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Measuring the Estimation Bias of Yield Response to N Using Combined On-Farm Experiment Data

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Abstract

Accurately evaluating yield response to nitrogen can increase crop management profitability and sustainability. Many studies estimate yield response by fitting a regression model to data collected from different fields. But analysing such combined data requires that heterogeneity across fields be accounted for in the regression analysis along with the variation in input rates. This study uses data from 27 large-scale on farm experiments to test the potential danger of getting biased estimates of yield response functions. Models with and without field fixed effects are run. The yield response functions from the two models showed different slopes, which provides a visual representation of the bias resulting from the pooled estimation. Use of the Mundlak approach indicated that ignoring the endogeneity of regressors with respect to field effects leads to an unreliable estimation of yield response to N.

Keywords

Field fixed effects, yield response, on-farm precision experimentation, endogeneity.

Presenter Profiles

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Introduction

Use of nitrogen (N) fertilizer in crop production is important both economically and environmentally. Over-fertilization can lead to N leaching, causing pollution, whereas under-fertilization may produce yield below the economic optimum (Schlegel, Dhuyvetter, and Havlin 1996; Magdoff 1991). Accurately evaluating the yield response to N can improve the accuracy of estimating economically optimal N rates, thereby increasing farmers profitability and improving the sustainability of agricultural activities (W. Raun et al. 2017; Ransom et al. 2020).

The supplemental N requirement of corn and supply from soil can vary substantially among fields (Bundy and Andraski 1995). Numerous studies have estimated yield responses to N for individual fields (Scharf and Lory 2002; Schmidt et al. 2002). However, since statistical analysis needs adequate variations in input levels and yield observations to provide understanding of yield response functions, in previous studies, researchers have been combining observed application data from multiple locations to estimate yield response to inputs (e.g., Spillman 1923; Tumusiime et al. 2011; Lory and Scharf 2003; Sela, Woodbury, and Van Es 2018; Wang, Shi, and Wen 2023). At the early stages of finding optimal corn N rates based on yield response data, yield response functions were estimated based on combined data from numerous experiments of N trials (Osterhaus, Bundy, and Andraski 2008; Scharf 2001; Oberle and Keeney 1990; Pias et al. 2022; Roberts et al. 2013; Lory and Scharf 2003). Among those N trials, the majority of them received different N rate treatments across different fields; some of them were based on the crop management history (Andraski and Bundy 2002), some of them were chosen by producers (Scharf et al. 2011), some of them have no information about how the trial rates were chosen (Vanotti and Bundy 1994a, 1994b; Lory and Scharf 2003; Barker and Sawyer 2010; Roberts et al. 2013). An N recommendation approach, Maximum Return to N (MRTN) (Morris et al. 2018; Sawyer et al. 2006; Nafziger 2018), is a good and significant example of using combined multiple N trials data to recover yield response. Since its goal is to have regional recommendations of nitrogen application rates, it incorporated data from diverse locations with varying N rates and a wide range of field characteristics into the model. Consequently, the MRTN research is conducted using data from hundreds of N trials in the database from each state or a specified region within the state, without specifying consistent N rates or increments across fields.

Even though some studies may have sufficient variations of N treatments within each trial, including more observations from multiple trials can provide additional information to the regression process. This, in turn, enhances the precision of the estimates and leads to the development of better decision-making tools (Bullock et al. 2019). Also, as the management of agricultural activities increasingly relies on big data and machine learning methods, the need to incorporate more observations into the analysis process is intensifying. More studies are now using a significantly larger volume of data than before, which often necessitates the combination of observations from multiple fields. (Van Klompenburg, Kassahun, and Catal 2020; Qin et al. 2018; Ransom et al. 2019; Su et al. 2022).

However, despite the benefits of combining data from separate field experiments, there are challenges in combining data from different trials. During the process of combining data, the heterogeneity of fields' characteristics will be brought into the regression analysis along with the variation in input rates. If these field characteristics are not controlled for in the regression, their effects on yield may be attributed to other variables. This can lead to a biased

estimation of the marginal effect of N on yield. Oglesby et al. (2022) compared the Economically Optimal Nitrogen Rate (EONR) and the Agronomically Optimal Nitrogen Rate (AONR) obtained from models analysing each field individually with those obtained by combining data by year or both field and year. They found that pooled data tends to mislead the estimation of impact of the input on yield. To address this issue, previous studies have proposed methods that incorporate location-specific models to potentially improve input rate recommendations (W. Raun et al. 2017; W. R. Raun et al. 2019).

