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Comparison of Welfare Results from Trade Liberalization in the

Armington, Krugman and Melitz Models: Impacts with features of real economies*

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Abstract: In this paper, we contribute to the literature about how the welfare effects of a reduction in trade costs are impacted by market structure assumptions. We compare the Armington structure of trade under perfect competition with the Krugman structure of trade under monopolistic competition and the Melitz structure of trade under monopolistic competition with heterogeneous firms. Given its proven importance to the welfare results, we hold the local trade response (as measured in gravity regressions) constant across the model comparison exercise. We start with highly simplified versions of these models where we reproduce the result of Arkolakis *et al.* (2012) that the welfare impacts are identical. We then show that the welfare results of these models differ when we introduce several features that are important to real economies, several of which have not yet been examined in the literature.

Keywords: heterogeneous firms, gains from trade, theory with numbers, exact hat algebra

JEL classification: F12, F18

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1. Introduction

In this paper, we contribute to the literature on how the welfare effects of a reduction in trade costs are impacted by market structure assumptions. We compare the Armington (1969) model of trade under perfect competition with the Krugman (1980) model of trade under monopolistic competition and the Melitz (2003) model of trade under monopolistic competition with heterogeneous firms. We contribute to the literature on how the welfare results depend on market structure when we introduce several model features that are important in applications to real economies, but which have not yet been investigated.

We start with highly stylized versions of these models where we reproduce the result of Arkolakis et al. (2012) that the welfare impacts are identical. In that stylized model Arkolakis et al. (2012) assume: the model contains one sector per country; has one factor of production; does not contain intermediates; there is no labor-leisure choice; trade of each country is balanced; there is no foreign direct investment; trade costs are iceberg and the trade shock moves the economy to autarky. In an excellent follow-up paper, Costinot and Rodriguez-Clare (2014) highlight and clarify the impact of relaxing several of the rather restrictive assumptions of the simple model of Arkolakis et al. (2012). Regarding their more realistic non-autarky comparative static exercises, they provide comparisons across market structures in models that include multiple sectors, a single aggregate tradeable intermediate good (where all sectors use intermediates in the same proportion) and changes in uniform tariffs; these models start from zero tariffs and zero trade balances. Our paper provides new results for the impact of the Armington, Krugman and Melitz market structures in multi-sector models that include: (i) intermediates with demand structures that reflect actual data on intermediate use; (ii) the impact of alternate model structures for intermediates; (iii) heterogeneous tariffs across sectors; (iv) examination of tariff changes without assuming a movement either from free trade or to autarky; (v) foreign direct investment (FDI); (vi) specific factors of production; (vii) trade imbalances; and (viii) import of primary factors such as specialized intermediate inputs.²

The work of Arkolakis, Costinot and Rodriguez-Clare provides significant guidance for future numerical evaluation of welfare impacts of trade costs. Beyond the fact that it enhances our understanding of the sources of welfare impacts across the different structures, it provides a concrete link between econometric and computational models. They show the importance of grounding numerical model

¹ If fixed exporting costs are paid in the destination country, it is not necessary to assume a movement to autarky.

² Costinot and Rodriguez-Clare (2014) address some of these issues under perfect competition. In particular, using the Armington model, they assess the impact of trade imbalances, heterogeneous tariffs across sectors, and intermediates with demand structures that reflect actual data. However, the relative impact of the Krugman or Melitz structures with these extensions that are an open question.

responses in the extensive literature on trade responses as measured using gravity models. In this paper, we parameterize each of our models in a way that is consistent, to the extent possible, with the estimated trade response from the gravity equations. Consequently, our comparisons of the Armington, Krugman, and Melitz models maintain consistent trade responses. Further, when we introduce FDI into the model, our models are the first to also hold the FDI response constant across the models to be consistent with econometric estimates of the responsiveness of investment to a reduction in barriers. The FDI response is a second constraint on the calibration of the elasticities of the model in addition to the trade response.

We begin our analysis by eliminating most of the details of the GTAP data to produce a model consistent with the simplest model of Arkolakis et al. (2012) (including untruncated Pareto productivity distributions). We first replicate the Arkolakis et al. (2012) equivalence result, then progressively introduce real features of the data. We find that trade imbalances alone are insufficient to break the equivalence result of Arkolakis et al. (2012). The introduction of intermediates in a single sector, one factor model with trade imbalances results, in all our simulations, in larger gains in the Melitz model than in the Krugman model and larger gains in the Krugman model than in the Armington model. If we add multiple sectors to the model with intermediates and trade imbalances, the ranking of Melitz greater than Krugman greater than Armington tends to hold. But there are terms of trade effects in the monopolistic competition models that significantly reverse that ranking for at least one of our ten regions. We show that the structure of intermediate demand and the use of real data on intermediate factor shares by sector make a significant difference in the comparative results across the models. With Cobb-Douglas intermediate demand and real data, we find that, for the average for the world, the ranking of the welfare gains is: Melitz larger than Krugman and Krugman larger than Armington. Leontief intermediate demand diminishes the impact of market structure so that, regarding the average for the world, there is no difference in the estimated welfare gains across market structures. However, the comparative ranking among the three models is not fully consistent across the ten regions, indicating that the ranking of the welfare results between Melitz, Krugman and Armington is parameter dependent.

The exact hat methodology for welfare calculations elaborated by Arkolakis *et al.* (2012) yields the parsimonious two parameter welfare calculation in their simple model. Costinot and Rodriguez-Clare have shown, however, that their exact hat calculation expands to a system of several thousand non-linear independent equations when a modest number of realistic features are introduced into their multi-region model. To date, the exact hat literature has not provided solutions for either of the monopolistic competition general equilibrium models with the more realistic features of the data are real economies, such as data on intermediate factor shares by sector with multiple sectors, trade imbalances, or non-zero initial tariffs. Most of these real economy features have been solved by the exact hat literature only in

perfect competition models. Therefore, there are many unanswered questions on the relative welfare impact of the Armington, Krugman and Melitz to which this paper contributes.

In section 2, we summarize the literature, with a focus in section 2.2 on what we know about the comparative welfare gains of the Armington, Krugman and Melitz models. This includes a discussion of how parsimonious is the exact hat calculus when realistic features of an economy are introduced. We present the equations of the model is section 3. In section 4, we discuss how we calibrate the trade response and the FDI response based on gravity models. We also describe the intermediate demand structure of Costinot and Rodriguez-Clare (2014) and two alternate measures that use real data on intermediates. We present the results of the simulations in section 5 and conclude in section 6.

2. Literature Review

2.1 Rationales for the Gains from Trade

One of the oldest propositions in economics is that there are gains from international trade. Ricardo (1817) elucidated the principle of comparative advantage as the source of gains from international trade and Samuelson (1939) established it rigorously. Krueger (1974) and Bhagwati (1982) showed that in the presence of "rent-seeking" the gains from trade liberalization would be significantly larger than from specialization gains from comparative advantage.³ Since 1979, numerous authors showed that under conditions of increasing returns to scale and imperfect competition, the gains from trade liberalization could be larger than under perfect competition for multiple reasons. The reasons included: (i) increased competition from international trade could lower markups, which would lead to rationalization gains as firms slide down their average cost curves, Krugman (1979); (ii) additional varieties in monopolistically competitive markets are a source of gains from trade, Krugman (1980); (iii) international trade could add additional varieties of intermediate inputs, Ethier (1982); (iv) foreign direct investment of multinationals could be a source of significant gains from trade in imperfectly competitive markets, especially in producer services markets, Markusen (1989; 2002), Markusen and Venables (1998); and Ethier and Markusen (1996). Beginning with Melitz (2003), many theoretical papers have emphasized the heterogeneous nature of firms in a monopolistic competition framework.⁴ These models of heterogeneous firms provide a further rationale for the gains from international trade, as the endogenous decisions of firms to enter or exit could lead to an increase in output by the more efficient firms and an increase in the gains from trade. Following the Melitz (2003) paper, there has been a substantial increase in research in international economics based on firm level data sets. Several new stylized facts about international trade

³ Bhagwati used the term "directly unproductive profit-seeking" activities.

