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Estimating Location Values of Agricultural Land

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Abstract

“Bodenrichtwerte” reflect the average location value of land plots within a specific area. They constitute an important source of information that contributes to price transparency on land markets. In Germany, “Bodenrichtwerte” are provided by publicly appointed expert groups (Gutachterausschüsse). Using empirical data from Mecklenburg-Western Pomerania between 2013 and 2015, this article examines the relation between “Bodenrichtwerten” and statistically determined location values. It turns out that “Bodenrichtwerte” tend to underestimate location values of arable land by 11.5% on average. This underestimation can be traced back to the pronounced increase of land prices in the observation period. As an alternative to the expert-based determination of location values, we suggest a nonparametric smoothing procedure that rests on the Propagation-Separation Approach. The application of this data-driven procedure achieves an accuracy comparable to that of official “Bodenrichtwerte” at the one-year ahead prediction of location values without the requirement of expert knowledge.

Key Words

land value; adaptive weight smoothing; agricultural land markets; propagation-separation approach; Bodenrichtwert

1 Introduction

Information about realized prices is crucial for the price formation process on land markets. An important source of information that contributes to price transparency on land markets are location values, estimates for which (referred to as *Bodenrichtwerte*, BRW) are provided by publicly appointed expert groups (*Gutachterausschüsse*) in Germany. According to the Federal Building Code (*BAUGESETZBUCH*), BRW are intended to reflect the average location value (per square meter) of pieces of land. The purpose of these values is to reduce transaction costs related to real estate transactions by offering reliable benchmarks for purchases and taxation.

Unfortunately, three features of land markets impede the accurate estimation of location values. First, land markets are characterised by a relatively low liquidity. For example, in Germany on average only less than one percent of the agricultural area is sold each year (STATISTISCHES BUNDESAMT, 2015). Actually, it may happen that only a few or even no land transactions take place within a particular sub-district (*Gemarkung*) during one or two years. As a consequence, estimating location values typically warrants pooling observations from sub-districts for which one can assume a similar location value. In practice, this entails a bias-variance trade-off: by including weighted observations from other sub-districts, one can reduce variance, but if the assumption of equal location value is violated, considerable bias may be incurred. The second feature that impedes estimation of location values is that land is an extremely heterogeneous asset: its value depends on a variety of attributes and conditioning variables, such as soil quality, plot size, land use systems, or distance to cities.¹ This heterogeneity complicates a direct comparison of observed prices. The third characteristic that complicates the determination of BRW is the dynamics inherent to land markets. Changes in the location value of land may arise from changes in interest rates or agricultural product prices, technological change, or changes in legislation. To capture these dynamics, BRW are updated every two years at the latest. The method to be applied in this task is comparative analysis, i.e., pooling prices of similar plots and adjusting prices for deviations of the underlying plot to make them comparable. For this purpose, homogeneous sub-districts showing similar price determining attributes, so-called location value zones (*Bodenrichtwertzonen*), are defined.

In view of the aforementioned characteristics of land markets, it is quite obvious that expert groups face a challenging statistical estimation problem. Observed transactions have to be filtered to reflect market conditions, i.e., purchases between family members, forced sales, or seizure should be ruled out.

¹ See HÜTTEL et al. (2013) and the literature cited therein for an overview on land price determinants.

Moreover, prices that are untypical need to be identified as outliers and either adjusted or dropped. Finally, observed transactions need to be ‘translated’ to reflect typical land characteristics of the sub-district, which implies that observed prices have to be weighted or otherwise adjusted. While there are some clear procedures for filtering, much intuition is required for adjusting and weighting observed land prices when updating the location value estimates. In practice, expert knowledge comes into play at this point. In the case that no sufficient amount of transactions for pooling is available, ‘deductive methods’ may be applied (BUNDESMINISTERIUM FÜR VERKEHR, BAU UND STADTENTWICKLUNG, 2011). These include the consideration of past location values and general market trends.

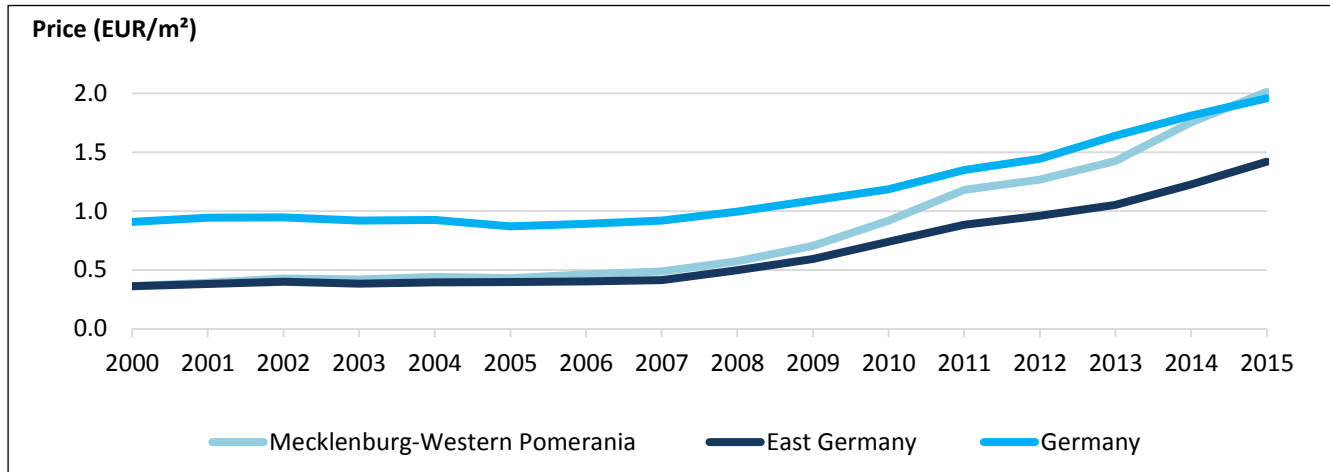
From a scientific point of view, the question arises if BRW actually reflect location values and how the procedure applied by the experts can be assessed. In particular, it would be interesting to analyse if BRW show systematic biases and if so, where and why these biases occur.² Any answer to these questions has to cope with the problem that location values are hypothetical values and thus unobservable. Nonetheless, given their definition, one would expect that BRW do not systematically deviate from realized prices in a location value zone.

