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WHAT MAKES THE PRICE OF OATS 1

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STATEMENT OF THE PROBLEM

The market price of oats, like the prices of all other farm products, changes from year to year, season to season, month to month, and day to day. It is commonly recognized that these price changes are caused by changes in supply or demand, or both; but the general phrase "supply and demand" furnishes no precise explanation of given variations in price. A detailed study is necessary to define the supply, allocate the demand, and furnish quantitative measures of the influence of the various price-making forces.

In recent years the application of statistical methods to economic problems has had remarkable development. Most of this development, however, in so far as it has been applied to forecasting the future, has been in the field of business statistics, and the problem of forecasting the prices of the various agricultural products has been comparatively neglected. The value of any method which would offer to the farmer or to the student of agricultural prices even an approximate means of estimating future prices is evident. To the farmer, its most important use would be in determining the best time to sell his

¹ E. M. Daggit, Associate Agricultural Economist, gave valuable assistance in the preparation of this bulletin.

crop, and in settling his age-old problem of whether to store or not to store. Good business management on the part of the present-day farmer requires, in addition to a knowledge of the best methods of production, as thorough an understanding as possible of the forces which determine the prices of his product; low profits may result as well from poor judgment in selling as from poor judgment in growing the crop.

It may be objected that the average farmer can not make use of scientific price studies because of their unavoidable technicality; but the development in recent years of trained intermediaries in the dissemination of market and other information among farmers and the growing up of a more scientific-minded farming class have brought to them more and more of the benefits of scientific studies of all kinds.

To the student of agricultural prices any thorough price study brings to light new methods of attacking the problem and new uses of old methods. It helps to point out the strength and weakness of the various statistical methods, to the end that their fields of usefulness may be more clearly defined for those who continue the work. For this purpose the mention of trials which have been found to give no

worth-while results should be of considerable value.

In any price analysis it is first necessary to determine the area of the market, for upon that depends in large measure the selection of methods that may be used. The difference in the scope of the market for wheat and oats, for example, makes a great difference in the characteristics of demand and supply for the two crops. Upon the area of the market and the characteristics of production depend the answer to the question as to whether, for the given crop, one may assume that there is a normal annual price—an average price at which the annual supply will be moved from the market. It is difficult to assume a normal annual price in the case of wheat, because of the influence of foreign production. On the other hand, such an annual price may be assumed for a crop which is grown and consumed almost entirely within the country for which the study is made and of which there is a a single annual supply which becomes available for the market within a short period of the year.

The oat crop of the United States is found to come within this classification. Normally the supply of oats in this country is produced and mostly consumed within the borders of the Nation. From 1909 to 1913, and since the war, our exports have averaged not more than 2 per cent of the crop and our imports have been still less. During the war, however, the demand for oats was abnormal and a considerable quantity was exported, causing a temporary widening

of the market.

Having decided that oats is a crop that may be treated in a price analysis by assuming a normal annual price, the problem is to discover the factors which determine this annual price and to measure their influence. This requires the bringing together of such factors as may be expected to influence the price of oats, the study of each by the application of various statistical methods, and the selection of those which are found to have a measurable influence for use in developing an estimating formula, by means of which the most probable average annual price may be estimated from given values of the selected factors.

Obtaining a method for estimating the annual price, however, is but one important step in the price analysis. The problem remains of explaining the variations in price during the year, in order that by using the annual price as a basis one may calculate the probable seasonal movement. It is this seasonal movement of prices, rather than the average annual price, which is of great importance to the farmer who has oats to sell. The statistical methods used in this part of the study differ from those used in the earlier part, and on

the whole the analysis offers greater difficulty.

The most difficult part of the crop year for those attempting to forecast prices is during the growing season. Once the supply is fairly well known the principal factor to be considered by the forecaster is changes in demand; but during the growing season not only demand, but supply as well, must be estimated. The problem is to discover some indicator of the volume of production which anticipates the harvest. Two of these, the price of September futures and the monthly condition of the crop as reported by the United States Department of Agriculture, are available. These must be compared by the use of statistical methods as to their relative accuracy in predicting the future prices, and the variations in accuracy as the

growing season progresses must be measured.

Finally, to make this study of greater value to those who may continue the work of analyzing grain prices, it has been thought advisable to apply to wheat some of the methods used in the analysis of oat prices, to emphasize the difference in the method of treatment necessary for this crop. The market for oats is a domestic market, and the price is determined very largely by the domestic supply. The demand for wheat, on the other hand, is a world demand, the supply a world supply. The price is determined in the world market and is affected comparatively little by the size of the crop of the United States, as is shown in this study. The application of the theory of an average annual price resulting from an annual supply is more difficult.

SOURCES OF DATA AND SCOPE OF ANALYSIS

The data on oat prices used in this study were obtained from the annual reports of the Chicago Board of Trade. The weekly high and low prices for No. 2 oats at Chicago were averaged to give monthly prices, and the monthly prices thus obtained were averaged for the crop years July to June, to obtain the yearly figures. In the study of the relation between cash and future prices a more accurate series was needed. For this purpose monthly cash and future prices were obtained by averaging the daily high and low prices.

Data on production were obtained, for the most part, from the Yearbooks of the United States Department of Agriculture. No figures were available regarding the world carry-over of wheat, so these were calculated for the period 1891 to 1923 from data obtained

from various sources, as explained in the Appendix.

The wheat prices were obtained from the annual reports of the Chicago Board of Trade. The monthly figures are averages of daily high and low prices. Owing to the changes in grades from time to time, there was some difficulty in getting comparable grades for the entire period. Those used were: July, 1890, to January, 1897, No. 2

Spring wheat; January, 1897, to January, 1898, No. 2 wheat; January, 1898, to March, 1903, regular No. 2; March, 1903, to

June, 1922, No. 2 Red wheat.

That the Chicago price is representative of prices for the United States as a whole is shown by the fact that correlation coefficients of +0.98 for oats and of +0.99 for wheat are obtained when Chicago prices are correlated with the December farm prices as estimated by the Department of Agriculture.

The period covered in the major part of the study is that from 1896 to 1922, omitting the years 1916, 1917, 1918, 1919, and 1920. The omission of these years was considered necessary for accurate results, since the abnormal conditions of demand and abnormal changes in the price level during this period would tend to obscure the effect of forces that under normal conditions would be operative in the oats market.

An examination of exports of oats during the war period as compared with years before and after the war will show the extent to which the export demand was abnormal during the period omitted in this study.

Table 1.—Exports of oats from the United States, years ending June 30 1

Year	Quantity
Av. 1910-1914 Av. 1915-1919 1920 1921	Bushels 8, 304, 000 96, 774, 000 53, 945, 000 4, 302, 000

¹ U. S. Dept. Agr., Yearbook, 1921, p. 74.

FACTORS AFFECTING ANNUAL PRICE OF OATS

PRODUCTION AND THE AREA OF THE OAT MARKET

A study of the production of oats in the United States shows that for 30 years or more preceding the World War the trend of production has been steadily upward, reaching its peak in 1917 with a production of 1,593 million bushels. Since 1917 the production has slightly declined, the 1923 figure being 1,300 million bushels. tically all of the oats produced in this country are consumed here. In the pre-war period, 1909 to 1913, the exports of oats from the United States averaged not quite 1 per cent of the crop, and imports were less.2 During the war an abnormal foreign demand increased our exports, but since the war they have returned to their former low figures.

Figure 1 represents graphically the production of oats during the period 1881-1922. Superimposed upon the graph of production is a straight line representing the trend of production during that

period.3

These figures regarding production, imports, and exports indicate at once that in spite of the enormous production of oats in this country the market area is limited to the United States, a fact which is of considerable importance in the selection of methods for the study of prices.

² U. S. Dept. Agr., Yearbook, 1921, p. 781, 551. ³ The method of calculating this trend is explained in Table I, Appendix A, p. 27.

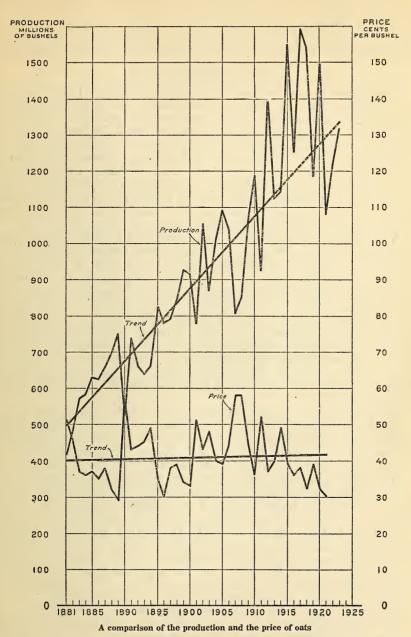


Fig. 1.—Although the production of oats has shown a downward tendency since 1917, the general trend since 1881 has been decidedly upward. The price of oats, corrected for changes in the general level of prices, has shown a slight upward trend for the period 1881–1922, though in recent years the tendency has been downward, in spite of the decrease in production. During most of the period the price was above the trend when production was below, and vice versa

Incidentally, an understanding of the size of the market is of considerable importance to farmers who are considering the shifting of acreage between wheat and oats, for a change in production which would cause a relatively small change in wheat prices might cause a great change in the price of oats, because oats are sold in a narrower market.

TREND OF PRICES OF OATS

The trend of oat prices for the period 1881 to 1922 has been less uniform than the trend of production. It tended downward from 1881 until the low point was reached during the nineties. After 1896 the trend was gradually upward until the close of the war period. The lack of uniformity in the trend of prices makes it impossible of representation by a straight line. There are actually two trends, one downward until 1896 and the other an irregular trend from 1896 to the present year in a general upward direction. methods of representing this trend are illustrated in Figure 2. One is the use of two straight lines to show the downward and upward

trends; the other is the use of a third degree parabola curve.

A comparative examination of the graphs of production and price in Figure 1, where the prices have been corrected for changes in the price level, shows that during the period from 1881 to 1913 prices were usually below the normal, represented by the trend line, when production was above, and above when production was below. fact, during much of the period one curve seems almost the exact opposite of the other, if allowance is made for the difference in trends. The closeness of the relationship as indicated by the two graphs shows clearly that the size of the oat crop in the United States has an important influence upon the year-to-year changes in price. Prices used in these two graphs are averages for crop years, September to August, instead of July to June, as used in the rest of the bulletin.

Graphs like these, useful as they are in showing the nature of the relationship between two factors, furnish no measure of the closeness of that relationship, nor do they provide a method of estimating one when the other is known. To obtain these two results it is

necessary to make use of the statistical device of correlation.4

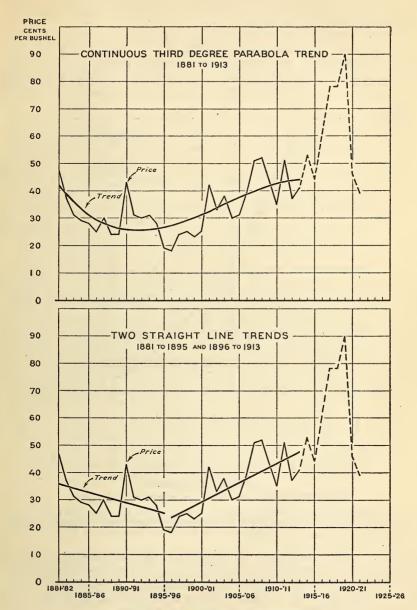
The relation between these two factors, when the ratio of production to the trend of production is correlated with the ratio of price to the trend of price, is expressed by a correlation coefficient of -0.82. The negative sign indicates that a change in one factor is accompanied by a change in the opposite direction in the other; and the size of the coefficient measures both the extent to which changes in one factor are associated with changes in the other and the accuracy with which values of one factor may be predicted from known values of the other during the period covered by the study, assuming that perfect correlation is represented by the coefficient ± 1.00 . Not the actual value of the coefficient, however, but the square

of the value represents the proportion of the change in price that is

accounted for by the change in the other variable.