⁴ See, for example, Arkolakis et al. (2008) and Bernard, Redding and Schott (2007).

have been identified, including that only the most productive firms export and trade liberalization induces an intra-industry reallocation of resources.

2.2 Exact Hat Literature for Welfare Calculations

2.2.1 Summary of Established Results. In their influential paper Arkolakis *et al.* (2012) construct stylized versions of the Armington, Krugman, and Melitz models. The surprising result they found in their simplest model was that the welfare impacts of reducing trade costs were equivalent across the three models. The simplifying assumptions of their simplest model include: it contains one sector per country; has one factor of production; does not contain intermediates; there is no labor-leisure choice; trade of each country is balanced; and there is no foreign direct investment. They show, under the restrictions of their simplest model, that the welfare gains from trade depend on only two statistics: changes in the domestic trade share (the "trade response") and the elasticity of trade with respect to variable trade costs. Their analysis is based on the "exact hat" methodology. Crucial to their result is the argument that given the wide acceptance of gravity models in international trade and importance of the trade response to the welfare results, the structural parameters of the three models must be adjusted to yield trade responses consistent with gravity models. Estimation of the gravity model yields an estimate of the trade elasticity, which determines the trade response and is important for the welfare calculation.

Balistreri, Hillberry and Rutherford (2010) were the first to point out that the Arkolakis et al. (2010; 2012) result in their highly stylized model was very fragile. They showed that the introduction of a labor-leisure choice (which in their model is equivalent to a second sector) would break the equivalence. They noted that, in addition to multiple sectors, intermediates would break the equivalence in the welfare results. This was also shown by Arkolakis, Costinot and Rodriguez-Clare (2012), who showed that with intermediates, the monopolistic competition models produce larger gains from trade liberalization than the perfect competition model. Melitz and Redding (2015) show that the Arkolakis *et al.* (2012) equivalence result in the highly stylized one sector model fails to hold if the Pareto distribution of productivity has a finite upper bound. Melitz and Redding find in that model that the endogenous decisions of heterogeneous firms to enter and exit the market provide "an extra adjustment margin" that augments the gains from international trade compared to a Krugman style homogeneous firms model. In their model, there are larger welfare gains from reductions in trade costs and smaller welfare losses from increases in trade costs. The generality of the Melitz and Redding result, regarding the welfare dominance

⁵ The term "exact-hat" refers to the characterization of equilibrium impacts in proportional changes. That is, if \hat{v} is the change in a variable denoted in the benchmark and counterfactual as v and v', respectively, then \hat{v} can be summarized as $\hat{v} = v / v$. See Dekle, Eaton and Kortum (2008) for an earlier application of the exact hat methodology.

of the model with heterogeneous firms and a truncated Pareto distribution, has not yet been examined in models with more general and realistic features.

Costinot and Rodriguez-Clare (2014) provide the most comprehensive investigation of the relative welfare impacts of Armington, Krugman and Melitz models. They begin in their section 3 with autarky exercises, where they examine the impact of relaxing some of the simplifying assumptions of the one sector model of Arkolakis *et al.* (2012). With multiple sectors, but no intermediates and zero trade imbalances, they show that there are no selection effects in these autarky exercises, so the Melitz and Krugman model results are identical. In their 34 regions and 31 sectors numerical model, they find that the relationship between the monopolistic competition models and the Armington model is ambiguous (Costinot and Rodriguez-Clare, 2014, 214-215). Using their 34 regions, 31 sectors model, Costinot and Rodriguez-Clare (2014, 219-220) consider a single aggregate intermediate good without real data (where all sectors use intermediates in the same proportions) and find that the Melitz model produces larger welfare gains than the Krugman model which, in turn, produces larger gains than the Armington model.

Costinot and Rodriguez-Clare (2014, section 4) assess tariff changes, rather than movements to autarky, what they refer to as their richer comparative static exercises. They compare the welfare effects of imposition of a uniform tariff in a model with ten regions, sixteen sectors, a single aggregate intermediate good without real data (where all sectors use intermediates in the same proportions), a single primary factor of production, zero trade balances and zero initial tariffs. In this model, Costinot and Rodriguez-Clare find that with multiple sectors, losses of the uniform tariff tend to be larger in the Krugman model compared with Armington (with exceptions), but are slightly lower in the Melitz model compared with Krugman. With a single aggregate intermediate, the losses are greatest in the Melitz model, next highest with Krugman and lowest with Armington (with some exceptions).

In summary, the literature to date indicates that the welfare ranking of Melitz to Krugman varies with the model, the region and the nature of the counterfactual experiment. As we elaborate in section 2.2.2 below, the literature to date has not shown the impact of the Armington, Krugman or Melitz models with heterogeneous tariffs, intermediates with real data on intermediate factor proportions, the impact of either Cobb-Douglas or Leontief demand for intermediates, trade imbalances, specific factors, multiple factors of production or foreign direct investment. In table 1, we summarize the literature results on comparing the three market structures, prior to this paper.

2.2.2 Does the Exact Hat Methodology Offer a Highly Parsimonious Approach for Calculating the General Equilibrium Welfare Gains from a Reduction in Trade Costs.

Part of the appeal of the exact hat calculus in Arkolakis *et al.* (2012) was that the general equilibrium welfare calculation could be calculated from two statistics: changes in the domestic trade share (the "trade response") and the elasticity of trade with respect to variable trade costs. In the case of an autarky exercise, the trade response is dependent only on initial data, so there is no need for a model to

make the calculation. However, just as the equivalence of the welfare impacts across the three market structures in the highly stylized model of Arkolakis et al. (2012) is very fragile, the sufficiency of the two statistics for the welfare calculation is also very fragile. In fact, although Costinot and Rodriguez-Clare succeed in defining equilibrium conditions for a general equilibrium trade model with realistic features, they have numerically solved their general model only for a special case.

To be more specific, in their online appendix, Costinot and Rodriguez-Clare (2013, pp.9-10) develop equilibrium conditions for a model with ten regions and sixteen sectors with realistic economy features. Their multi-sector theoretical model (of their section 4) allows tariff changes that potentially vary by sector and region, includes intermediates with intermediate factor proportions varying by sector and includes unbalanced trade. Importantly, the exercises are comparative static, rather than movements to autarky. They show that they this model is a system of $3nS + 2n^2S$ simultaneous independent nonlinear equations, where S is the number of sectors and n is the number of regions. For the model with 10 regions and 16 sectors they employ, this is 3680 independent non-linear equations. If the number of regions is 15, this is 7920 independent nonlinear equations. Although with their autarky exercises, Costinot and Rodriguez-Clare consider 34 regions and 31 sectors, they reduce the model to 10 regions and 16 sectors "to ease the computational burden." When they solve a version of this model for the Melitz, Krugman and Armington cases, they make the following simplifying assumptions: (i) there is an aggregate intermediate good where all sectors consume intermediate factors in the same proportion (see section 4.2.2 below for details); (ii) all tariffs are zero in the initial equilibrium; (iii) only a change in uniform tariffs is considered; (iv) all trade balances are zero.

Costinot and Rodriguez-Clare subsequently assess the impact of relaxing assumptions by assessing in their Armington model only: trade balances different from zero initially; heterogeneous tariff changes; and multiple factors of production. The subsequent evaluations of Costinot and Rodriguez-Clare are useful for understanding impacts in the Armington model. Crucially, however, despite showing the results for the ranking of the welfare results across the three market structures in a model with several simplifying assumptions, and then assessing the impact of simplifying assumptions in a perfect competition model, to date the impacts of these simplifying assumptions have not been evaluated in the Krugman or Melitz models and not been compared to Armington. The results in table 4 below for China and the United States, provide examples that the impact of the simplifying assumptions in the Armington model could have an opposite impact in the Krugman or Melitz model. Knowledge of the impact of a modeling assumption in the Armington model is insufficient to infer the impact of the same modeling assumption in the Krugman or Melitz models. Consequently, in our summary table of known results from the literature, we do not report comparative results across these three market structures for the more complicated model features.