The main objective of this study is to examine the potential bias in estimating the causal effects of N on yield due to omitted variable bias when using combined data from multiple fields. I will use unique datasets from the Data Intensive Farm Management project (DIFM) (Bullock et al. 2019) that allow us to test this hypothesis. The DIFM uses precision agricultural technology to conduct on-farm experiments (OFPE) in large-scale farm trials in different states. Because the initial goal of DIFM is to generate profit-enhancing information for each specific participating farmer, targeted input rate are decided upon separately by each field. Given that the amounts of N treatment are determined by farmers for individual fields and may correlate with their fields' characteristics, combining the DIFM data should present the endogeneity problem previously mentioned. On the other hand, multiple (usually 5 to 7) treatment rates are applied by variable rate technology in each field based on Latin square trial design maps, making sure the input rates and other elements are independent. These project protocols introduce two dimensions of N variation when combining data from multiple fields: within-field N variation and across-fields N variation. Of these, only the within-field N variation is independent to other elements within each field, ensuring the yield response curve reflects the real impact of N on yield. This provides a great opportunity to test the potential danger of getting biased yield response to N using combined fields data.

Models with and without adding field fixed effects were estimated using on-farm experimental data combined across fields. The results show that the estimated marginal impact of N on yield were different from the two models and the two yield response curve showed different slopes, resulting in different EONR estimations. This is consistent with my hypothesis, which is that the correlation between the unobserved farm characteristics and the choice of N treatments will cause omitted variable bias in the analysis. Mundlak's method (Mundlak 1978) was applied to check for endogeneity. Results show that ignoring the endogeneity of regressors with respect to field characteristics leads to an unreliable estimation of yield response to N. It is very important to be aware of this problem, as this issue has not been widely recognized in previous literature and the use of big data, machine learning, or on-farm experiments for managing agricultural activities has increased dramatically, which increasingly necessitates the combination of observations from multiple fields.

Methods

Experimental Data

The Data Intensive Farm Management (DIFM) project (Bullock et al. 2019) works with participating farmers conducting on-farm precision experiments (OFPE) on fields. Latin square field trial design is established by researchers at the beginning of each growing season for each trial. The N treatment rates were determined around farmers' status quo rates, which were chosen based on farmers' experience and expectations for the field. The dimension of the plots was designed to fit the swath width of the machinery available. Other farming

practices stayed the same throughout the field. Figure 1 shows an example of a trial design. This field was partitioned into 253 plots and each plot is assigned to one of the N treatment rates around 117 lb/ac N.

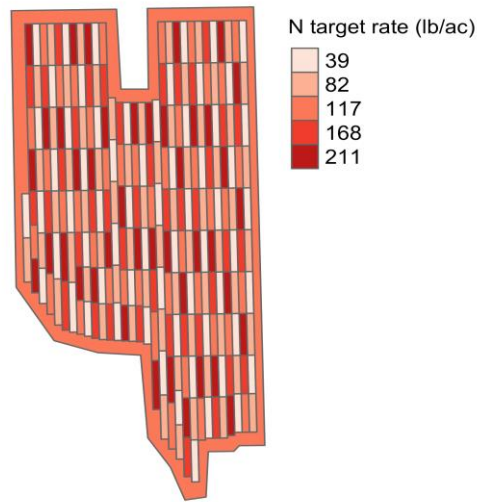


Figure.1: An example Latin square trial design map

Twenty-seven corn N trials in 2021 (15 trials) and 2022 (12 trials) growing season from the DIFM project were used for this study. These trials were conducted across Illinois, Ohio, Arkansas, and Oklahoma in the U.S., as well as in Quebec, Canada. N treatments were implemented in the field using variable rate applicators according to the trial design. Figure 2 shows the applied N treatments for each trial. The red points represent the average N rate in each field, it varies across different fields because farmers chose different status quo rates.

In October, yield monitors were at harvest to collect yield level data. See Figure 3 shows an example of applied variable N trial and observed yield data.

