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# Uniform nonparametric inference for time series using Stata

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**Abstract.** In this article, we introduce a command, `tssreg`, that conducts nonparametric series estimation and uniform inference for time-series data, including the case with independent data as a special case. This command can be used to nonparametrically estimate the conditional expectation function and the uniform confidence band at a user-specified confidence level, based on an econometric theory that accommodates general time-series dependence. The uniform inference tool can also be used to perform nonparametric specification tests for conditional moment restrictions commonly seen in dynamic equilibrium models.

**Keywords:** st0614, `tssreg`, nonparametric regression, Newey–West standard error, series estimation, specification test, uniform inference

## 1 Introduction

Nonparametric problems arise routinely from applied work because the economic intuition of the guiding economic theory often does not depend on stylized parametric model assumptions. A leading approach is to approximate the unknown function using a large number of basis functions; see, for example, Andrews (1991), Newey (1997), Chen (2007), Belloni et al. (2015), and Chen and Christensen (2015). The series estimation method is intuitively appealing, and an empirical researcher’s “flexible” regression specification can often be given a formal nonparametric interpretation as a series estimator.

In a companion article, Li and Liao (Forthcoming) propose an econometric method for making uniform nonparametric inference in a general time-series setting based on series estimation. The proposed uniform confidence band allows the empirical researcher to make a formal statistical statement on the entire conditional expectation function. This “global” inference differs from the conventional pointwise inference theory, as the latter only concerns the unknown function at a specific point and is thus “local” in nature. The inference method can also be conveniently used to conduct nonparametric specification tests for conditional moment restrictions that often stem from dynamic equilibrium models.

This article introduces the new command `tssreg`, which stands for time-series series regression. Based on the econometric theory in Li and Liao (Forthcoming), this command can be used to conduct two types of empirical analysis. One is to nonparametrically estimate a conditional expectation function and its uniform confidence band. The other is a sup-t test for conditional moment restrictions. We illustrate the method using the empirical example of Li and Liao (Forthcoming) and further extend their analysis.

This article is organized as follows. Section 2 provides some background on the underlying econometric method. Section 3 describes the basic features of the `tssreg` command. Section 4 provides a concrete illustration of the command in an empirical example and concludes.

## 2 Background on the uniform series inference method

This section provides an overview of the econometric method. Consider the following nonparametric time-series regression,

$$Y_t = h(X_t) + \epsilon_t \quad E(\epsilon_t|X_t) = 0 \quad 1 \leq t \leq n$$

where the dependent variable  $Y_t$  and the conditioning variable  $X_t$  are both univariate time series. Our econometric interest is to nonparametrically estimate the unknown function  $h(\cdot)$  and make a uniform inference for it. More precisely, we aim to construct a  $(1 - \alpha)$ -level confidence band  $[\widehat{L}(\cdot), \widehat{U}(\cdot)]$ , such that

$$P \left\{ \widehat{L}(x) \leq h(x) \leq \widehat{U}(x) \text{ for all } x \in \mathcal{X} \right\} \rightarrow 1 - \alpha \quad (1)$$

as the sample size asymptotically goes to infinity, where  $\mathcal{X}$  is (possibly a subset of) the observed support of the conditioning variable.

We implement the econometric procedure proposed by Li and Liao (Forthcoming). These authors conduct nonparametric estimation using series regression and propose a confidence band that satisfies the uniform coverage property described in (1). Their method is justified by a strong approximation theory for time-series data. We refer the readers to Li and Liao (Forthcoming) for theoretical details.

The econometric procedure contains a few steps. In the first step, we conduct series estimation by regressing  $Y_t$  on a set of approximating functions of  $X_t$ , denoted by

$$\mathbf{P}(X_t) = \{p_1(X_t), \dots, p_m(X_t)\}'$$

Among many possible choices of approximating functions, we use the following:

$$p_j(x) = L_{j-1}\{f(x)\} \quad (2)$$

where  $L_j(\cdot)$  denotes the  $j$ th Legendre polynomial, and  $f(\cdot)$  is a fixed, strictly increasing transformation that serves the purpose of “rescaling” the conditioning variable  $X_t$ , as we will discuss in more detail below. The resulting regression coefficient is

$$\hat{\mathbf{b}} = \left\{ \sum_{t=1}^n \mathbf{P}(X_t) \mathbf{P}(X_t)' \right\}^{-1} \left\{ \sum_{t=1}^n \mathbf{P}(X_t) Y_t \right\}$$

and the series estimator of  $h(x)$  is subsequently given by

$$\hat{h}(x) = \mathbf{P}(x)' \hat{\mathbf{b}}$$

The approximating functions in (2) are adopted to minimize the issue of multicollinearity, which is particularly relevant when the regression involves many series terms (that is, when  $m$  is large). To see how this works, let us first recall some basic properties of Legendre polynomials. These functions can be defined recursively as follows:  $L_0(x) = 1$ ,  $L_1(x) = x$ , and

$$L_j(x) = \frac{2j-1}{j} x L_{j-1}(x) - \frac{j-1}{j} L_{j-2}(x) \quad j \geq 2$$