Against this background the contribution of this paper is twofold. First, we aim at the evaluation of BRW as indicators of location values of agricultural land through a comparison of BRW and sample statistics of observed land prices. Second, we propose a statistical smoothing procedure as a data driven alternative to the expert-based approach. More specifically, we make use of an adaptive smoothing procedure that has been introduced as the “Propagation-Separation Approach” (PSA) by POLZEHL and SPOKOINY (2006) into the literature. This method was originally developed as “Adaptive Weights Smoothing” in the context of image denoising (POLZEHL and SPOKOINY, 2000). Recently, it has also been used in geology for the estimation of seismic parameter fields (GITIS et al., 2015). The paper most similar to ours is KOLBE et al. (2015) who use PSA for the estimation of land values in an urban context. We follow their statistical procedure, but in contrast to KOLBE et al. (2015) we create a benchmark that allows us to compare the BRW with

the PSA-based estimation. Moreover, we assess the predictive performance of the BRW and PSA in terms of out-of-sample evaluation. PSA is a nonparametric regression method that allows separating the underlying structure in the data from distorting noise by means of an iterative locally adaptive smoothing algorithm. Unlike conventional smoothing algorithms, such as fixed-bandwidth kernel regression, PSA does not only consider the distance between two locations when determining the weight of observations; rather, it adds a second component that takes into account the difference in resulting regression estimates. The attractiveness of PSA is based on an appealing statistical property: the estimator obeys a “small modelling bias condition” meaning that it shows the smallest variance given a predetermined bias which can be controlled by the econometrician (POLZEHL and SPOKOINY, 2006). Thus, PSA addresses the variance-bias trade-off in pooling observations from different sub-districts. Previous applications have documented that PSA performs well, if data show large homogeneous zones that are separated by sharp discontinuities (BECKER and MATHÉ, 2013). In contrast, SHEN et al. (2016) report that PSA has difficulties to identify outliers in otherwise homogeneous data. Thus, it is not clear whether PSA constitutes a viable alternative to the expert-based determination of location values. The application and the evaluation of this rather new statistical method constitutes the second contribution of our study. We note that we do not aim at developing a superior statistical method in order to substitute BRW; rather, we are interested in exploring if PSA may be used as a complement or a benchmark for official BRW.

The remainder of the article is organized as follows: Section 2 describes the land transaction data from Mecklenburg-Western Pomerania that we use as the empirical basis of our analysis. Afterwards, we derive a benchmark for assessing the performance of location value estimators. In Section 3, we analyse whether BRW show a significant bias and what factors this hinges on. In particular, we are interested in whether there are any significant differences in bias between different expert groups. In Section 4, we introduce the PSA method in general and demonstrate how it can be applied to our data. Section 5 presents the results of an out-of-sample forecast application, which compares the performance of BRW and PSA at the one-year ahead prediction of location value. The paper ends with an assessment of the current practice of calculating BRW and answers the question if the use of formal statistical procedures can improve the informational content of BRW.

² Biases of BRW could be rooted in the underlying methodological procedure. Apart from that, expert groups might have a tendency to update BRW conservatively in phases of booming land prices to dampen further price increases.

Figure 1. Prices for arable land 2000–2015 in Mecklenburg-Western Pomerania, East Germany, and whole Germany

Source: STATISTISCHES BUNDESAMT

2 Empirical Data and Derivation of a Benchmark

Mecklenburg-Western Pomerania is one of the former East German states and is located in the northeast of Germany. Its land market is characterised by one of the highest turnover rates in Germany: in 2014, 2.7% of the agricultural land were sold, whereas the average in Germany amounts to 0.8%. About 30% of the transactions are conducted by the Bodenverwertungs- und -verwaltungs GmbH (BVVG). As in most German states, the prices for agricultural land experienced a strong rise after 2007: the price for arable land increased from almost 0.50 EUR/m² in 2007 to around 2 EUR/m² in 2015, which means a growth by factor 4 (see Figure 1). Remarkably, the prices in Mecklenburg-Western Pomerania stagnated around the average prices in East Germany for a long period, but have caught up to the average prices for the whole of Germany since 2007. This means that the increase in prices was much stronger in Mecklenburg-Western Pomerania than in other East German states.

In this study, we use a data set of purchases of arable land in Mecklenburg-Western Pomerania through the years 2013–2015.³ We drop some transactions that are labelled as ‘unsuited to analysis’ since they took place between family members or show other irregularities that mark them as not being representative. We also cut off prices below the first per-

centile and above the 99th percentile for each year from 2013–2015. This serves to remove extreme prices, which are unrealistic for agricultural land and are therefore most likely affected by some sort of error, e.g., a misplaced decimal point, or are a very untypical sale.⁴ Altogether, we obtain 4,374 observations over three years. The summary statistics in Table 1 depict an almost linear increase in mean land prices of about 0.23 EUR/m² from 2013 to 2015. The distribution of prices in the years 2013–2015 is depicted in Figure 2. The spatial unit of analysis that is used for location value estimation is the sub-district (*Gemarkung*), a historic administrative unit that is usually situated at a sub-municipality level. In Mecklenburg-Western Pomerania, there are 3,557 sub-districts altogether, which implies that in most years there is not even one observation per sub-district available. This gives rise to the necessity of using observations from several years for location value prediction. Experts may use deductive methods and their experience for this purpose. For PSA, we will pool time-adjusted prices from 2013 and 2014 as the basis for predicting the location values of 2015.

³ Data source: *Landesweite Datensammlung des Oberen Gutachterausschusses für Grundstückswerte im Land Mecklenburg-Vorpommern (OGAA M-V)*

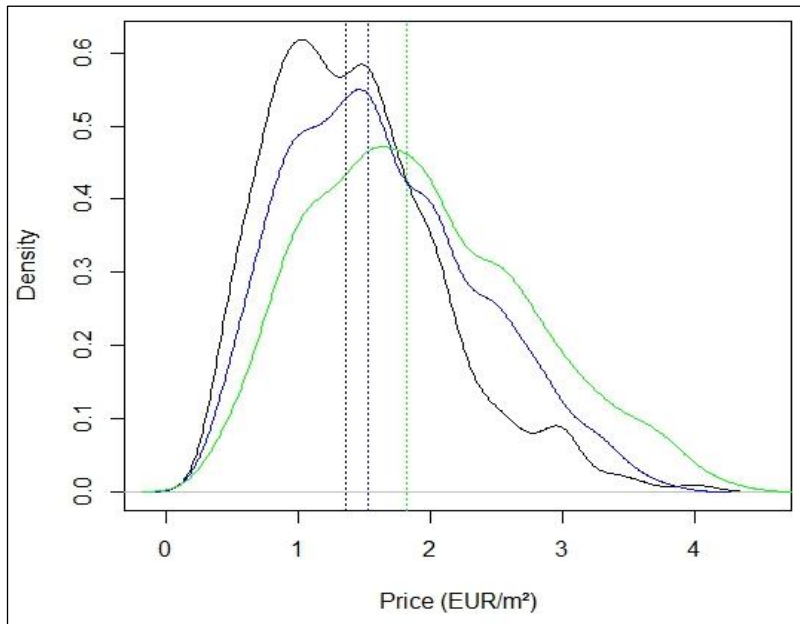
⁴ While the values we cut off at the upper price range are clearly outliers (the 99th percentile differs from the mean by up to 3.5 standard deviations), the first percentile only differs by 1.5 standard deviations on average. We consider the prices below that mark unrealistically low, but to safeguard against distortions introduced by a hypothetical inadequate outlier removal, we also performed all the computations in this paper on the data without removing data below the first percentile. The results differ only slightly and are equivalent in terms of our research questions.

Table 1. Summary statistics of observed purchase prices, plot size and soil quality of sold pieces of land

Summary statistics	Plot size (ha)	Soil quality	Prices (EUR/m ²)	Prices 2013 (EUR/m ²)	Prices 2014 (EUR/m ²)	Prices 2015 (EUR/m ²)
Mean	8.89	38.18	1.64	1.43	1.64	1.92
Standard Deviation	19.94	8.14	0.76	0.66	0.72	0.82
Observations	4,374	4,278	4,374	1,651	1,479	1,244

Note: Soil quality is measured on a scale from 0 to 120 in ascending order. Different total counts result from missing soil quality values in the data set. In the subsequent analyses, the largest possible datasets are used.