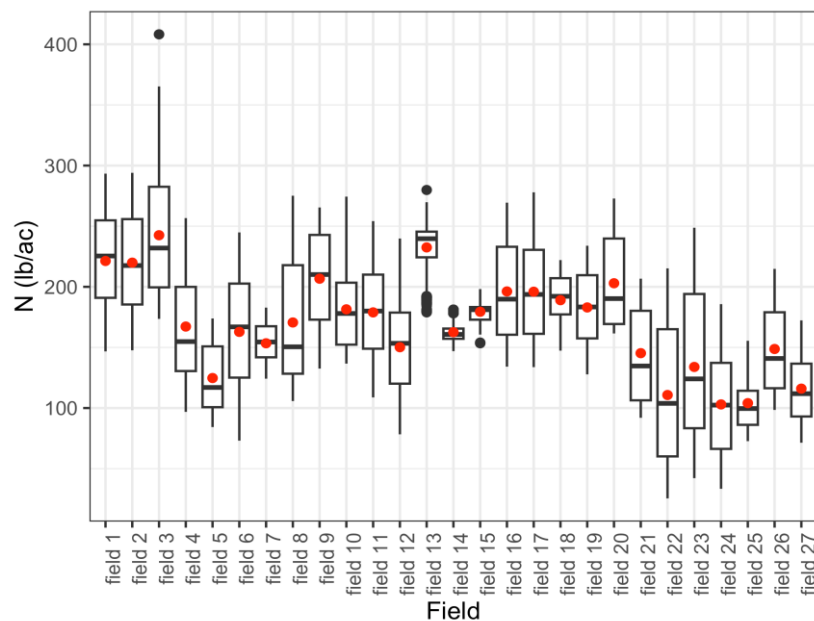


Figure 2: N treatment rates in each field

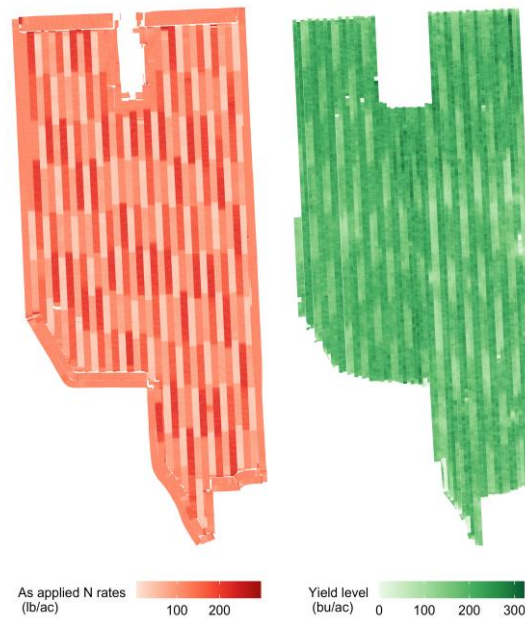


Figure 3: As-applied N rates and observed yield

Data quality was maintained through data cleaning and processing, as discussed briefly by Bullock et al. (2019). Through data processing, extreme as-applied rates and yield were removed from raw data retrieved directly from applicators and yield monitors. Data from side-of-field, headlands, too-small plots, geometrically irregular areas was excluded from the experiment, since the farming practice in these cases are less consistent than the interior of the field due to different machine driving speed, potential application overlaps, etc. An approximately 10m-long “transitional buffer zones” were applied at the end of each plot to mitigate the yield monitors’ reading delays between different yield zones.

The georeferenced raw yield data were used to generate yield polygons, which were used as the “observation units” in analysis. The creation of these polygons depended on factors such as the plot’s original length, swath width, headings, and the distance between points. Within each field, the area of each polygon remained constant. The N rate assigned to each polygon was calculated as the average value of the as-applied N rates falling within that specific polygon. If the N treatment values at points within a yield polygon exceed three times of their standard deviation, the polygon is removed from the analysis, ensuring that the yield observations originate from a single N treatment rate.

Since DIFM runs OFPE in large-scale farms, the abundance of observations within each farm (Figure 4) provides sufficient treatment variation to estimate its yield response function. Considering that the OFPE are conducted at multiple locations and farmers select the central treatment rates, the combined DIFM data can reflect the variations of N demands both across different fields and within each individual field. This combination of two different dimensions of data enables the estimation of both the pooled yield response, incorporating variations in N levels across all fields, as well as field-specific yield response, accounting only for within-field N variations.