Unlike the ordinary polynomial functions, the Legendre polynomials are orthogonal on the  $[-1, 1]$  interval with respect to the uniform distribution, that is, for  $j \neq k$ ,

$$\int_{-1}^1 L_j(x) L_k(x) dx = 0$$

If  $X_t$  is uniformly distributed over  $[-1, 1]$ , the variables  $\{L_j(X_t)\}_{j \geq 0}$  are uncorrelated; hence, a regression on these variables does not suffer from the issue of multicollinearity. More generally, if the distribution function of  $X_t$  is  $F_X$ , the transformed variable  $f(X_t)$ , with  $f(x) = 2F_X(x) - 1$ , is uniformly distributed over  $[-1, 1]$ . In this case, the regressors  $\{p_j(X_t)\}_{1 \leq j \leq m}$  are mutually orthogonal. The **tssreg** command provides a few options for calibrating the  $f(\cdot)$  transformation so as to “nearly” achieve this orthogonalization. By doing so, this command can accommodate a relatively large number of series terms without running into numerical instability issues. We also note that many other orthogonal basis functions, such as trigonometric series and Haar wavelets, may also be used for the same purpose. We do not intend to be exhaustive on these choices, leaving such extension to interested readers in the Stata community.

Li and Liao (Forthcoming) show that the estimation error  $\hat{h}(x) - h(x)$  can be approximately represented as  $\mathbf{P}(x)' \boldsymbol{\xi}$  in a well-defined theoretical sense, where  $\boldsymbol{\xi} \sim N(\mathbf{0}, \mathbf{V})$  and  $\mathbf{V}$  is the estimated variance-covariance matrix of  $\hat{\mathbf{b}}$ . In the time-series context here,  $\mathbf{V}$  generally accounts for serial dependence of the data, and we adopt the Newey-West estimator for this purpose (also see [TS] **newey**). The estimated standard error of  $\hat{h}(x)$  is thus

$$\sigma(x) = \sqrt{\mathbf{P}(x)' \mathbf{V} \mathbf{P}(x)}$$

The uniform inference on the  $h(\cdot)$  function is based on the sup-t statistic defined as

$$\text{sup-t} = \sup_{x \in \mathcal{X}} \left| \frac{\hat{h}(x) - h(x)}{\sigma(x)} \right|$$

which can then be approximately represented by

$$\sup_{x \in \mathcal{X}} \left| \frac{\mathbf{P}(x)' \boldsymbol{\xi}}{\sigma(x)} \right|$$

Hence, we can compute the critical value (CV) at significance level  $\alpha$  for the sup-t statistic, denoted by  $\text{CV}_\alpha$  below, as the  $1 - \alpha$  quantile of this random variable. This computation is carried out via simulation, for which we draw  $\boldsymbol{\xi}$  from the  $N(\mathbf{0}, \mathbf{V})$  distribution and approximate  $\mathcal{X}$  with a subset of grid points for calculating the supremum.

It can be shown that in large samples

$$P(\text{sup-t} > \text{CV}_\alpha) = P \left( \sup_{x \in \mathcal{X}} \left| \frac{\widehat{h}(x) - h(x)}{\sigma(x)} \right| > \text{CV}_\alpha \right) \rightarrow \alpha$$

That is, the sup-t test provides correct size control under the null hypothesis

$$H_0: E(Y_t | X_t = x) = h(x) \quad \text{all } x \in \mathcal{X}$$

We can also define the two-sided  $(1 - \alpha)$ -level confidence band as

$$\widehat{L}(x) = \widehat{h}(x) - \text{CV}_\alpha \sigma(x) \quad \widehat{U}(x) = \widehat{h}(x) + \text{CV}_\alpha \sigma(x)$$

which satisfies the desired uniform coverage property:

$$P \left\{ \widehat{L}(x) \leq h(x) \leq \widehat{U}(x) \text{ for all } x \in \mathcal{X} \right\} \rightarrow 1 - \alpha$$

