Panel stochastic frontier models with endogeneity

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Abstract. In this article, I introduce `xtsfkk` as a new command for fitting panel stochastic frontier models with endogeneity. The advantage of `xtsfkk` is that it can control for the endogenous variables in the frontier and the inefficiency term in a longitudinal setting. Hence, `xtsfkk` performs better than standard panel frontier estimators such as `xtfrontier` that overlook endogeneity by design. Moreover, `xtsfkk` uses Mata's `moptimize()` functions for substantially faster execution and completion speeds. I also present a set of Monte Carlo simulations and examples demonstrating the performance and usage of `xtsfkk`.

Keywords: st0686, xtsfkk, panel stochastic frontier models, longitudinal data, endogeneity, production frontier, cost frontier, endogenous inefficiency

1 Introduction

It has been more than 40 years since Aigner, Lovell, and Schmidt (1977) and Meeusen and van den Broeck (1977) introduced stochastic frontier models. These models are composed of a deterministic part identifying the frontier goal, a stochastic part for the two-sided error term, and a one-sided inefficiency error term identifying the distance from the stochastic frontier. They can be used to study production, cost, revenue, profit, or other goals within various industries. Over the years, these models have become quite common in the literature as empirical researchers have applied them in their research articles and theoretical researchers have modified them to address further needs. Kumbhakar and Lovell (2000) review this literature and summarize numerous applications of these models in many different industries, such as accounting, advertising, banks, education, financial markets, environment, hospitals, hotels, labor markets, military, police, real estate, sports, transportation, and utilities.

Stata provides the `frontier` command to estimate the parameters of a stochastic frontier model. Petrin, Poi, and Levinsohn (2004) offer a new command called `levpet` to estimate production functions using the econometric methodology of Levinsohn and Petrin (2003). Yasar, Raciborski, and Poi (2008) offer another command called `opreg` to estimate production functions with selection bias or simultaneity by implementing the methodology of Olley and Pakes (1996). Amadou (2012) provides the `frontierhtail` command to fit stochastic frontier models with fat tails as outlined by Gupta and Nguyen (2010). Belotti et al. (2013) introduce a command called `sfcross` that mirrors Stata's `frontier` command with additional functionality, options, and models. Fé and Hofler (2020) provide a new command called `sfcount` that fits cross-sectional stochastic frontier models with a dependent count variable in the style of Fé and Hofler (2013).

However, the literature on stochastic frontier models, various commands, and the estimator options in other general-purpose statistical software packages does not offer a way to control for endogeneity that can exist in these models. If the determinants of the frontier or the inefficiency term are correlated with the two-sided error term of the model, then the outcomes of the standard estimators would be contaminated by endogeneity. Intrigued by this shortage in the literature, Kutlu (2010) addresses the endogeneity issue in stochastic frontier models in his article. Karakaplan and Kutlu (2017a) develop a model to handle endogeneity due to the determinants of the frontier or the inefficiency term, or both. Furthermore, Karakaplan (2017) offers a new command called `sfkk` to make it easy for researchers to analyze empirical stochastic frontier models with endogeneity. As a result of these efforts, many research articles such as Xu and Chen (2018), Germeshausen, Panke, and Wetzel (2020), and Karakaplan and Kutlu (2019) applied these methodologies and published various empirical findings.

Karakaplan and Kutlu (2017a) and the `sfkk` command of Karakaplan (2017) are designed to be cross-sectional. Karakaplan and Kutlu (2017b), on the other hand, design a stochastic frontier estimator that would resolve endogeneity issues in a panel setting. The standard `xtfrontier` command of Stata and `sfpanel` command of Belotti et al. (2013) fit panel stochastic frontier models but ignore the endogeneity issues identified by Karakaplan and Kutlu (2017b). Therefore, in this article, I introduce a new command, `xtsfkk`, for fitting panel stochastic frontier models with endogeneity in Stata.

2   The model

Karakaplan and Kutlu (2017b) present the following panel stochastic frontier model with endogenous explanatory variables in the frontier and inefficiency terms (for full model, see Karakaplan and Kutlu [2017b]):

$$\ln L_i = \ln L_{i,y|x} + \ln L_{i,x} \tag{1}$$

$$\ln L_{i,y|x} = -\frac{1}{2}\left\{ T_i \ln(2\pi\sigma_w^2) + \frac{\mathbf{e}_{i.}'\mathbf{e}_{i.}}{\sigma_w^2} + \left(\frac{\mu^2}{\sigma_u^2} - \frac{\mu_{i*}^2}{\sigma_{i*}^2} \right) \right\} + \ln\left\{ \frac{\sigma_{i*}\Phi\left(\frac{\mu_{i*}}{\sigma_{i*}}\right)}{\sigma_u\Phi\left(\frac{\mu}{\sigma_u}\right)} \right\}$$

$$\ln L_{i,x} = -\frac{1}{2}\sum_{t=1}^{T_i}\left\{ \ln\left(|2\pi\boldsymbol{\Omega}|\right) + \boldsymbol{\epsilon}_{it}'\boldsymbol{\Omega}^{-1}\boldsymbol{\epsilon}_{it} \right\}$$

$$\mu_{i*} = \frac{\sigma_w^2\mu - s\sigma_u^2\mathbf{e}_{i.}'\mathbf{h}_{i.}}{\sigma_u^2\mathbf{h}_{i.}'\mathbf{h}_{i.} + \sigma_w^2}$$

$$\sigma_{i*}^2 = \frac{\sigma_u^2\sigma_w^2}{\sigma_u^2\mathbf{h}_{i.}'\mathbf{h}_{i.} + \sigma_w^2}$$

$$e_{it} = y_{it} - \mathbf{x}_{1it}'\boldsymbol{\beta} - \boldsymbol{\epsilon}_{it}'\boldsymbol{\eta}$$