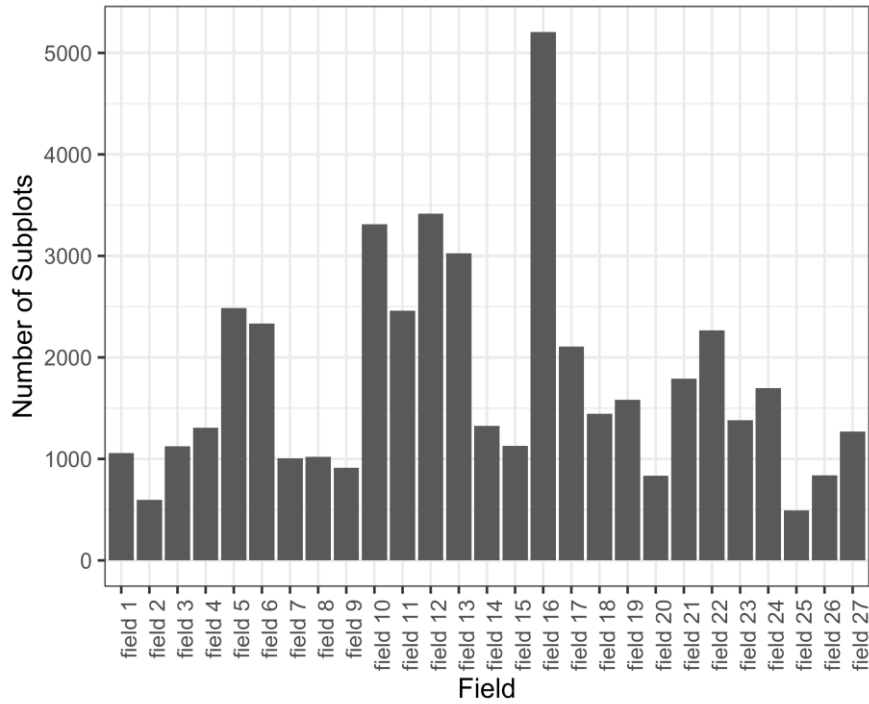


Figure 4: Number of observations in each trial

Non-experimental data

The soil and weather data were obtained using R software (R Core Team 2022). Elevation data for each field was obtained using the elevatr package (Hollister et al. 2022). Digital elevation maps were used to calculate the values of terrain slope and curvature. Slope data was obtained using the raster package (Jacob van Etten 2012). Curvature data was obtained using the spatialEco package (Evans and Murphy 2023). All of the soil data was calculated from subplot-level measurements, consistent with the observation unit.

Daily weather data is obtained from Daymet (Thornton et al. 2022). Monthly precipitation and the number of extreme degree days (EDD) (Schlenker and Roberts 2009) are included in the regression analysis. Precipitation and temperature are assumed to stay the same in the fields in northern Illinois, central Illinois, southern Illinois, Ohio, Arkansas, and Oklahoma. The number of EDD were calculated as follows:

$$EDD = \sum_{i=1}^n \max(0, T_{max,i} - T_c),$$

where $T_{max,i}$ is the maximum temperature on the i th day from April to September, T_c , $29^{\circ}C$ for corn (Schlenker and Roberts 2009), is the critical temperature threshold that will lower yield.

Data merging

Soil data was computed for each observational unit in analysis. The average values for elevation, slope, and curvature from each subplot were merged with applied N and yield levels, using their geographic references through R programming. Weather information was integrated into the dataset based on the fields' locations.

Econometric Model and Analysis

Potential endogeneity problem when using data from multiple fields

As discussed, many studies estimated yield response by fitting a regression model to data collected from different fields without accounting for the unobserved heterogeneity among those different fields. Figure 5 illustrates a potential problem of this approach. As found in previous literature, field-specific characteristics vary from field to field, leading to different yield potentials. For example, consider a two-field case, where field 1 reaches a higher yield potential compared to field 2 due to field or soil characteristics that are not observed by researchers. It is known that some farmers follow yield-based management algorithm, where farmers tend to apply more N for the fields with higher yield potentials (Rodriguez, Bullock, and Boerngen 2019). In this example, farmers tend to apply more N in field 1 (the orange points has higher average than the blue points). The points represent the as-applied N rates and yield level observed by researchers in each field, capturing their own yield response. However, when combining the observed data from both fields, the cross-sectional fit is the black line, consequently biasing the estimation of the relationship between N response and yield.