The uniform confidence band is directly useful for making functional inference on the relation between the dependent variable  $Y_t$  and the conditioning variable  $X_t$ . Changing the perspective slightly, we further note that this method can be conveniently used to test conditional moment restrictions. Dynamic equilibrium models often imply conditional moment restrictions of the form

$$E \{g(\mathbf{Y}_t^*; \boldsymbol{\gamma}_0) | X_t\} = 0$$

where  $\mathbf{Y}_t^*$  is an observed time series and  $\boldsymbol{\gamma}_0$  is a finite-dimensional vector of structural parameters. We can test this conditional moment restriction by nonparametrically regressing  $Y_t = g(\mathbf{Y}_t^*; \boldsymbol{\gamma}_0)$  on  $X_t$ . If the parameter  $\boldsymbol{\gamma}_0$  is unknown, we can replace it with a preliminary estimator  $\widehat{\boldsymbol{\gamma}}$  and proceed as if  $\widehat{\boldsymbol{\gamma}} = \boldsymbol{\gamma}_0$ . The theoretical justification for ignoring the estimation error in  $\widehat{\boldsymbol{\gamma}}$  is discussed in Li and Liao (Forthcoming). Intuitively, the inference is asymptotically valid because the rate of convergence of  $\widehat{\boldsymbol{\gamma}}$  is faster than that of the nonparametric estimator  $\widehat{h}(\cdot)$ ; hence, the estimation error in  $\widehat{\boldsymbol{\gamma}}$  is asymptotically negligible relative to that in the nonparametric test. Under the null hypothesis of correct specification,  $h(x) = E(Y_t | X_t = x)$  should be identically 0 for all  $x \in \mathcal{X}$ . We reject the null hypothesis if the corresponding sup-t statistic is greater than the CV. Equivalently, we can visually examine whether the uniform confidence band covers 0 for all  $x \in \mathcal{X}$ . The conditional moment restriction is rejected if this is not the case.

### 3 The tssreg command

This section describes the basic features of the `tssreg` command. This command requires the `moremata` package (Jann 2005), which can be installed using the command `ssc install moremata`.

#### 3.1 Syntax

The syntax of the `tssreg` command is as follows:

```
tssreg depvar condvar [ controlvar] [ if] [ in] [ , lag(#) m(#)
method(transtype) confidencelevel(#) ngrid(#) trim(#) mc(#) table
plot excel]
```

where `depvar` is the dependent variable, `condvar` is the conditioning variable, and `controlvar` is a list of additional control variables.

#### 3.2 Options

`lag(#)` specifies the maximum number of lags for computing the Newey–West estimator of the long-run covariance matrix; see [TS] `newey`. The default is `lag(0)`.

`m(#)` specifies the number of Legendre polynomial terms used in the nonparametric series regression. The default is `m(6)`.

`method(transtype)` specifies the transformation applied to the conditioning variable. The approximating functions are Legendre polynomials of the transformed variable. The following transformations are supported in the current version. The default is `method(rank)`.

`rank`:  $x \mapsto 2q(x) - 1$ , where  $q(x)$  is the empirical quantile of  $x$ ;

`affine`: affine transformation  $x \mapsto [2\{x - \min(x)\}]/\{\max(x) - \min(x)\} - 1$ ;

`normal`: normal transformation  $x \mapsto 2\Phi\{(x - \bar{x})/\sigma\} - 1$ , where  $\bar{x}$  and  $\sigma$  are the sample mean and standard deviation of  $x$ , and  $\Phi$  is the cumulative distribution function of the standard normal distribution;

`lognormal`: log-normal transformation  $x \mapsto 2\Phi\{(\log x - \overline{\log x})/\Sigma\} - 1$ , where  $\overline{\log x}$  and  $\Sigma$  are the sample mean and standard deviation of  $\log x$ , and  $\Phi$  is the cumulative distribution function of the standard normal distribution;

`none`: no transformation.

`confidencelevel(#)` specifies the confidence level, as a percentage, for the uniform confidence band. The default is `confidencelevel(95)`.

`ngrid(#)` specifies the number of grid points used for discretizing the support of the conditioning variable. The default is `ngrid(100)`.

`trim(#)` specifies the level of trimming in the computation of the sup-t statistic and its CV. Setting `trim(#)` restricts the domain of `condvar` between its  $#/2$  and  $1 - #/2$  empirical quantiles. The default is `trim(0)`.

`mc(#)` specifies the number of Monte Carlo simulations used to compute the CVs. The default is `mc(5000)`.