$$\boldsymbol{\epsilon}_{it} = \mathbf{x}_{it} - \mathbf{Z}_{it}\delta$$

where a vector of observations corresponding to the panel i is represented by a subscript $i.$; T_i is the number of time periods for panel i; $s = 1$ for cost functions or $s = -1$ for production functions; y_{it} is the logarithm of the production or cost of the ith productive unit at time t; $\mathbf{x}_{yit}$ is a vector of exogenous and endogenous variables; $\mathbf{x}_{it}$ is a vector of all endogenous explanatory variables; $\mathbf{Z}_{it} = \mathbf{I}_p \bigotimes \mathbf{z}_{it}'$ where $\mathbf{z}_{it}$ is a vector of all exogenous variables; $\mathbf{v}_{it}$ and $\boldsymbol{\epsilon}_{it}$ are two-sided error terms; $\mathbf{u}_{it} \geq 0$ is a one-sided error term capturing inefficiency; $h_{it} = h(\mathbf{x}_{uit}'\boldsymbol{\varphi}_u) > 0$; $\mathbf{x}_{uit}$ is a vector of exogenous and endogenous variables excluding the constant; $\mathbf{u}_i^*$ is a producer-specific random component independent from $\mathbf{v}_{it}$ and $\boldsymbol{\epsilon}_{it}$; $\boldsymbol{\Omega}$ is the variance–covariance matrix of $\boldsymbol{\epsilon}_{it}$; σ_v^2 is the variance of $\mathbf{v}_{it}$; $\boldsymbol{\rho}$ is the vector representing correlation between $\widetilde{\boldsymbol{\epsilon}}_{it}$ and $\mathbf{v}_{it}$; $\mathbf{w}_{it} = \sigma_v\sqrt{1 - \boldsymbol{\rho}'\boldsymbol{\rho}}\widetilde{\mathbf{w}}_{it} = \sigma_w\widetilde{\mathbf{w}}_{it}$; $\boldsymbol{\eta} = \sigma_w\boldsymbol{\Omega}^{-1/2}\boldsymbol{\rho}/\sqrt{1 - \boldsymbol{\rho}'\boldsymbol{\rho}}$; e_{it} is conditionally independent from the regressors given $\mathbf{x}_{it}$ and $\mathbf{z}_{it}$; Φ denote the standard normal cumulative distribution function; $\mathbf{u}_i^* \sim N^+(\mu, \sigma_u^2)$ (N^+ is standard notation for half-normal distribution); and $h_{it}^2 = \exp(\mathbf{x}_{uit}'\boldsymbol{\varphi}_u)$. Karakaplan and Kutlu (2017b) provide all the details about assumptions and how they derived the estimator.

Furthermore, to predict efficiency, $\mathbf{Eff}_{it} = \exp(-\mathbf{u}_{it})$, Karakaplan and Kutlu (2017b) give the following formula:

$$\exp\{-E(\mathbf{u}_{it}|\mathbf{e}_i)\} = \exp\left[-h_{it}\left\{ \mu_{i*} + \frac{\sigma_{i*}\phi\left(\frac{\mu_{i*}}{\sigma_{i*}}\right)}{\Phi\left(\frac{\mu_{i*}}{\sigma_{i*}}\right)} \right\} \right] \tag{2}$$

where ϕ denotes the standard normal probability distribution function.

Finally, Karakaplan and Kutlu (2017b) offer a test for endogeneity based on a reasoning similar to that of the standard Durbin–Wu–Hausman test. The test here is

conducted by looking at the joint significance of the components of the $\boldsymbol{\eta}$ term. If the components of the $\boldsymbol{\eta}$ term are jointly significant, then that would tell us there is endogeneity in the model and a correction through (1) would be needed. If, on the other hand, the joint significance of the components is rejected, then correction for endogeneity would not be needed and the model can be fit by traditional frontier models.

3 The xtsfkk command

Using Mata's maximum-likelihood estimator tools (the `moptimize()` functions), and the exceptional guidance provided by Gould, Pitblado, and Poi (2010) and Kumbhakar, Wang, and Horncastle (2015), I programmed the `xtsfkk` command, which can calculate (1) and (2). There are two files that are included in the `xtsfkk` command package: `xtsfkk.ado`, containing the main estimation syntax and the evaluator subroutines that `xtsfkk` calls behind the scenes, and `xtsfkk.sthlp`, containing helpful information about the command, which users can access by typing `help xtsfkk` in Stata. All front-end interaction with `xtsfkk` and most postestimation routines, including the output style, efficiency prediction, and endogeneity tests, are carried by the `xtsfkk.ado` file. The main evaluator subroutine runs with method d0, which calculates the overall log likelihood. Finally, the unabridged versions of the subsequent sections on syntax, options, and stored results are available in the `xtsfkk` help file.

3.1 Estimation syntax and options

Below is an abridged list of the options provided by `xtsfkk` presenting the most important features of the command. Users can type `help xtsfkk` in Stata for the full-length documentation of the `xtsfkk` syntax, options, stored results, and other details.

3.1.1 Syntax

`xtsfkk` *depvar* [*indepvars*] [*if*] [*in*] [*weight*] [, *options*]

pweights, aweights, fweights, and iweights are allowed; see [U] **11.1.6 weight**.

3.1.2 Options

See the help file for a full list of options.

<u>produc</u>tion specifies that the model be fit as a production frontier model. This option is the default and thus may be omitted.

cost specifies that the model be fit as a cost frontier model.