A coefficient of correlation, squared, measures between X and Y the proportion of variation in Y that can be accounted for by variations in X, provided one is defining variability as the standard

⁴ The method of obtaining the coefficient of correlation is explained in Appendix A, Table II. p. 28.



Two methods of representing the trend of oat prices

Fig. 2.—It is impossible to represent the trend of actual oat prices by a single straight line. The trend of the price of oats was downward from the Civil War period until 1896, and upward from 1896 to 1919. A parabola and two straight lines are used in this figure to represent the trend of oat prices from 1881 to 1913

deviation squared. Ratios to trends are used here as a method of eliminating the influence of the upward tendency of production and the downward and upward trends of price which would partially obscure the relationship between the two factors and result in a lower coefficient of correlation.

To predict the average annual price of oats when the production is known, an "estimating equation" must be worked out from the results obtained in the correlation. This equation has the form y=a+bx, in which y is the price to be estimated, x is the production during the given year, and a and b are constant terms that must be

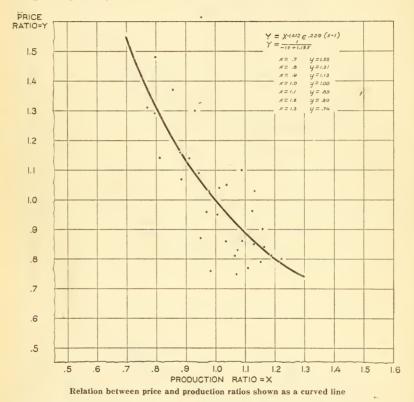


Fig. 3.—A curved line describes the relation between price and production better than does a straight line. If the relation were perfect, all of the dots in the scatter diagram would fall exactly on the line. The curve in this figure is described by two formulae, a reciprocal formula used by Working coinciding with an exponential formula used by Moore

calculated from the data. A coefficient of 0.82, however, is not large enough to give sufficiently accurate results in forecasting prices. Other factors must be considered in addition to production, so that more of the variation in price will be accounted for than that due to production alone.

The equation just given assumes that the relation between the two factors is expressed graphically by a straight line; that is, that regardless of the size of the factors, a given change in one is always associated with the same estimated change in the other. Consideration of the theory of elasticity of demand and the concept of diminishing utility suggests that a straight line may not represent most

accurately the relation between production and price, but that better results might be obtained through the use of curvilinear functions such as those employed by Moore ⁵ and Working. ⁶ A curvilinear relation suggests, that, for example, the addition of 50 million bushels of oats to a 1,400 million bushel crop may lower the price per bushel less than the addition of the same amount to a crop of only 800 million bushels.

In Figure 3 curves of the type referred to are fitted to the scatter diagram of production ratio and price ratio of oats. A curve of the

type used by Working described by the equation $Y = \frac{1}{-.19 + 1.19X}$

coincides approximately with a curve of the type used by Moore described by the equation $Y = X^{-1.412} \epsilon^{.229(x-1)}$ where Y and X are price ratio and production ratio, respectively, and ϵ is a constant. A curve described by either formula fits the data somewhat more closely than a straight line; that is, the sum of the squares of the deviations or residuals from the curves is less than the sum of the squares of the deviations from a best fitting straight line fitted by the method of least squares. Several other curves were tried and found not to fit the data as well as those illustrated.

COMPARISON OF THE VALUES OF LARGE AND OF SMALL CROPS

The fact that the relation between production and price is found to be represented by a curved line of the type illustrated in Figure 3 suggests an interesting problem regarding the values of oat crops of various sizes. It is commonly said that a large crop may often be worth less than a small crop. This idea is borne out by a study of Figure 3. Here it is found that a decrease of 10 per cent from normal, from 1.0 on the scale to 0.9, is accompanied by an increase of 13 per cent in price, whereas an increase of 10 per cent above normal is accompanied by a decrease of 11 per cent in price. The values of production multiplied by price in both cases are illustrated in Table 2.

Table 2.—Product of price multiplied by production when production is below and when production is above normal

t	Produc- tion in erms of normal	Corresponding price in terms of normal	Product of pro- duction and price
	0. 90	1. 13	1. 017
	1. 10	. 89	. 979

These conclusions may be applied to actual data by comparing the values of the large crops of 1902, 1904, 1905, and 1906, with the values of the small crops of 1901, 1903, 1907, and 1908. Table 3

⁵ H. L. Moore. Elasticity of demand and flexibility of prices. In Jour. Amer. Statis. Assoc., March,

Holbrook Working. Factors determining the price of potatoes in St. Paul and Minneapolis. Minn. Agr. Exp. Sta. Tech. Bul. 10. 1922.
 The value of ε, the base of the Naperian system of logarithms, is 2.7182818. The common logarithm

of ϵ is 0.343. The common logarithm of ϵ is 0.3435. The common logarithm of ϵ is 0.3436. The common logarithm of ϵ is 0.3436.

shows that, after the prices were adjusted for changes in the general price level, the total value of the four large crops was \$69,000,000 less than the total value of the four small crops.

Table 3.—Value product of oats for large and small crop years

La	arge crop y	ears		Small crop years				
Year	Production, United States	Price adjusted for changes in price level ¹	Value of product	Year	Production, United States	Price adjusted for changes in price level ¹	Value of product	
1902	Million bushels 1, 053 1, 009 1, 090 1, 036	Cents per bushel 27 27 27 24 25	Million dollars 284 272 262 259	1901 1903 1907 1908 Total	Million bushels 778 869 805 851	Cents per bushel 36 30 35 38	Million dollars 280 261 282 323 1,146	

¹ Price divided by the Bureau of Labor Statistics index number of all commodities, base 1890-1899, converted to the crop year by averaging monthly relatives, July to June. See Wholesale Prices 1890 to 1913. U.S. Bur. Labor Statis. Bul. 149, 1914.

APPLICATION TO A COOPERATIVE MARKETING PROBLEM

The foregoing study suggests a possible method of stabilizing oat prices. For 50 years farmers' organizations in the United States have tried in a variety of ways, ranging from prohibition of future trading to monopoly control, to reduce the fluctuations in the prices of farm products. At the present time two of the chief purposes of the American Farm Bureau Federation are (1) to extend the cooperative marketing of farm products, and (2) so to estimate the effective world supply of any farm product and so to regulate the flow to market as to eliminate sharp and extreme price fluctuations.

During the period 1881 to 1913 the oat crops of the United States were above the trend of production 11 times, below the trend 14 times, and about normal 6 times. There was no regularity in the sequence of large and small crops. Under the existing marketing system limited quantities of oats are carried from one crop year to the next. Carry-over figures 9 show that quantities consumed annually from 1896 to 1913 closely followed production and were not uniform from year to year. The question arises as to what would be the effect upon the gross value of oats if the surpluses from bounteous years were carried over to years in which the crop was small.

The gross value of the oats consumed in the United States from 1895 to 1913, on the basis of the December 1 farm price, was \$5,964,-000,000.10 Assuming that price would have followed the trend of prices, 1895 to 1913, had the supply of oats put on the market been made to conform to the trend of production or consumption by carrying surpluses from years of overproduction to years of relative shortage, the most probable value of these crops is \$6,135,000,000. The difference, or gain to the producers, is \$171,000,000, or approximately 9 cents a bushel for the carry over from surplus years.

Using estimates for the period 1881 to 1913 and Chicago prices gave similar results. Of course, these findings are not conclusive, because at best they are estimates and because considerations such as local prices, differences due to grades, and cost of storage have not been taken into account. However, they do suggest that there is an economic basis for efforts to distribute the supply in a more orderly manner.

MULTIPLE CORRELATION OF PRICE FACTORS

Since a correlation high enough to furnish an accurate basis for forecasting prices can not be obtained by using production alone, it will be necessary to look for other factors that have an influence upon the price of oats and to measure their influence. Those factors which may be expected to have some effect include: (1) Changes in the general price level; (2) the year-to-year carry over of oats; (3) substitute crops, such as corn; and (4) production of oats in Canada.

The effects of long-time changes in the general price level were taken account of to some extent in the first correlation by eliminating the long-time price trends. This is not an accurate method for the trend corresponds only roughly with the actual year-to-year changes in the price level. By the use of multiple correlation the general price level may be treated as a separate factor or variable, along with production and price. The annual carry over of oats, which is, in effect, merely an addition to the annual production, may be taken

care of by adding it to the production for each year.

A multiple correlation 11 using (1) the percentage change in the price per bushel over the price of the previous year, (2) the percentage change in the index number 12 and (3) the percentage change in the United States production of oats plus carry over 13 gave a coefficient The inclusion of two additional factors has thus raised the coefficient by four points. The significance of a coefficient of multiple correlation differs somewhat from that of a coefficient of simple correlation. It indicates the closeness of the relation between the dependent variable and the independent variables, but not the nature of the relationship, as does the coefficient of simple correlation. Accordingly, it is not accompanied by a positive or negative sign.

Additional correlations, using the other factors mentioned, show that corn added as a fourth variable does not increase the coefficient of correlation. This may be partly owing to the fact that the corn crop tends to be small when the oat crop is small and large when the oat crop is large. Using the index number of all commodities of the Bureau of Labor Statistics in place of the index number of farm products gives a correlation that is still 0.86. Adding Canadian production to the above, as a fourth variable, does not raise the coefficient. The period covered in each of the correlations was 1896 to 1922, with the omission of the crop years 1916, 1917, 1918, 1919, and 1920.

¹¹ The method of working out a correlation of three variables is explained in Table IV, Appendix A, p. 31.

12 The index of farm products of the United States Bureau of Labor Statistics converted to the crop year, July to June, by averaging the monthly index numbers back to 1913. Previous to 1913 the annual index numbers for two calendar years were averaged to give an index number for the crop year.

13 Carry over includes old stocks of oats on farms August 1, 1895 to 1923, obtained from the publication Weather Crops and Markets, United States Department of Agriculture, August 11 and 18, 1923, and the visible supply of oats on August 1, as reported by the Yearbooks of the United States Department of Agriculture.

An estimating equation may now be calculated from the data which gives the highest correlation with price. The equation is $x_1=4.20+2.03$ $x_2-1.16$ x_3 . Here x_1 is the percentage change in price per bushel over that of the previous year; x_2 is the percentage change in the index number; and x_3 is the percentage change in the production of the United States plus carry over.¹⁴

Figure 4 is a comparison of the annual prices as estimated from the equation just given and the actual prices during that period. The average error for the 22 years is 3.6 cents, or 9.8 per cent of the aver-

age price.

In the correlation just described changes in the price level were taken account of by using the index number of prices of farm products as a separate variable. Approximately the same results would be



A comparison of the actual price of oats at Chicago with the price estimated by the use of the estimating formula

Fig. 4.—The accuracy with which oat prices may be estimated by use of the formula developed in this bulletin is indicated. The inaccuracy during certain years may have been due to unusual changes in demand, to inaccuracy in the estimate of production, or to other factors not accounted for in the estimating equation

secured by dividing the price of oats by the corresponding index number.