`table` reports the estimates of the regression coefficients and standard errors.

`plot` produces a graph with the nonparametric estimate of the conditional expectation function, along with its uniform confidence band.

`excel` generates an Excel file that contains nonparametric estimates and the associated uniform confidence band.

### 3.3 Stored results

`tssreg` stores the following in `e()`:

Scalars			
<code>e(N)</code>	number of observations	<code>e(supt)</code>	sup-t statistic
<code>e(df_r)</code>	residual degrees of freedom	<code>e(cv)</code>	CV of sup-t statistic
Macros			
<code>e(cmd)</code>	<code>tssreg</code>	<code>e(condvar)</code>	name of conditioning variable
<code>e(depvar)</code>	name of dependent variable	<code>e(method)</code>	transformation
Matrices			
<code>e(b)</code>	regression coefficients	<code>e(xgrid)</code>	grid points of the
<code>e(ygrid)</code>	nonparametric estimate		conditioning variable
<code>e(se)</code>	standard errors of regression	<code>e(sigma)</code>	estimate of standard error
	coefficients		function
<code>e(V)</code>	variance-covariance matrix of		
	regression coefficients		
Function			
<code>e(sample)</code>	marks estimation sample		

## 4 Illustration of the method

### 4.1 Basic applications

A basic application of the `tssreg` command is to conduct a sup-t test for the conditional moment restriction

$$E(Y_t|X_t = x) = 0 \quad \text{for } x \in \mathcal{X}$$

where  $\mathcal{X}$  is the observed support of  $X_t$ . In dynamic stochastic equilibrium models, this restriction can be derived from the martingale-difference property of the  $Y$  series with respect to an information filtration, according to Euler or Bellman equations in the structural model. Hence, under the null hypothesis, we can compute standard errors without accounting for autocorrelations of error terms. This can be done using the default option `lag(0)`.

To illustrate, we use the dataset from the empirical study of Li and Liao (Forthcoming). `data.dta` contains three variables: `timevar` is the time index, the conditioning variable `x` is productivity, and the dependent variable `y` is generated according to the equilibrium conditions of a standard search-and-matching model. We set up the time-series structure<sup>1</sup> using `tsset` (see [TS] `tsset`), and then implement the sup-t test as follows:

```
. use data
. tsset timevar
    time variable: timevar, 1 to 215
          delta: 1 unit
. tssreg y x

```

Transformation:	sup-t	5% critical value	P> t
Rank	11.1841	2.8545	0.000

With the default options, we carry out the test by nonparametrically fitting `y` using a fifth-order Legendre polynomial of the rank-transformed `x`. As shown in the table above, Stata reports the value of the sup-t statistic as 11.1841, which is far above the 5% CV.<sup>2</sup> The *p*-value is virtually 0, suggesting a strong rejection of the hypothesis that  $E(y|x) = 0$ ; that is, the equilibrium condition is not compatible with observed data.

Furthermore, if we use the `table` option, `tssreg` also reports the regression coefficients and the associated sampling information. For example,

```
. tssreg y x, table

```

Number of obs = 215						
Newey-West maximum lag = 0						
	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval
p_1(x)	-.0265563	.0015124	-17.56	0.000	-.0295378	-.0235748
p_2(x)	.0112508	.0026945	4.18	0.000	.0059389	.0165627
p_3(x)	.0013992	.0032379	0.43	0.666	-.0049839	.0077824
p_4(x)	.0029088	.0038347	0.76	0.449	-.0046509	.0104684
p_5(x)	-.0031211	.0041851	-0.75	0.457	-.0113717	.0051294
p_6(x)	-.0037121	.0047803	-0.78	0.438	-.0131359	.0057116

Transformation:	sup-t	5% critical value	P> t
Rank	11.1841	2.8452	0.000

Another important use of the `tssreg` command is to nonparametrically estimate the conditional expectation function  $h(x) = E(Y_t|X_t = x)$  and its uniform confidence band. The corresponding result can be visualized using the `plot` option and is presented as figure 1.