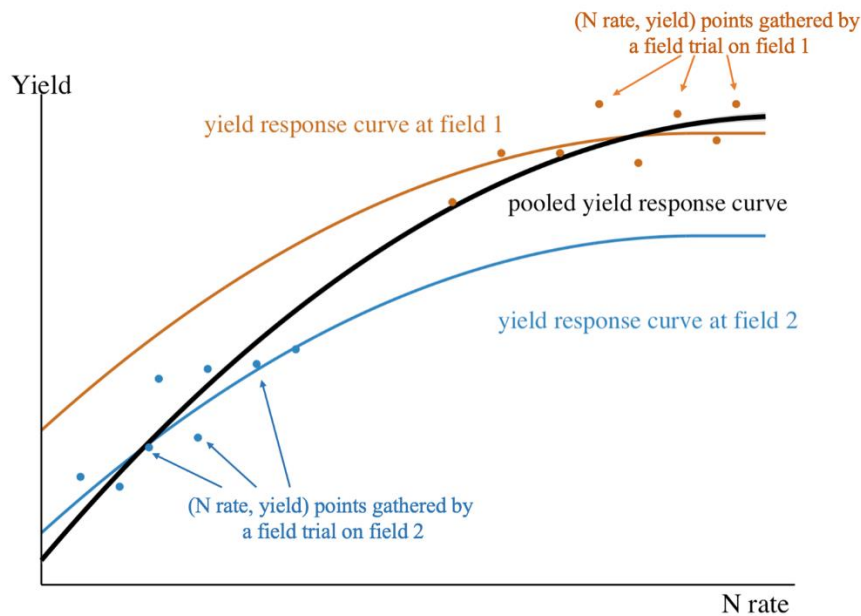


Figure 5: Conceptual demonstration of the potential endogeneity problem when using data from multiple fields.

The fact that farmers select N rates based on their understanding of the fields, accounting for unobserved field characteristics, is not the sole cause of leading to the endogeneity problem from using a pooled model with data from multiple fields. Weather, varies from location to location, can significantly change yield response to N. However, there are numerous approaches to representing weather variables, which can be calculated using minimum, maximum, or average values on a daily, weekly, monthly, or entire growing season basis. Diverse criteria can also be used to construct weather variables. For instance, one could use the absolute temperature or precipitation values or count the number of days surpassing specific thresholds. More importantly, it is nearly impossible to model the interactive and non-linear weather effects on corn yield response (Schlenker and Roberts 2006; Bassu et al. 2014).

Therefore, it is not realistic to perfectly account for weather variables in regression analysis, meaning that the unaccounted impacts will be left in the error term. This idea also applies to soil variables. The Soil Survey Geographic Database (SSURGO), soil tests from experimental fields, etc. are common sources of soil information. However, the accuracy of soil data can limit the extent to which can be controlled for the impact of soil characteristics on yield in regression analysis. This can, again, result omitted variable bias in the yield response estimation.

For the sake of demonstration, assume yield response follows linear functional form

$$y_{fi} = \mathbf{X}_{fi}\boldsymbol{\beta} + v_{fi} \quad (1)$$

$$v_{fi} \equiv c_f + u_{fi} \quad (2)$$

where y_{fi} is the yield level in field f and subplot i , X_{fi} is a vector of all the independent variables including N treatment rates and other controlled covariates.

The error term v_{fi} contains all of the factors that affect yield but are not measurable or controllable (not in \mathbf{X}_{fi}). Equation (2) decomposed it into two parts. u_{fi} is the idiosyncratic error across all subplots. c_f represents the unobserved field characteristics, which are assumed to be constant within each field but vary across locations. Examples of c_f are unobserved the farmer's human capital or management ability, and non-measurable soil characteristics. However, these unobserved field characteristics can impact the yield level and subsequently influence the N rates chosen by farmers. For instance, farmers tend to apply more N on the fields that have historically shown higher yields. Consequently, the correlation between uncontrollable field characteristics and N treatment rates causes an endogeneity problem. This is, $E(\mathbf{N}_f^{gc'} \mathbf{c}_f) \neq 0$, then pooled OLS estimator will be biased, $E[\hat{\boldsymbol{\beta}}|X] \neq \boldsymbol{\beta}$.

Field fixed effects

Thanks to the protocols of the DIFM trial design, the across-field heterogeneity was caused by the trial design rates being centered on farmers' status quo rates and the Latin square trial design was implemented to ensure clean variation in N levels within each field. Therefore, the combined fields data provides a great opportunity testing the potential danger of getting biased estimated yield response functions ignoring field heterogeneity. To eliminate the heterogeneity across fields in the regression analysis, the fixed effects model (Mundlak 1978) can be applied. By including field fixed effects, only the variation within a field is used as identifying information to estimate β^N , which can solve the endogeneity problem due to unobserved field-specific characteristics.