Source: own elaboration

Figure 2. Density plots of price distribution for the years 2013, 2014 and 2015

Note: 2013 (black), 2014 (blue) and 2015 (green). Dashed lines indicate the median. The kernel bandwidth used for estimating the densities is 0.13.

Source: own elaboration

In order to assess the predictive performance of BRW and PSA, we need to establish a benchmark, given that the true location values are not observable. We call this benchmark empirical location values (ELV). An important property of ELV is that by design they are an unbiased estimator of location value. Briefly, they are obtained by calculating the average price of sold arable land in a sub-district in a given year. However, we first perform an adjustment of the observed purchase prices. This step serves to reduce the variance of ELV by shifting observed prices towards the expected value, which is particularly useful to mitigate extreme prices and to some extent should compensate the fact that in many sub-districts only few transactions are observed per year. Adjustment consists in subtracting from the observed prices the effects of certain individual plot characteristics, e.g.,

an above-average fertility, so that we obtain the price that would have been realised had the transacted plot been ‘typical’ for its sub-district.

To calculate the effects of conditioning variables, we set up a linear regression model for (log) land-prices. We consider soil quality and plot size as covariates. Soil quality is known to have a considerable influence on land prices (e.g., HENNIG et al., 2014). Plot size on the other hand is included because we hypothesize that large plot sizes tend to be sold by the federal trust (BVVG) that is in charge of administering formerly state owned land. It is not unlikely that the prices from these sales differ from sales among private parties (HÜTTEL et al., 2016). Given the observed linear trend in our data, we also account for temporal effects by including time dummy variables. Moreover, regional dummy variables are

included to reduce the risk of omitted variable bias. Through temporal and spatial dummy variables, all unobserved effects that are constant over time or space are captured. Finally, we also include the quadratic soil quality and plot size terms, since we found that the corresponding model achieves a lower BIC than the one with only the linear terms. Hence, we fit the following log-linear regression model to our data (see next paragraph for details):

$$\begin{aligned}
 \log(p_{i,j,t}) = & \alpha_1 s_{i,j,t} + \alpha_2 s_{i,j,t}^2 + \beta_1 q_{i,j,t} \\
 & + \beta_2 q_{i,j,t}^2 + \gamma I_{i,j,t,2014} \\
 & + \delta I_{i,j,t,2015} + \sum_{k=2}^6 \vartheta_k J_{i,j,t,k} \\
 & + b + \varepsilon_{i,j,t}
 \end{aligned} \quad (1)$$

where $s_{i,j,t}$ denotes plot size of transaction i in sub-district j in year t , $q_{i,j,t}$ denotes the corresponding soil quality, $I_{i,j,t,2014}$ and $I_{i,j,t,2015}$ are time dummy variables indicating the year the transaction took place in. The $J_{i,j,t,k}$ are dummy variables indicating which region the area is located in, and b is a constant. The subsequent adjustment step corrects actual prices for effects of above-average or below-average values of soil quality and plot size:⁵

$$\begin{aligned} \log(\tilde{p}_{i,j,t}) = & \log(p_{i,j,t}) - \hat{\alpha}_1(s_{i,j,t} - \bar{s}_j) \\ & - \hat{\alpha}_2(s_{i,j,t}^2 - \bar{s}_j^2) \\ & - \hat{\beta}_1(q_{i,j,t} - \bar{q}_j) - \hat{\beta}_2(q_{i,j,t}^2 - \bar{q}_j^2) \end{aligned} \quad (2)$$

where $\tilde{p}_{i,j,t}$ denotes adjusted prices. We determine average soil quality \bar{q}_j and average plot size \bar{s}_j of sub-district j by taking the mean soil quality and plot size of all sold plots in that sub-district from 2013–15 (see Table 1 for summary statistics). Note that we do not adjust for temporal effects, because we want to estimate time-varying location values. In a final step, the ELV $\tilde{\theta}_{j,t}$ of sub-district j in year t is derived by re-transforming the adjusted log-price with the exponential and taking the sub-district- and year-wise mean of the adjusted prices:

$$\tilde{\theta}_{j,t} = \frac{1}{n_{j,t}} \sum_{i=1}^{n_{j,t}} \tilde{p}_{i,j,t} \quad (3)$$

where $n_{j,t}$ denotes the number of observations in sub-district j in year t .

The model in Equation (1) is estimated with OLS yielding highly significant effects for all covariates, as displayed in Table 2. The effects of the years 2014 and 2015 reflect the upward trend of land prices observed in our data. Soil quality has a positive effect on land prices as expected. Plot size, too, shows a positive effect. We are aware that the rather simple model in Equation (1) may not capture heterogeneity of land prices completely, but the moderate model fit suggests

that ELV constitute a fair approximation of the true location value.

Table 2. Regression model for price adjustment

Covariate	Effect (EUR/m ²)	Standard error
Intercept	-0.8972***	0.1280
Year 2014	0.1240***	0.0153
Year 2015	0.2592***	0.0158
Soil Quality	0.0412***	0.0070
Soil Quality Squared	-0.0003***	9.5635e-05
Plot Size (ha)	0.0082***	0.0008
Plot Size Squared (ha)	-2.2212e-05***	5.2412e-06
Expert Group 2	0.2541***	0.0208
Expert Group 3	0.1148***	0.0239
Expert Group 4	0.2027***	0.0276
Expert Group 5	-0.0539**	0.0245
Expert Group 6	-0.0686***	0.0217

Note: The effects refer to log-prices. $R^2 = 0.30$. *** denotes significance at the 1% level, ** at the 5% level. Standard errors are robust.

Source: own elaboration

To measure the performance of a location value predictor, we use the mean squared error (MSE) and the bias, as explained in the following. The calculation basis for these measures is the so-termed ‘observed deviation’, which denotes the deviation $\hat{\theta}_{j,t} - \tilde{\theta}_{j,t}$ of a predicted value $\hat{\theta}_{j,t}$ from the ELV $\tilde{\theta}_{j,t}$, that we observe for each sub-district j and year t . Being a common measure of predictive performance, the MSE is usually computed with regard to the true value that is to be estimated. Seeing as true location values are not observable, however, we can only compute the MSE with respect to ELV. The relationship between the MSE with respect to a benchmark and the MSE with respect to the true location value can be derived from the decomposition $MSE = E[(\hat{\theta} - \theta)^2] = E[(\hat{\theta} - \tilde{\theta})^2] + E[(\tilde{\theta} - \theta)^2] + 2E[(\hat{\theta} - \tilde{\theta})(\tilde{\theta} - \theta)]$.

More than in the MSE itself, we are interested in the MSE difference between two predictors $\hat{\theta}_1$ and $\hat{\theta}_2$. We have $MSE_2 - MSE_1 = E[(\hat{\theta}_2 - \tilde{\theta})^2] - E[(\hat{\theta}_1 - \tilde{\theta})^2] + 2E[(\hat{\theta}_2 - \hat{\theta}_1)(\tilde{\theta} - \theta)]$. If the deviations $(\hat{\theta}_2 - \hat{\theta}_1)$ and $(\tilde{\theta} - \theta)$ have a low correlation, then $E[(\hat{\theta}_2 - \hat{\theta}_1)(\tilde{\theta} - \theta)] \approx E[(\hat{\theta}_2 - \hat{\theta}_1)]E[(\tilde{\theta} - \theta)] = 0$.⁶ It follows that the MSE with respect to the

⁵ The fact that average soil quality and average plot size refer to sub-districts (Gemarkungen) and not to location value zones (Bodenrichtwertzonen) may drive a wedge between BRW and ELV. However, we expect this potential deviation to be small, since location value zones, which typically comprise several sub-districts, are by definition regions of homogeneous natural conditions.