<u>end</u>ogenous(*endovarlist*) specifies that the variables in *endovarlist* be treated as endogenous. By default, `xtsfkk` assumes that the model is exogenous.

instruments(*ivarlist*) specifies that the variables in *ivarlist* be used as instrumental variables (IVs) to handle endogeneity. By default, xtsfkk assumes that the model is exogenous.

uhet(*uvarlist*[, noconstant]) specifies the inefficiency component is heteroskedastic, with the variance function depending on a linear combination of *uvarlist*. Specifying noconstant suppresses the constant term from the variance function.

whet(*wvarlist*) specifies that the idiosyncratic error component is heteroskedastic, with the variance function depending on a linear combination of *wvarlist*.

header displays a summary of the model constraints in the beginning of the regression. header provides a way to check the model specifications quickly while the estimation is running or a guide to distinguish different regression results that are kept in a single log file.

compare fits the specified model with the exogeneity assumption and displays the regression results after displaying the endogenous model regression results.

efficiency(*effvar*[, replace]) generates the production or cost efficiency variable *effvar*_EN once the estimation is completed and displays its summary statistics in detail. Notice that the option automatically extends any specified variable name *effvar* with _EN. If the compare option is specified, the efficiency() option also generates *effvar*_EX, the production or cost efficiency variable of the exogenous model, and displays its summary statistics. Specifying replace replaces the contents of the existing *effvar*_EN and *effvar*_EX with the new efficiency values from the current model.

test provides a method to test the endogeneity in the model. test tests the joint significance of the components of the eta term and reports the findings after displaying the regression results. For more information about test, see Karakaplan and Kutlu (2017b).

nicely displays the regression results nicely in a single table. nicely uses estout, a community-contributed command by Jann (2005), to format some parts of the table, and xtsfkk table style resembles that of Karakaplan and Kutlu (2017b). The nicely option checks whether the estout package is installed on Stata, and if not, then the nicely option installs the package. If the compare option is specified along with nicely, then the table displays the exogenous and endogenous models with their corresponding equations and statistics side by side in a single table for easy comparison. nicely estimates the production or cost efficiency and tests endogeneity, and reports them in the table even if the efficiency() or test option is not specified.

Two unique functionalities that come with xtsfkk are save()/load() and beep:

save(*filename*) saves the current status of the estimation to the hard drive in every iteration while the estimation is running. Saving is especially useful if the user thinks that intentional breaks may be needed or unintentional interruptions (such as a power outage) may happen while the estimation is running. The save() option

allows stopping the estimation temporarily to release memory for other tasks, and then continuing from where the estimation was left by using the `load()` option. Even if the computer completely shuts down for some external reason, as long as the `save()` option is specified, the estimation can continue from where it was with use of the `load()` option.

`load(`*filename*`)` loads the estimation from a previously saved file to continue from where the estimation was. The model specification with the `load()` option needs to be the same as the specification in the saved file. The `save()` and `load()` options use `matin4-matout4` by Baum and Gould (2004).

`beep`$\big[$`(`#`)`$\big]$ is useful for multitasking. `beep` produces a single beep when `xtsfkk` reports all the findings. When `beep(`#`)` is specified with a positive number, it produces # beeps when the results are ready. If # is a negative number, then beep acts like an alarm and produces continuous beeps until the user stops them. With the `beep` option, the user would not need to constantly monitor the Stata Results window for the outcome. Instead, the user can do other things until the computer starts beeping. This functionality is especially useful if the model is complicated and the panel dataset is large so that the estimation may take hours to complete, and the user wants to know when the outcome is ready.

4   Monte Carlo simulations

I implement Monte Carlo simulations to examine the performance of `xtsfkk`. I analyze three simulation scenarios in three tables: table 1 is for the effects of different panel data sizes; table 2 is for the effects of different IV strengths; and table 3 is for the effects of different degrees of endogeneity. Without loss of generality, I set up the scenarios as cost models, and put one endogenous variable ($\mathbf{z}_1$) in the frontier and one endogenous variable ($\mathbf{z}_2$) in the cost inefficiency. The setting and the data-generation process are summarized below:

$$\mathbf{y} = \beta_{c1} + \beta_{x1}\mathbf{x}_1 + \beta_{z1}\mathbf{z}_1 + \mathbf{u} + \mathbf{v}$$
$$\sigma_u^2 = \exp\left(\beta_{c2} + \beta_{x2}\mathbf{x}_2 + \beta_{z2}\mathbf{z}_2\right)$$
$$\mathbf{u}^* \sim N^+(0,1)$$
$$\mathbf{u} = \sigma_u \mathbf{u}^*$$

where $\mathbf{x}_1$ and $\mathbf{x}_2$ are exogenous variables, and $\mathbf{z}_1$ and $\mathbf{z}_2$ are endogenous variables. In the true model, all coefficients are set to 0.5, and all variables are generated randomly from the normal distribution with a mean of 0 and a standard deviation of 1. I use the `gentrun` command by Wang (1999) to create $\mathbf{u}^*$. The endogeneity of $\mathbf{z}_1$ and $\mathbf{z}_2$ are independently and randomly generated from the normal distribution with a mean of $\mathbf{v} \times \varrho$ and a standard deviation of $1 - \varrho$, where the degree of endogeneity increases with the ϱ parameter. The IVs $\mathbf{iv}_1$ and $\mathbf{iv}_2$ are also independently and randomly generated from the normal distribution with a mean of $\mathbf{z}_1 \times \delta$ and $\mathbf{z}_2 \times \delta$, respectively, and a standard deviation of $1 - \delta$, where the strength of IVs increases with the δ parameter.

I use the `psimulate2` parallel simulation command in the `simulate2` package by Ditzen (2019) to run the Monte Carlo simulations with 500 repetitions each. All tables present average estimated coefficients, mean squared errors (MSE) of the estimated coefficients, mean and median cost efficiency scores, MSEs of the cost efficiency scores, and Pearson and Spearman correlations between cost efficiency scores of the true model and the analyzed model. Model EX is the model that ignores endogeneity, and model EN is the model that handles endogeneity.

Table 1 presents the simulation results with different data sizes ranging from 500 to 200,000 observations. The number of individual productive units, N, ranges from 100 to 5,000, and the number of time periods, T, ranges from 5 to 40. Additionally, ϱ and δ are set to 0.9 (high endogeneity and strong IVs). Compared with model EX, model EN's average coefficient estimates are more similar to the true model in all columns of table 1, and the coefficient MSEs of model EN are mostly smaller than that of model EX. In terms of cost efficiency scores, model EN seems to perform better as the size of the data increases. When T is too small ($T < 8$), Pearson and Spearman correlations of model EN start dropping below that of model EX. However, the MSEs of the efficiency scores are still smaller in model EN when $T = 5$. Table 1 provides an impression that, with different sizes of data, model EN generally performs better than model EX.

