 3. For fields that are all in management zone 1 ($\lambda_1 = 1$, $\lambda_2 = 0$, and $\lambda_3 = 0$), $RVRT^* = 0$ because the weighted average response function and the response function for management zone 1 are the same. Fields with a positive λ_2 and/or λ_3 ($0 < \lambda_1 < 1$) have multiple management zones and farmers can consider using VRT. Since optimization of input use with VRT is more suited to the site-specific yield response functions than to the field-average response function, $RVRT^*$ now becomes positive and continues to increase to a maximum as λ_1 decreases over some range.

Spatial Break-even Variability Proportions (SBVPs) (English, Roberts, and Mahajanashetti; Mahajanashetti; Roberts, English, and Mahajanashetti) are defined as the lower and upper limits of λ_{m-2} , λ_{m-1} , and λ_m for given levels of $\lambda_1, \lambda_2, \dots, \lambda_{m-3}$, P_Y , P_j , and V_1 such

that $RVRT^* = V_1$, where V_1 is the additional application cost of using VRT compared to URT.

Mathematically, equation (5) can be modified as follows and used to locate the SBVPs for λ_{m-2} ,

λ_{m-1} , and λ_m .

$$(6) \quad RVRT^* = RVRT^*(\lambda_{m-1}, \lambda_{m-2} \mid \bar{\lambda}_1, \bar{\lambda}_2, \dots, \bar{\lambda}_{m-3}, \bar{P}_Y, \bar{P}_1, \dots, \bar{P}_n) = \bar{V}_1$$

where $\bar{\lambda}_1, \bar{\lambda}_2, \dots, \bar{\lambda}_{m-2}, \bar{P}_Y, \bar{P}_j$ ($j=1, \dots, n$), and \bar{V}_1 are given levels of the respective variables and

$$\lambda_m = 1 - \lambda_{m-2} - \lambda_{m-1} - \sum_{i=1}^{m-3} \bar{\lambda}_i.$$

As a more specific example using a concave functional form, assume three management zones and express equations (1) as quadratic yield response functions containing two inputs with interaction between the inputs. Given these assumptions, the functional forms of equations (2), (4), and (5) can be determined and the SBVPs can be identified. Let the respective management-zone proportions be λ_1 , λ_2 , and λ_3 , and let equations (1) be represented by equations (7), (8), and (9).

$$(7) \quad Y_1 = a_1 + b_1 X_{11} + c_1 X_{11}^2 + d_1 X_{12} + e_1 X_{12}^2 + f_1 X_{11} X_{12}$$

$$(8) \quad Y_2 = a_2 + b_2 X_{21} + c_2 X_{21}^2 + d_2 X_{22} + e_2 X_{22}^2 + f_2 X_{21} X_{22}$$

$$(9) \quad Y_3 = a_3 + b_3 X_{31} + c_3 X_{31}^2 + d_3 X_{32} + e_3 X_{32}^2 + f_3 X_{31} X_{32}$$

where Y_i and X_{ij} are defined in equations (1) for $m = 3$ management zones ($i=1, 2$, and 3) and $n = 2$ inputs ($j=1$ and 2).

For VRT, take the partial derivative of the yield response function for management zone I with respect to inputs 1 and 2, set these derivatives equal to the price of input j divided by the price of the output, and solve the two equation simultaneously (Heady and Dillon) for X_{i1}^* and X_{i2}^* (Equations 10 and 11).

$$(10) \quad X_{i1}^* = \left[\left((P_2 f_i) + (2d_i P_1) / P_y \right) - (2b_i d_i + c_i f_i) \right] / (f_i^2 - 4c_i e_i)$$

$$(11) \quad X_{2i}^* = \left[\left((P_1 f_i) + (2c_i P_2) / P_y \right) - (2c_i d_i + b_i f_i) \right] / (f_i^2 - 4c_i e_i)$$

Substitute these optimal input rates into equations (7, 8, and 9), substitute the resulting optimal yields into equation (2) to determine the net return for management zone i , do the same for each management zone, and weight these net returns based on λ_i to get R_{VRT}^* . For URT, substitute equations (7), (8), and (9) into equation (3) and set $X_{1j} = X_{2j} = X_{3j} = X_{uj}$ ($j=1$ and 2). Set the derivative of the resulting field-average yield response function equal to P_j/P_Y and solve for X_{uj}^* . Substitute these optimal uniform input application rates into equation (3) and substitute the resulting optimal field-average yield into equation (4) to get R_{URT}^* . Calculation of $RVRT^*$ is straight forward from equation (5).