To date, without assuming movements to autarky, the exact hat methodology has not yet produced solutions to the Melitz or Krugman models with realistic features of economies, including actual initial data on tariffs, real data on intermediates in multi-sector models and trade imbalances. Thus, it remains to be shown that the exact hat approach offers a significantly simpler method for calculating the welfare impacts of trade cost changes in realistic monopolistic competition models compared with models defined in levels. Further, the exact hat methodology of Costinot and Rodriguez-Clare (2014) comes at the cost of losing much sector and factor detail.

2.3 CGE literature on the welfare gains from trade liberalization (a brief overview)

The early CGE literature was based on constant returns to scale models, where the gains were based on comparative advantage and calculated from "Harberger triangles." The estimated gains from trade liberalization were sometimes characterized by the "Harberger constant," i.e., the gains were generally less than one percent of GDP from trade liberalization. Among others, de Melo and Tarr (1990) and Jensen and Tarr (2003) showed that, even in a perfect competition constant returns to scale model, if there were rents involved, the gains could be many multiples of the gains from the "Harberger triangles."

Regarding imperfect competition models with homogeneous firms, the path breaking article was by Harris (1984), who showed that the gains might be much larger if the behavioral interaction of oligopolists is altered by the trade policy. Harrison, Rutherford and Tarr (1997) estimated that the impact of rationalization gains (sliding down the average cost curve) were small in a quantity adjusting model of oligopoly. Rutherford and Tarr (2002) showed that in a fully dynamic model based on Paul Romer style endogenous growth with gains from variety, the gains from trade liberalization would be many multiples of the gains in a model with constant returns to scale. Markusen, Rutherford and Tarr (2005) and Rutherford and Tarr (2008) showed that introducing foreign direct investment in services with Dixit-Stiglitz endogenous productivity effects would substantially increase the welfare gains. Francois, Manchin and Martin (2013) have summarized many approaches to modeling market structure in CGE models and suggested ways that the alternate model structures could be tested.

Regarding heterogeneous firms, the first effort at a CGE model was by Zhai (2008). His model was developed into an application to the Trans Pacific Partnership in Petri, Plummer and Zhai (2012) and employed in the Global Economic Prospects of the World Bank (2016). Unlike the Melitz model, however, neither Zhai's model, nor the model of Petri, Plummer and Zhai, allow entry or exit of firms, nor does it allow uncertainly about the productivity (Zhai, 2008, pp. 7, 8). But their models do allow existing firms to enter new markets and that type of entry creates a new variety and a welfare gain. Since domestic firms face increased competition from foreign entry, some would be expected to exit. The model of Zhai, however, does not allow firm exit; consequently, the model exaggerates the variety externality. This explains why Petri, Plummer and Zhai obtain such large increases in the variety externality in their

model. Dixon, Jerie and Rimmer (2015) developed a stylized CGE model in which the Armington, Krugman and Melitz models are special cases. As in the simplest Arkolakis, Costinot and Rodriguez-Clare model, they find equivalent welfare results across market structure assumptions when the trade response is held constant across the models. Their model, however, is not applied to data from an actual economy or economies; in particular, all sectors in their model have identical factor shares, both within and across countries. As discussed above, several papers have shown that the equivalence results found by Dixon, Jerie and Rimmer (2015) fail to generalize when more complex features of actual economies are brought into the model. The first CGE model of real economies consistent with the full Melitz structure is Balistreri, Hillberry and Rutherford (2011). In their multi-region model they find that the welfare gains from tariff reductions are several times larger than with an Armington trade model. Balistreri, Hillberry and Rutherford (2011), however, did not hold the trade response constant across the market structures. Recently other authors have adopted a computational setting for welfare analysis in advanced frameworks with heterogeneous firms. The paper by Caliendo, Feenstra, Romalis and Taylor (2015) is a good example. Their approach is in the tradition of solving models in percentage change (exact-hat algebra); as we discussed above in reference to the approach of Arkolakis et al. (2012), it first involves solving a system of independent, non-linear equations similar to modern CGE analysis.

3. Armington, Krugman and Melitz Model Structures

Consider a world economy with goods $i \in I$, regions $r \in R$, and factors $f \in F$. Now let us indicate the trade structures applied to each good using subsets of I: Armington goods are indexed by; $j \in J \subseteq I$; Krugman goods are indexed by $k \in K \subseteq I$; and Melitz goods are indexed by $m \in M \subseteq I$. Abstracting from the broader general equilibrium, let $Q_{i,r}$ be the total quantity demanded (absorption) of the composite good i (made up of domestic and imported varieties) in region r, and let Y_{ir} be the gross output of good i in region r. In the context of the monopolistic competition structures, output, Y_{ir} , is a composite input commodity used by firms with a simple increasing-returns technology. With total demand and supply of each good (or composite input) well specified we can focus on a description of the trade equilibria across structures.

3.1Armington Structure

Consider that the composite good, satisfying demand $Q_{i,r}$ is an optimal CES aggregate of domestically supplied and imported goods. This is typically indicated as the Armington aggregation. It is convenient to represent this aggregation using a dual unit cost function. The dual representation

simultaneously embeds the technology and optimization. Let P_{js} be the minimized unit cost (true price index) of composite commodity j available in region s, and let c_{jr} be the price of regionally differentiated goods sourced from r. The CES unit cost function is given by:

$$P_{js} = \left[\sum_{r} (\tau_{jrs} c_{jr})^{1-\sigma_j} \right]^{1/(1-\sigma_j)}.,$$

where τ_{jrs} is the iceberg trade-cost factor and σ_j is the elasticity of substitution. Demand for the domestic and each imported variety can be derived by applying Shephard's lemma to the unit cost function scaled up by the activity level given by Q_{js} . Summing across demand from all trade partners we have the market clearance condition for output of good j from region r:

$$Y_{jr} = \Sigma_s \tau_{jrs} Q_{j,s} \left(\frac{P_{js}}{\tau_{jrs} c_{jr}} \right)^{\sigma_j}.$$

This completes the Armington trade formulation. Gross output from region r is exhausted on demand from each bilateral link, and it is assumed that the aggregation of imports and domestic goods occurs via a CES activity.

3.2 Krugman Structure

Under the Krugman structure the aggregation is also CES, but it is assumed that the varieties are distinguished at the firm level. Each region r has a number of firms measured by mass N_{kr} producing commodity k. Let us denote p_{krs} as the, gross of trade and transport-cost, price charged in market s by each of the symmetric firms from region r. Firms are assumed to produce under an increasing returns technology with a fixed cost and constant marginal cost.

Similar to the Armington aggregation the dual function that embeds the technology and optimization is given by

$$P_{ks} = \left[\sum_{r} N_{kr} p_{krs}^{1-\sigma_k} \right]^{1/(1-\sigma_k)},$$

In this case we use Shephard's lemma to derive firm-level demand:

$$q_{krs} = Q_{ks} \left(\frac{P_{ks}}{p_{krs}} \right)^{\sigma_k}.$$

This demand function has a constant elasticity of σ_k . We assume that each firm is small in that, from the firm's perspective, the price index (P_{ks}) is not affected by the firm's decision on its own price P_{krs} .