In table 2, the simulation results are presented with different strengths of IVs, with ϱ set to 0.9 (high endogeneity), N set to 500, and T set to 20. This table demonstrates that with stronger IVs ($\delta > 0.6$), model EN performs better than model EX, but as the strength of IVs decreases, the performance of model EN deteriorates. This situation is clearly reflected in the misestimated coefficients of the endogenous variables, $\mathbf{z}_1$ and $\mathbf{z}_2$, and their high MSEs in model EN. Hence, as expected, model EN works better with stronger IVs.

Finally, table 3 reports the simulation results with different degrees of endogeneity, with δ set to 0.9 (strong IVs). Again, N is set to 500, and T is set to 20. This table shows that with higher endogeneity ($\varrho > 0.6$), model EN performs better than model EX, but as the degree of endogeneity decreases, the performance of model EX becomes somewhat equivalent to that of model EN. Also, tables 2 and 3 jointly imply that if the degree of endogeneity is very low, then it may be better to use model EX, because model EN's performance requires finding strong IVs.

Table 1. Monte Carlo simulations with different sizes of data

| | True model | Smaller data ◄ | | | | | | | | | | Bigger data ► | |
| | | $N = 100$ $T = 5$ | | $N = 500$ $T = 10$ | | $N = 1000$ $T = 10$ | | $N = 500$ $T = 20$ | | $N = 1000$ $T = 20$ | | $N = 5000$ $T = 40$ | |
Reps = 500	$\delta = 0.9$ $\varrho = 0.9$	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN
$E(\hat{\beta}_{c1})$	0.500	−0.186	0.494	−0.614	0.481	−0.617	0.481	−0.862	0.465	−0.862	0.465	−1.000	0.442
$E(\hat{\beta}_{x1})$	0.500	0.499	0.501	0.500	0.500	0.500	0.500	0.500	0.500	0.500	0.500	0.500	0.500
$E(\hat{\beta}_{z1})$	0.500	0.701	0.497	0.682	0.495	0.682	0.495	0.674	0.493	0.674	0.493	0.670	0.494
$E(\hat{\beta}_{c2})$	0.500	1.237	0.527	1.639	0.553	1.643	0.556	1.841	0.577	1.842	0.578	1.945	0.606
$E(\hat{\beta}_{x2})$	0.500	0.341	0.508	0.278	0.501	0.278	0.501	0.251	0.497	0.251	0.497	0.238	0.494
$E(\hat{\beta}_{z2})$	0.500	0.824	0.511	0.709	0.503	0.708	0.503	0.656	0.499	0.656	0.500	0.629	0.497
$\mathrm{MSE}(\hat{\beta}_{c1})$		0.471	0.000	1.242	0.000	1.249	0.000	1.856	0.001	1.855	0.001	2.251	0.003
$\mathrm{MSE}(\hat{\beta}_{x1})$		0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$\mathrm{MSE}(\hat{\beta}_{z1})$		0.040	0.000	0.033	0.000	0.033	0.000	0.030	0.000	0.030	0.000	0.029	0.000
$\mathrm{MSE}(\hat{\beta}_{c2})$		0.544	0.001	1.297	0.003	1.307	0.003	1.799	0.006	1.801	0.006	2.089	0.011
$\mathrm{MSE}(\hat{\beta}_{x2})$		0.025	0.000	0.049	0.000	0.049	0.000	0.062	0.000	0.062	0.000	0.068	0.000
$\mathrm{MSE}(\hat{\beta}_{z2})$		0.105	0.000	0.044	0.000	0.043	0.000	0.024	0.000	0.024	0.000	0.017	0.000
Med(Eff)	0.438	0.220	0.424	0.139	0.415	0.139	0.415	0.108	0.408	0.108	0.408	0.093	0.399
E(Eff)	0.445	0.246	0.447	0.161	0.441	0.161	0.441	0.127	0.435	0.127	0.435	0.111	0.426
MSE(Eff)		0.048	0.025	0.112	0.019	0.097	0.016	0.141	0.011	0.133	0.011	0.156	0.008
MSE$\{E$(Eff)$\}$		0.037	0.002	0.076	0.000	0.076	0.000	0.101	0.000	0.101	0.000	0.114	0.001
Pearson corr		0.846	0.806	0.848	0.871	0.849	0.872	0.845	0.915	0.845	0.915	0.842	0.942
Spearman corr		0.864	0.811	0.878	0.879	0.878	0.880	0.881	0.921	0.881	0.922	0.882	0.946
Observations	$N \times T$	500		5,000		10,000		10,000		20,000		200,000	