Models with and without field fixed effects are run respectively using the 27 corn-N trials. Quadratic model was used to estimate the impact of N on yield. The quadratic functional form of crop yield functions remains attractive as it is simple to implement, easy to understand, and it can capture the non-linearity of yield response to inputs. The shape-constrained generalized additive (SCAM) model (Pya and Wood 2015) is also applied to estimate the yield response to N. Instead of defining a specific functional form, SCAM lets the data determine the nature of the relationship between inputs and output, which allows for a more flexible specification of yield response function. The results from SCAM and quadratic models are very similar (Figure S1 in Appendix). Based on the simplicity of the quadratic model, we used it for this study.

The statistical model can be written as Equation (3),

$$y_{fi} = \mathbf{N}_{fi}\boldsymbol{\beta}^N + \mathbf{X}_{fi}\boldsymbol{\beta}^X + v_{fi} \quad (3)$$

where \mathbf{N} contains the N treatment rates in each subplot and their quadratic term, \mathbf{X} includes all other subplots-level soil and weather covariates, including elevation, slope, curvature, monthly precipitation from April to September and EDD. All yield, N, and soil features are in site-specific level with f representing field and i representing subplot.

The error term v_{fi} has the same structure as Equation (2). Since N treatment rates were applied based on Latin square trial design, it is orthogonal to any other factors that affect yield. However, as mentioned earlier, the presence of unobserved field characteristics is highly likely to influence farmers' chosen rates, resulting in a correlation with the input treatment rates. These implies,

$$E(N_{fi} v_{fi}) = 0, \forall f \in \{1, 2, \dots, F\}$$

$$E(\mathbf{N}^{gc'}_f \mathbf{c}_f) \neq 0$$

where \mathbf{N}^{gc} is a $(F \times 1)$ matrix contains all the grower chosen N rates, which are the centers of the variable Nitrogen rates in each field. Again, \mathbf{c} is a matrix contains unobserved field-level characteristics.

Combining Equation (3) and Equation (2) yields:

$$y_{fi} = \mathbf{N}_{fi}\boldsymbol{\beta}^N + \mathbf{X}_{fi}\boldsymbol{\beta}^X + c_f + u_{fi} \quad (4)$$

Note, since c_f are the field-level characteristics, the impact of it on yield stays the same in each farm f and doesn't vary among subplots i within the field. The fact of $\bar{c}_{fi} \equiv c_f$ for each field f provides the condition that including field fixed effects can eliminate cross-field variation and only use within-field variation to estimate the yield response curve.

Taking average of the independent and dependent variables in Equation (4) over each farm f can get,

$$\bar{y}_f = \bar{\mathbf{N}}_f\boldsymbol{\beta}^N + \bar{\mathbf{X}}_f\boldsymbol{\beta}^X + c_f + \bar{u}_f \quad (5)$$

Subtract equation Equation (5) from Equation (4) yields Equation (6).

$$y_{fi} - \bar{y}_f = (\mathbf{N}_{fi} - \bar{\mathbf{N}}_f)\boldsymbol{\beta}^N + (\mathbf{X}_{fi} - \bar{\mathbf{X}}_f)\boldsymbol{\beta}^X + u_{fi} - \bar{u}_f \quad (6)$$

Define $\check{y}_{fi} = y_{fi} - \bar{y}_f$, $\check{\mathbf{N}}_{fi} = \mathbf{N}_{fi} - \bar{\mathbf{N}}_f$, $\check{\mathbf{X}}_{fi} = \mathbf{X}_{fi} - \bar{\mathbf{X}}_f$, and $\check{u}_{fi} = u_{fi} - \bar{u}_f$, Equation (6) can be written as:

$$\check{y}_{fi} = \check{\mathbf{N}}_{fi}\boldsymbol{\beta}^N + \check{\mathbf{X}}_{fi}\boldsymbol{\beta}^X + \check{u}_{fi} \quad (7)$$

In this case, $E[\widehat{\boldsymbol{\beta}}^N | \check{\mathbf{N}}; \check{\mathbf{X}}] = \boldsymbol{\beta}^N$ due to the orthogonality of N treatments (\mathbf{N}_{fi}) and other covariates (\mathbf{X}_{fi}) from Latin square trial design. This will lead to an unbiased estimation of causal impact of Nitrogen on yield, generating an unbiased yield response function.