Inclusive of iceberg transport costs the firm optimally prices in each market according to the standard optimal markup:

$$p_{krs} = \frac{\tau_{krs} c_{kr}}{1 - 1/\sigma_k}.$$

Under an assumption of free entry firm profits from each market (s) will just cover the cost of entry:

$$c_{kr}f_k = \sum_{s} \left[\frac{p_{krs}q_{krs}}{\sigma_k} \right].$$

The final equilibrium condition for the Krugman structure is market clearance for output of the composite-input commodity k in region r. Output of composite-input commodity k is used by each firm to cover fixed and variable cost (inclusive of iceberg trade costs). Considering the number of firms operating the market clearance condition is given by

$$Y_{kr} = N_{kr} \left(f_k + \Sigma_s \tau_{krs} q_{krs} \right).$$

3.3 Melitz Structure

The Melitz structure follows closely the Krugman structure, but because firms face a set of, ex post, different technologies (marginal costs) the equilibrium includes a number of extensions. These extensions are simplified by defining the equilibrium in terms of a representative firm (following Melitz, 2003). Consider the price index defined on the price of the representative firm:

$$P_{hs} = \left[\sum_{r} N_{hrs} \tilde{p}_{hrs}^{1-\sigma_h} \right]^{1/(1-\sigma_h)}.,$$

where the measure of the number of firms now tracks the number of firms operating on a given bilateral link. Just as in the Krugman model firm level demand is given by

$$\tilde{q}_{hrs} = Q_{hs} \left(\frac{P_s}{\tilde{p}_{rs}} \right)^{\sigma_h}$$
. Optimal pricing follows with the inclusion of φ_{hrs} as the measure of the

representative firm's productivity.

$$\tilde{p}_{hrs} = \frac{c_{hr}\tau_{hrs}}{\tilde{\varphi}_{hrs}(1-1/\sigma_h)}.$$

Under a Pareto distribution of productivity draws (with shape parameter a) we can represent the zero-cutoff-profits condition in terms of the representative firm:

$$c_{hr}f_{hrs} = \tilde{p}_{hrs}\tilde{q}_{hrs}\frac{(a+1-\sigma_h)}{a\sigma_h}.$$

This condition indicates that out of the mass of available firms (M_{hr}), those selecting into market s must earn non-negative profits. The marginal firm earns zero profits and we relate the revenues of the marginal

to the representative firm through the Pareto distribution. While operating firms earn profits, in expectation, free entry insures zero profits. A firm that enters can expect to earn the profits of the representative firm weighted by the probability of operating in that market (N_{hrs}/M_{hr}). These expected profits must cover the annualized sunk cost of entry. The free entry condition is thus given by

$$c_{hr}\delta f_{hrs} = \Sigma_s \left[\tilde{p}_{hrs}\tilde{q}_{hrs} \frac{(\sigma_h - 1)}{a\sigma_h} \frac{N_{hrs}}{M_{hr}} \right]$$

where δ is the probability that firm fails to survive into the next year. Next, we must determine the productivity of the representative firm. Under the Pareto distribution (with support b) and operating firms and entered firms determined by the zero-cutoff-profit and free-entry conditions the representative firm's productivity is given by

$$\tilde{\varphi}_{hrs} = b \left(\frac{a}{a+1-\sigma_h} \right)^{1/(\sigma_h-1)} \left(\frac{N_{hrs}}{M_{hr}} \right)^{-1/a}.$$

Finally, we have the market clearance condition for output of composite-input commodity h in region r

$$Y_{hr} = \delta f_{hrs} M_{hr} + \sum_{s} N_{hrs} \left(f_{hrs} + \frac{\tau_{hrs} q_{hrs}}{\tilde{\varphi}_{hrs}} \right).$$

Composite inputs are used to cover sunk, fixed-operating, and variable costs.

4. Gravity, Trade and FDI Responses and Calibration Strategy

4.1 Gravity-equation Estimation and Trade Responses

Our intent is to estimate trade responses directly from the GTAP 9 data using current structural-gravity techniques. We take parameters based on econometric estimates for the Melitz model and adjust elasticities in the Krugman and Armington model so that the trade response is the same.

To be precise, let λ_w indicate the share of global expenditures that are spent on goods that are produced in their respective home region:

$$\lambda_{W} \equiv \frac{\Sigma_{r} X_{rr}}{\Sigma_{r,s} X_{sr}},$$

where X_{sr} is the total value of country r's expenditures on goods from country s. If λ_W is the domestic trade share in the benchmark data and λ_W' is the domestic trade share in the in the counterfactual equilibrium, then $1-\lambda_W$ is the percentage change in the global trade share where $\hat{\lambda}_W$ is defined by:

$$\hat{\lambda}_{W} \equiv rac{\lambda_{W}^{'}}{\lambda_{W}}.$$

Note that in the special case of a movement to autarky, in the counterfactual, $\lambda_W = 1$. Then $\hat{\lambda}_W = \frac{1}{\lambda_W}$ and

the change in the trade response may be calculated from initial data and the trade elasticity without the need of a model. We adjust the Armington and Krugman elasticities to match the observed percentage increase in global trade intensity from the Melitz model. This gives us a fair comparison across structures where they are parameterized to generate an equivalent aggregate trade response.

The calculation of the trade response is nontrivial in a multi-sector model. Although the trade response is unique in a one sector model, and may be calibrated consistent with a unique trade elasticity from a gravity model, in a multi-sector model, there are trade responses in each sector. Further, depending on model assumptions, the trade elasticity may not be constant.⁶ In this paper, we hold the aggregate trade response constant across the Armington, Krugman and Melitz models, which means that trade responses at the sector level are not necessarily constant across the models.

For the Pareto distribution shape parameter in the Melitz model, we choose the value 4.58 from the structural estimation of Balistreri, Hillberry and Rutherford (2011). Arkolakis *et al.* (2012) have shown that in the one sector Melitz model, the Pareto shape parameter is equal to the trade elasticity; in particular, the trade elasticity is independent of the Dixit-Stiglitz demand elasticity. The Dixit-Stiglitz elasticity remains relevant, however, in models with realistic features as it affects the value to consumers of additional varieties. For the value of the Dixit-Stiglitz trade elasticity in the Melitz model, we take the value of 5.0 that Hillberry and Hummels (2014, p.1240) report as the median estimate from cross section and panel estimates.

For the Krugman model, we adjust the Dixit-Stiglitz elasticities of substitution so that the trade response is the same as in the Melitz model. The selection effect magnifies the trade response in the Melitz model, but this effect is absent in the Krugman model. To obtain the same trade response in the Krugman model as in the Melitz model, we must impose larger Dixit-Stiglitz elasticities. This means that the value of an additional variety will be greater in the Melitz model compared to the Krugman model. This will be important in interpreting our numerical results.

By similar reasoning, to hold the trade response constant, we find that we must choose the Armington elasticities of substitution to be larger than the Dixit-Stiglitz elasticities of the Melitz model. In the Melitz model, the value of 4.58 for the shape parameter and 5.0 for the Dixit-Stiglitz elasticities are

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⁶ Melitz and Redding (2015) showed that the "existence of a single constant trade elasticity and its sufficiency property for welfare are highly sensitive to small departures from those Arkolakis, Costinot and Rodriguez-Clare parameter restrictions."

invariant across the scenarios. In the case of the Armington and Krugman models, the Armington and Dixit-Stiglitz elasticities vary with the scenario, and those values are in the tables of results.

In an effort to keep the love of variety effect constant in the Krugman and Melitz models, one might consider the following alternate calibration strategy. We would start with the Krugman model and calibrate the Dixit-Stiglitz elasticities of substitution to be consistent with an estimate of the trade elasticity from a gravity model. Then we would attempt to impose those same Dixit-Stiglitz elasticities of substitution in the Melitz model so the love of variety effect is held constant. To hold the trade response in the Melitz model consistent with the gravity estimate, we would then attempt to adjust the Pareto shape parameter in the Melitz model to achieve a trade response in the Melitz model consistent with the trade elasticity from gravity. The problem we encountered with calibration strategy is that it required a value of the Pareto shape parameter very close to $\sigma-1$, where σ is the Dixit-Stiglitz elasticity of substitution. At $a=\sigma-1$ it is well known that the Melitz equilibrium is ill defined (as the productivity of the representative firm, and all the aggregates dependent on it, are unbounded). As a matter of computation, the Melitz models fail to solve reliability as the value of the Pareto shape parameter approaches $\sigma-1$ from above. The intuition for why this calibration strategy is not feasible is twofold. First the mathematical intuition. Costinot and Rodriguez-Clare (2014) have shown that the following relationship among these parameters holds:

$$\varepsilon = (\sigma - 1)(1 + \eta)$$
,

where ε is the trade elasticity from a gravity model, a is the shape parameter from the Pareto distribution and $\eta = \frac{a}{\sigma - 1} - 1$. Costinot and Rodriguez-Clare (2014, equation 14) show that when $\eta = 0$, there are no selection effects. If we insist on the same value of σ as in the Krugman model, we must have $\eta = 0$, which can occur iff $a = \sigma - 1$. For a solution to the Melitz model, however, we must have $a > \sigma - 1$. Otherwise the representative firm productivity, and all the aggregates dependent on it, are unbounded. Consequently, our algorithm for a solution to the Melitz model fails to converge as a approaches $\sigma - 1$ from above. The second explanation is that the Melitz model entails trade responsiveness from both entry and selection effects, whereas the Krugman model has only entry effects. If we calibrate the Melitz model to identical entry effects (by an identical σ), we will have to eliminate selection effects to attain the same trade response. Reducing the Pareto shape parameter allows us to get closer to the trade response from gravity, but calibration often encounters the problem of no solution to the Melitz model as a approaches $\sigma - 1$.