Table 2. Monte Carlo simulations with different strengths of IVs

| | | Weaker IVs ◀ | | | | | | | | | | | Stronger IVs ▶ | |
| | True model | $\delta = 0.1$ $\varrho = 0.9$ | | $\delta = 0.2$ $\varrho = 0.9$ | | $\delta = 0.4$ $\varrho = 0.9$ | | $\delta = 0.6$ $\varrho = 0.9$ | | $\delta = 0.8$ $\varrho = 0.9$ | | $\delta = 0.9$ $\varrho = 0.9$ | |
$N = 500$ $T = 20$		Model EX	Model EN	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN	Model EX	Model EN
Reps = 500													
$E(\widehat{\beta}_{c1})$	0.500	−0.315	0.504	−0.364	0.518	−0.433	0.500	−0.581	0.497	−0.796	0.471	−0.862	0.465
$E(\widehat{\beta}_{x1})$	0.500	0.500	0.505	0.501	0.504	0.500	0.500	0.500	0.499	0.500	0.500	0.500	0.500
$E(\widehat{\beta}_{z1})$	0.500	0.525	3.940	0.580	3.439	0.679	1.779	0.722	0.563	0.700	0.525	0.674	0.493
$E(\widehat{\beta}_{c2})$	0.500	1.386	0.546	1.429	0.539	1.495	0.551	1.622	0.547	1.793	0.573	1.841	0.577
$E(\widehat{\beta}_{x2})$	0.500	0.311	0.509	0.305	0.508	0.299	0.504	0.282	0.501	0.258	0.497	0.251	0.497
$E(\widehat{\beta}_{z2})$	0.500	0.708	0.053	0.716	0.116	0.703	0.267	0.682	0.386	0.663	0.485	0.656	0.499
MSE$(\widehat{\beta}_{c1})$		0.665	0.000	0.746	0.000	0.870	0.000	1.169	0.000	1.680	0.001	1.856	0.001
MSE$(\widehat{\beta}_{x1})$		0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
MSE$(\widehat{\beta}_{z1})$		0.001	11.831	0.006	8.636	0.032	1.635	0.049	0.004	0.040	0.001	0.030	0.000
MSE$(\widehat{\beta}_{c2})$		0.786	0.002	0.863	0.002	0.990	0.003	1.259	0.002	1.671	0.005	1.799	0.006
MSE$(\widehat{\beta}_{x2})$		0.036	0.000	0.038	0.000	0.040	0.000	0.048	0.000	0.058	0.000	0.062	0.000
MSE$(\widehat{\beta}_{z2})$		0.043	0.200	0.047	0.148	0.041	0.054	0.033	0.013	0.027	0.000	0.024	0.000
Med(Eff)	0.438	0.186	0.425	0.178	0.426	0.167	0.421	0.143	0.420	0.115	0.410	0.108	0.408
E(Eff)	0.445	0.212	0.445	0.202	0.447	0.189	0.446	0.164	0.446	0.134	0.437	0.127	0.435
MSE(Eff)		0.079	0.014	0.087	0.013	0.091	0.014	0.112	0.013	0.135	0.012	0.141	0.011
MSE$\{E$(Eff)$\}$		0.055	0.000	0.059	0.000	0.066	0.000	0.079	0.000	0.096	0.000	0.101	0.000
Pearson corr		0.814	0.897	0.820	0.896	0.842	0.900	0.851	0.905	0.847	0.912	0.845	0.915
Spearman corr		0.832	0.900	0.840	0.899	0.863	0.905	0.876	0.910	0.880	0.919	0.881	0.921
Observations	10,000	10,000		10,000		10,000		10,000		10,000		10,000	

Table 3. Monte Carlo simulations with different degrees of endogeneity

Reps = 500 $N = 500$ $T = 20$	True model	$\delta = 0.9$ $\varrho = 0.1$ Model EX	Model EN	$\delta = 0.9$ $\varrho = 0.2$ Model EX	Model EN	$\delta = 0.9$ $\varrho = 0.4$ Model EX	Model EN	$\delta = 0.9$ $\varrho = 0.6$ Model EX	Model EN	$\delta = 0.9$ $\varrho = 0.8$ Model EX	Model EN	$\delta = 0.9$ $\varrho = 0.9$ Model EX	Model EN
		◄ Lower endogeneity										Higher endogeneity ►	
$E(\hat\beta_{c1})$	0.500	0.454	0.448	0.356	0.445	−0.040	0.438	−0.588	0.431	−0.852	0.450	−0.862	0.465
$E(\hat\beta_{x1})$	0.500	0.499	0.499	0.500	0.499	0.500	0.499	0.500	0.499	0.500	0.500	0.500	0.500
$E(\hat\beta_{z1})$	0.500	0.372	0.557	0.499	0.556	0.693	0.554	0.744	0.546	0.706	0.519	0.674	0.493
$E(\hat\beta_{c2})$	0.500	0.563	0.569	0.661	0.571	1.083	0.583	1.604	0.599	1.827	0.587	1.841	0.577
$E(\hat\beta_{x2})$	0.500	0.483	0.481	0.450	0.480	0.359	0.481	0.279	0.484	0.252	0.494	0.251	0.497
$E(\hat\beta_{z2})$	0.500	0.533	0.542	0.719	0.607	0.901	0.680	0.817	0.653	0.702	0.551	0.656	0.499
$MSE(\hat\beta_{c1})$		0.002	0.003	0.021	0.003	0.291	0.004	1.183	0.005	1.829	0.003	1.856	0.001
$MSE(\hat\beta_{x1})$		0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
$MSE(\hat\beta_{z1})$		0.016	0.003	0.000	0.003	0.037	0.003	0.060	0.002	0.042	0.000	0.030	0.000
$MSE(\hat\beta_{c2})$		0.004	0.005	0.026	0.005	0.339	0.007	1.219	0.010	1.762	0.008	1.799	0.006
$MSE(\hat\beta_{x2})$		0.000	0.000	0.003	0.000	0.020	0.000	0.049	0.000	0.062	0.000	0.062	0.000
$MSE(\hat\beta_{z2})$		0.001	0.002	0.048	0.011	0.161	0.032	0.101	0.023	0.041	0.003	0.024	0.000
Med(Eff)	0.438	0.414	0.411	0.376	0.410	0.254	0.405	0.145	0.400	0.110	0.404	0.108	0.408
E(Eff)	0.445	0.426	0.424	0.395	0.424	0.282	0.425	0.169	0.423	0.129	0.430	0.127	0.435
MSE(Eff)		0.004	0.004	0.008	0.004	0.043	0.008	0.109	0.010	0.139	0.011	0.141	0.011
MSE{E(Eff)}		0.000	0.000	0.002	0.000	0.027	0.000	0.076	0.001	0.100	0.000	0.101	0.000
Pearson corr		0.969	0.972	0.959	0.969	0.923	0.951	0.891	0.935	0.881	0.925	0.881	0.921
Spearman corr		0.969	0.972	0.959	0.969	0.911	0.949	0.861	0.930	0.844	0.919	0.845	0.915
Observations	10,000	10,000	10,000	10,000	10,000	10,000	10,000	10,000	10,000	10,000	10,000	10,000	10,000

5 Empirical examples

In this section, I present three different examples to illustrate the usage of `xtsfkk`. In all examples, eta endogeneity test results show that there are endogeneity problems in the models, and the results that correct for the endogeneity are substantially different than the results that ignore endogeneity.