Specification test

Mundlak's method (Mundlak 1978) is used to test the statistical significance of the unobserved field heterogeneity, which lead to the endogeneity of the model. A Wald test based on the coefficients on the means of the field varying variables from a random effect model (Equation 8) was performed to identify if the observed variables are statistically significantly correlated with the unobserved field characteristics.

$$y_{fi} = \alpha + \mathbf{N}_{fi}\boldsymbol{\beta}^N + \mathbf{X}_{fi}\boldsymbol{\beta}^X + \bar{\mathbf{N}}_f\boldsymbol{\beta}^{\bar{N}} + \bar{\mathbf{X}}_f\boldsymbol{\beta}^{\bar{X}} + v_{fi} \quad (8)$$

where \mathbf{N}_{fi} and \mathbf{X}_{fi} contains the same variables as Equation (3). $\bar{\mathbf{N}}_f$ and $\bar{\mathbf{X}}_f$ have all the mean values of each variable by field.

The Null hypothesis has all the coefficients on the means ($\beta^{\bar{N}}$ and $\beta^{\bar{X}}$) are zero indicates that there's no endogeneity in the pooled regression.

Results

Table 1 shows the regression results of the models, both with and without including field fixed effects, respectively. After adding field fixed effects into the model, the coefficient of the N variable changed from 0.494 to 0.407 and became less significant. Moreover, the quadratic N term turned no longer significant. Since N is orthogonal to any other factor that might influence the yield level within field, the coefficients from the model with fixed effects truly represent the marginal effect of N on yield. This provides evidence that using pooled model can bias the yield response to N. The impact of slope on yield changed from positive to negative after including field fixed effects, this is more consistent with agronomic expectations as steeper slopes can lead to poor water drainage, increased runoff, shallow soil depth, and challenges related to planting and N application. The elevation and curvature also became less significant after including field fixed effects into the model, indicating that these factors showed effects on yield beyond their individual influences in the pooled model.

Table 1: Regression results from pooled model and field fixed effects model

	Pooled Model	Field Fixed Effects Model
N	0.494*** (0.015)	0.407+ (0.231)
N ²	-0.001*** (0.000)	-0.001 (0.001)
elevation	0.058*** (0.002)	-0.079* (0.035)
slope	0.283*** (0.030)	-0.134* (0.051)
curvature	0.000*** (0.000)	0.000* (0.000)
Apr precipitation	-0.233*** (0.019)	
May precipitation	-0.335*** (0.009)	
Jun precipitation	0.123*** (0.006)	
Jul precipitation	0.220*** (0.011)	
Aug precipitation	-0.164*** (0.021)	
Sep precipitation	-0.945*** (0.012)	
EDD	-0.041*** (0.002)	
Num.Obs.	47405	47405
Std.Errors	IID	by: field
FE: field		X

+ p < 0.1, * p < 0.05, ** p < 0.01, *** p < 0.001

From the results, all the monthly precipitation and EDD variables are statistically significant (weather was assumed to be consistent within each field and were thus controlled by field fixed effects). This aligns with the agronomic expectation that weather influences yield levels. However, as previously mentioned, it is nearly impossible to perfectly reflect the impacts of weather and soil on yield in regressions. Therefore, it is very likely that there is omitted variable bias in the pooled yield response regression analysis.

Figure 6 shows the results of estimated yield response curves from the pooled model and the fixed effect model. The figure shows that the two models resulted in two yield response functions with different slopes, providing a visual representation of the bias resulting from the pooled estimation. Because the field fixed effect eliminated the heterogeneity across fields and only used the N variation within each field for the regression. As N is orthogonal to other factors based on the trial design, the within-field N variation can be considered clean. Therefore, the yield curve depicted by the red line represents the true yield response to N. Any deviation between the two curves can be attributed to the bias arising from the estimation conducted using the pooled model.