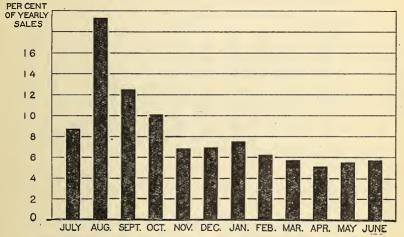
The variables were expressed as percentage changes over the preceding year because it was impossible to extend satisfactory trends through the war years. The difficulty will be recognized by an inspection of the price and production graphs in Figure 1. A first difference or percentage change over the previous year is more or less free from cumulative error, and may be used satisfactorily in such a situation. Percentage changes, however, are subject to a type of error similar to that described by Fisher in "The making of index numbers," that is, rising prices tend to augment the percentage changes, whereas falling prices have an opposite effect. It may be possible to correct this error by the use of percentage changes over the average of the figures for the current and the preceding years.

¹⁴ See Table V, Appendix A, p. 33, for the method of estimating prices by the use of an estimating equation.
15 Irving Fisher. The making of index numbers. 1922.

That part of the change in price which has not been accounted for by the factors included in this correlation may be due to the interaction of many factors, each in itself of minor importance. Unusually large or small substitute crops may affect the price of oats in some years; the estimates of production may not correspond to the actual production; industrial conditions may affect the price of oats in a way that is not accounted for by correcting for changes in the price level. Other methods of analysis may give more accurate results.

SEASONAL VARIATIONS IN OAT PRICES

The price of practically every farm product is subject to variations resulting from changes in the seasonal conditions of demand and supply. In most cases, as is especially true with those products which become marketable during a short period of the year, the influence of the supply conditions predominates. In the case of prod-



Monthly marketings of oats by farmers in terms of percentages of the year's sales

Fig. 5.—The heaviest marketings of oats come in August and September, immediately after the crop is threshed; the lightest marketings occur during seeding time in April. Prices show an opposite tendency, being lowest in August and September and highest in the spring

ucts which are consumed more heavily at one time of the year than at another the conditions of demand may be of more importance. The supply of some products, such as meats, butter, and eggs, may be partially adjusted to meet seasonal changes in demand.

The price of oats is subject to seasonal variations resulting principally from the fact that the supply becomes available for market during a short period of the year and must be carried at some expense throughout the crop year to meet the demands of consumers. The size of the crop also has an important influence upon the seasonal

trend, as will be shown in the following pages.

Table 4 gives the quantities of oats marketed monthly by farmers, with the percentage which each month is of the year's sales. Figure 5 represents this graphically. It will be seen that the heaviest marketing comes in August, September, and October, with August leading during each of the five years. Table 5 shows that the lowest

prices have come at about the time of the heaviest marketing, during August and September, and that the highest prices have come oftenest in May and July. This indicates that there may be a relationship between the quantities marketed and the price. If there is such a relationship, that is, if a large crop causes an undue depression in the price during the heavy marketing period, there should be a correspondingly large rise in price after the marketing period is over. This may be studied by comparing the movement of prices after a large crop with the movement of prices after small and normal crops.

Table 4.—Oats: Monthly marketings by farmers, 1916-1921 1

Month		ated q ners of nels)					Per cent of year's sales					
	1916- 17	1917- 18	1918- 19	1919- 20	1920- 21	5-yr. aver.	1916- 17	1917- 18	1918– 19	1919– 20	1920- 21	5-yr. aver.
July	31 87 51 40 30 21 28 20 20 14 17	24 82 67 56 38 39 42 40 35 33 20 24	34 82 50 42 30 28 28 19 23 27 29 28	47 60 33 30 19 27 26 21 16 14 17	36 80 59 41 24 25 28 28 26 20 29 34	34 78 52 42 28 28 30 26 24 22 22 23	8. 3 23. 3 13. 5 10. 7 8. 0 5. 7 7. 5 5. 3 5. 2 3. 8 4. 4 4. 3	4. 7 16. 4 13. 5 11. 1 7. 7 7. 8 8. 3 8. 0 7. 1 6. 5 4. 0 4. 9	8. 0 19. 6 11. 9 9. 9 7. 2 6. 7 4. 5 5. 5 6. 3 7. 0 6. 7	14. 4 18. 4 10. 1 9. 2 5. 8 8. 3 8. 2 6. 6 4. 9 4. 3 5. 2 4. 6	8. 3 18. 7 13. 8 9. 5 5. 5 5. 8 6. 6 6. 0 4. 6 6. 8 7. 8	8. 7 19. 3 12. 5 10. 1 6. 8 6. 9 7. 5 6. 2 5. 7 5. 1 5. 5
Season	375	500	420	325	430	409	100.0	100. 0	100. 0	100. 0	100. 0	100.0

¹ U. S. Dept. Agr., Yearbook; 1921, p. 545.

Table 5.—Frequency in occurrence of lowest average monthly prices and of highest average monthly prices of oats, July to following June, for 33 years, 1881 to 1914

	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	Feb.	Mar.	Apr.	May	June
Times lowest Times highest	4 14	7	12 1	2 0	0	2 0	0 2	1 1	3 0	1 2	0 6	1 5

Table 6 compares the September with the May prices during years (1) when production was about normal, as measured by the straight-line trend of production, (2) when production was 5 per cent or more below normal, and (3) when production was 5 per cent or more above normal. In the first group, including the 8 years about normal, the average rise from September to May was 5.9 cents, or 23.6 per cent over the September price. In the second group, including 11 years with production below normal, the average rise was 6.3 cents, or 16.5 per cent. In the third group, including 14 years when production was above normal, the average rise was 3.8 cents, or 14.9 per cent. These results would indicate that a large crop does not unduly depress the price during the heavy marketing season below a price fixed by the interaction of demand and supply throughout the 12 months' period of consumption.

¹⁶ The high showing of prices in July can not, in most instances, be considered as due to the crop of the season in which it is included in this table, but to a relatively smaller crop of the preceding year.

The seasonal trend may be calculated by averaging the monthly prices for the period 1881 to 1913 and correcting for the trend in prices. This will give a trend expressed in average monthly prices. This is not so useful for estimating purposes, however, as a seasonal

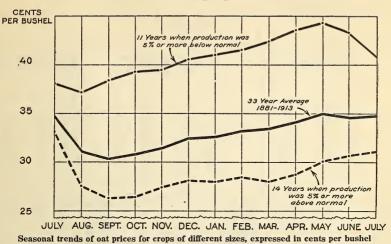


Fig. 6.—Although the seasonal trends in oat prices after August or September are very nearly the same, regardless of the size of the crop, the levels of prices are very different. Furthermore, the smaller the crop the sooner the price tends to rise after the decline in July and August due to heavy marketings

index expressed in percentages. Two methods of calculating such an index are illustrated in Table 7.

Since it was found that there was considerable difference in the seasonal movement of prices during years of large crops as compared

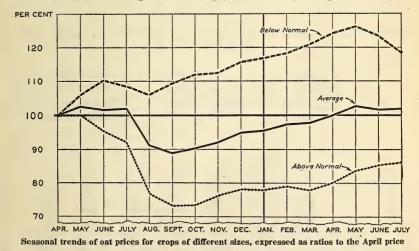


Fig. 7.—Nearly all of the difference in the seasonal trends of oat prices as between crops of different sizes occurs during the growing and harvesting period

with years of small crops, three seasonal trends were calculated, as given in Table 8. One is the trend for the entire period, the second for 14 years when production was above normal, and the third for 11 years when production was below normal. These are illustrated

in Figure 6. Figure 7 represents the average trends of prices for 16 months during the growing and marketing period. Values are expressed as ratios to the beginning April price on the assumption that this price is not influenced by the crop of that year.

Table 6.—Variations in oat prices, per bushel, September to the following May, 1881-1913

	Whe	en pro about	ductio	n was	When production was 5 per cent or more be- below normal					When production was 5 per cent or more above normal				
Year	September price 1	Following May price ¹	Spread between September and May		Year	September price 1	Following May price ¹	May price tween Sep nd May		Year	September price 1	Following May price ¹	Spread between Sep-	tember and May
1882-83	Cts. 33 16 20 21 222 31 322 40	Cts. 41 18 30 27 29 31 43 43	$ \begin{array}{c c} +2 \\ +10 \\ +6 \\ +7 \\ 0 \end{array} $	P. ct. +24. 2 +12. 5 +50. 0 +28. 6 +31. 8 +34. 4 +7. 5 +23. 6-	1881-82	Cts. 39 37 34 26 30 35 49 50 45 43	Cts. 53 51 31 35 29 43 40 53 60 56 41	Cts. +14 +14 -3 +9 -1 +8 +5 +4 +10 +11 -2 +6.3	P. ct. +35.9 +37.8 -8.8 +34.6 -3.3 +22.9 +14.3 +8.2 +20.0 -424.4 -4.7 +16.5	1883-84 1884-85 1885-86 1886-87 1887-88 1889-90 1891-92 1899-1900 1902-03 1905-06 1910-11 1912-13 Av	Cts. 27 25 25 25 24 20 32 20 22 29 26 34 34	Cts. 32 35 29 26 35 23 28 31 19 23 33 35 39	Cts. +5 +10 +4 +1 +10 -1 +8 -1 -1 +1 +4 +7 +1 +5 +3.8	1. ct. +18. 5 +40. 0 +4. 0 +4. 0 +4. 0 -4. 2 +40. 0 -3. 1 -5. 0 +4. 5 +13. 8 +2. 9 +14. 7 +14. 9

¹ Average monthly price.

Table 7.—Seasonal variations in prices of oats figured by two methods, 1895-96 to 1912-13

Month	Average monthly price per bushel not corrected for trend	Correction for trend 1	Average monthly price corrected for trend	Average of monthly prices per bushel, each corrected separately for trend	Trend	Seasona Method of averages ²	Method of link relatives 3	Column IV divided by its average
	I	II	III	IV	v	VI	VII	VIII
September October November December January February March April May June July August	Cents 31, 83 32, 53 33, 00 34, 23 35, 18 35, 88 36, 35 36, 65 37, 41 37, 65 37, 59 33, 88	Cents +. 715 +. 585 +. 455 +. 325 +. 195 +. 065 065 195 325 455 585 715	Cents 32.54 33.12 33.46 34.56 35.38 35.94 36.28 37.08 37.00 33.16	Cents 32, 53 33, 11 23, 57 34, 62 35, 37 35, 94 36, 06 36, 45 37, 09 37, 19 37, 12 33, 76	Cents 33, 99 34, 12 34, 25 34, 38 34, 51 34, 64 34, 76 35, 02 35, 15 35, 28 35, 41	94 95 96 100 102 104 105 105 107 107 96	94 96 96 98 100 101 102 104 106 106 105 95	92 94 95 98 100 102 103 105 106 105 96

¹ An average price would ordinarily be expressed to the nearest whole number, therefore, the correction for trend is of minor significance for practical uses.