⁶ We have $E[(\tilde{\theta} - \theta)] = 0$, because ELV is an unbiased location value estimator.

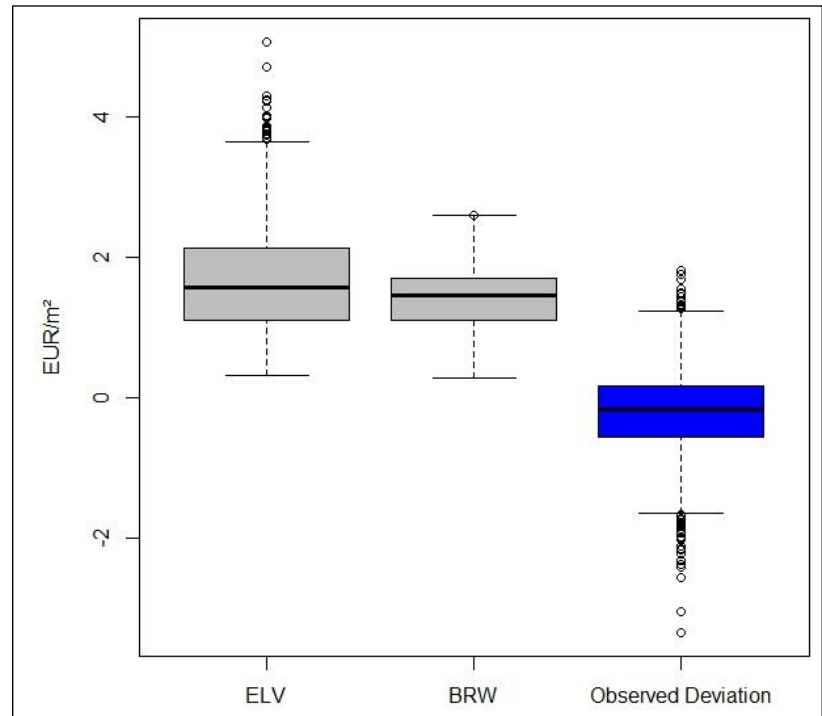
benchmark (i.e., computed on the basis of the observed deviation) is equivalent to the MSE with respect to the true location value for comparing predictors. Therefore, we use the MSE with respect to ELV as a measure of performance in this study. Finally, we are interested in the bias of a predictor, which we estimate with the mean observed deviation.

3 Analysing BRW Bias and Deviations from Empirical Location Values

In this section, we will have a closer look at BRW as one-year ahead predictor with the goal of assessing bias and identifying the factors that explain the observed deviation. It is important to note that our data set does not contain BRW for all sub-districts, so we have to perform this analysis on the subset ('BRW test set') of sub-districts and years for which we have a BRW and at least one suitable transaction. This leaves us with 900 (in 2013), 664 (in 2014) and 808 (in 2015) sub-districts, respectively.

Figure 3 displays boxplots of ELV, BRW, and the observed deviation of BRW. We find that compared to ELV, BRW show a smaller variability as well as a lower price level, which indicates an underestimation of location values. We, therefore, expect to find a significant bias for BRW. For the test set, we obtain for BRW a bias of -0.22 EUR/m². This means an underestimation by 11.5% in relation to average land prices in 2015. In order to infer whether this figure is statistically significant, we perform a one-sample t-test for the null hypothesis of zero bias. From the resulting p-value $< 10^{-15}$ we conclude that BRW has a significant, negative bias. To make our result more robust to violations of the normality assumption underlying the t-test, we also perform Wilcoxon's signed-rank test for the null-hypothesis of the median being equal to zero. This test only requires the weaker assumption that the distribution of the observed deviation is symmetric, which is approximately given, as illustrated by Figure 3. Here again we obtain a p-value $< 10^{-15}$, which corroborates the previous result. This shows that BRW actually tend to underestimate location values.

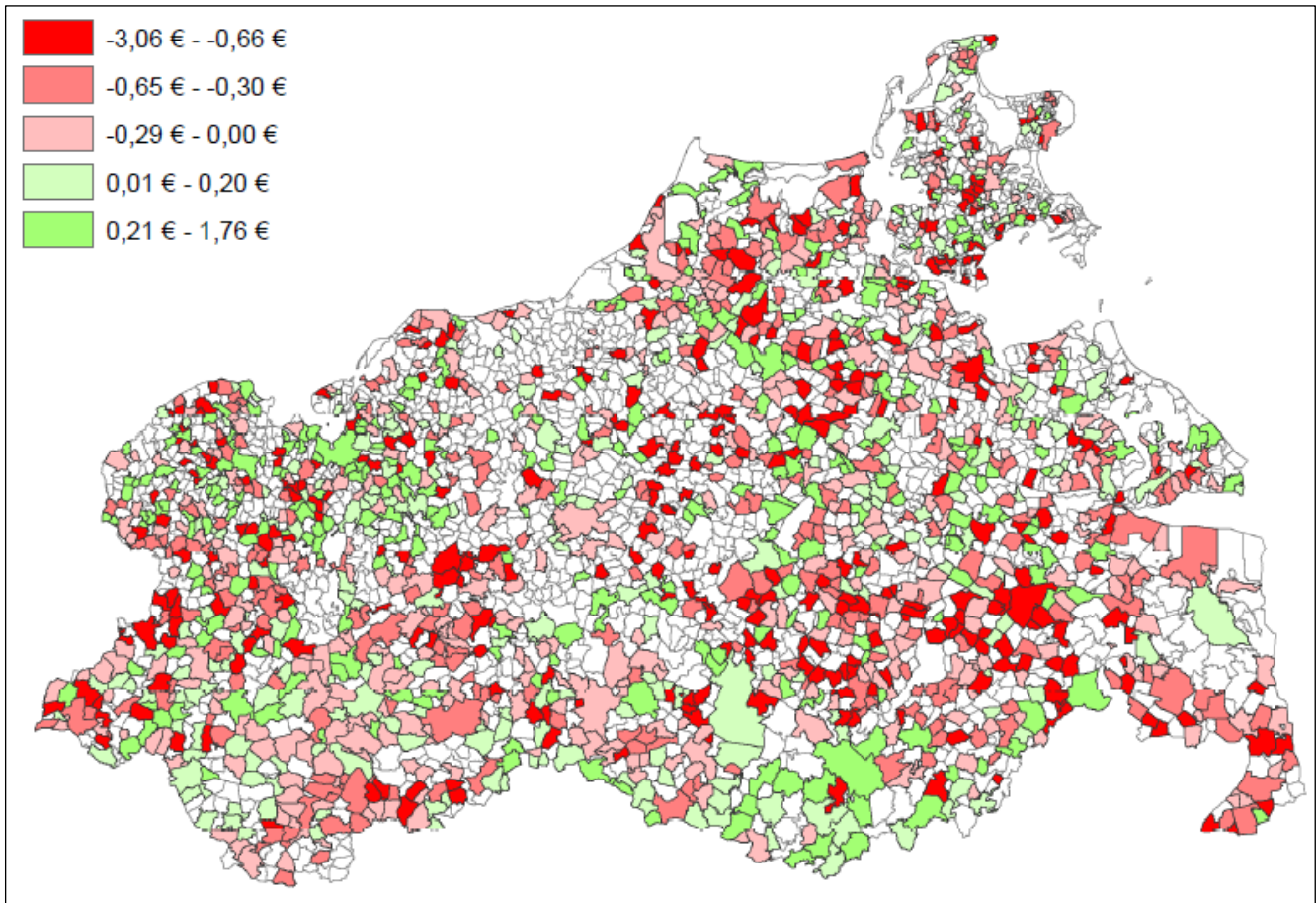
Figure 3. Distribution of ELV and BRW, as well as observed deviation in the BRW test set