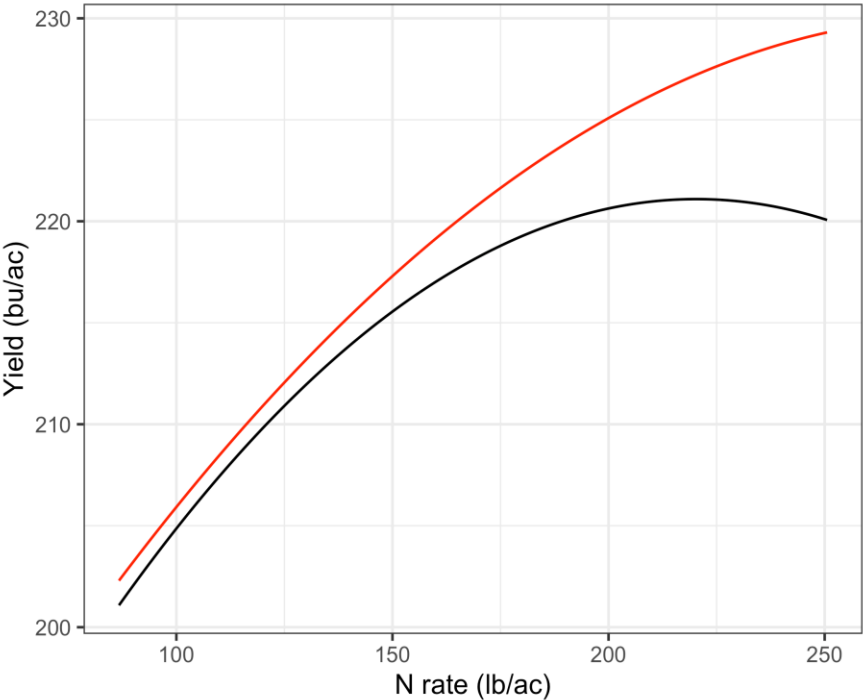


Figure 6: Predicted yield response functions with and without field fixed effects (black is pooled)

Following the Mundlak approach, the Wald test yielded a χ^2 statistic of 116.9, which rejected the Null hypothesis indicating that ignoring the endogeneity of regressors with respect to field effects leads to an unreliable estimation of the yield response to N. This is important, As EONR is found as the solution to the problem of applying N at the profit maximizing rate, which happens when the yield response curve has the same slope as the crop-N price ratio, the estimation of the yield response to N directly affect the estimation of EONR. More accurate N fertilizer guidelines can help with raising farm profits and reducing environmental damage. In this study, for example, the EONR estimated for each individual field is 214 lb/ac, while the EONR estimated from the pooled regression is 176 lb/ac. The difference between the two

EONR comes from the biased estimated yield response function using pooled data without recognizing field heterogeneity.

Sufficiently many N input rates and observations are essential to the accurate estimation of yield response. Many researchers have obtained data from multiple sites or studies, as combining yield and N data from various site-years is an easy-to-implement and cost-effective process. However, the results from this study showed the potential bias arising from ignoring unobserved field heterogeneity when analyzing datasets obtained from multiple site-years. It is important to acknowledge this, as managing agricultural activities using big data and machine learning methods have become hot topics, those studies now require much larger volumes of data, necessitating the combination of observations from multiple fields.

Conclusion

Accurately evaluating yield response to N can increase crop management profitability and sustainability. Many studies estimate yield response by fitting a regression model to data collected from different fields, as statistical analysis requires varied input application levels. Even with sufficient variation in N treatments within each trial, having more observations contributes to a more continuous distribution of N and field characteristics, which is desirable for developing N recommendation approaches. One way to attain additional observations, of course, is to combine data from multiple fields. But analyzing such combined data requires that heterogeneity across fields be accounted for in the regression analysis along with the variation in input rates. In other words, noisy variation among different fields may challenge yield response estimation for each field.

This study used data from 27 large-scale on-farm precision experiments with trial design rates centered on farmers' status quo rates to test the potential danger of generating biased estimates of yield response functions. A Latin square trial design was used to make N orthogonal to other factors, so within-field N variation can be considered clean. The field fixed effects in the model eliminated cross-field variation and only used the input variation within each field as identifying information to estimated yield response, ensuring an unbiased measurement of the response to N. Models with and without field fixed effects were run. The yield response functions from the two models showed different slopes, which provided a visual representation of the bias resulting from the pooled estimation. The results of this study indicated that ignoring the endogeneity of regressors with respect to field effects leads to an unreliable estimation of yield response to N. It is important to recognize this potential problem when use combined data from multiple locations, particularly as studies now demand vast amounts of data with the rise of big data, machine learning, and OFPE in agriculture management.

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