4.2 Gravity Equation Estimation of the FDI Response

Although Arkolakis *et al.* (2012) did not model foreign direct investment (FDI), the logic of their argument that the trade response should be based on a gravity estimate and be consistent across the model structures would suggest a similar argument with respect to FDI. That is, the logic would suggest that the change in FDI should be based on an empirical estimate of the responsiveness of investment to a change in the barriers and should be consistent across the three model structures. Consequently, we hold the FDI response constant across the three model structures.

We base the responsiveness of investment to barriers to investment on the work of Alesina *et al.* (2005), who employed data on regulatory barriers to investment for OECD countries. Due to data availability, they examine data in either 2 or 3 sectors: (i) electricity, gas, water; (ii) communications and post; and (iii) transport and storage. If separate data are unavailable, then communications, transport and storage aggregated. They estimate the investment-capital stock ratio as a function of the regulatory barriers, the lagged investment-capital ratio and various fixed effects. Their preferred model examines the impact of the sum of the barriers two periods lagged on the investment-capital ratio. In their preferred model, they estimate that a one unit reduction in their regulatory index results in an increase in the investment to capital stock ratio of 1.1 percentage points.⁷ That is, other things equal, they estimate that:

$$\Delta \left[\frac{I}{K} \right] = 1.1(\Delta b)$$

where 1.1 is the Alesina *et al.* estimate of the elasticity of the investment-capital stock ratio with respect to a change in the barriers, $\Delta \mathbf{b}$ is the change in their index of barriers (the index ranges from zero to six), I is the level of investment in each period with the status quo level of barriers, K is the capital stock. Since we are considering a change in barriers against FDI, we apply this estimate to foreign affiliate sales (FAS).

Since the capital stock changes much more slowly than investment, and the estimates are for a two-period lag only, we assume that the investment-capital stock ratio changes with respect to investment only. Then we have:

⁷ They take the example of Italy and say, assume its regulatory index falls from its value of 4.57 to that of the US, which is 0.8. The difference is 3.77. Then the model predicts that the investment to capital ratio of Italy would increase by 3.77 times 1.1 percentage points, or 4.15 percentage points, or from an investment-capital ratio in Italy of 6.8 to 10. 9.

Checking the model backwards, they note that the UK reduced its regulation index in the transport and communication sector from 3.75 (in 1975-1984) to .78 (in 1994-1998). The model predicts and increase in the investment-output ratio by (1.1)(3.75-.78) = 3.27 percentage points. Since the investment-output ratio was 4.96 percent in the earlier period, the model predicts that it would increase to 8.23 percent in the later period. The actual increase was 3.03 percent (from 4.96 percent to 7.99 percent).

$$\Delta \left\lceil \frac{I}{K} \right\rceil = \frac{I + \Delta I}{K} - \frac{I}{K} = \frac{\Delta I}{K} = 1.1(\Delta b)$$

where I changes to $I + \Delta I$ because of the change in barriers. Then $\Delta I = 1.1(\Delta b)K$

If the capital stock is governed by the perpetual inventory model, then, in the infinite horizon with a constant flow of investment per period, we have K = I/(1-d), where **d** is the depreciation rate. With an increase in investment, the new long run capital stock K' will increase to:

$$K + \Delta K = \mathbf{K}' = (\mathbf{I} + \Delta I) / (\mathbf{1} - \mathbf{d}) = \frac{I}{(1 - d)} + \frac{\Delta I}{1 - d} = K + \frac{1.1(\Delta b)K}{1 - d}$$

That is
$$\Delta K = 1.1(\Delta b)K/(1-d)$$
 and $\frac{\Delta K}{K} = 1.1(\Delta b)/(1-d)$

We assume these equations hold at the sector level and we assume a depreciation rate of 0.05. Our estimates of the of the ad valorem equivalents, AVE_i , of the FDI barriers range from 0 to 1, whereas the Alesina $et\ al.$ estimates range from 0 to 6. We define a transformation of our ad valorem equivalents in sector i into an index b_i consistent with Alesina $et\ al.$ (2005) as follows, $T:\ 6*AVE_i=b_i$. Given a change in the ad valorem equivalents of the barriers is a sector by some percentage, we calculate the change in the index of barriers from our transformation and use that change to calculate the change in the capital stock or the percentage change in the capital stock.

We adjust the shape parameter in the Melitz version of business services sectors such that the percentage change in the capital stock is consistent with this predicted percentage change in the capital stock of the multinational firms based on Alesina *et al.* (2005). In the Krugman and Armington models, we adjust the Dixit-Stiglitz and Armington elasticities to yield the same percentage change in the capital stock of the multinationals.

4.3 Intermediate Demand Structures

We consider three intermediate demand structures and examine the impact of market structure in the three: (i) Cobb-Douglas demand using the data on intermediate use in the input-output tables at the sector level; (ii) Leontief demand using the data on intermediate use in the input-output tables at the sector level; and (iii) Cobb-Douglas demand with an aggregate intermediate which assumes that all sectors use intermediates in the same proportions. Given that the structure is the same across regions, we suppress subscripts for the region in the equations of this section describing these intermediate use and demand structures.

4.3.1 Cobb-Douglas Demand with data on intermediate use.

Define:

 x_{ii} as expenditure by firm i on intermediate goods in sector j;

 $x_i = \sum_i x_{ij}$ as the total expenditure on intermediate goods in sector j;

$$\theta_{ij} = x_{ij} / \Sigma_i x_{ij} = x_{ij} / x_j$$

Total intermediate use is a Cobb-Douglas aggregate of intermediates uses in the sector.

$$Z_i = \prod_i x_{ii}^{\theta_{ij}}$$

When we model intermediates as Cobb-Douglas, we also assume the production function in sector i is Cobb-Douglas; then output in sector i is:

$$Q_i = K_i^{\alpha_i} L_i^{\beta_i} Z_i^{1-\alpha_i-\beta_i}$$

4.3.2 Cobb-Douglas Demand with an aggregate intermediate good.

Costinot and Rodriguez-Clare (2014) and Balistreri *et al.* (2011) employ a simplifying assumption regarding intermediate goods—they assume an aggregate intermediate good. Use of the aggregate good implies that, given an aggregate amount of intermediate purchases, factor proportions among intermediate goods are identical across sectors. For example, if autos and accounting services are two sectors in the model, the share of steel as an intermediate good is the same in the two sectors. To be more precise, define the following:

 x_{ih} as expenditure by household h on consumption goods in sector i;

 $A_j = \Sigma_h x_{jh} + \Sigma_i x_{ij}$ as the total expenditure on goods in sector i for both consumption and intermediate use;

 θ_i as the share of total expenditure on both intermediate and final goods that is spent on good i

$$\theta_i = A_i / \Sigma_i A_i$$

Z as a Cobb-Douglas aggregate good of all intermediate and final purchases:

$$Z = \prod_i x_i^{\theta_i}$$

In this model, all firms use only the single composite commodity as its intermediates. That is, in all sectors, output is a Cobb-Douglas aggregate of labor, capital and the composite commodity Z:

$$Q_i = K_i^{\alpha_i} L_i^{\beta_i} Z^{1-\alpha_i-\beta_i}$$

The production function in sector i varies with capital and labor used in sector i, but, unlike with real data on intermediates, intermediate demand is not indexed by sector. It means that all firms allocate expenditure on intermediates from different sectors in the same proportions, not different intermediates based on the proportions in which they use the intermediates based on the actual data. Further, in this model, utility of consumers is a function of the composite commodity Z (which includes intermediates), rather than the final goods alone. We investigate the impact of this simplifying assumption below.