Illustrative Example

To illustrate the concepts presented above, assume hypothetical fields suited to cotton production can be classified into three management zones and that the following quadratic functions represent cotton yield response to fertilizer nitrogen and irrigation plus initial moisture (W) for the management zones.

$$(12) \quad Y_1 = 233.72 + 23.65 * W_1 - 0.182 * W_1^2 + 0.439 * N_1 - 0.0033 * N_1^2 + 0.021 * W_1 * N_1$$

$$(13) \quad Y_2 = -1103.6 + 118.35 * W_2 - 1.63 * W_2^2 + 2.85 * N_2 - 0.004 * N_2^2 - 0.046 * W_2 * N_2$$

$$(14) \quad Y_3 = -170.93 + 32.45 * W_3 - 0.022 * W_3^2 + 3.74 * N_3 - 0.011 * N_3^2 + 0.022 * W_3 * N_3$$

where Y_1 , Y_2 , and Y_3 are cotton lint yields (lb/acre); W_1 , W_2 , and W_3 are the amounts of water applied plus 5 inches of available preplant moisture plus 1 inch of rainfall (acre-inches); N_1 , N_2 , and N_3 are nitrogen application rates (lb/acre); and the subscripts represent the three management

zones. These equations were estimated by Hexem and Heady in the mid 1970's using field data. They were estimated as quadratic yield response functions similar to those in Arce-Diaz et al., Agrawal and Heady, Mjelde et al., Vanotti and Bundy, and Schlegel and Havlin. These functions would be somewhat different if estimated with current data. Nevertheless, they are plausible irrigated cotton yield response functions, chosen for illustrative purposes to serve as examples in this paper. Their use facilitates exposition of the aforementioned concepts because they are continuous and concave. The response functions are portrayed graphically in Figure 1.

An average cotton lint price received by farmers ($\bar{P}_Y = \$0.52/\text{lb}$) and an average nitrogen price ($\bar{P}_N = \$0.26/\text{lb}$) over the 2000-2003 period and an irrigation water price of \$4.00/acre-inch were used in the analysis. Optimal yields, input application rates, and net returns above input costs were determined for each management zone (Table 1). R_{VRT}^* was determined as a weighted average of the last column in Table 1, given the assumptions about the λ_i s. R_{URT}^* was calculated using the field-average yield response function to determine optimal field-average input application rates, corresponding yields, and net returns above input costs for each management zone, weighted by the assumed λ_i s. In this example, RVRT* was evaluated for hypothetical cotton fields for all combinations of the λ_i s when each λ varied between 0.0 and 0.9 in increments of 0.1 (eg., $\lambda_1 = 0.0$, $\lambda_2 = 0.4$, and $\lambda_3 = 0.6$ or $\lambda_1 = 0.2$, $\lambda_2 = 0.5$, and $\lambda_3 = 0.3$).

For illustrative purposes, Table 2 presents average RVRT* s for all combinations of two λ_i s assuming the λ for one management zone is fixed at the level in the first column. For example, if the proportion of the field in management zone 1 is fixed at $\lambda_1 = 0.0$, the average RVRT* is \$44.41/acre for fields with all combinations of λ_2 and λ_3 between 0.0 and 0.9.

Average $RVRT^*$ declines as the proportion of land in management zone 1 increases.

Management zone 1 is the least profitable management zone and increasing its proportion relative to the other two management zones decreases expected profit and impacts $RVRT^*$. If management zone 2 is either non-existent or makes up 90% of the field, $RVRT^*$ is less than \$10/acre. The highest $RVRT^*$ for management zone 2 is reached when it constitutes between 20 and 30% of the field. The highest $RVRT^*$ for management zone 3 is reached when the field has about 60% of its area in this management zone.

The additional charge for VRT versus URT application of inputs can be separated into two components $\bar{V}_1 = \bar{V}_{IN} + \bar{V}_{IW}$, where \bar{V}_{IN} is the difference between the cost of VRT versus URT application of nitrogen and \bar{V}_{IW} is the difference between the cost of VRT versus URT application of irrigation water. The additional custom charge for variable-rate nitrogen application compared to uniform-rate application was assumed to be $\bar{V}_{IN} = \$3.00/\text{acre}$. This additional charge was close to the mean of \$3.08/ac (range \$1.50 to \$5.50/acre) obtained from personal telephone interviews with firms providing precision farming services to Tennessee farmers (Roberts, English, and Sleigh). Responding firms indicated that the additional charge would include the difference in application costs for VRT versus URT and a charge to create a nitrogen application map based on soil survey maps in conjunction with the consultant's knowledge about corn response on various soils, a visit to the field to observe conditions, and an interview with the farmer about historical yields. Based on information developed in Georgia (Fairchild), a center pivot system can be retrofitted for somewhere in the \$5,000-to-\$10,000 range depending on the number of sprinklers controlled. Assuming a 5-year life, no salvage value and a 150-acre irrigation system, the additional cost is \$9 to \$18/acre. Therefore, a farmer

would have to receive an RVRT* of between \$12 and \$21/acre to break even with URT application of these two inputs. This increase in net returns would have to come from either increased yields and/or decreased input usage compared to URT application of nitrogen and water.