2 Column I divided by Column V. For method of averages see Introduction to Economic Statistics, by G. R. Davies, 1922.

3 For method of link relatives see The Review of Economic Statistics, preliminary vol. 1, 1919.

Table 8.—Seasonal price trends of oats, 1881 to 1913

Month	Av	erage sea 1881-		ices	Seasonal prices when produc- tion was 5 per cent or more above normal trend		Seasonal prices when production was 5 per cent or more below normal trend			
	Average month-ly price	Correction for trend 1	Cor- rected price	Ratios to sea- sonal aver- age	Average month- ly price 2	Ratios to sea- sonal aver- age	Average month-ly price	Correction for trend 1	Cor- rected price	Ratios to sea- sonal aver- age
July	31. 0 31. 7 32. 7 33. 0 33. 6 33. 9 34. 7	Cents 0.06 .11 .17 .22 .27 .33 .38 .44 .50 .55 .61 .66	Cents 34. 7 31. 1 30. 3 30. 8 31. 4 32. 4 32. 6 33. 2 33. 4 34. 1 35. 0 34. 6	105. 8 94. 8 92. 4 93. 9 95. 7 98. 8 99. 4 101. 2 101. 8 104. 0 106. 7 105. 5	Cents 33. 1 27. 6 26. 3 26. 4 27. 4 28. 1 28. 0 28. 4 28. 0 28. 8 30. 1 30. 7	115. 8 96. 6 92. 1 92. 4 95. 9 98. 3 98. 0 99. 4 98. 0 100. 8 105. 3 107. 4	Cents 38. 1 37. 3 38. 5 39. 4 29. 7 40. 8 41. 2 41. 8 42. 7 44. 0 44. 7 43. 7	Cents 0. 04 . 07 . 11 . 14 . 18 . 22 . 25 . 29 . 32 . 36 . 40 . 43	Cents 38. 1 37. 2 38. 4 39. 3 39. 5 40. 6 41. 0 41. 5 42. 4 43. 6 44. 3 43. 3	93. 5 91. 3 94. 2 96. 4 96. 9 99. 6 100. 6 101. 8 104. 0 106. 9 108. 7 106. 2
Average			32, 8		28, 6				40. 8	

¹ The correction for trend is little greater than the probable error of the price arrived at by averaging weekly high and low quotations.

² The correction for trend is negligible—only 0.12 cents per year.

In order to see how closely the 33-year seasonal average reflects price movements for any one month, the standard deviations of the monthly averages have been calculated. (See Table 9.) These show that the September price is most accurately measured by the average price for that month, for the deviations of prices during that month from the average price have been least. The May price has the greatest deviation from its average.

APPLICATION OF SEASONAL TREND IN ESTIMATING PRICE

After having estimated the annual average price an index of seasonal price movements may be used for two purposes: To determine whether the price for any given month is above or below the normal level of seasonal prices and to indicate the probable trend of prices during the following months of the crop year. For these purposes the ratios of monthly average prices to the yearly average are most useful. (See Table 8.) These should be used with reference to whether the crop is about normal, below normal, or above normal, the normal production being represented by a trend which indicates as accurately as possible the general direction in which production is going. A price at the beginning of the crop year, then, which seems considerably above the normal seasonal price as indicated by the ratio for the given month, may be expected to fall below the estimated seasonal price before the end of the crop year.

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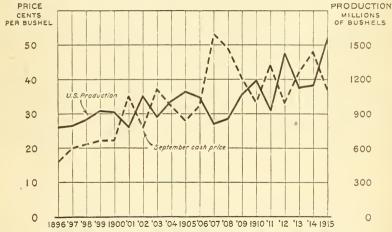
Table 9.—Average monthly prices of oats, 1881-1913, and their standard deviations

Month	Price	Standard deviation	Month	Price	Standard deviation
July	Cents 34.8 31.2 30.5 31.0 31.7 32.7 33.0	10. 1 8. 6 8. 4 8. 7 8. 5 9. 1 9. 3	February	Cents = 33. 5 33. 9 34. 6 35. 6 35. 3 33. 0	9. 6 10. 0 10. 2 10. 3 9. 7

With reference to this subject, Working says: 17

A properly adjusted price would remain the same throughout the season, except for a gradual advance to cover cost of storage, and would maintain a fairly uniform consumption throughout the season. But since an abnormally high price early in the season causes small consumption, it must be compensated by an abnormally low price during the remainder of the season or not all the crop can be sold.

Similarly, he says that if the price is abnormally low early in the season the supply will be exhausted too rapidly, and for the resulting



A comparison of the United States production of oats and the September price

Fig. 8.—The inverse relation between the production of oats and the September price is clearly shown.

small supply later in the year abnormally high prices will be paid, the result being that, although the price at any one time may differ from the normal price justified by demand and supply conditions, the average price for a season will come very close to the normal. This statement regarding potato prices may likewise be applied to out prices, with the modification that variations in the carry over of oats may cause the influence of one crop to extend into the following season.

SEPTEMBER PRICE AS A BASIS FOR ESTIMATING SEASONAL PRICES

The fact that the standard deviation of the September price from the average for the period studied is less than that of any other month and less than that of the average annual price suggests that it may

¹⁷ See footnote 5.

¹⁸ Another method of taking account of seasonal variation is to correlate prices of each month with the price-making factors.

be more accurate as a basis for estimating the seasonal trend of prices than is the average annual price heretofore used. That the September price can be predicted with greater accuracy than the annual price is shown by the fact that a correlation coefficient of -0.85 is obtained when the year-to-year changes in the September cash price are correlated with the changes in the final estimate of oat production of the Department of Agriculture as compared with a coefficient of -0.82 when the annual price is used. If to the production figure is added the carry over from the previous year, and changes in this new figure representing supply are correlated with changes in the September price, a coefficient of -0.91 is obtained.¹⁹ Figure 8 represents graphically the close relationship between production and the September price.

DISCUSSION OF METHOD

As indication of the relative effectiveness of using percentage changes as compared with absolute changes in correlating the September price with production plus carry over, four correlations were carried out, using different combinations of the two methods. The resulting coefficients are given in Table 10.

Table 10.—Correlation of changes in September price and production plus carry over of oats, 1896 to 1913

Variables	Coeffi- cient	Standard error
(a) Price: Percentage change over that of the preceding year. (b) Production plus carry over: Percentage change over that of the preceding year. (c) Price: Change in cents per bushel over that of the preceding year. (d) Production and carry over: Percentage change over that of the preceding year. (a) Price: Change in cents per bushel over that of the preceding year. (b) Production plus carry over: Percentage change over the average figure of the	00	Cents 1 6. 1 3. 8
preceding and current years	} 91	3, 5

Approximate standard error 18.6+per cent of average price, 33 cents.

A correlation using absolute changes (first differences) does not require the elimination of a straight-line trend which may be present, for this method of correlation is itself a method of eliminating such trends, owing to the fact that the trend affects the change from year to year by a constant amount. Adding a constant to a series does not affect the deviations from the average of the series, since each item is increased as much as any other and the relationship between them remains the same.²⁰ It is necessary, however, in first difference correlations, to make corrections for nonlinear trends which may disturb the price series, either by dividing each price item by its

¹º A correlation for the period 1895 to 1915 gives a coefficient of 0.94 when the September cash price, the Bureau of Labor Statistics all-commodities index number for September, and the final estimates of production plus carry over were correlated as changes over the values for the preceding years. Expressing changes in the average September price in cents per bushel as x_1 ; changes in the index number as x_2 ; and changes in the estimated production, plus old stocks on farms August 1, plus visible supply July 1, in 10,000,000 of bushels, as x_3 , the estimating equation is x_1 =0.388 x_2 =0.446 x_3 . Applying this equation to the 20 years covered by the correlations, an average error of 3 cents per bushel in predicting the September price is found. This may be compared with the average error of 3.6 cents in predicting the annual price. (See p. 12.) The error is less than 3 cents for 13 of the 20 years.
2º B. B. Smith. The use of punched card tabulating equipment in multiple correlation problems; collected and prepared for the use of statisticians of the Bureau of Agricultural Economics, U. S. Department of Agriculture. 1923. Mimeographed.

corresponding index number or by using first differences of the index number as a separate variable in the correlation with first differences of price uncorrected. This was done in all the correlations mentioned, using either an all-commodity index or a commodity group index.

With no correction for the nonlinear trend in the series of September prices, 1901 to 1921, the correlation with production plus carry over resulted in a coefficient of only -0.43. Dividing the price by the Bureau of Labor Statistics index number of all commodities for September resulted in a correlation of -0.73. Using first differences of this index number as a separate variable, instead of dividing the price by the index number, raised the correlation to -0.86. In this case the latter method gave better results.

FUTURE PRICES AND CONDITION REPORTS AS PRICE INDICATORS

During the growing season, when the price forecaster must estimate supply as well as demand and when the price of oats is being influenced by the past year's crop as well as by the crop which is maturing, the movement of prices is most difficult to predict. Two indicators of price movements are available to farmers during this period: (1) The condition reports for the oat crop issued periodically by the United States Department of Agriculture; and (2) the price of September futures, which represents the best opinion of the grain trade as to the probable September cash price.

The Department of Agriculture issues in the spring a preliminary estimate of acreage planted and early in June issues the first of a series of monthly condition reports and production forecasts. Early in March an estimate of stocks of oats on farms is published. A final estimate of acreage, yield, and production is made in December. These data are among those used by dealers in oats to estimate the

probable future prices.

Future prices are quoted throughout the year for oats to be delivered during specified delivery months, usually September, December, May, and July. It may thus be said that the oat crop is bargained for on the grain exchanges before it is planted, and at the time of harvest sales and purchases are made for delivery eight or nine months later. The fact that in making these sales for future delivery grain men must look ahead and estimate the probable price conditions at the date of delivery results in making the prices of oat futures an indicator of future cash prices. Just how good an indicator they are can be established by correlating future prices with cash prices during the corresponding delivery months.

RELATION OF FUTURE PRICES TO SUPPLY AND TO CASH PRICES

The quantity of new oats harvested ordinarily determines in large measure not only the September cash price of oats but also the September price of May futures. As compared with the -0.91 correlation between September cash price and the new supply of oats, the correlation between the September price of May futures and the new supply of oats is -0.93; that is, prices of May futures are strongly influenced by the supply of oats available in September. By May, however, the closeness of agreement between cash prices and the

supply of oats apparent in September has become diminished some-

what, for it is measured by a coefficient of -0.87.

The correlation between visible supply plus stocks on farms March 1 and the May cash price is -0.85, whereas consumption to March 1 seems to maintain a practically constant relationship to production the correlation between final estimate of production plus carry over and the stocks on farms plus visible supply March 1 is +0.97. Thus the September price of May futures, although closely in line with production and carry over at the end of the harvest, may be somewhat out of line with the cash price which has come to prevail in May.

As between May and the following September a somewhat similar but more complex condition exists. For a period of 18 typical years, 1896 to 1913, inclusive, the May prices of September futures were in line neither with the quantity of new oats yet to be matured and harvested nor with the September cash prices. The correlation between May prices of September futures and final estimates of the new crop is measured by a coefficient of +0.31.21 Instead of showing the negative relationship usually assumed between production and price, this coefficient indicates a slight tendency for May prices of September futures to be high when the new crop is large, and vice versa.²² It suggests, therefore, that the size of the new crop has no significant effect as early as May upon prices of contracts for future delivery. May prices of September futures appear in fact to be influenced more by prevailing cash prices than by any other factor.

As the season progresses, however, and as forecasts of the new crop become more and more accurate, prices of September futures are gradually adjusted toward the average September cash price, until in August the average price of September futures corresponds very closely with the September cash price. The closeness of agreement at this time is measured by a coefficient of +0.95. The relation between the price of September futures and the August cash price is measured by a smaller coefficient, +0.86, showing that the September cash price can be predicted more accurately from the August price of

September futures than from the August cash price.

Table 11 shows the gradually increasing closeness of the relationship between cash and future prices as the harvest season approaches. The variables in these correlations are expressed in terms of changes in cents per bushel over the corresponding months of preceding years. These coefficients indicate the increasing accuracy with which September cash prices can be estimated from the prices of September futures.