5.1 Panel stochastic production frontier model with endogeneity

The first example analyzes a randomly generated longitudinal dataset in a production setting. This dataset is for illustrative purposes and does not represent a particular industry. The unbalanced panel dataset has a total of 2,000 observations of 140 firms between 1991 and 2015. Production (`y`) is modeled by some frontier variables (`x1`, `x2`, `x3`, and `z1`), and inefficiency is modeled by a different variable (`z2`). Two variables, one in the frontier and one in the inefficiency function (`z1` and `z2`), are assumed to be endogenous, and two IVs (`iv1` and `iv2`) are used to handle the endogeneity. To display the model fully, the `header` option is added to the command line.

```
. use xtsfkkprod
. xtset firm year
Panel variable: firm (unbalanced)
 Time variable: year, 1991 to 2015, but with gaps
         Delta: 1 unit
. xtsfkk y x1 x2 x3 z1, production uhet(z2) endogenous(z1 z2)
> instruments(iv1 iv2) header efficiency(efv) test timer

 7 Dec 2020 21:37:00

ENDOGENOUS PANEL STOCHASTIC PRODUCTION FRONTIER MODEL (MODEL EN)

Dependent Variable: y

Frontier Variables: Constant x1 x2 x3 z1

U Variables: Constant z2

W Variable: Constant

Endogenous Variables: z1 z2

Added Instruments: iv1 iv2

Exogenous Variables: iv1 iv2 x1 x2 x3

Panel Variable: firm

Time Variable: year

initial:       Model EN log likelihood =     -<inf>  (could not be evaluated)
feasible:      Model EN log likelihood = -14107.075
rescale:       Model EN log likelihood = -11232.026
rescale eq:    Model EN log likelihood = -1178.2399
Iteration 0:   Model EN log likelihood = -1178.2399
Iteration 1:   Model EN log likelihood = -1109.8613  (backed up)
Iteration 2:   Model EN log likelihood = -1044.2072  (backed up)
Iteration 3:   Model EN log likelihood = -409.48474  (backed up)
   (output omitted)
```

```
Iteration 97:  Model EN log likelihood =  5614.6132
Iteration 98:  Model EN log likelihood =  5614.6133
Iteration 99:  Model EN log likelihood =  5614.6133
Iteration 100: Model EN log likelihood =  5614.6133
Iteration 101: Model EN log likelihood =  5614.6133
Model converged!
```

Endogenous stochastic prod frontier model with normal/half-normal specification

Model EN log likelihood = 5614.6133   Number of obs = 2,000

	Coefficient	Std. err.	z	P>|z|	[95% conf. interval]	
frontier_y						
x1	.0424713	.0156223	2.72	0.007	.0118521	.0730906
x2	−.275394	.1166701	−2.36	0.018	−.5040632	−.0467247
x3	−.1004069	.0500784	−2.00	0.045	−.1985588	−.0022551
z1	.461508	.1744954	2.64	0.008	.1195034	.8035127
_cons	.703658	.0343724	20.47	0.000	.6362894	.7710266
lnsig2u						
z2	2.468718	.2651657	9.31	0.000	1.949002	2.988433
_cons	−7.598463	.2257404	−33.66	0.000	−8.040906	−7.15602
lnsig2w						
_cons	−9.052407	.034144	−265.12	0.000	−9.119328	−8.985486
ivr1_z1						
iv1	−.2310554	.0832553	−2.78	0.006	−.3942328	−.0678781
iv2	.0356556	.0196424	1.82	0.069	−.0028428	.0741541
x1	−.0859004	.0099144	−8.66	0.000	−.1053323	−.0664686
x2	.653102	.0170333	38.34	0.000	.6197173	.6864868
x3	.2928773	.0153035	19.14	0.000	.262883	.3228717
_cons	.3694245	.0690111	5.35	0.000	.2341653	.5046837
ivr2_z2						
iv1	.5447541	.0566707	9.61	0.000	.4336816	.6558265
iv2	.9374176	.0402402	23.30	0.000	.8585482	1.016287
x1	−.0133303	.0067896	−1.96	0.050	−.0266377	−.0000229
x2	−.0270647	.0116898	−2.32	0.021	−.0499762	−.0041531
x3	−.0200798	.0106513	−1.89	0.059	−.0409559	.0007963
_cons	−.1320416	.046939	−2.81	0.005	−.2240403	−.040043
/eta1_z1	−.4572485	.1745281	−2.62	0.009	−.7993173	−.1151797
/eta2_z2	.0227879	.0065443	3.48	0.000	.0099614	.0356144
/le1	.3203268	.0050652	63.24	0.000	.3103993	.3302543
/le2	−.010222	.0049013	−2.09	0.037	−.0198283	−.0006156
/le3	.2189846	.0034624	63.25	0.000	.2121984	.2257709

                        eta Endogeneity Test

Ho: Correction for endogeneity is not necessary.
Ha: There is endogeneity in the model and correction is needed.

 (1) [/]eta1_z1 = 0
 (2) [/]eta2_z2 = 0

          chi2(2) =   19.01
        Prob > chi2 =   0.0001

Result: Reject Ho at 0.1% level.

```
              Summary of Model EN Tech Efficiency
─────────────────────────────────────────────────────
Mean Efficiency          .9718788
Median Efficiency        .9721585
Minimum Efficiency       .79962053
Maximum Efficiency       .99961415
Standard Deviation       .01449759

where
0 = Perfect tech inefficiency
1 = Perfect tech efficiency
```
   (*output omitted*)
```
Completed in 6 seconds.
```

Raw estimation results are presented in the table; eta terms for `z1` and `z2` are both statistically significant in the table. Also, because the `test` option was specified, eta endogeneity test results are presented, showing that the null hypothesis is rejected at the 0.1% level and correction for endogeneity is needed. Looking at the coefficients of the endogenous variables, `z1` and `z2` are both positive and statistically significant. If the `compare` option had been specified, the results from the exogenous comparison model would show that the coefficients of `z1` and `z2` are substantially smaller than they are in the displayed model corrected for endogeneity.