Source: own elaboration

Figure 4 depicts the spatial distribution of observed differences between BRW and ELV. Apparently, there are some regional clusters, in particular in the Southern half. This observation suggests that systematic factors exist that explain the bias of BRW. To analyse the observed deviation of BRW from ELV further, we develop a linear regression model for the absolute value of the observed deviation – this does not cover the direction of the deviation, but only its magnitude. To determine what factors lead to an over- or underestimation, we furthermore perform a logistic regression of the sign of observed deviation against the same factors. As explanatory variables in both models, we consider the indicators of average soil quality and average plot size computed as in Equation (2), a time dummy and a categorical variable indicating which expert group determined the BRW.⁷ The rationale of choosing these covariates is as follows: one might conjecture that experts tend to oversmooth location values in areas with high soil quality, i.e., high land prices. Likewise, experts may have difficulties to smooth prices for small plots, which are often sold at high prices (per square meter). Moreover, since BRW are not continuously updated, they may lag

⁷ There are six expert groups in our BRW test set, with 506, 300, 462, 389, 259, and 552 observations, respectively.

Figure 4. Mean deviation of BRW from ELV per sub-district from 2013 to 2015

Note: Categories are based on quintiles. The blank sub-districts are owing to a lack of BRW values and/or transactions for our analysis.
Source: own elaboration

behind the actual development of location values, particularly during a period of booming prices. Finally, the expert groups themselves may have an impact on the bias, because BRW are not calculated with a clear algorithm but involve personal judgements that may differ among expert groups. However, the effect of this variable has to be interpreted with caution, because it is difficult to separate the impact of experts from unobserved regional effects. As both expert group and year are categorical variables and we use a model without a constant, we have to exclude one dummy variable from the model. We chose the time dummy for 2013, which is then the reference year. All expert group dummies are included so that they can be interpreted as regional fixed effects. To better quantify the regional effects, we use centred versions of the variables 'average plot size' and 'average soil quality' by subtracting their individual means.

Table 3 summarises the results of the regression model estimated with OLS. Since a Breusch-Pagan test rejected the hypothesis of homoscedastic residuals (p-value 5.817e-08), we computed robust standard

errors for the estimated coefficients. Both years as well as average plot size and average soil quality are significant at least at the 5% level. Note that we have already adjusted ELV for the effects of soil quality and plot size of individual transactions. The effects of this regression model, therefore, refer to properties of a sub-district, not of transactions. The effect of average plot size is significant at the 1% level, yet – at less than 0.01 EUR/ha and 0.05 EUR for a sub-district with mean average plot size \bar{s}_j of 9.77 ha – rather small in magnitude. Average soil quality has an effect of 0.16 EUR/m² for a sub-district of mean average soil quality \bar{q}_j of 38.94. Temporal effects are in the same order of magnitude as average soil quality. The magnitude of bias in BRW increases with every year, which we attribute to the linear increase in mean land prices that we have observed between 2013 and 2015. It seems as though BRW do not sufficiently take market trends into account. As for expert effects, we find that all expert groups show effects significant at the 1% level, ranging from 0.36 EUR/m² to 0.48 EUR/m². This means that there is a significant deviation in

2013 for all expert groups, which even increases in the following years. To determine, however, if a systematic over- or underestimation is present, we perform a logistic regression.

Table 4 summarises the effects of our covariates on the probability of BRW overestimating (positive sign) or underestimating (negative sign) location value. We find that average plot size shows a significant negative effect, meaning that the larger transacted plots in a sub-district on average, the more does BRW tend to underestimate its location value. The results for average soil quality do not show any significant effect for the direction of the bias. Finally, we see that all expert groups tend to underestimate location values in 2013,

even though this effect is comparatively weak and not significant for Group 4. In the years 2014 and 2015, no significant change occurs in this regard.

To summarise the findings of this section, our analysis shows that there is a significant negative bias in BRW – meaning that experts systematically underestimate location value in our BRW test set. This underestimation may be linked to the fact that in the years covered by our study, we observe a nearly linear increase in land prices, suggesting that experts do not sufficiently take the trend into consideration, which is corroborated by our regression analysis of BRW deviation from ELV. This analysis has further shown that high average soil quality in a sub-district likewise increases deviation, but in both directions; market trend therefore does not appear to be the only source of erroneous assessment, but it accounts more than other factors for the observed bias. Finally, we have found some heterogeneity between expert groups, which can also be interpreted as regional heterogeneity.

Table 3. Coefficients of absolute value of BRW deviation (OLS linear regression).

Covariate	Coeff.	Std. error
Year 2014	0.0496**	0.0207
Year 2015	0.1084***	0.0199
Avg. Plot Size (ha)	0.0061***	0.0008
Avg. Soil Quality	0.0041***	0.0015
Expert Group 1	0.4493***	0.0204
Expert Group 2	0.4531***	0.0299
Expert Group 3	0.4813***	0.0232
Expert Group 4	0.4630***	0.0266
Expert Group 5	0.4135***	0.0260
Expert Group 6	0.3645***	0.0228

Note: Dependent variable is the absolute value of deviation. $\rho^2 = 0.09$. ** and *** denote significance at the 5 and 1% levels, respectively. Standard errors are robust.

Source: own elaboration

Table 4. Coefficients of direction of BRW deviation (logistic regression).

Covariate	Coeff.	Std. error
Year 2014	0.0215	0.1107
Year 2015	0.0995	0.1034
Avg. Plot Size (ha)	-0.0378***	0.0054
Avg. Soil Quality	-0.0068	0.0077
Expert Group 1	-0.6761***	0.1124
Expert Group 2	-0.9148***	0.1645
Expert Group 3	-0.5953***	0.1174
Expert Group 4	-0.0762	0.1378
Expert Group 5	-1.0220***	0.1541
Expert Group 6	-0.6559***	0.1208

Note: Dependent variable is the sign of deviation (1 = non-negative, 0 = negative). The model has been fit with ML. Nagelkerke pseudo- $R^2 = 0.06$. *** denotes significance at the 1% level.