4.3.3 Leontief Demand for Intermediates with actual data on intermediate use.

In this formulation, value-added is a CES aggregate of primary inputs:

$$VA_{j} = \left(\alpha_{j}K_{j}^{\rho} + \beta_{j}L_{j}^{\rho}\right)^{\frac{1}{\rho}} \qquad 0 < \rho < 1,$$

When we have Leontief demand for intermediates, we have that output is:

$$Q_{j} = \min \left[VA_{j}, \frac{X_{1j}}{a_{1j}}, ..., \frac{X_{nj}}{a_{nj}} \right]$$

where a_{ii} is the amount of input i needed to produce one unit of output j.

5. Computational Simulations

5.1 Model with One Sector, One Factor, No Intermediates and Balanced Trade

Our simulations begin in table 2 with a replication of the welfare calculations of Arkolakis, Costinot and Rodriguez-Clare (2012) in their simplest model, i.e., in a model with one-sector, one primary factor of production, no intermediate inputs, iceberg trade costs, balanced trade, no labor-leisure choice and untruncated Pareto probability distributions of productivity. The counterfactual shock that we consider is a global uniform reduction in variable trade costs of 10%. In column 2, we show the welfare impact using the exact-hat methodology of Arkolakis, Costinot and Rodriguez-Clare (2012). In columns 3-5, we present our CGE computations under each of the three market structures. Our CGE model calculations replicate the result of Arkolakis *et al.* (2012) that the alternative market structures generate identical welfare impacts. Further, the table shows that the welfare can be derived from a very simple calculation based only on the domestic expenditure share trade response and the trade elasticity. In this simple model, conditional on a consistent trade response across the models, the Armington, Krugman and Melitz models produce identical welfare estimates. These are precisely the points made by Arkolakis *et al.* (2012).

5.2 Trade Imbalances, Intermediate Goods and Multiple Sectors

In table 3, we sequentially introduce features important to real economies. In columns 1-3, we incorporate actual trade imbalances. Costinot and Rodriguez-Clare have identified multiple sectors and intermediates as the features that most strongly break the equivalence between market structures. Consequently, in columns 4-6, we add intermediates to trade imbalances; and in section 7-9, we add multiple sectors. In our Krugman and Melitz models in these scenarios, all the sectors are monopolistically competitive, and the demand for intermediates is Cobb-Douglas with shares based on data from the input-output tables. (We discuss the modeling of intermediates in the next section.)

5.2.1 Trade Imbalances. Note that the domestic expenditure shares λ_{rr} are different than in table 2, even in the context of the one-sector, one-factor model that does not include intermediates. This reflects the incorporation of the benchmark trade imbalance, so that we are considering a model consistent with the actual GTAP data. In all the subsequent simulations, we assume that the observed current-account imbalances are held fixed (in units of US consumption). Costinot and Rodriguez-Clare (2014) explain how the exact-hat welfare calculations need to be modified to incorporate benchmark trade imbalances and the ambiguity this creates in terms of setting up the counterfactual. In our case, the numeraire is chosen to be the aggregate price index in the US, and so we simply hold the value of each region's current account fixed in these units. In all subsequent scenarios in this paper, we incorporate the trade imbalance.

In columns 1-3, we find that, at the single decimal point, incorporating trade imbalances alone is insufficient to break the equivalence result regarding the welfare impacts in Armington, Krugman or Melitz. We see that for all ten regions, the welfare result is within ten percent of the welfare result in table 2, i.e., welfare results are usually close to those where trade is balanced.

5.2.2 Intermediates. The impact of adding intermediates in a single sector model are shown in columns 4-6 of table 2. In all regions of the model, there are larger welfare gains in Krugman over Armington; and Melitz provides larger gains relative to Krugman. The Krugman model provides larger gains than Armington due to variety gains that are induced from entry in the Krugman model. The Melitz model provides additional gains relative to Krugman in these simulations. Although this model departs in multiple ways from the model of Melitz and Redding (2015), since it contains intermediates, a trade imbalance and untruncated Pareto distributions, it is consistent with the conclusion of Melitz and Redding (2015). They state that the endogenous decisions of heterogeneous firms to enter and exit the market provide "an extra adjustment margin" that augments the gains from international trade compared to a Krugman style homogeneous firms model. It is also consistent with Costinot and Rodriguez-Clare (2014, p. 220) who find that the "gains from trade are slightly higher under monopolistic competition than perfect competition" and "the gains are even higher when we allow for firm level heterogeneity." As we mentioned above, given the selection effect in the Melitz model, calibration of the trade response in all the models to a common gravity estimate requires that the value of a variety is greater in the Melitz model, and this explains the larger gains from trade in the Melitz model.

5.2.3. Multiple Sectors with Intermediates. In columns 7-9, we present results with Cobb-Douglas demand for intermediates, using the full data on the input-output matrix (see section 4.3.1). Comparing columns 7 and 8, we see that adding additional sectors in the Krugman model results in larger estimated gains than the Armington model on average and for all regions, except for the low and middle-

income country aggregate regions. Again, reduction in trade costs results in more varieties available worldwide, which explains the increase in most regions in the Krugman model compared with the Armington model. With heterogeneous firms, the estimated welfare gains increase further, both on average and for seven of the ten regions, except for the low-income countries and to a much lesser extent the middle-income countries and Australia. The selection effects explain the larger welfare gains on average.

The most significant exception to this pattern is the region we call "Low Income (NEC)."

Comparing column 7 with columns 8 and 9, we see that the estimated welfare gains are lower in the Krugman model compared with Armington, and lower in the Melitz model compared Krugman. Key to the explanation is to note that our Low Income region follows the more general pattern in columns 4-6, where we introduce intermediates, but retain the single sector model. That is, with a single sector, the introduction of intermediates leads to larger gains in the Krugman model compared with Armington and larger gains in Melitz compare with Krugman. With an identical single sector in all regions, there are no terms of trade effects between regions. In the four-sector model, however, the results show an adverse terms of trade effect for the three regions in the model that most intensively produce agricultural products. The fact that not all regions follow the pattern of the average is consistent with the result of Costinot and Rodriguez-Clare (2014, table 4.3, columns 4-6), where three of their ten regions move in the opposite direction to the average in the Krugman versus Armington case and one moves in the opposite direction in the Melitz versus Krugman comparison.⁸

5.3 Impact of Alternate Structures for Intermediate Demand

In table 4, we assess the impact of three alternate structures of intermediate demand that we explained in section 4.3. In columns 1-3, we show the welfare results based on the assumption of Costinot and Rodriguez-Clare (2014) and Balistreri *et al.* (2011), i.e., there is a single aggregate intermediate good (see section 4.3.2). With this assumption, all sectors use intermediates in the same proportions, where the proportions are defined by the composite intermediate good. The aggregate intermediate may be used as both a consumption and intermediate input. In columns 4-6, we see the results based on the full information in the input-output accounts where we assume a Cobb-Douglas production function that combines intermediates and value-added inputs in the same nest (see section 4.3.1). These columns reproduce the results of table 3, columns 7-9. In columns 7-9, we display the results of the typical approach in CGE analysis discussed in section 4.3.3. In this approach, we use the full information in the input-output accounts with a Leontief production function. This approach does not allow substitution of intermediates in any sector with each other or with value-added.