1. Note that the user can treat a cross section of independent observations as a “time series” by simply setting the “time” index to be `n`.
2. Note that the CV is generated via simulation and thus varies slightly across implementations.

```
. tssreg y x, plot
```

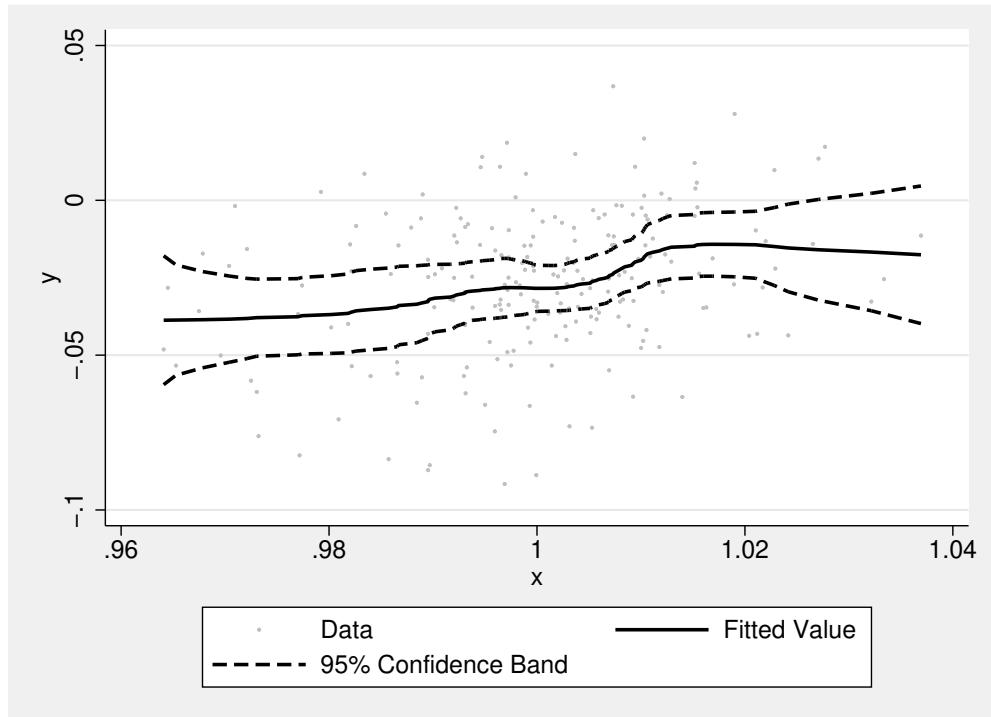


Figure 1. Nonparametric fit and uniform confidence band without heteroskedasticity- and autocorrelation-consistent estimation

We stress that the confidence band plotted in figure 1 is uniformly valid over the support of the conditioning variable displayed on the horizontal axis. In this example, the 95% confidence band does not always cover 0, suggesting that the conditional expectation function deviates from 0 at the 5% significance level. This finding is consistent with the aforementioned testing result. The figure also reveals that the rejection mainly occurs over the region where  $x$  is low.

When computing standard errors, the default setting `lag(0)` only accounts for conditional heteroskedasticity, ignoring all autocorrelations. This is appropriate if the error term  $Y_t - E(Y_t|X_t)$  forms a martingale-difference sequence, which typically holds under the null hypothesis that the dynamic equilibrium model is correctly specified. However, if the empirical goal is to make a uniform inference on the conditional expectation function  $x \mapsto E(Y_t|X_t = x)$ , one should generally take into account time-series dependence by properly setting the lag parameter in the Newey–West estimator, analogous to the application of Stata's built-in `newey` command (see [TS] `newey`). The following implementation sets the Newey–West lag parameter to 5 (and we also set the confidence level to 99% to illustrate the use of the `confidencelevel()` option). The resulting nonparametric estimate and confidence band are displayed in figure 2.

```
. tssreg y x, lag(5) confidencelevel(99) plot
```