RELATION BETWEEN CROP CONDITION ESTIMATES AND PRODUCTION

In recent years the United States Department of Agriculture has published monthly forecasts of production for the principal grains, including oats, during the latter part of the growing season. are available for only a part of the period covered in this study, but

21 The correlation between corresponding changes in the May price of September futures and the Sep-

tember cash price is measured by a coefficient of -0.03.

21 This positive correlation is probably due to some tendency for a large crop to be followed by a small one, and vice versa, and not to any real relation between the May price of September futures and the size of the new crop. Since the May price of September futures is influenced more by the size of the preceding crop than by any other factor, the actual relation measured by the correlation coefficient is that between the crop of one were and a price beside or the crop of the preceding to the crop of one year and a price based on the crop of the preceding year.

condition estimates were available from 1890 to date. A study of the relation between the condition estimates and the final estimate of production for the years 1896–1913 showed that the condition estimates came more and more to agree with the final estimate of production as the harvest season approached. Since there is close relationship between the final estimate of production plus carry over and the September price, as indicated by a correlation coefficient of +0.91, the coefficients can be taken as approximately measuring the increasing accuracy with which the September price could be estimated from the monthly condition estimates, using condition estimate in place of production as one factor in the estimating equation.

The monthly forecasts of production during the growing season, which are available since 1912, make it unnecessary to take account of condition estimates in predicting the September price, for the forecasts of production can be used directly in the estimating equation. These production estimates would undoubtedly be more accurate than the condition estimates, though their relative accuracy as the harvest season approached would approximately compare with the coefficients in Table 11. The variables are expressed in terms of changes over preceding years. The unit employed for condition estimates is that used by the Department of Agriculture.

Table 11.—Correlation of September future prices of oats during the growing season with cash prices in September

September cash price correlated with—	Coeffi- cient
May prices of September futures. June prices of September futures. July prices of September futures. August prices of September futures	-0.03 +.25 +.79 +.95

Table 12.—Correlation coefficients of preliminary condition and final production estimates of oats, 1896–1913 ¹

Final production estimate correlated with—	Coeffi- cient
June 1 condition estimate July 1 condition estimate August 1 condition estimate September 1 condition estimate	+0.45 +.77 +.86 +.94

¹ In these correlations changes in acreage are not taken into account. When preliminary estimates of acreage are multiplied by September estimates of condition for the period 1896 to 1922, inclusive, and the result correlated with the final estimates of production for the same period, a higher coefficient is obtained, +0.97. All variables were expressed as changes from the corresponding months of preceding years.

CONCLUSIONS REGARDING FUTURE PRICES

The conclusions from this part of the study may be summarized in two brief statements:

Both cash and future prices of oats are highly sensitive to changes

in the supply of oats when the supply is known.

Future prices, unlike cash prices, anticipate supply. Consequently, future prices which span the gap between one crop year and the next vary, as a rule, as widely from cash prices at the time of delivery as forecasts of production and carry over at the time contracts are made vary from the final measure of supply.

Three significant relationships between cash and future prices have been brought out:

(1) May prices of September futures are strongly influenced by

prevailing May cash prices.

(2) May cash prices of oats conform to supply of oats as measured by the production plus carry over of the previous fall.

(3) September cash prices conform to supply as measured by the

size of the new crop and carry over.

By virtue of these facts, cash prices in May following a large crop and carry over of the previous fall will tend to be relatively low, and consequently the May prices of September futures will be lower than the cash prices in September, unless the new crop also is unusually

large.

However, the fact that in years when the supply of oats is above normal, as indicated by the straight-line trend of production plus carry over, May prices of September futures are below cash prices of the following September, does not necessarily mean that in these years it will always pay to hold oats from May to September. May prices are normally above September cash prices because of the expense of carrying oats from September to May.

A COMPARATIVE STUDY OF WHEAT PRICES

EXTENT OF WHEAT MARKET, AND ITS INFLUENCE ON CHICAGO PRICE

The price of wheat, unlike that of oats, is determined in large measure in the world market by the world crop. This fact is brought out by a study of the extent of the market and by correlations showing the degree of relationship between the Chicago price of wheat and the

production of wheat in the United States and in the world.

Table 13 gives an idea of the extent of the market by showing the principal countries which import and export wheat, with average imports and exports of wheat and flour for the period 1909–10 to 1913–14. The United States during this period was the second most important exporting country, exceeded only by Russia in the volume of exports. The fact that the United States must seek a foreign market for a large part of its wheat crop, where its wheat comes into competition with wheat from other parts of the world, would suggest that the production in other countries should have considerable influence upon the price of wheat in this country.

Correlations given in Table 14 show that the influence of the crop of the United States upon the price of wheat at Chicago is measured by a coefficient of only -0.32, whereas the influence of the crop of the entire world is measured by a coefficient of -0.71. The table shows also that the price of wheat is influenced to some extent by the production of rye. The Chicago price is very closely related to the price at Liverpool, as indicated by a coefficient of +0.93 when the prices at these two markets are correlated during the period 1890 to 1921.

Table 13.—Wheat, including flour: International trade, average of years 1909-10 to 1913-14

Principal importing	countries		Principal exporting countries						
Country	Imports	Exports	Country	Imports	Exports				
United Kingdom Germany Netherlands Belgium Italy France Brazil Switzerland Austria Egypt Denmark Sweden Union of South Africa 1 Spain	80, 702 73, 398 56, 784 44, 822 20, 495 16, 937 11, 402 8, 244 7, 155 7, 080	1,000 bushels 3,768 23,264 58,435 23,045 3,682 1,203 14 871 59 597 23 253 70	Russia United States Canada Argentina ¹ Rumania British India Australia ² Hungary. Bulgaria Algeria Chile ¹	7, 214	1,000 bushels 164, 861 110, 076 95, 828 95, 246 54, 630 49, 886 49, 732 49, 116 11, 185 5, 936 2, 593				

¹ Calendar years, 1909 to 1922.

International Institute of Agriculture, except figures with footnotes 1 and 2, which are compiled from

Table 14.—Correlation coefficients relating to the price of wheat 1

Item	Coeffi- cient
Ratio of price of wheat correlated with: ² Period 1891-1913, inclusive— Ratio of United States production of wheat. Ratio of world production of wheat. Ratio of world production plus world carry over	-0.32 71 80
Multiple correlation— (a) Ratio of world production plus world carry over— (b) Ratio of world production of rye————————————————————————————————————	
Period 1900–1914— ³ Ratio of world production of barley	44 29

A coefficient of net correlation shows the effect of one independent variable in a multiple correlation upon the dependent variable when the other independent variables are held constant. The coefficient of net correlation between the ratio of price and the ratio of United States production is -0.47, as compared with a coefficient of -0.66for the net correlation between the ratio of price and the ratio of production outside of the United States. This shows that the wheat crop of the remainder of the world has a greater net effect upon the price of wheat at Chicago than has the production of wheat in the United States.

The meaning of these coefficients is suggested by the fact that prices of wheat declined following the short United States crop of 1893 when world production was large, whereas they rose after the short crops of the United States and of the world, 1907, 1908, and 1911, and declined again in 1913 when the crop of the United States

was normal and the world crop was large.

² Years ended June 30.

All variables are expressed as ratios to their straight-line trends.
 Ratio of Chicago average crop-year price per bushel of wheat, divided by the Bureau of Labor Statistics farm products index, to the straight-line trend of price so corrected.
 World production statistics of barley are available only from 1994, and of potatoes only from 1900.

Table 15 shows the coefficients of correlation resulting from the use of different methods of treating the variables, as in the study of prices of oats. It will be seen that with wheat the results were approximately the same in the three cases.

NOTES ON METHOD

As a study of wheat and oat prices has expanded, so also has the statistical technique employed been adapted to new uses. At the beginning, for example, variables were expressed as ratios to trends. Later, variables expressed as percentage changes over the preceding year were used for comparisons extending through and beyond the period of the World War, because straight-line trends could not be satisfactorily extended through that period.

Table 15.—Table of coefficients of multiple correlation relative to wheat prices, period 1895 to 1914

Dependent variable	Independent variables	Coeffi- cient
(a) Ratio of price divided by farm products relative to its straight-line trend.	(b) Ratio of world production plus carry over of wheat to its straight-line trend. (c) Ratio of world production of barley to its straight-line trend. (d) Ratio of world production of rye to its straight-line trend. (b) Ratio of world production plus carry over of wheat to	0.83
(a) Ratio of price divided by farm products relative to the same of the preceding year.	the same of preceding year. (c) Ratio of world production of barley to that of preceding year. (d) Ratio of world production of rye to that of the preceding year.	.82
(a) Ratio of price, uncorrected, to that of preceding year.	 (b) Ratio of farm products index number to that of preceding year. (c) Ratio of world production plus carry over of wheat to the same of the preceding year. (d) Ratio of world production of barley to that of the preceding year. (e) Ratio of world production of rye to that of the preceding year. 	.82

On page 12 it was suggested that variables be expressed as percentage changes over the average of the figures for the preceding and current years. Finally variables expressed as simple changes in cents, tens of millions of bushels, and points of an index have come to be used. Table 10 shows that for the purpose at hand variables expressed in this way were relatively accurate as well as simple, direct, and convenient.

No generalizations are made to show the superiority of any method. In one case it may be desirable to sacrifice exactness for the sake of simplicity; in another inaccuracy may be too high a price to pay for simplicity; whereas in some instances simplicity may accord with the greatest accuracy. In the first part of the bulletin straight-line trends were used because they best described the data. Linear comparisons were used in relating oat prices to production because, for the data at hand, curves suggested but slightly closer agreement and involved considerably more work. For expressing seasonal variation the methods of link relatives and averages gave closely comparable results.

Higher coefficients of correlation were obtained when a farmproducts index was used to correct for changes in the price level, than

when an all-commodities index was used.

"Index numbers made from the prices of raw materials or of raw materials and slightly manufactured products must be expected to show wider oscillations than index numbers including a liberal representation of finished commodities," says Mitchell.²³ Thus the farm products relative would be expected to vary more than the index number of all commodities, which is desirable for the purposes of a price study.

The fact that the farm-products relative is more susceptible to change caused by changes in the demand for farm products as a group is an argument in favor of this relative for purposes of estimating the price of wheat or oats. On the other hand, the fact that wheat and oats have more influence to change the index number of farm products than to change the index of all commodities is an argument against using the farm-products index for price estimating purposes.

The combination of an index of manufactured products to reflect changes in the purchasing power of money and some index to reflect changes in demand for the product under consideration should be more accurate for purposes of price estimating than either the farm-

products or the all-commodities index.

There was little difference in the correlation coefficients when the index number was run as a separate variable and when prices corrected by the index number were correlated directly. In most cases the index number was run as a separate variable because this method was more direct.

²³ W. C. Mitchell. Index numbers of wholesale prices in the United States and foreign countries. 1921.
U. S. Bur. Labor Statis. Bul. 284.