Source: own elaboration

4 A Propagation-Separation Approach for Estimating Location Value

In the introduction to this paper, we have pointed out that data scarcity requires to pool observations from different sub-districts to estimate location values. Depending on how the pooling is carried out, it trades a reduced variance for an increased bias. In the previous section, we have seen that BRW show a relatively low variance compared to the benchmark, but at the same time are afflicted by a significant bias. In the present section, we introduce a statistical procedure, which unlike BRW selects the sub-districts used for pooling in a purely data-driven way for every sub-district.

The “Propagation-Separation Approach” (PSA; POLZEHL and SPOKOINY, 2006) is an iterative, adaptive procedure based on local constant regression. The underlying idea of this approach is to find for every point x_i a maximal local neighbourhood in which the local constant parametric assumption is not violated – in other words, in which we can assume equal location value. At the beginning of the procedure, a small neighbourhood $U^0(x_i)$ of every point x_i is considered to estimate the location value $\theta(x_i)$.⁸ Afterwards, in

⁸ For our analysis, the initial neighbourhood includes only x_i itself.

each step k , we update the initial location value estimate by including new points x_j from an extended neighbourhood $U^k(x_i)$; but those candidates x_j are tested for homogeneous location value and only used for re-estimation of location value if the hypothesis of local homogeneity $\theta(x_i) = \theta(x_j)$ is not rejected. This iterative procedure is continued until we reach a pre-defined maximal radius of the neighbourhood.

Following KOLBE et al. (2015), the underlying local regression model for estimating the location values can be described as

$$y_i = \theta(x_i) + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma_i^2) \quad (4)$$

where y_i denotes the observed log price of agricultural land, x_i is a vector of explanatory variables which determine the distribution of observation y_i . It is worth mentioning that PSA in general would be able to detect stable trends as well, which is not done here due to the short observation period of three years. This requires the specification of an appropriate parametric model. When Equation (4) is assumed to be a local parametric model such as a time trend model, PSA can determine the longest homogeneous time intervals where the same parameter coefficients hold. In fact, PSA has been successfully applied to capture temporal structure breaks in finance and insurance (SHEN ET AL., 2016; CHEN and NIU, 2014; CHEN et al., 2010). Since we are interested in finding sub-districts with homogeneous location values, x_i simply refers to location coordinates $[x_{1i}, x_{2i}]$ in our case.⁹ In a local regression model, the local parameter $\theta(x_i)$ can be estimated by the weighted maximum likelihood estimation where a nonnegative weight $w_{ij} = w_{ij}(x_i) \leq 1$ is given to each observation y_j , $i, j = 1, \dots, n$. The corresponding local maximum likelihood estimator for a fixed x_i is given by:

$$\tilde{\theta}(x_i) = \underset{\theta}{\operatorname{argmax}} \sum_{j=1}^n w_{ij}(x_i) \log p(y_j, \theta), \quad (5)$$

where $p(\cdot, \theta)$ denotes the density function. If the density function $p(\cdot, \theta)$ belongs to the exponential family, for instance a Gaussian distribution, POLZEHL and SPOKOINY (2006) have shown that the explicit solution of (5) is in fact a Nadaraya-Watson estimator:

$$\tilde{\theta}(x_i) = \frac{\sum_{j=1}^n w_{ij}(x_i) y_j}{\sum_{j=1}^n w_{ij}(x_i)}. \quad (6)$$

As above mentioned, the PS approach is an iterative procedure, and in each iteration step, the local estimator is defined as a weighted mean of observations. Therefore, in iteration step k (i.e., within the neighbourhood $U^k(x_i)$), the adaptive local estimator $\tilde{\theta}^k(x_i)$ is

$$\tilde{\theta}^k(x_i) = \frac{\sum_{j=1}^n w_{ij}^k(x_i) y_j}{\sum_{j=1}^n w_{ij}^k(x_i)}. \quad (7)$$

The main advantage of the PS approach arises from the construction of the weights $w_{ij}^k(x_i)$. The determination of weights in the PS approach not only considers the likeness of the data with the sub-district of interest, but also controls the bias possibly introduced from the extension of data samples. To be specific, the weights depend on the product of two components: the location component K_{loc} and the homogeneity component K_{hom} :

$$w_{ij}^k = K_{\text{loc}}(l_{ij}^k) K_{\text{hom}}(s_{ij}^k), \quad (8)$$

where $K_{\text{loc}}(\cdot)$ and $K_{\text{hom}}(\cdot)$ are two kernel functions that are non-negative and strictly monotonically decreasing on the support $[0, 1]$, for example the triangular kernel function. Similar to the standard nonparametric regression, the argument in the location component K_{loc} is the Euclidean distance measure between the locations i and j divided by the bandwidth h^k :

$$l_{ij}^k = \frac{\rho(x_i, x_j)}{h^k} \quad (9)$$

On the other hand, s_{ij}^k in the homogeneity component is a statistical penalty:

$$s_{ij}^k = \frac{T_{ij}^k}{\lambda}, \quad (10)$$

where T_{ij}^k is the test statistic for a constant local parametric estimate and λ is the critical value of the test statistic T_{ij}^k . The homogeneity component $K_{\text{hom}}(s_{ij}^k)$ becomes relevant for controlling the bias when extending the size of neighbourhood $U^k(x_i)$. To test the hypothesis of local homogeneity $\theta(x_i) = \theta(x_j)$ at each step k , the estimates $\tilde{\theta}_i^{k-1}(x_i)$ and $\tilde{\theta}_j^{k-1}(x_j)$ obtained from the previous iteration is compared.

⁹ We use the coordinates of a sub-district's centre point as coordinates of the sub-district.

Following POLZEHL and SPOKOINY (2006) and BECKER and MATHÉ (2013), the test statistic T_{ij}^k is constructed based on the Kullback-Leibler divergence between the pointwise parameter estimates of the previous iteration step at two different points. Formally it states

$$T_{ij}^k = N_i^{k-1} \mathcal{KL}(\tilde{\theta}_i^{k-1}, \tilde{\theta}_j^{k-1}) \quad (11)$$

where $N_i^k = \sum_{j=1}^n w_{ij}^k(x_i)$. The decision rule of the test requires to compare T_{ij}^k with the corresponding critical values λ . The null hypothesis of parameter homogeneity is rejected if $T_{ij}^k > \lambda$. As a result, $s_{ij}^k = \frac{T_{ij}^k}{\lambda} > 1$, $K_{\text{hom}}(s_{ij}^k) = 0$ and $w_{ij}^k = 0$, i.e., observation x_j does not belong to $U^k(x_i)$ and will not be used to estimate $\theta(x_i)$. These two characteristics of the PS approach are very desirable: it extends the homogeneous neighbourhood with non-zero weights to reduce the variance of the estimates, and separates every two regions with different parameter values to control the bias.