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⁸ Balistreri and Olekseyuk (2017) found that Ukraine would gain less from its this result for Ukraine in analyzing the free trade agreement between the EU and Ukraine.

The results show that the intermediate structure can have a strong impact on the results. We see that the Leontief assumption reduces the estimated welfare gains in all cases. If we compare the results in column 4 to column 7; column 5 to column 8 or column 6 to column 9, we are holding other things equal except for either the Cobb-Douglas or Leontief intermediate structure. In all 30 of these cases, the Cobb-Douglas intermediate structure produces uniformly larger welfare gains than the Leontief structure. Given the Le Chatelier principle, this is an expected result.

A second result, is that the simplifying assumption of a single aggregate intermediate as opposed to real data on intermediates, can significantly impact the results. In the cases of four regions (Low Income, Middle Income, Australia-New Zealand and Canada) and either the Krugman or Melitz model, the estimated gains are much larger with the Cobb-Douglas formulation and real input output data than with the single aggregate intermediate (, i.e., column 5 is larger than column 2, and column 6 is larger than column 3). But the result is opposite for The Philippines, indicating that the impact of this intermediate structure is parameter dependent.

Regarding the impact of market structure, with Cobb-Douglas demand, either as a single aggregate intermediate or real data, we find that, for the average for the world, the ranking of the welfare gains is: Melitz larger than Krugman and Krugman larger than Armington. Although we have discussed exceptions, this ranking tends to be a consistent result in the presence of intermediates for reasons explained above. Leontief intermediate demand diminishes the impact of market structure so that, regarding the average for the world, there is no difference in the estimated welfare gains across market structures.

A fourth result from table 4 is that it provides concrete examples to the logical point that knowledge of the impact of a modeling assumption in the Armington model is insufficient to infer the impact of the same modeling assumption in the Krugman or Melitz models. Take the example of the simplifying assumption of a single aggregate Cobb-Douglas intermediate good. What is its impact versus a Cobb-Douglas intermediate demand function with full data from the input-output matrix? If we compare the welfare gains for the United States and especially China shown in columns 1 and 4, they are smaller with the real data. But if we compare columns 2 with 5 or columns 3 with 6, we see that under the Krugman or Melitz models, the welfare gains are larger with real data for China and the United States. When Costinot and Rodriguez-Clare (2014) investigate the impact of market structure in their model with ten regions and 16 sectors and also consider their more realistic comparative static exercises, they employ a series of simplifying assumptions. The simplifying assumptions include a single aggregate intermediate good without real data, uniform tariffs, zero trade balances, initial tariffs of zero, one primary factor of production, no specific factors and no FDI. They produce comparative results for the Armington, Krugman and Melitz models under these simplifying assumptions. Subsequently they assess the impact of

many of the simplifying assumptions in the Armington model, but not the Krugman or Melitz models. The subsequent evaluations of Costinot and Rodriguez-Clare are useful for understanding impacts in the Armington model. But the results in table 4 for China and the United States, provide examples that the impact of the simplifying assumptions could have an opposite impact in the Krugman or Melitz model. And crucially, despite showing the results for the ranking of the welfare results across the three market structures in a model with simplifying assumptions and the impact of the simplifying assumptions in the Armington model, the ranking of the welfare impacts across the three market structures has not been established for these more complicated models prior to this paper.

6. Conclusion

In this paper, we have produced new results for the relative welfare impacts of the Armington, Krugman and Melitz models for a range of modeling features that have not previously been examined in the literature. The calculations are empirically based on GTAP 9 data. Following Costinot and Rodriguez-Clare (2014), we hold the trade response constant across the three models consistent with gravity estimates of the trade response. For our model with foreign direct investment, we extend the logic of a constant trade response to FDI and these models are the first to hold the FDI response constant across the three models consistent with econometric estimates of the responsiveness of investment to a reduction in barriers to investment.

We first replicated the basic result of Arkolakis *et al.* (2012) of the welfare equivalence across the models in their highly stylized model. We then progressively added more features of the data and model realism including intermediate inputs, multiple sectors, trade imbalances, alternate intermediate structures, FDI and factors of production. All these features, except for trade imbalances, break the welfare equivalence of the market structures. We find that welfare analysis of integration is highly dependent on the assumed market structure, even while maintaining consistent trade responses across the structures.

The innovation relative to Costinot and Rodriguez-Clare (2014) and Arkolakis *et al.* (2012) is the following. We can extend the literature on what is known about the relative impacts of Melitz, Krugman or Armington in several ways that have not yet been established. This includes our new results on: intermediates with factor proportions that depend on real data on sector differences; the impact of different intermediate demand structures; unbalanced trade; heterogeneous tariffs; foreign direct investment; specific factors; and comparative static exercises with tariffs that are neither autarky exercises nor start from zero tariffs. We noted that the parsimonious two sufficient statistics methodology for welfare calculations of Arkolakis et al. (2012) and Costinot and Rodriguez-Clare (2014), explodes to a

system of several thousand non-linear independent equations when realistic features are introduced; and to date, the exact hat literature has not produced a solution to the Krugman or Melitz models that incorporates realistic features of economies. Further, our general equilibrium model in levels (rather than changes) and which uses the Hicksian equivalent variation measure, fully captures the benchmark and counterfactual social accounts. In this way, all the data from the benchmark accounts can be used, and results important to policy-makers such as output changes by sector and relative factor prices can be easily extracted.

We find that, relative to the widely used Armington structure, although there are exceptions, the Krugman and Melitz structures generally indicate higher gains from integration. This is especially true with the introduction of intermediate goods. A further explanation for why the Melitz structure tends to generate greater gains than the Krugman structure is that there is a selection effect in the Melitz model, controlled by the Pareto shape parameter. That is, under the Melitz structure, the trade response controlled through the Pareto shape parameter (indicating the degree of firm-level heterogeneity and the elasticity of substitution between firm-level goods), and the Dixit-Stiglitz elasticity of substitution is a free parameter based on econometric estimates. In contrast in the Krugman model there is only one parameter (the elasticity of substitution between firm-level goods) to calibrate the trade response consistent with gravity. To match the trade responses generated from the Melitz structure the elasticity of substitution in the Krugman model must be set at a level that generates a smaller love-of-variety effect. This explains a tendency for the Melitz model to produce larger welfare impacts.

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Table 1: Literature Results on the Ranking of Welfare Gains in the Armington,

Krugman and Melitz Models

	Ranking of							
	Welfare Gains							
Model Assumptions	Key: A = Armin	gton; K =	Krugman	; M = Mel	itz ²			
One Sector, No Intermediates, One Factor, Zero Trade Balance, Iceberg Trade costs	A=K=M	A=K=M Arkolakis, Costinot and Rodriguez-Clare (20						
with Labor-Leisure choice and positive elasticity of labor supply 1	M>A	Balistreri, I	Hillberry and	Rutherford	(2010)			
with upper bound on the Pareto Probablity Distribution of Productivity	M>K	Melitz and	Redding (20	015)				
Autarky Excercises, 33 Regions, 31 Sectors with One Primaty Factor, Zero Trade B	alance, Iceberg Tra	de Costs (r	umerical re	esults)				
Muliple sectors	M=K≠A	Costinot an	d Rodriguez	-Clare (201	4, 214-215)			
One aggregate intermediate good	M>K>A	Costinot and Rodriguez-Clare (2014, 219-220)						
Comparative Static Exercises: Losses from imposing a Uniform Tariff in Ten Regio	 n, Sixteen Sector M	odel (nume	rical results)				
Assumptions: Zero Tariffs, Zero Trade Balances, one Primary Factor of Production								
(ranking based on absolute value of losses)								
Multiple sectors	K>A; K>M	Costinot an	d Rodriguez	-Clare (201	4, 231-233)			
One aggregate intermediate good M>K>A Costinot and Rodriguez-Clare (2014, 231-233								
^{1.} If the elasticity of labor supply to the traded goods sector is negative (zero), the estimate welfare gain under Melitz is less than (equal to) Armington.								
2 M > K (M = K) if and only if the Melitz model produces greater (equal) welfare gains than H	Krugman.							