Transformation:	sup-t	1% critical value	P> t
Rank	9.8340	3.4123	0.000

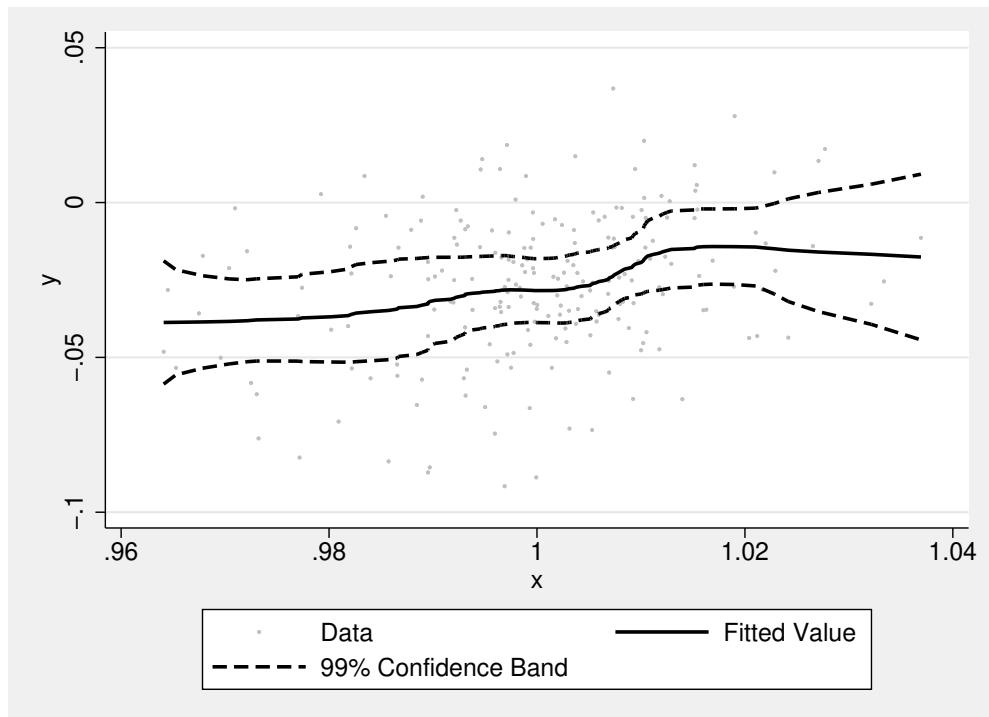


Figure 2. Uniform confidence band with user-specified Newey–West lag parameter and confidence level

## 4.2 Choice of approximating functions

Series estimation involves choosing approximating functions and the number of series terms. While the default setting of `tssreg` provides a reasonable benchmark, applied users are encouraged to experiment with alternative specifications to check the robustness of their empirical findings with respect to these choices. In the current version, the approximating functions are constructed as Legendre polynomials of the transformed conditioning variable, where the specific transformation is set through the `method()` option. Legendre polynomials are orthogonal on the  $[-1, 1]$  interval. With a proper transformation, the distribution of the transformed conditioning variable can be made close to uniform on  $[-1, 1]$ , which mitigates the issue of multicollinearity when many series terms are included in the regression.

Four types of transformations are available in the current version: **affine**, **normal**, **lognormal**, and **rank**. The common idea is first to fit the distribution of  $X_t$ , parametrically or nonparametrically, and then to use the fitted distribution function to transform the conditioning variable into a uniform distribution. Specifically, the options **affine**, **normal**, and **lognormal** correspond to parametrically fitting uniform, normal, and log-normal distributions, respectively. The default **rank** option implements a nonparametric transformation using the ranks (or, equivalently, the empirical distribution function) of the observed  $X_t$  data. The user can also use untransformed data by explicitly setting the **method**(**none**) option.

The number of series terms is determined by the **m(#)** option. The constant term is always included. Hence, **m(#)** corresponds to a  $(\#-1)$ -order Legendre polynomial. Recall that a fifth-order Legendre polynomial is fit under the default setting.

As an example, we can examine the sensitivity of the empirical findings in the running example with respect to these choices. Sensitivity analysis like this is often needed in empirical work. We experiment with three transformations **affine**, **normal**, and **rank**. In addition, besides the default fifth-order Legendre polynomial, we also fit an eighth-order Legendre polynomial by using the **m(9)** option. The resulting plots are collected in figure 3.

<b>. tssreg y x, method(affine) plot</b>			
Transformation:	sup-t	5% critical value	P> t
Affine	13.5659	2.8957	0.000
<b>. tssreg y x, method(normal) plot</b>			
Transformation:	sup-t	5% critical value	P> t
Normal	11.4933	2.8497	0.000
<b>. tssreg y x, method(rank) plot</b>			
Transformation:	sup-t	5% critical value	P> t
Rank	11.1841	2.8096	0.000
<b>. tssreg y x, method(affine) m(9) plot</b>			
Transformation:	sup-t	5% critical value	P> t
Affine	11.7011	2.9492	0.000
<b>. tssreg y x, method(normal) m(9) plot</b>			
Transformation:	sup-t	5% critical value	P> t
Normal	9.8378	3.0461	0.000