If the field has no area in management zone 1 (Figure 2), management zone 2 must be greater than 4% or less than 90% of the field for VRT application of nitrogen and water to provide equal or higher net returns than URT application and management zone 3 has to be between 96% ($100\% - 4\%$) and 10% ($100\% - 90\%$) of the field because management zones 2 and 3 comprise 100% of the field. If the field is 30% management zone 2 and 0% management zone 1, the expected net return to VRT is \$77/acre (RVRT*) minus \$21/acre (\bar{V}_1) or \$56/acre. As the percentage of a field in management zone 1 increases, the SBVP's become narrower. If the proportion of management zone 1 is 60%, the SBVPs for management zone 2 (management zone 3) are 7.5% ($32.5\% = 100\% - 60\% - 7.5\%$) and 38% ($2\% = 100\% - 60\% - 38\%$). Within these ranges of λ_2 and λ_3 (given $\lambda_1 = 0.6$), $RVRT^* - \bar{V}_1$ is greater than or equal to zero and the farmer at least breaks even by using VRT.

Conclusions

The extent that multiple-input VRT is adopted will depend on the expected net economic benefits received by potential adopters. Fields generally exhibit yield variability; however, as demonstrated in this paper, not all fields warrant VRT from an economic standpoint. Farmers are interested in knowing whether VRT is economically viable on their fields. The answer to this question varies from field to field depending on spatial variability as well as yield response variability among management zones. The answer also varies with the crop, the inputs, their prices, and the cost of using VRT relative to URT. In the end, no general formula exists for

determining whether VRT or URT should be used on a particular field because each field presents a different case. Nevertheless, for the case presented in this paper, a wide range of spatial variability would provide increased net returns for VRT application of nitrogen and water relative to URT application.

To utilize this methodology, farmers need knowledge of the field-specific management zones for a particular crop and inputs, including the parameters of the corresponding yield response functions. Unfortunately, this knowledge is difficult to obtain with certainty, but farmers are currently using other precision farming technologies (eg., yield monitors, grid soil sampling, field mapping) that can be used to identify management zones and their yield response potentials (English, Roberts, and Sleight). Even when information about the management zones and yield response functions is not known, these methods can be used to obtain rough estimates about whether investment in obtaining additional spatial information to more precisely identify management zones and estimate their corresponding yield response functions is potentially worthwhile.

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Table 1. Optimal Yields, Input Application Rates, and Net Returns above Input Costs for Management Zones 1 through 3

Management Zone	Yield	Nitrogen	Water	Net Returns
	lb/acre	lb/acre	Acre-inches	\$/acre
Management Zone 1	1,140	160	53	339.08
Management Zone 2	1,120	107	32	424.96
Management Zone 3	1,628	214	67	522.75

Table 2. Average Returns to Variable-Rate Application of Nitrogen and Water (RVRT*) for Selected Management Zone Proportions

Proportion of Field	Average RVRT* ^a		
	Management Zone 1	Management Zone 2	Management Zone 3
0	\$44.41	\$2.92	\$10.72
0.1	\$41.74	\$41.59	\$22.14
0.2	\$38.92	\$50.33	\$31.69
0.3	\$35.91	\$50.36	\$39.60
0.4	\$35.71	\$47.93	\$42.54
0.5	\$29.19	\$40.94	\$50.25
0.6	\$25.33	\$34.04	\$52.25
0.7	\$20.97	\$26.34	\$50.98
0.8	\$15.86	\$18.05	\$44.80
0.9	\$9.43	\$9.26	\$30.45

^a Average RVRT*, represented by the fixed λ in the first column and the management zone in the column, is determined by averaging the RVRT*s for fields with all combinations of the other two λ s. For instance, the \$9.43/acre return in the column headed Management Zone 1 is the average return when the field is 90% management zone 1 and either 10% management zone 2 (\$16.38/acre) or 10% management zone 3 (\$2.37/acre).