In summary, the procedure for a fixed location x_0 is provided as follows:

- 1) Start with the smallest initial bandwidth h^0 , compute the initial estimate $\tilde{\theta}^0(x_i)$ according to (6) with $w_{ij}^0 = K_{\text{loc}}(l_{ij}^0)$. $N_i^0 = \sum_{j=1}^n w_{ij}^0(x_i)$
- 2) For $k = 1$, the bandwidth is extended to h^1 . Calculate the components $l_{ij}^1 = \frac{\rho(x_i, x_j)}{h^1}$ and $s_{ij}^1 = \frac{T_{ij}^1}{\lambda} = \lambda^{-1} N_i^0 \mathcal{KL}(\tilde{\theta}_i^0, \tilde{\theta}_j^0)$. Then derive the adaptive weights $w_{ij}^1 = K_{\text{loc}}(l_{ij}^1) K_{\text{hom}}(s_{ij}^1)$ and estimate $\tilde{\theta}^1(x_i)$.
- 3) For $k \geq 2$, the bandwidth increase to h^k . Derive the adaptive weights $w_{ij}^k = K_{\text{loc}}(l_{ij}^k) K_{\text{hom}}(s_{ij}^k)$ with $l_{ij}^k = \frac{\rho(x_i, x_j)}{h^k}$ and $s_{ij}^k = \frac{T_{ij}^k}{\lambda} = \lambda^{-1} N_i^{k-1} \mathcal{KL}(\tilde{\theta}_i^{k-1}, \tilde{\theta}_j^{k-1})$ and $N_i^k = \sum_{j=1}^n w_{ij}^k(x_i)$. Then estimate $\tilde{\theta}^k(x_i)$.
- 4) The procedure stops if $k = k^*$, otherwise $k = k + 1$. k^* indicates that the bandwidth h^k reaches the pre-defined maximum bandwidth h^* .¹⁰

The crucial parameter of PS approach is the critical value λ that determines the number of observations to be used in the estimation of each location value. Greater values of λ allow the inclusion of more points into a homogeneous region, leading to a smoother parameter surface and potentially a higher bias at reduced variance. In fact, for $\lambda \rightarrow \infty$, we obtain a non-adaptive kernel smoother. On the other hand, smaller values of λ will lead to a stricter selection of homogeneous regions and less points being included into the estimation. As a result, less available information is used and the variance of the estimate is generally higher. Due to the multiple testing procedure in this adaptive algorithm, there is no well-defined unique choice of λ (KOLBE et al., 2015). POLZEHL and SPOKOINY (2006) suggest performing Monte Carlo simulations of the relevant likelihood function with globally constant parameters on the design space. λ can then be chosen as the smallest value that ensures the homogeneity assumption holds everywhere with a high probability. For computing λ and the corresponding PSA estimates, we use the package ‘aws’ for the statistical software R (POLZEHL, 2016).

5 Comparing BRW and PSA

In this section, we compare the performance of BRW and PSA at the one-year ahead prediction of location values. For this purpose, we use a training set for PSA based on adjusted prices from 2013 and 2014, and a test set of ELV from 2015 for validation purposes. As explained in Section 2, the low number of observations in 2014 requires that we pool data from 2013 and 2014. Moreover, it is convenient that for obtaining our training set, we use the same procedure that we previously applied to compute ELV, but only taking into account observations from 2013 and 2014 since we cannot include information from the test set. In particular, we use Equation (2) for price adjustment where we furthermore add the estimated temporal effect $\hat{\gamma}$ to observations from the year 2014. This approach to temporal pooling is very similar to the deductive methods available to land price experts. The resulting prices reflect the 2014 price level of typical plots. As with ELV, we compute the mean per sub-district and obtain a training set of 1,556 average prices that represent the initial location value estimates for PSA. There are, however, 3,557 sub-districts in Mecklenburg-Western Pomerania, so we do not have PSA estimates of the 2015 location values for all sub-districts; moreover, we do not have corresponding

¹⁰ Note that the iteration is continued even if the homogeneity hypothesis is rejected for all x_i in $U^k(x_i)$. The procedure does not require that “homogeneous areas” be contiguous.

BRW for all sub-districts, either. Consequently, we have to filter the 2015 ELV data by selecting only those sub-districts, for which we have a value in the PSA training set and a BRW to enable a fair comparison. This reduces the number of sub-districts in the test set to 502.

As explained above, PSA has two parameters λ and h_{max} that control the threshold of the homogeneity test and the maximum distance of observations that are included in local estimation, respectively. For our PSA baseline predictor, λ is 9.72 as determined by Monte Carlo simulation (POLZEHL and SPOKOINY, 2006) (cf. Section 4). h_{max} can be selected such that for any cell on the grid, all other cells lie within the maximum distance. As we use a 100x100 grid, we set h_{max} to 150, which is slightly greater than the length of the grid's diagonal. This is the configuration of our default PSA predictor 'PSA1'.

To demonstrate the sensitivity of the results to parameter choice, we also perform PSA with a reduced value of h_{max} ('PSA2') as well as with greater ('PSA4') and smaller ('PSA3') values of λ . Furthermore, we seek to account for the fact that expert-based estimates can leverage trends observed during the past years for prediction, whereas PSA is limited to synchronous data. To reflect this possibility, we combine PSA with a linear trend, based on the effect γ from the regression model in Equation (1) fitted to the 2013/14 data. We compute this trend-adjusted predictor ('PSA5') as $\frac{\hat{p}}{e^{\hat{\gamma}}}$, where \hat{p} is the PSA baseline predictor. The rationale behind this expression is the following. We assume that there is a linear upward trend in the data from 2014 to 2015, adding a fixed quantity to the 2014 log-prices, i.e., $\log(p_{j,2015}) = \log(p_{j,2014}) + \gamma$. In order to de-trend PSA, we need to subtract this shift γ , which is estimated as $\hat{\gamma}$ with the regression model in Equation (1) based on 2013/14 log-prices. Hence, we have $\log(\tilde{p}_j) = \log(\hat{p}_j) - \hat{\gamma}$ and accordingly $\tilde{p}_j = \exp(\log(\hat{p}_j) - \hat{\gamma}) = \frac{\hat{p}_j}{e^{\hat{\gamma}}}$, where \hat{p}_j is the PSA-estimate for the price in 2015 of area j and \tilde{p}_j is the corresponding de-trended estimate. If no abrupt change in trend is expected for the

Table 5. Characteristics of the used predictors

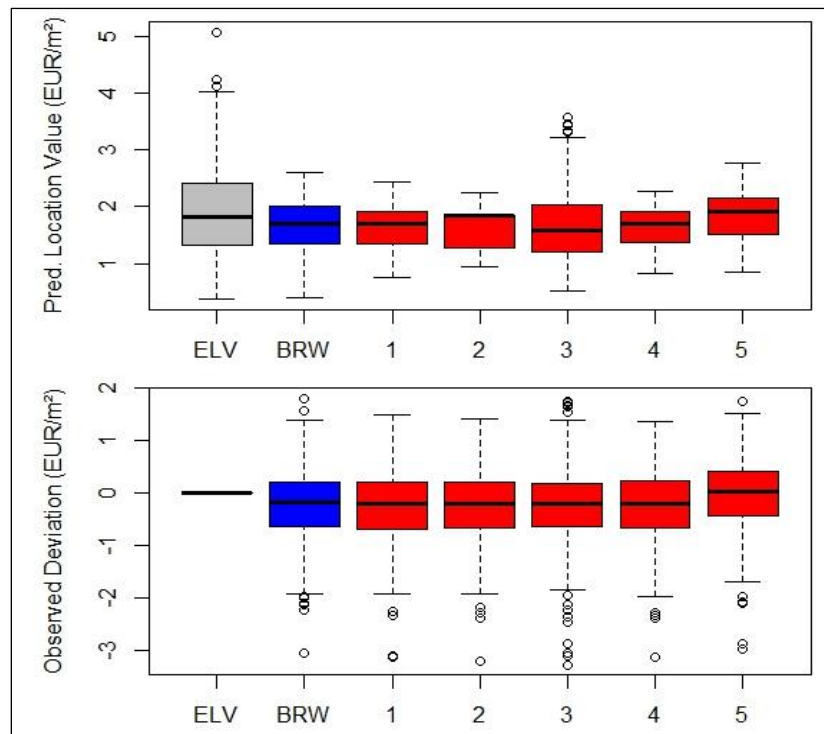
Predictor	Description
BRW	Expert based location value
PSA1	$\lambda = 9.72$; $h_{max} = 150$
PSA2	$\lambda = 9.72$; $h_{max} = 10$
PSA3	$\lambda = 0.972$; $h_{max} = 150$
PSA4	$\lambda = 97.2$; $h_{max} = 150$
PSA5	PSA1 trend-adjusted

Source: own elaboration

next year, this should improve the PSA estimate significantly. An overview of the predictors used in our analysis and of their characteristics is provided in Table 5.