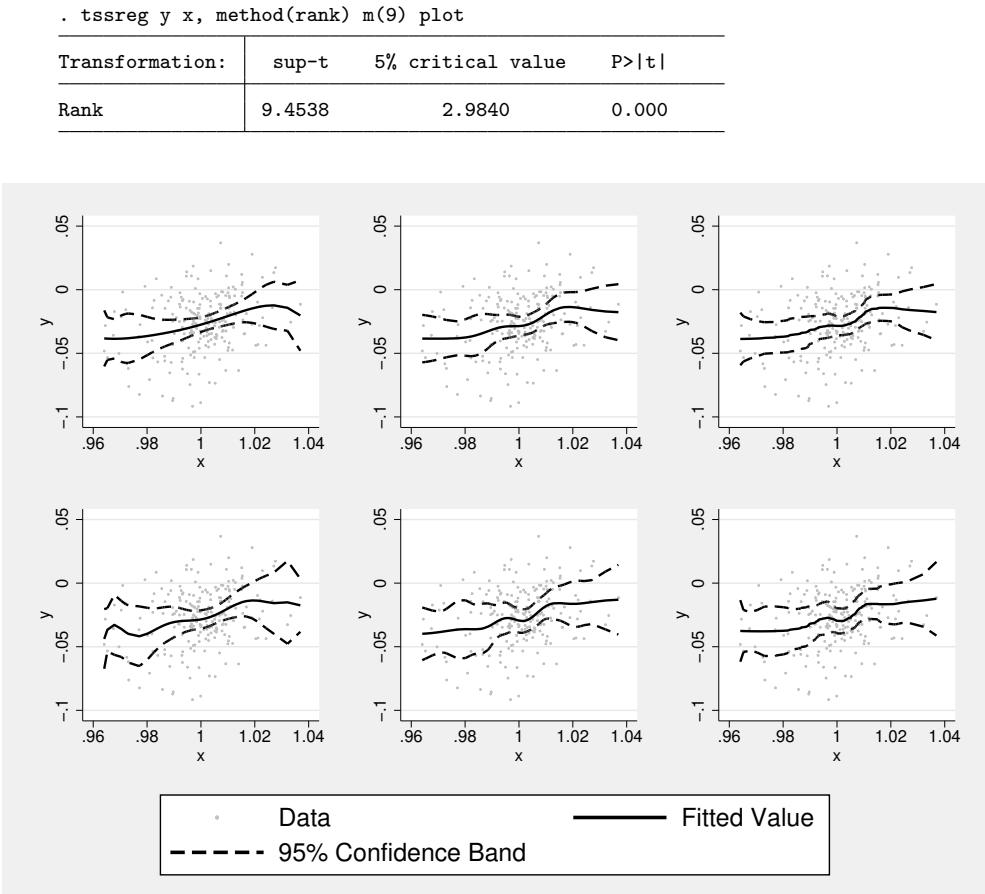


Figure 3. Nonparametric estimates and uniform confidence bands using different series approximations. Estimation in the top (respective bottom) row is conducted using 6 (respective 9) series terms. The left, middle, and right columns are generated using the `affine`, `normal`, and `rank` transformations, respectively. Individual graphs are combined using the `grcileg` command (Wiggins 2010).

In all implementations, the null hypothesis  $E(Y_t|X_t) = 0$  is strongly rejected as before. Figure 3 also shows that essential features of the nonparametric estimation are robust with respect to the choice of approximating function and series terms.

### 4.3 Partial linear model and additional control variables

`tssreg` also accommodates additional control variables in a partially linear model:

$$Y_t = h(X_t) + \beta' \mathbf{Z}_t + \epsilon_t$$

where  $\mathbf{Z}_t$  is a list of control variables that are collected in *controlvar*. With these control variables, **tssreg** tests the null hypothesis

$$h(x) = 0 \quad \text{all } x \in \mathcal{X}$$

and the **plot** option will display the nonparametric estimate and the uniform confidence band of the  $h(\cdot)$  function. The **table** option reports regression coefficients of all series terms of  $X_t$  and control variables.

To illustrate, we include two randomly generated variables, **z1** and **z2**, as *controlvar* in the running example. The results are displayed below.

. generate z1 = rnormal() . generate z2 = rnormal() . tssreg y x z1 z2, table plot						
		Number of obs	=	215		
		Newey-West maximum lag	=	0		
	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
p_1(x)	-.0265895	.0015114	-17.59	0.000	-.0295692	-.0236098
p_2(x)	.0114864	.0026989	4.26	0.000	.0061655	.0168073
p_3(x)	.0011594	.003255	0.36	0.722	-.0052579	.0075767
p_4(x)	.0021964	.0038403	0.57	0.568	-.0053747	.0097675
p_5(x)	-.0024858	.0042217	-0.59	0.557	-.0108088	.0058371
p_6(x)	-.0033754	.0047209	-0.71	0.475	-.0126827	.0059318
z1	-.0000595	.0015734	-0.04	0.970	-.0031614	.0030423
z2	.0016694	.0013786	1.21	0.227	-.0010484	.0043872