Table 2: Equivalence of Welfare Results Across Market Structures in the Simplest One Sector Model.***

Impacts of Ten Percent Reduction in Iceberg Trade Costs

Results are Hicksian Equivalent Variation as a Percent of Consumption

	1	2	3	4	5
	domestic trade	"Exact Hat"	CGE	Model Calcul	ations
	share	Calculations**	Armington	Krugman	Melitz
Region	λ_{rr}	ε = 4.58*	$\sigma(D,M) = 5.58*$	σ = 5.58*	σ=5.0; a=4.58*
Australia-New Zealand	77.2%	3.0%	3.0%	3.0%	3.0%
Canada	70.1%	4.1%	4.1%	4.1%	4.1%
China	72.1%	3.7%	3.7%	3.7%	3.7%
Japan	83.0%	2.1%	2.1%	2.1%	2.1%
Mexico-Chile-Peru	67.0%	4.6%	4.6%	4.6%	4.6%
Low Income NEC	55.5%	6.4%	6.4%	6.4%	6.4%
Middle Income NEC	75.6%	3.2%	3.2%	3.2%	3.2%
OECD NEC	81.4%	2.3%	2.3%	2.3%	2.3%
Philippines	62.9%	5.1%	5.1%	5.1%	5.1%
United States	84.6%	1.9%	1.9%	1.9%	1.9%
average for the World	79.0%		2.7%	2.7%	2.7%

^{*} ϵ is the trade elasticity from gravity; $\sigma(D, M) = 5.58$ is the Armington elasticity of substitution between imports and domestic goods; $\sigma = 5.58$ is the Dixit-Stiglitz elasticity of substitution between varieties in a sector; and "a" is the shape parameter in the Pareto distribution.

Source: Authors' calculations

^{**}Exact hat calculation in this simple model is $\lambda_{jj}^{1/\varepsilon}$.

^{***}Model with One Sector, One Factor, No Intermediates, Zero Trade Balance, Untruncated Pareto distribution of productivity.

Table 3: Impact of Incorporating Trade Imbalances, Intermediates and Multiple Sectors (with a single primary factor)

Impact of Ten Percent Reduction in Iceberg Trade Costs

Results are Hicksian Equivalent Variation as a Percent of Consumption

				All scenari	All scenarios incorporate trade imbalances						
		1	2	3	4	5	6	7	8	9	
	domestic trade	Single Sec	tor-No Inte	rmediates	Single Sect	Single Sector-With Intermediates			s-With Inte	rmediates**	domestic trade
	share with	Armington	Krugman	Melitz	Armington	Krugman	Melitz	Armington	Krugman	Melitz	share with
Region	no intermediates	σ(D,M) = 5.58*	σ = 5.58*	σ=5.0; a=4.58*	σ(D,M) = 5.58*	$\sigma = 5.58*$	σ=5.0; a=4.58*	σ(D,M) = 6.13*	$\sigma = 5.65*$	σ=5.0; a=4.58*	intermedjates
Australia-New Zealand	77.2%	3.1%	3.1%	3.1%	3.2%	4.2%	4.4%	3.6%	3.7%	3.7%	89.3%
Canada	70.1%	4.1%	4.1%	4.1%	4.1%	5.1%	5.3%	4.2%	6.3%	6.9%	84.4%
China	72.1%	4.0%	4.0%	4.0%	3.9%	6.7%	7.5%	3.5%	9.7%	12.5%	91.1%
Japan	83.0%	2.1%	2.1%	2.1%	2.3%	2.9%	3.1%	2.1%	4.3%	4.9%	91.6%
Mexico-Chile-Peru	67.0%	4.8%	4.8%	4.8%	4.7%	5.9%	6.1%	4.9%	6.4%	6.8%	82.9%
Low Income NEC	55.5%	5.8%	5.8%	5.8%	5.7%	7.4%	7.7%	6.5%	5.8%	5.5%	76.9%
Middle Income NEC	75.6%	3.3%	3.3%	3.3%	3.4%	4.4%	4.6%	3.7%	3.7%	3.6%	88.3%
OECD NEC	81.4%	2.3%	2.3%	2.3%	2.4%	3.2%	3.4%	2.3%	3.8%	4.2%	91.4%
Philippines	62.9%	4.6%	4.6%	4.6%	4.7%	5.9%	6.1%	4.8%	7.2%	7.8%	79.2%
United States	84.6%	1.7%	1.7%	1.7%	1.9%	2.3%	2.4%	1.9%	2.8%	3.0%	90.6%
average for the World	79.0%	2.7%	2.7%	2.7%	2.8%	3.8%	4.0%	2.8%	4.3%	4.8%	90.0%

^{*} σ(D,M) is the Armington elasticity of substitution between imports and domestic goods; σ is the Dixit-Stiglitz elasticity of substitution between varieties in a sector; and "a" is the shape parameter in the Pareto distribution.

Source: Authors' calculations.

Table 4: Impact of Intermediate Modeling Structure: (1) Single Composite Intermediate; (2) Cobb-Douglas Demand; or (3) Leontief Demand**

Impact of Ten Percent Reduction in Iceberg Trade Costs

Results are Hicksian Equivalent Variation as a Percent of Consumption

All scenarios with four sectors and trade imbalances incorporate

			All scenarios with four sectors and trade imbalances incorporated; but single primary factor								
			1	2	3	4	5	6	7	8	9
		domestic trade	Single Com	nposite Intermediate (Cobb-Douglas Demand for Intermediates (real data)			Leontief Demand for Intermediates		
		share	Armington	Krugman	Melitz	Armington	Krugman	Melitz	Armington	Krugman	Melitz
Region		λ_{rr}	$\sigma(D,M) = 5.80*$	$\sigma = 5.51*$	σ=5.0; a=4.58*	$\sigma(D,M) = 6.2*$	$\sigma = 5.61*$	σ=5.0; a=4.58*	$\sigma(D,M) = 5.9*$	$\sigma = 5.54*$	σ=5.0; a=4.58*
Australia-New Zeal		89.3%	2.7%	2.0%	2.0%	3.6%	3.7%	3.7%	3.6%	2.7%	2.6%
Canada		84.4%	4.2%	5.2%	5.5%	4.2%	6.3%	6.9%	4.2%	4.2%	4.2%
China		91.1%	4.4%	9.3%	10.7%	3.5%	9.7%	12.5%	3.4%	4.4%	4.6%
Japan		91.6%	3.0%	4.6%	4.9%	2.1%	4.3%	4.9%	2.0%	2.6%	2.7%
Mexico-Chil	Mexico-Chile-Peru		4.5%	5.9%	6.2%	4.9%	6.4%	6.8%	4.8%	4.7%	4.7%
Low Income NEC		76.9%	5.1%	2.8%	2.7%	6.5%	5.8%	5.5%	6.5%	4.4%	4.1%
Middle Income NEC		88.3%	2.5%	2.0%	2.0%	3.7%	3.7%	3.6%	3.6%	2.7%	2.6%
OECD NEC		91.4%	2.6%	3.8%	4.1%	2.3%	3.8%	4.2%	2.2%	2.5%	2.5%
Philippines		79.2%	5.4%	8.0%	8.5%	4.8%	7.2%	7.8%	4.7%	5.0%	5.0%
United State	United States		2.0%	2.6%	2.7%	1.9%	2.8%	3.0%	1.9%	1.9%	1.9%
average for	the World	90.0%	2.9%	4.1%	4.4%	2.8%	4.3%	4.8%	2.7%	2.7%	2.7%

^{*} σ(D,M) is the Armington elasticity of substitution between imports and domestic goods; σ is the Dixit-Stiglitz elasticity of substitution between varieties in a sector; and "a" is the shape parameter in the Pareto distribution.

Source: Authors' calculations.

^{**}Demand for intermediates is Cobb-Douglas with shares at the sector level determined data in the input-output matrices; see section 4.3.1.

^{**}For details of intermediate modeling, see section 4.3.