Management Zone 1

Management Zone 2

Management Zone 3

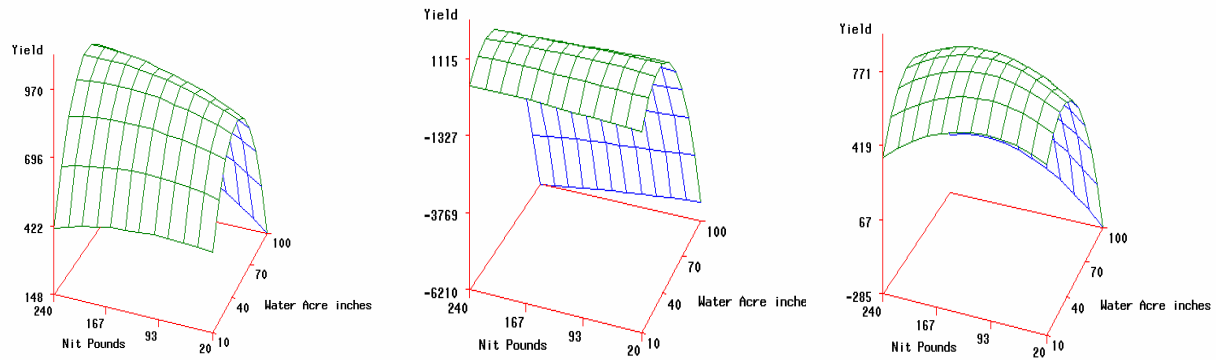


Figure 1. Graphical Portrayal of the Cotton Yield Response Functions Used in the Analysis

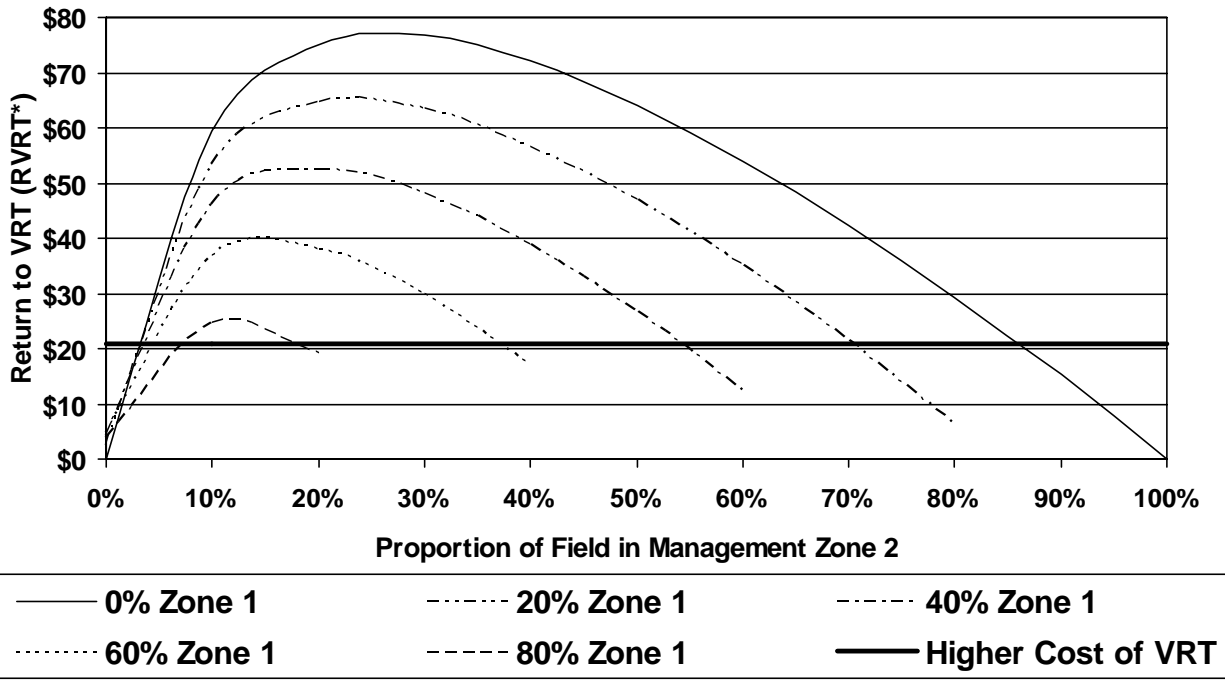


Figure 2. Spatial Breakeven Variability Proportions for Management Zones 2 and 3 Given a Predetermined Proportion for Management Zone 1