Transformation:	sup-t	5% critical value	P> t
Rank	11.0334	2.8674	0.000

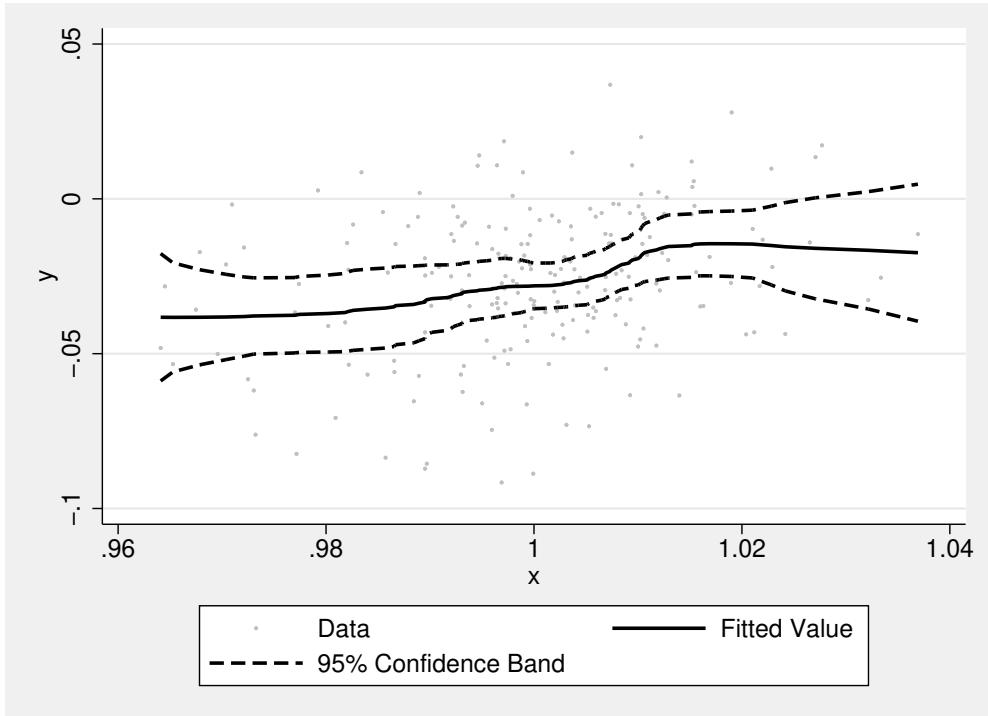


Figure 4. Nonparametric estimate and uniform confidence band with additional controls

Not surprisingly, because the additional control variables are in fact irrelevant in this example, the testing result remains the same, and the nonparametric estimates displayed in figure 4 are very close to those in figure 1.

#### 4.4 Additional options

The `ngrid()` option sets the number of grid points used to discretize the support of  $X_t$ . Discretization is needed to compute the sup-t statistic, which is theoretically defined as the supremum over the support of the conditioning variable. The default is `ngrid(100)`. Setting this parameter to a higher level reduces the approximation error from the discretization, while adding computational cost.

The `trim()` option allows the user to restrict the index set  $\mathcal{X}$  over which the sup-t statistic is computed. Specifically, `trim(#)` restricts  $\mathcal{X}$  as  $[Q_{\#}/2, Q_{1-\#}/2]$ , where  $Q_q$  is the  $q$  quantile of  $X_t$ . This option is useful if one's empirical goal is to make a uniform inference only over the restricted region. Note that the underlying nonparametric series estimation is always based on all available data, whereas the trimming only affects the computation of the sup-t statistic and its CV.

The `mc()` option sets the number of simulations used to compute the CV. The default is `mc(5000)`, which is adequate in most empirical contexts. The user may increase this number to improve the Monte Carlo approximation accuracy or decrease this number to reduce computation time.

The `excel` option saves information for reconstructing the nonparametric plots like figure 1. The output Excel file contains four columns: grid points of the conditioning variable, fitted values of the conditional expectation function, and lower and upper confidence bands at the user-specified confidence level.

## 5 Programs and supplemental materials

To install a snapshot of the corresponding software files as they existed at the time of publication of this article, type

```
. net sj 20-3
. net install st0614      (to install program files, if available)
. net get st0614         (to install ancillary files, if available)
```

## 6 References

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