APPENDIX A

OAT AND WHEAT STATISTICS AND CALCULATIONS

Table I.—Trend of oat production in the United States 1881 to 1913

Year	y Produc- tion ¹	x Origin 1897	x 2	xy	Straight- line trend 1881 to 1913 ²
1881	Million bushcls 4188 571 583 629 624 644 659 701 751 523 738 661 639 602 824 7800 791 843 926 914 778 1,053 869 1,009 1,036 805 851 1,168 1,186 81 1,122 26,930	-16	256 225 196 169 144 121 100 81 64 49 36 625 16 9 4 1 1 4- 9 16 25 36 49 64 81 100 121 144 169 225 256 2,992	-6, 656 -7, 320 -7, 994 -7, 579 -7, 548 -6, 590 -6, 308 -3, 661 -4, 428 -3, 305 -1, 648 -780 0 +843 +1, 852 +2, 742 +5, 265 +4, 7, 063 +8, 720 +8, 050 +9, 324 +12, 816 +15, 418 +12, 908 +21, 270 +141, 910 -81, 232 +141, 910 -81, 232 +60, 678	Million bushels 496 516 556 556 556 656 666 676 696 716 736 816 836 856 876 996 1,016 1,036 1,056 1,056 1,076 1,116 1,136
Slope (00,078 divided by 2,992)				= +20	

U. S. Dept. Agr. Yearbooks.
 For discussion of method see A Study of Statistical Method, by W. M. Persons in Review of Economic Statistics, preliminary vol. 1, 1919; Graphical and Mechanical Computation, by Joseph Lipka, 1918; Introduction to Economic Statistics, by G. R. Davies, 1922; or other standard texts dealing with the method of least squares.

A verage.

Table II.—Correlation of Chicago price and United States production of oats

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		United	States pr	roduc-	Chicago price per bushel			Variation me				
Million Million Dushits bushels bush	Year	Total	line	to		line	to	tion ratios	ratios	x 2	y 3	xy
	1882 1883 1884 1885 1884 1885 1886 1887 1886 1887 1888 1890 1890 1890 1890 1890 1900 1901 1902 1900 1901 1902 1906 1907 1908 1907 1908 1909 1901 1901 1901 1902 1903 1904 1909 1901 1901 1901 1902 1903 1904 1909 1901 1901 1901 1903 1904 1909 1901 1901 1903 1904 1909 1901 1901 1901 1903 1904 1909 1909 1901 1908 1909 1901 1901 1911 191	bushels 418 488 571 583 629 624 659 701 751 523 738 661 639 662 824 780 791 843 926 1,090 1,036 805 1,068 1,186 1,186 1,186 1,186 1,181 1,122	bushels 496 516 536 536 556 666 666 666 676 696 716 736 816 836 856 876 996 1,016 1,036 1,056 1,076 1,076 1,116 1,136	, 95 1, 07 1, 05 1, 09 1, 05 1, 07 1, 10 1, 14 7, 7 88 1, 06 98 98 1, 01 1, 08 1, 08 1, 08 1, 08 1, 08 1, 08 1, 08 1, 08 1, 10 1, 10	477 377 311 299 28 255 300 24 43 311 329 18 24 42 25 42 25 42 25 42 25 42 25 45 31 33 38 30 30 31 31 51 51 52 33 35 51 51 37 37	Cents 36. 0 35. 3 34. 6 34. 0 33. 2 5 31. 2 5 29. 8 29. 0 28. 3 27. 5 26. 8 26. 1 25. 3 23. 6 25. 0 40. 4 27. 8 29. 2 30. 6 32. 0 0 40. 4 41. 8 43. 2 44. 6 46. 0	1. 05 .90 .85 .84 .77 .96 .79 .81 1. 10 1. 10 1. 10 .75 .76 .95 .83 .86 1. 37 1. 14 .86 1. 31 1. 29 1. 31 1. 42 1. 31 1. 43 1.	05 +.07 +.05 +.09 +.05 +.07 +.10 08 13 12 +.06 02 03 12 +.06 +.06 02 02 03 +.01 +.04 +.04 +.04 +.13 +.15 07 +.04 +.05 +.05 07 +.05 07 +.05 07 +.05 07 +.05 08 08 08 08 08 08 08 08	+ . 05 10 15 16 23 04 19 + . 10 + . 10 + . 10 25 24 04 05 24 04 37 + . 03 + . 14 14 + . 04 + . 31 + . 31 + . 29 + . 19 + . 29 + . 20 + . 20	0025 0049 0025 0081 0090 0196 0529 0086 0064 0196 0090 0100 0090 0014 0009 0001 0066 0169 0225 0049 0036 0144 0016 0169 0225 049 0366 0144 0010 0606 01729 0001	0025 0100 0225 0256 0529 0016 0441 0361 2304 0100 081 0256 0049 0625 0576 0016 0025 0228 0196 0196 0196 0196 0196 0196 0196 0196	0025 0070 0075 0144 0015 0028 0210 0236 0144 0060 0072 0208 0084 0150 0150 0150 0016 0150 0016 0056 0150 0016 0056 0150 0056 0150 0056 0150 0056 0150 0056 0150 0056 0150 0056 0150 0056 0150 0056 0150 0056 005

 $\sigma x = \sqrt{\frac{0.4369}{33}} = 0.115. \quad y\sqrt{\frac{1.2289}{33}} = 0.193. \quad r = \frac{-.5989}{33 \times 0.115 \times 0.193} = \frac{-0.5989}{0.7324} = -0.82.$

Table III.—Value of oats produced and consumed in the United States, 1895-1913

		iction States		etual condi		With a uniform increase in consumption				
Year	Actual	Trend	Annual con- sump- tion ¹	December farm price per bushel 2	Total value	Annual con- sump- tion ³	Esti- mated Decem- ber farm price per bushel ⁴	Esti- mated total value	Neces- sary ad- dition to carry over ⁵	
1895	1, 068 1, 186 922 1, 418 1, 122	bushels 776 796 816 836 836 876 896 916 936 956 1,016 1,036 1,056 1,076 1,116 1,136	Million bushels 746 820 822 835 535 920 919 810 1,004 902 989 1,076 1,040 840 863 1,030 1,179 961 1,338 1,172	Cents 20 19 21 26 25 26 40 31 34 41 31 29 32 44 47 40 34 45 32 39	Million dollars 149 1566 173 2217 2300 2399 3224 3111 3007 307 3112 333 3700 4406 4412 4428 4457	Million bushels 776 796 816 836 836 856 916 936 956 976 976 1,016 968 1,030 1,076 1,116 1,136	Cents 22. 1 23. 2 24. 4 25. 5 26. 7 27. 8 29. 0 30. 1 31. 3 32. 4 33. 6 34. 7 35. 9 40. 0 39. 0 39. 0 39. 3 42. 0 41. 6 42. 8	Million dollars 171 1855 199 213 229 244 2600 276 293 310 3288 346 365 387 402 423 424 426 6,135 -5,964 171	Million bushels 0 24 30 29 93 136 50 138 104 137 237 281 105 6 68 6 26 103 6 32 222 258	

cents) less the value of 30 million bushels carried from 1894 to 1895 at the 1895 price.

Production plus carry over from previous year less carry over to following year.
 From U. S. Dept. Agr. Yearbooks.
 Same as trend of production except for the deficit years 1908, 1909, and 1911, when the sum of carry over

³ Same as trend of production except for the deficit years 1908, 1909, and 1911, when the sum of carry over plus production was less than the trend of production.
⁴ Straight-line trend of price except for the deficit years, 1908, 1909, and 1911, when price was estimated on the basis of percentage changes.
⁶ Obtained by subtracting the production trend figure from the actual consumption figure and adding the necessary additional carry over from the preceding year. For example the 1897 carry over figure of 30 is obtained by subtracting the trend figure (816) from consumption (822) and adding the addition to carry over (24) to the remainder. This figure, therefore, signifies hypothetical addition to actual carry over.
⁶ Consumption for year computed is greater than production.
⁷ The figure 107 represents the value of 258 million bushels carried from 1913 to 1914 at the 1914 price (44 cents) less the value of 30 million bushels carried from 1807 price.

Table IV A.—Statistics of price and price determining factors of oats

Year beginning July 1	Chicago price of oats ¹	Change over preceding year	Bureau of labor statistics index of farm products ²	Change over preceding year	Production oats in the United States 3	Old stocks on farms Aug. 1, in the United States 4	United States visible supply of oats July 15	United States produc- tion of oats plus old stocks on farms plus visible supply	Change over preceding year
1895	Cents 17 23 25 23 24 44 40 31 31 37 50 53 44 35 50 67 77 71 88 54 39 41	Per cent -15 +35 +9 -8 +44 +67 -15 +122 -16 -3 +19 +35 +6 -17 -20 +43 -26 +11 +24 -44 +38 -8 -8 +24 -39 -28 +5	588 577 611 644 677 722 788 799 800 80 80 98 97 100 102 104 114 156 204 224 111 128 139	Per cent -2 +7 +5 +5 +5 +7 +7 +8 -11 0 +1 0 +5 +2 +7 +9 -2 -1 1 +3 +2 +10 -3 +3 +3 +10 -24 -24 -9 +9	Million bushels 824 780 791 843 926 9144 778 1,053 869 1,090 1,036 8055 851 1,068 9122 1,141 1,549 1,252 1,593 1,538 1,184 1,496 1,076	Million bushels 43 119 80 51 55 322 79 46 63 78 41 27 67 68 35 104 62 56 6114 48 81 93 55 70	Million bushels 7 9 9 8 6 6 6 7 7 111 2 2 4 4 4 7 7 6 6 7 7 4 4 10 10 13 3 18 8 4 4 4 3 3 4 4 4 3	Million bushels 874 908 879 9000 9911 9855 844 41,087 952 1,160 11,120 8865 896 1,101 1, 257 1,000 1,457 1,241 1,210 1,609 1,378 1,651 1,651 1,651 1,651 1,555 1,273 1,333	Per cent +4 -3 +10 -11 -14 +29 -12 +11 +10 -3 -21 +11 +23 +24 -15 -3 -3 +33 -33 -34 +20 -1 -21 +20 -1 +20 -1 +20 -1 +5

¹ Average of monthly prices of No. 2 oats July to following June. Monthly prices obtained by averaging weekly high and low prices as quoted in the Chicago Board of Trade Annual Reports.
² From 1913 to 1922 monthly index numbers, July to June, were averaged, to convert to a crop year basis. Previous to 1913 the annual index numbers for each two consecutive calendar years were averaged for the July to June crop year index.
² U. S. Dept. Of Agr., Yearbooks.
² U. S. Dept. Agr., Weather, Crops and Markets, Aug. 11, 18, 1923.
² U. S. Dept. Agr., Yearbooks, or Chicago Board of Trade Annual Reports.