Figure 5 contains in its upper panel boxplots of the distributions of empirical location values in the test set and the predicted values. The lower panel displays boxplots of the differences between predicted and empirical location values. The more a predictor's deviations from ELV are centred around zero, the less bias it has. A first impression is that BRW as well as PSA predictors have a significant bias, with the single exception to the trend-adjusted PSA5. Altogether, the distributions of observed deviation are quite similar.

Figure 5. Top: Empirical and predicted location values for 2015. Bottom: Observed deviation in 2015.



Note: Observed deviation is the differences between predicted and empirical location value. 1-5 denote PSA1-PSA5.

Source: own elaboration

To formally compare the predictors, we compute the MSE and test whether the predictors (i) have a bias significantly different from zero and (ii) have a significantly smaller bias than BRW. For (i), we perform one-sample t-tests assuming a non-homogeneous variance, and additional non-parametric Wilcoxon's signed-rank tests as in Section 3. For (ii), we carry out two-sample t-tests assuming a non-homogeneous variance (Welch test) and, to make the results robust against a violation of the t-test's normality assumption, Wilcoxon's rank-sum test.

Table 6 lists the results of these tests as well as the MSE for every predictor. We find that all predictors have a significant, negative bias in the same order of magnitude. The single exception to this is PSA5, that shows a smaller negative bias which is only significant at the 10% level. The MSE, too, indicates a similar performance of all PSA predictors and BRW, with the MSE of PSA5 of course being lower due to its reduced bias.

In summary, our results show that PSA in various configurations can reach the same level of accuracy in terms of MSE and bias as BRW. Since, apart from PSA5, none of the PSA estimators have shown less bias than BRW, we find that its data-driven approach to pooling does not show any apparent advantage over the fixed BRW zones. The substantial improvement of PSA5 achieved by considering linear trend on top of PSA indicates how strongly the general market trend from 2013-2015 impacts on the performance of predictors. The fact that, like PSA, BRW does not seem to take trend into consideration would explain the negative bias, especially seeing as the increase in mean land prices from 2014 to 2015 (0.28 EUR/m²) lies in the same order of magnitude.

6 Discussion and Conclusion

In our analysis of sales prices of arable land in Mecklenburg-Western Pomerania over the years 2013-2015, we have found that BRW significantly underestimates location values of the following year. A regression analysis of the observed deviation has pointed towards regional heterogeneity, soil quality, and temporal effects as explanatory factors of this deviation. Indeed, we observe a strong linear increase in mean land prices for every year from 2013-2015, which suggests that the time trend is not sufficiently taken into account in BRW estimation. However, soil quality also shows a strong effect, suggesting that experts have difficulties in correctly considering soil quality for location value estimation. Secondly, we find that on our 2015 test data, PSA predicts location values with an accuracy comparable to that of BRW, both in terms of bias and MSE. These findings are in line with KOLBE et al. (2015), who find that PSA is able to replicate BRW in an urban context. The performance depends to a limited degree on the choice of the algorithm's parameters, but neither bias nor MSE have proven too sensitive in this regard. Since PSA does not achieve a reduction of bias, it appears as though its adaptive approach does not hold any advantage over fixed BRW zones in the estimation of location values of agricultural land aside from the automated and objective procedure. The performance improvement when a linear trend is taken into consideration, however, hints at a potential for improving BRW or PSA as location value estimators by complementing these approaches with conventional forecasting techniques. It should be emphasized, however, that this finding is specific to the observation period in

Table 6. Estimated bias, test statistics of the applied tests and the mean squared error (MSE) w.r.t. ELV

Predictor	Bias (EUR/m ²)	Test (i): One-sample t-test	Test (i): Wilcoxon signed rank test	Test (ii): Welch test	Test (ii): Wilcoxon rank sum test	MSE (EUR/m ²) ²
BRW	-0.25	-8.3069***	38835***	-	-	0.5143
PSA1	-0.27	-9.2707***	36889***	-0.5686	124360	0.5107
PSA2	-0.28	-9.4556***	36698***	-0.7162	123940	0.5167
PSA3	-0.26	-8.2711***	37092***	-0.2607	123980	0.5665
PSA4	-0.27	-9.1851***	37403***	-0.4924	124780	0.5067
PSA5	-0.05	-1.8638*	60394	4.6367***	148140***	0.4352

Note: *** denotes significance at the 1%, * at the 10% significance level.

Source: own elaboration

this study that is characterized by a steady increase of land prices. Extrapolating a linear trend when prices begin to stagnate will result in a bias as well. It is noteworthy at this point that PSA in a different configuration could also be used to identify structural breaks in the price trend.

A further comment seems apposite at this point. One might argue that BRW are not intended to forecast location values and even trying to do so may fail in information efficient markets. On the other hand, market participants may use BRW as a yardstick for their price expectations of prospective land transactions. Thus, BRW should be up-to-date and not lag behind current market conditions. In a rapidly changing environment a biannual update of BRW, as requested by law, may lead to a sluggish adjustment of location values.

A practical issue with PSA is that outliers are usually not smoothed by PSA – the reason being that the homogeneity test, that is performed at every iteration when smoothing the sub-district with the outlier, will most certainly result in zero weights for most values other than the outlier itself. On the one hand, this is precisely the sort of behaviour that we wish, because it keeps the bias low when pooling values. On the other hand, it does not allow us to reach a reasonable estimate for the outlier itself. The reasons for the occurrence of such singular values may be manifold, and it is impractical to derive a general rule of treating them – in this analysis, we have opted for an *a priori* removal of the highest and lowest percentiles of prices. Our original concern that the results might be too sensitive to the choice of parameters has proven unjustified after this outlier removal. It seems that results for different parameters diverge more strongly in the presence of extreme values.

One limitation to our results is that our data set is of rather limited size. Carrying out similar calculations for other regions with a longer time series of land prices and BRW could improve the reliability of our findings. Moreover, our observation period is characterised by a strong linear upward trend of mean land prices. Further assessment of BRW and PSA on data without such a trend might elucidate if the performance of PSA holds under different market conditions, too. This caveat notwithstanding, we have found PSA to be a convenient tool for the automatic estimation of location value of agricultural land in a transparent way since no expert knowledge is required for the procedure. Such a tool can complement the expert-based approach and serve as a benchmark.

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