Because the `efficiency()` option was specified in the command line, technical efficiency scores are saved as a variable and this variable's summary statistics are presented. In this model, mean technical efficiency is 0.9719 and median technical efficiency is 0.9722. If the `compare` option had been specified, the `efficiency()` option would also save the efficiency scores from the model that ignores endogeneity. A comparison of technical efficiencies from these two models would indicate that some producers are not as efficient in production as they would appear in a standard frontier model that ignores endogeneity.

5.2   Panel stochastic cost frontier model with endogeneity

In this example, the longitudinal data include 85 individuals and a total of 300 observations between 2011 and 2015. This unbalanced dataset is for illustrative purposes and does not characterize a certain sector. The cost (`y`) is modeled as a function of two frontier variables (`x1` and `z1`), and cost inefficiency is modeled as a function of a variable (`z2`). Two IVs (`iv1` and `iv2`) are used to handle the potential endogeneity of two variables (`z1` and `z2`) in the model. The `header` option displays the model fully.

```
. use xtsfkkcost, clear

. xtset id t
Panel variable: id (unbalanced)
 Time variable: t, 2011 to 2015, but with gaps
         Delta: 1 unit
```

```
. xtsfkk y x1 z1, cost uhet(z2) endogenous(z1 z2) instruments(iv1 iv2) header
> compare nicely

13 Dec 2020 20:41:10

ENDOGENOUS PANEL STOCHASTIC COST FRONTIER MODEL (MODEL EN)

Dependent Variable: y

Frontier Variables: Constant x1 z1

U Variables: Constant z2

W Variable: Constant

Endogenous Variables: z1 z2

Added Instruments: iv1 iv2

Exogenous Variables: iv1 iv2 x1

Panel Variable: id

Time Variable: t

initial:       Model EN log likelihood =      -<inf>  (could not be evaluated)
feasible:      Model EN log likelihood = -1681.3015
rescale:       Model EN log likelihood = -1280.7454
rescale eq:    Model EN log likelihood = -1103.6189
Iteration 0:   Model EN log likelihood = -1103.6189
Iteration 1:   Model EN log likelihood = -1070.1485  (backed up)
Iteration 2:   Model EN log likelihood =  -1015.916  (backed up)
Iteration 3:   Model EN log likelihood =  -1002.332  (backed up)
   (output omitted)
Iteration 29:  Model EN log likelihood =  -782.6236
Iteration 30:  Model EN log likelihood = -782.62356
Iteration 31:  Model EN log likelihood = -782.62356
Model converged!

Analyzing the exogenous model (Model EX)...
initial:       Model EX log likelihood = -889.19726
alternative:   Model EX log likelihood = -673.58288
rescale:       Model EX log likelihood = -603.89561
rescale eq:    Model EX log likelihood =  -588.8592
Iteration 0:   Model EX log likelihood =  -588.8592
Iteration 1:   Model EX log likelihood = -560.33106  (backed up)
Iteration 2:   Model EX log likelihood = -452.58101  (backed up)
Iteration 3:   Model EX log likelihood = -436.04682  (backed up)
   (output omitted)
Iteration 18:  Model EX log likelihood = -302.44416
Iteration 19:  Model EX log likelihood = -302.44416
Iteration 20:  Model EX log likelihood = -302.44416
Model converged!
```

```
Table: Estimation Results
```

	Model EX		Model EN	
Dep.var: y				
Constant	0.391**	(0.129)	0.295*	(0.136)
x1	0.136*	(0.068)	0.494***	(0.092)
z1	0.963***	(0.047)	0.746***	(0.097)
Dep.var: $\ln(\sigma^2\_u)$				
Constant	-0.544*	(0.251)	-0.944***	(0.215)
z2	1.190***	(0.068)	1.131***	(0.063)
Dep.var: $\ln(\sigma^2\_v)$				
Constant	-1.503***	(0.097)		
Dep.var: $\ln(\sigma^2\_w)$				
Constant			-1.918***	(0.094)
eta1 (z1)			0.421***	(0.109)
eta2 (z2)			0.568***	(0.055)
eta Endogeneity Test			X2=138.67	p=0.000
Observations	300		300	
Log Likelihood	-302.44		-782.62	
Mean Cost Efficiency	0.3625		0.4838	
Median Cost Efficiency	0.3341		0.4976	

```
Notes: Standard errors are in parentheses. Symbols indicate
significance at the 0.1% (***), 1% (**), 5% (*), and 10% (†)
levels.
```

(output omitted)

The output table above presents the estimation results. Because the `compare` and `nicely` options were specified, there are two columns of results: model EX is the model that ignores endogeneity, and model EN is the model that handles endogeneity. Individual eta terms for `z1` and `z2` are both statistically significant at the 0.1% level, and the eta endogeneity test result rejects the null hypothesis at the 0.1% level, which indicates that a correction for endogeneity in the model is necessary.

Statistical significance and magnitudes of coefficients are different in model EX and model EN. The coefficients of `z1` and `z2` in model EX are positive and statistically significant. In model EN, these coefficients are significant and positive but smaller. Moreover, mean cost efficiency in model EX is 0.3625, while in model EN, the same statistic is 0.4838. This tells us that individuals in the model with endogeneity are more cost efficient than they would be in the model that overlooks endogeneity.