Table IV B.—Oats: Multiple correlation of price of oats, index of prices of farm products, and United States production plus carryover of oats, in terms of percentage changes over preceding years

	Perce	entage ch	anges							
Year beginning July 1	Price,	\inf_{x_2}	U.S. prod. oats plus carry-over,	x_{1}^{2}	<i>x</i> ₁₂	<i>x</i> ₁₃	x_2^2	<i>x</i> ₂₃	x ² 3	
1896 1897 1898 1898 1899 1900 1901 1902 1903 1905 1906 1907 1908 1909 1910 1910 1911 1912 1913 1914 1915 (1)	-15 +35 +49 +8 +4 +47 +67 -155 +66 -177 -20 +431 +24 +11 +24 +12 +12 +12 +12 +12 +12 +12 +12 +12 +12	-2 +75 +55 +55 +77 +8 +11 0 0 +5 +2 +2 +2 +2 +2 +13 +2 +2 +10	$\begin{array}{c} +4\\ -3\\ -3\\ +2\\ +10\\ -11\\ -14\\ +29\\ -12\\ +11\\ +10\\ -3\\ -21\\ +14\\ +20\\ -46\\ -15\\ -3\\ -3\\ +33\\ \end{array}$	2255 1, 2256 81 64 64 4, 489 2255 1444 2566 9 361 1, 225 366 289 400 1, 849 676 121 576 144	-45 -40 +28 +536 -15 0 -16 -16 -0 +42 -153 +40 -43 -78 +22 +48	-105 +118 -80 -4 -938 -435 -144 -176 -30 -57 -735 +6 -391 -280 -860 -1,196 -165 -72	49 25 25 49 64 1 0 1 0 25 4 49 81 4	$\begin{array}{c} -2\overline{1} \\ +10 \\ +50 \\ -7 \\ -112 \\ +29 \\ 0 \\ +111 \\ 01 \\ -15 \\ -422 \\ +7 \\ +207 \\ -288 \\ +20 \\ -138 \\ -30 \\ -6 \end{array}$	9 4 100 11 19 841 144 121 100 9 441 1 529 196 400 2,116 225	
1921 1922	-28 +5	-25 +9	-18 +5	784 25				+450 +45		
	+270 -160	+83 -30	+188 -110		+1,946 -465	-6,124 +553		+1,297 -269		
Total	+110	+53	+78	13, 220	+1,481	-5,571	1, 205	+1,028	6,896	
A verage Squares Subtract	+5.00 +25.0000	+2.41 +5.8038	+3.54 +12.5706			-253.2273 $+317.7275$			+313. 4545 +12.5706	
				575. 9091 σx_1^2	$+ 55.2727$ ρx_{12}	-270.9548 ρx_{13}	$+48.9689$ $\sigma x_{2^{2}}$	$+38.1858$ ρx_{23}	$+300.8839$ σx_3^2	

¹War years omitted. ² Product of 5×2.41. ³ Product of 5×3.54. ⁴ Product of 2.41×3.54.

Table IV c.—Solution of simultaneous equations involving (x₁) price, (x₂) index, and (x3) United States production plus carryover of oats 1

Equations:

1. σx^2 $b_{12} + \rho x_{23} b_{13} = \rho x_{12}$ 2. $(\rho x_{23} \ b_{12}) + \sigma x_{3}^{2} \ b_{13} = \rho x_{13}$

Substituting actual values, as calculated in IV B.

First equation, $+48.97 \ b_{12} + 38.19 \ b_{13} = +55.27$. Second equation, $(+38.19 \ b_{12}) + 300.88 \ b_{13} = -270.95$.

	b_{12}	b ₁₃	p	Cheek sum
1. Bring down first equation 2. Divide by first term with sign changed, or -48.97= 3. Bring down second equation 4. Multiply line (2) by +38.19= 5. Add above 2 lines 6. Divide by first term with sign changed, or -271.10=		$ \begin{array}{r}7799 \\ +300.88 \\ -29.78 \\ +271.10 \end{array} $	$=+55.27$ $=-1.1287$ $=-270.95$ $=-43.11$ $=-314.06$ $=+1_{6}1585$	$ \begin{array}{r} -2.9086 \\ +68.12 \\ -111.08 \\ -42.96 \end{array} $

Change signs of values in column (p), lines (6) and (2), then $b_{13} = -1.1585$

$$b_{12} = +1.1383$$

 $b_{12} = +1.1287 + (-1.1585 \times -0.7799) = +2.0322$.

Product moments:

$$\begin{array}{l} b_{13}x_{13} = -1.1585 \times +270.95 = 313.90 \\ b_{12}x_{12} = +2.0322 \times + 55.27 = 112.32 \end{array}$$

The coefficient of multiple correlation,
$$R = \sqrt{\frac{P. M.}{\sigma x_1^2}}$$

$$= \sqrt{\frac{426.22}{\sqrt{575.91}}}$$

$$= 0.86$$

The estimating equation is $x_1 = a + b_{12} x_2 + b_{13} x_3$ Solve for "a" by substitution as follows: $+5.00 = a + (2.0322 \times 10^{-3})$

2.41) + (-1.1585 × 3.54). a = +4.20.

Inserting known values for the constants: a, b_{12} , and b_{13} , the estimating equation becomes $x_1 = 4.20 + 2.03x_2 - 1.16x_3$.

¹ The method used in solving the simultaneous equations is "The Doolittle method." See Geodesy—Application of Theory of Least Squares to the Adjustment of Triangulation, by O. S. Adams, 1915; also A Method of Handling Multiple Correlation Problems, by H. R. Tolley and M. J. B. Ezekiel, in Journal American Statistical Association, December, 1923.

Table V.—Chicago price of oats estimated from changes in the United States production plus carry over of oats and the index number ¹

Year beginning July 1	Percentage change over preceding year Farm products index x2 United States products tion plus carry over x3		Farm products index x2 carry over		$2.03x_{2}$	1.16x3	Esti- mated change in price	Same expressed in round numbers	Actual price	Esti- mated price	Residuals
1895					Per cent	Per cent	Cents 20	Cents	Cents		
1896	-2 +7 +5 +5 +7 +8 +1 0 0 +1 +1 0 +5 +2 +7 +7 +7 +7 +7 +7 +1 1 +3 +2 +10 +3 +3 +11 +10 1 1 1 1	+4 -3 +22 +10 -1 -14 +29 -12 +111 +10 -3 -21 +14 +20 +46 -15 -3 -3 -14 +20 -1 -1	-4. 06 +14. 21 +10. 15 +10. 15 +14. 21 +16. 24 +2. 03 0 +2. 03 0 +10. 15 +4. 06 +14. 21 +18. 27 -4. 06 -2. 03 +6. 09 +4. 06 +20. 30	-4. 64 +3. 48 -2. 32 -11. 60 +1. 16 +16. 24 +33. 64 +13. 92 -12. 76 -11. 60 -1. 16 -26. 68 -1. 62 +23. 20 -53. 36 +17. 40 +3. 48 -38. 28	-4. 50 +21. 89 +12. 03 +2. 75 +19. 57 +36. 68 -27. 41 +18. 12 -6. 53 -7. 40 +17. 83 +32. 62 +17. 25 -4. 21 -6. 10 +25. 37 -43. 07 +25. 66 +11. 78	-5 +22 +12 +3 +20 +37 -27 +18 -7 -7 +18 +33 +17 -44 -16 +25 -43 +26 +12	17 23 25 24 40 38 32 31 37 50 53 54 41 45 56 77 71 88	19 21 26 62 28 33 29 40 0 35 30 37 49 59 51 37 44 28 47 46 44	+2 -22 +1 +3 +4 -7 -5 +22 +3 -1 0 -1 +6 +7 +2 -6 -9 +6 -5 -1		
1920 1921 1922	-24 -25 +9	+20 -18 +5	-50.75 +18.27	+20.88 -5.80	$-25.67 \\ +16.67$	-26 +17	54 39 41	40 46	+1 +5		

¹ The equation is $x_1=4.20+2.03x_2-1.16x_3$

Table VI.—Monthly average cash prices of oats, Chicago, July, 1881, to June, 1923 1

Year	July	Aug.	Sept.	Oct.	Nov.	Dec.	Jan.	Feb.	Mar.	Apr.	May	June	Aver- age
	Cents												
1881-82	41	36	39	45	44	45	44	42	43	49	53	51	44
1882-83	56	48	33	34	35	38	36	39	41	42	41	38	40
1883-84	34	27	27	28	29	33	33	33	32	30	32	33	31
1884-85	30	27	25	26	26	24	27	29	28	31	35	33	28
1885-86	32	26	25	26	28	28	29	30	30	29	29	27	28
1886-87	29	27	25	25	26	27	23	25	24	27	26	26	26
1887-88	26	25	25	26	27	31	31	29	30	31	35	32	29
1888-89	31	26	24	24	26	26	25	26	25	23	23	23	25
1889-90	22	20	20	19	20	21	21	20	21	24	28	28	22
1890-91	30	37	37	41	43	43	43	46	51	55	51 31	41	43
1891-92	36	29	32	28	32	33	30	30	29	29 29	31	33	31
1892-93 1893-94	32 28	33 24	34 26	31 28	32 28	31 29	32 28	32 28	31 30	32	35	30 41	31 30
1894-95	39	30	30	28	25	30	30	28	29	30	29	29	30
1894-95	24	21	20	19	19	17	18	20	29	20	19	18	20
1896-97	17	17	16	18	19	18	17	16	17	18	18	18	17
1897-98	18	19	20	19	21	23	23	26	27	27	30	28	23
1898-99	23	22	21	23	26	27	27	28	27	27	27	25	25
1899-1900	25	21	22	23	23	23	23	23	24	25	23	23	23
1900-01	24	22	22	22	22	23	24	24	26	26	29	29	24
1901-02	29	36	35	35	39	46	46	44	44	43	43	44	40
1902-03	50	35	29	30	30	32	34	35	34	33	33	37	34
1903-04	36	33	35	37	35	35	38	41	41	40	40	40	38
1904-05	38	34.	31	30	30	30	31	31	32	30	31	31	32
1905-06	32	26	26	29	30	31	31	30	30	32	33	37	31
1906-07	37	30	32	33	33	34	36	39	42	42	34	45	37
1907-08	44	49	49	50	48	49	51	51	51	52	53	52	50
1908-09	53	48	50	48	49	50	51	54	55	56	60	58	53
1909-10	52	41	40	41	41	45	49	48	46	45	43	39	44
1910-11	42	37	34	33	33	33	33	32	31	33	35	39	35
1911-12	45	41	45	48	49	49	50	53	54	58	56	54	50
1912-13	51	39	34	34	34	34	34	35	34	36	39	41	37
1913-14	42	43	43	41	41	42	40	41	41	40	41	41	41
1914-15	38	42	50	48	50	49	54	59	58	58	54	50	51
1915-16	54	54	40	39	39	44	49	49	43	46	47	41	45
1916-17	42	45	47	51	57	53	57	57	61	70	71	67	56
1917-18	78	67	61	61	66	77	83	89	94	91	79	78	77
1918-19	79	72	72	70	74	74	68	61	65	70	72	71	71
1919-20	77	76	70	73	75	84	87	87	93	103	112	117	88
1920-21	102	76	65	56	52	50	45	43	44	39	39	39	54
1921-22	38	37	39	36	36	39	40	41	40	41	42	40	39
1922-23	39	35	39	43	45	46							
	1												

Averages of weekly high and low prices of No. 2 oats, Chicago Board of Trade. Annual reports.

Table VII.—Oats: Cash and future prices, per bushel, in cents, 1892-1921 1

Year when delivery is due	September prices of May oats	May cash price of oats	May prices of Septem- ber oats	June prices of Septem- ber oats	July prices of Septem- ber oats	August prices of Septem- ber oats	Septem- ber cash prices of oats
1892 1893 1894 1894 1895 1896 1897 1898 1899 1900 1900 1902 1903 1904 1905 1906 1907 1908 1909 1910 1911 1911 1912 1913 1914 1915 1916 1917 1918 1919 1919 1919 1919 1919 1919	Cents 32 37 31 35 21 19 23 22 23 (2) 38 32 39 35 30 34 45 42 42 42 42 42 48 47 54 47 54 38 51 61 (2) 73 66	Cents 31 30 30 35 29 19 18 30 66 22 29 44 36 42 311 33 34 66 55 59 41 34 55 55 58 58 37 68 68 67 70 112 39	Cents 29 27 26 28 (2) 18 24 21 (2) 26 29 31 1 28 30 31 28 33 34 34 33 44 35 45 55 (2) 66 66 74 1	Cents 31 26 30 29 18 18 21 21 (2) 26 29 30 30 35 37 38 44 47 40 41 40 40 40 40 40 40 40 40 40 40 40 40 40	Cents 31 25 29 23 177 18 20 20 20 24 32 33 34 33 34 41 36 36 38 40 57 77 77 40	Cents 34 24 30 20 117 18 220 25 35 27 33 36 47 47 48 37 36 42 43 39 45 56 67 73 68 69 95	Cents 33 26 29 19 16 20 21 21 22 22 22 35 26 37 32 28 32 49 40 33 44 33 42 48 37 46 59 72 70 63 39

¹ Arithmetic average of daily high and low quotations of No. 2 oats, 1892 to 1902; standard oats, 1903; contract grade, 1904 to 1921 (standard and No. 2 oats on contract grades). The quotations are taken from the Chicago Board of Trade Annual Reports. They are not available for earlier years.
² No quotations.