5.3 Example from the U.S. banking sector

In this last example, we examine a panel stochastic production frontier model with a real dataset that comes from the U.S. banking sector. The main panel data are from the

Federal Financial Institutions Examination Council Central Data Repository. This main panel dataset consists of 19,304 year-end observations of 4,408 U.S. banks from 2010 to 2016. We follow the model in Berger et al. (2017) and, for simplicity, design a simpler loan production model where the dependent variable is the natural logarithm of total small loans (`loans`). Production frontier variables include natural logarithms of core deposits (`cdep`), other hot money (`hotm`), and gross total assets (`gta`). Also, the frontier function includes bank return on equity (`roe`) and a dummy variable (`big`) that is equal to 1 if the gross total assets of the bank is greater than $1 billion. Technical inefficiency is modeled with a Herfindahl–Hirschman index (`hhi`) of market concentration ranging between 0 and 1, with 1 indicating a monopoly setting. We control for the endogeneity of `loans` and `hhi` by using the leading political party's voter representation percentage in a county.[1]

We specify the `compare`, `nicely`, `header`, `save()`, and `load()` options in this example. Model EX, which does not handle endogeneity, is comparable with a standard `xtfrontier` command estimation. The coefficient of `hhi` is expected to be negative. Looking at the results, we see that the eta term of `hhi` is significant at the 0.1% level, and the eta endogeneity test result tells us that correction for endogeneity is necessary. As shown in the output table below, the coefficient of `hhi` is negative and significant in model EX, but in model EN, the coefficient is substantially smaller (bigger negative impact) and significant.

```
. use xtsfkkbank, clear

. xtset id year
Panel variable: id (unbalanced)
 Time variable: year, 2010 to 2016, but with gaps
         Delta: 1 unit

. xtsfkk loans cdep hotm gta roe big, uhet(hhi) endogenous(hhi) instruments(rep)
> iterate(5) save("banks.est")
initial:       Model EN log likelihood =     -<inf>  (could not be evaluated)
feasible:      Model EN log likelihood = -669859.93
rescale:       Model EN log likelihood = -182739.03
rescale eq:    Model EN log likelihood =  -65950.66
Iteration 0:   Model EN log likelihood =  -65950.66
Iteration 1:   Model EN log likelihood = -64617.692  (backed up)
Iteration 2:   Model EN log likelihood = -61470.412  (backed up)
Iteration 3:   Model EN log likelihood = -59672.694  (backed up)
Iteration 4:   Model EN log likelihood =  -59508.14  (backed up)
Iteration 5:   Model EN log likelihood = -58708.949  (backed up)

   (output omitted )
```

---

1. The election data come from the MIT Election Data and Science Lab.

```
. xtsfkk loans cdep hotm gta roe big, uhet(hhi) endogenous(hhi) instruments(rep)
> header compare nicely timer beep(3) load("banks.est")

13 Dec 2020 20:08:42

ENDOGENOUS PANEL STOCHASTIC PRODUCTION FRONTIER MODEL (MODEL EN)

Dependent Variable: loans

Frontier Variables: Constant cdep hotm gta roe big

U Variables: Constant hhi

W Variable: Constant

Endogenous Variable: hhi

Added Instrument: rep

Exogenous Variables: rep cdep hotm gta roe big

Panel Variable: id

Time Variable: year

initial:        Model EN log likelihood = -58708.949
rescale:        Model EN log likelihood = -58708.949
rescale eq:     Model EN log likelihood = -58708.949
Iteration 0:    Model EN log likelihood = -58708.949
Iteration 1:    Model EN log likelihood = -57945.227  (backed up)
Iteration 2:    Model EN log likelihood =  -54228.19  (backed up)
   (output omitted)
Iteration 58:  Model EN log likelihood = -7242.2345
Model converged!

Analyzing the exogenous model (Model EX)...
initial:        Model EX log likelihood = -1156049.1
alternative:    Model EX log likelihood = -657187.45
rescale:        Model EX log likelihood =  -71965.71
rescale eq:     Model EX log likelihood = -16548.717
Iteration 0:    Model EX log likelihood = -16548.717
Iteration 1:    Model EX log likelihood = -16396.439  (backed up)
Iteration 2:    Model EX log likelihood = -16291.778  (backed up)
   (output omitted)
Iteration 29:  Model EX log likelihood = -4805.2929
Model converged!
```

```
Table: Estimation Results
```

	Model EX		Model EN	
Dep.var: loans				
Constant	1.210***	(0.076)	1.171***	(0.076)
cdep	-0.015*	(0.007)	-0.017*	(0.007)
hotm	0.010***	(0.002)	0.011***	(0.002)
gta	0.821***	(0.009)	0.825***	(0.009)
roe	0.049***	(0.007)	0.046***	(0.008)
big	-0.019	(0.027)	-0.020	(0.027)
Dep.var: $\ln(\sigma^2\_u)$				
Constant	0.486***	(0.027)	0.551***	(0.029)
hhi	-0.310***	(0.034)	-0.476***	(0.042)
Dep.var: $\ln(\sigma^2\_v)$				
Constant	-3.136***	(0.012)		
Dep.var: $\ln(\sigma^2\_w)$				
Constant			-3.138***	(0.012)
eta1 (hhi)			-0.141***	(0.021)
eta Endogeneity Test			X2=45.50	p=0.000
Observations	19304		19304	
Log Likelihood	-4805.29		-7242.23	
Mean Tech Efficiency	0.4729		0.4729	
Median Tech Efficiency	0.4683		0.4669	

```
Notes: Standard errors are in parentheses. Symbols indicate
significance at the 0.1% (***), 1% (**), 5% (*), and 10% (†)
levels.
```

   (output omitted)

```
Completed in 28 seconds.
```

6   Conclusion

In this article, I offered a new command called `xtsfkk` to fit endogenous stochastic panel frontier models, presented by Karakaplan and Kutlu (2017a). `xtsfkk` can control for the endogenous variables in both the frontier and the inefficiency term. With some Monte Carlo simulations and examples, I showed that `xtsfkk` outperforms the standard panel frontier estimation methods that ignore endogeneity. Moreover, `xtsfkk` comes with various options that can be useful in panel research settings.

7   Acknowledgments

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8 Programs and supplemental materials

To install a snapshot of the corresponding software files as they existed at the time of publication of this article, type

```
. net sj 22-3
. net install st0686      (to install program files, if available)
. net get st0686          (to install ancillary files, if available)
```

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