Table VIII.—Oats: United States Department of Agriculture estimates of acreage and of condition, 1895–1923

	Acreage,	Estimates of condition by months 2			
Year	preliminary estimate, June 1 1	June	July	Aug.	Sept
1895	Thousand acres 27, 878 27, 566 25, 730 25, 321 25, 608 27, 365 26, 315 28, 653 27, 732 27, 648 27, 688 27, 688 27, 688 27, 678 31, 491 31, 837 32, 422 234, 380 35, 250 37, 441 38, 383 40, 193 40, 780 43, 161 44, 475 42, 169 41, 032 44, 829 41, 822 40, 768	Per cent 84.3 98.0 98.0 98.0 98.0 98.7 91.7 85.3 90.6 85.5 89.2 92.9 92.9 88.7 91.1 87.0 89.5 92.2 86.9 88.8 93.2 93.2 87.8 88.5 7 85.5 85.6	Per cent 83. 2 96. 3 87. 5 92. 8 90. 0 85. 5 83. 7 92. 1 84. 3 89. 8 92. 1 84. 0 81. 0 85. 7 88. 3 82. 2 68. 8 89. 2 76. 3 84. 3 85. 5 87. 0 84. 7 77. 6 74. 4 83. 5	Per cent 84.5 87.3 86.0 84.2 90.8 85.0 73.6 89.4 79.5 86.6 90.8 82.8 84.5 76.8 85.5 81.5 85.7 90.3 73.8 79.4 91.6 81.5 87.2 82.8 87.6 87.6 87.6 87.6 87.6 87.6 87.6 87	Per cent 86.0 74.0 84.6 79.0 87.2 82.9 97.2.1 87.2 75.7 85.6 90.3 81.9 65.5 69.7 83.8 83.3 74.0 75.8 90.1 90.4 84.4 73.0 88.3 61.1 74.9 98.0 88.3

¹ The June 1 estimate of acreage is the only preliminary estimate of acreage made. ² Percentage of normal. See The Use of "Pars" and "Normals" in Forecasting Crop Production, by W. F. Callander and J. A. Becker, in Jour. Farm Economics, Oct., 1923.

Table IX.—Production statistics of wheat and rue

Year	United States produc- tion 1	World produc- tion 2 *	World carry over 3	World produc- tion plus carry over	Rye, world produc- tion 4
1890	Million bushels 378	Million bushels 1,964	Million bushels	Million bushels	Million bushels
1891 1892 1893 1894 1894 1895 1896 1897 1897 1898 1899 1900 1901 1902 1903 1904 1904 1905 1906 1907 1906 1907 1908 1909 1910 1910 1911 1911	585 528 4288 516 569 544 610 772 772 772 772 777 638 645 645 645 645 645 647 763 647 763 647 763	1, 964 2, 033 2, 242 2, 338 2, 420 2, 376 2, 303 2, 050 2, 821 2, 591 2, 463 2, 714 2, 902 3, 047 3, 150 2, 852 2, 852 2, 852 3, 320 3, 205 3, 320 3,	132 193 241 1219 192 181 116 112 218 210 176 152 144 165 146 180 220 133 106 157 157 157 157 157 157 157 157 157 157	2, 165 2, 417 2, 579 2, 639 2, 568 2, 484 2, 166 2, 933 3, 054 3, 158 3, 084 3, 138 3, 330 3, 072 2, 998 3, 426 3, 418 3, 430 3, 675 3, 888	1, 006 1, 238 1, 450 1, 1550 1, 1414 1, 450 1, 240 1, 557 1, 546 1, 394 1, 593 1, 611 1, 611 1, 612 1, 622 1, 534 1, 834 1, 834 1, 834
1914 1915 1916 1917 1917 1918	891 1,026 636 637 921 968	3, 226	163 147 355 330 261 307	3, 389	1, 526
1920 1921 1922 1923	833 815 862 1 793	⁵ 2, 884 3, 079 3, 096 3, 434	242 220 174 172	3, 126 3, 299 3, 270 3, 606	5 609 848 839 970

¹ U. S. Dept. Agr. Yearbooks. The 1923 figure is the August forecast.
² The countries included in the total, 1890–1914, are United Kingdom, Sweden, Denmark, Netherlands, France, Spain, Belgium, Canada, United States, British India, Japan, Argentina, Australia, New Zealand, Algeria, Italy, Germany, Austria, Hungary, Rumania, Russia. Source: U. S. Dept. of Agr., Bur. Agr. Econ., Div. Statistical and Historical Research.
³ See Table XI, Appendix.
⁴ Production of 14 countries, 1890 to 1914, including Sweden, Denmark, Netherlands, France, Spain, Belgium, Finland, Algeria, United States, Germany, Austria, Hungary, Rumania, Russia. Source: U. S. Dept. Agr. Bureau of Agricultural Economics, Division of Statistical and Historical Research.
⁵ Total world countries reporting and estimated. See U. S. Dept. Agr. unnumbered report, "The Wheat Situation," Russia omitted, additional countries included, 1920–1923.

Table X.—Wheat prices

Year beginning Aug. 1	Chicago price, average of daily high and low ¹	Chicago price, average of monthly high and low ²	Farm price, December ³	Liverpool price, average of monthly high and low 4	Bureau of Labor Statistics index of farm products ⁵	Chicago price, adjusted by farm products index
1890	Cents 97 89 73 60 57 61 70 97 70 69 73 72 75 90 110 86 77 95 114 115 99 105 93 127	Cents 97 88 73 60 588 62 74 101 71 69 74 73 75 89 106 88 79 100 113 115 101 105 100 92 129	Cents 84 62 54 49 51 72 81 58 59 62 63 70 92 75 67 87 99 103 90 90 83 81 109	Cents 111 115 86 75 68 78 78 88 116 86 86 87 87 90 6 95 7 98 93 110 120 120 120 120 120 120 120 120 120	75 72 70 66 61 58 57 61 64 67 72 78 80 80 84 86 92 1000 98 97 100 102 104 114 144	Cents 129 124 104 91 93 105 123 159 109 103 101 92 95 114 138 108 92 110 124 115 97 102 105 91
1916 1917 1918 1919 1920 1921 1922	193 219 235 251 200 127 122	194 225 237 272 199 138 124	162 206 210 227 172 106 101	224 235 240 215 223 149	156 204 224 224 171 128 139	124 107 105 112 117 99 88

¹ No. 2 Spring wheat, cosh July, 1890, to January, 1897; No. 2 wheat, January, 1897, to January, 1898; regular No. 2 January, 1898, to March, 1903; No. 2 red, March, 1903, to June, 1922. Average of daily high and low prices as quoted in the Chicago Board of Trade Annual Reports.

² Prices published in National Grange Monthly, July, 1921, p. 11. The grade is No. 2 Spring wheat. The prices were compiled from Chicago papers by a representative of the National Grange working in cooperation with the Bureau of Agricultural Economics, U. S. Department of Agriculture.

³ U. S. Dept. Agr., Yearbooks. December 1, farm price, 1890-91 to 1908-9; average yearly price, 1908-9

to 1922-23.

4 Compiled by Market Statistics Section, Bureau of Agricultural Economics, U. S. Department of Agriculture; 1890 to 1903, compiled from Broomhall's 1904 Corn Trade Year Book, p. 136; 1914 to 1920 from Broomhall's 1921 Corn Trade Year Book. Remainder of the table from Broomhall's Corn Trade News. Conversions at par, 1862 to 1912. Current exchange rate for remainder of period. Prices of red wheat supplemented with prices of American wheat for some months, the margin between which is practically negligible. See U. S. Dept. Agr., Yearbook, 1922.

5 Two-year average of Bureau of Labor Statistics calendar year relative of prices of farm products from 1890-91 to 1913-14. Average of monthly relatives, July to following June after 1914.

6 Five months' average.

Table XI.—Wheat: Estimated world visible supply on July 1 for the years

Year	Bushels	Remarks
891	132, 472, 385	To the "Corn Trade" figures were added 3,214,285 bushels for flour in the United Kingdom, 25,000,000 United States farm stocks, 2,800,000 other Europe, 709,000
		Argentina, and 1,735,000 Australia.
892	193, 225, 845	To the "Red Book" figures were added 55,000,000 United States farm stocks, 2,800,000 other Europe, 1,153,000 Argentina, and 2,213,000 Australia.
893	240, 671, 000	Added 50,000,000 United States farm stocks, 1,620,000 Argentina, and 2,507,000 Australia.
894	218, 901, 000	Added 40,000,000 United States farm stocks, 1,209,000 Argentina, and 1,880,000 Australia.
805	191, 513, 180	Added 914,000 Argentina and 1,233,000 Australia.
896		Added Argentina stocks on page 118, Corn Trade Yearbook 1901–02, and 1,410,000
		Australia.
897		Argentina same as 1896; Australia, 1,906,000 added.
898		Argentina same as 1896; Australia, 2,796,000 added.
899		Argentina same as 1896; Australia, 2,884,000 added.
900		Argentina same as 1896; Australia, 2,784,000 added.
901		Argentina included in "Red Book"; Australia, 3,367,000 added.
902		Added Australia, 2,685,000.
903		Added Australia, 862,000.
904	165, 123, 889	Added Australia, 5,163,000; Australia included remainder of time.
905	145, 967, 184	
906		
907		
908	133, 128, 000	
909	105, 532, 000	
910	157, 202, 000	
911	185, 185, 000	
912		
913		
914		
915		Australia out.
916	355, 192, 000	France, Germany, Belgium, Holland, Russia, Danubian States, other Europe out for remainder of time.
917	329, 579, 000	Stocks affoat, Argentina, Australia, and American stocks and United Kingdom only,
918	260, 953, 000	Same as 1917.
919	306, 539, 000	
920		
921	219, 769, 000	
	174, 342, 000	
923		Minneapolis Market Record. July 14, 1923.

U. S. Dept. Agr., Yearbook, 1922, p. 607. Australian average carry over, 1905-1914, inclusive, 5,433,000. Continent omitted 1916 to 1923; carry over averaged 13,584,000—1905–1914.

Table XI was compiled from data of Broomhall's Corn Trade News. Minneapolis Daily Market Record, and Chicago Daily Trade Bulletin. which is published in the Red Books of Howard, Bartels & Co., from 1892-1922 under heading of "Monthly Supply of Breadstuffs." The "visible" included stocks of wheat and flour afloat for United Kingdom and the Continent; stocks in store in United Kingdom, France, Germany, Belgium, Holland, Russia, Danubian States, other portions of Europe, Argentina, Australia, United States, and Canada. the "Red Book" total has been added United States farm stocks on The data for 1891 taken from the 1901-1922 Broomhall's July 1. Corn Trade Year Book, pages 114, 115, 116, 117, and 122. from "Red Book" were checked with Broomhall's Corn Trade Year Book figures from 1892 to 1901. The changes from the original data are noted after each number. The farm stocks of 1891–1894 were estimated; the remainder of the years are official.

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