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MULTIPLE REGIMES AND CROSS-COUNTRY GROWTH BEHAVIOR

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SOCIAL SYSTEMS RESEARCH INSTITUTE

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Summary

This paper provides some new evidence on the behavior of cross-country growth rates. We reject the linear model commonly used to study cross-country growth behavior in favor of a multiple regime alternative in which different economies obey different linear models when grouped according to initial conditions. Further, the marginal product of capital is shown to vary with the level of economic development. These results are consistent with growth models which exhibit multiple steady states. Our results call into question inferences that have been made in favor of the convergence hypothesis and further suggest that the explanatory power of the Solow growth model may be enhanced with a theory of aggregate production function differences.

Introduction

Starting with Baumol (1986), many authors have explored the behavior of output growth across aggregate economies. Much of this research has been interested in determining whether economies exhibit convergence — defined as the tendency for per capita output differences due to initial conditions to disappear over time. The convergence question has important implications for growth theory. Convergence holds in the classic Solow growth model given a concave aggregate production function. In contrast, the new growth theory pioneered by Romer (1986) and Lucas (1988) shows how increasing returns to scale can cause differences in initial conditions to persist.

Much of the empirical work on convergence has been concerned with identifying a negative coefficient in the regression of a country's growth over a fixed period on its initial output, so that poorer countries grow faster on average than richer ones. As initially shown in Barro (1991) this negative coefficient may be found for a large cross-section of countries when one controls for factors such as education, investment rates and political stability. Perhaps the most persuasive evidence in this regard is due to Mankiw, Romer and Weil (1992) who study a regression in which the control variables are those directly suggested by a human capital-augmented version of the Solow model. These authors not only find strong evidence of convergence, but that the regression fulfills the cross-coefficient restrictions imposed by the Solow model.

One important assumption underlying the bulk of cross-country growth studies is

that all countries obey a common linear specification. While a linear specification holds under the Solow model, it does not hold for some new growth alternatives. A class of growth models, starting with Azariadis and Drazen (1990), produces multiple locally stable steady states in per capita output. Cross-country growth behavior in these models is typically nonlinear, exhibiting multiple regimes as countries associated with the same steady state obey a common linear regression. Conventional convergence tests will have difficulty distinguishing between these multiple steady state models and the Solow model. As shown in Bernard and Durlauf (1993), a linear regression applied to data generated by economies converging to multiple steady states can produce a negative initial income coefficient. Intuitively, the initial income coefficient in the misspecified linear model inherits the convergence exhibited among countries associated with a common steady state in the correctly specified multiple regime growth process.

This paper reexamines the Summers-Heston data set in order to identify whether multiple regimes in cross-country growth behavior are present. This exercise is of interest both from the perspective of better understanding the statistical properties of the data set results as well as evaluating the compatibility of cross-country growth patterns with multiple steady state models. Our conclusions are twofold. First, we reject the null hypothesis that all countries obey a common linear model. This means that the equation estimated by previous authors to show the presence of convergence is misspecified. Second, by using regression tree analysis to identify countries obeying a common linear model, we find subsets of countries which appear to possess very different production functions. These differences in turn suggest that more developed countries have higher output-labor ratios than implied by their capital-labor ratios alone.

Section 1 reviews the link between some growth models and cross-section regressions. Section 2 describes the data we analyze. Section 3 performs specification tests on cross-country regressions. Using initial output and literacy rates to segregate countries, a single regime specification is rejected. Section 4 uses regression tree techniques to identify groups of countries obeying a common linear model. Section 5 provides some caveats to the interpretation of our results. Section 6 contains summary and conclusions. Data and technical appendices follow.

1. Convergence and cross-section behavior

To derive the cross-country implications of the Solow growth model, we follow the analysis in Mankiw, Romer and Weil (1992), which we subsequently denote as M-R-W, and consider the case where aggregate output in country i at t, $Y_{i,t}$, is determined by a Cobb-Douglas production function taking as arguments the level of technology A_t , labor input $L_{i,t}$, physical capital input $K_{i,t}$ and human capital input $H_{i,t}$

$$Y_{i,t} = \phi K_{i,t}^{\alpha} H_{i,t}^{\gamma} (A_t L_{i,t})^{1-\alpha-\gamma}. \tag{1}$$

All variables are assumed to evolve in continuous time. The level of technology and labor grow at constant rates g and n_i respectively. Each country augments its physical and human capital stocks at the constant savings rates s_i^k and s_i^h while both stocks depreciate at the same rate δ . This induces capital accumulation equations of the form $dK_{i,t}/dt = s_i^k Y_{i,t} - \delta K_{i,t}$ and $dH_{i,t}/dt = s_i^h Y_{i,t} - \delta H_{i,t}$. As a result, over any interval T to $T+\tau$ output per worker, $(Y/L)_{i,t}$, obeys

$$\ln(Y/L)_{i,T+\tau} - \ln(Y/L)_{i,T} = g\tau + (1 - e^{-\lambda_i \tau}) \left(\Theta + \frac{\alpha}{1 - \alpha - \gamma} \ln(s_i^k) + \frac{\gamma}{1 - \alpha - \gamma} \ln(s_i^h) - \frac{\alpha + \gamma}{1 - \alpha - \gamma} \ln(n_i + g + \delta) - \ln(Y/L)_{i,T}\right)$$
(2)

Here, $\Theta = \frac{1}{1-\alpha-\gamma}ln(\phi) - ln(A_0) - gT$ and $\lambda_i = (1-\alpha-\gamma)(n_i+g+\delta)$; λ_i is the country-specific convergence rate towards the steady state.

Equation (2) explains cross-country growth rates as the result of a common technology which is concave in the two capital stocks and country-specific input growth. The equation places nonlinear restrictions across the regression coefficients and is typically referred to as the "constrained" version of the Solow model. Relaxation of these restrictions while assuming that $\lambda_i = \lambda \ \forall i$, as M-R-W do, produces the "unconstrained" law of motion estimated by Barro and others,

$$ln(Y/L)_{i,T+\tau} - ln(Y/L)_{i,T} = \zeta + \beta ln(Y/L)_{i,T} + \prod_{i} X_i + \epsilon_i, \quad i = 1,...,N.$$
 (3)

where $X_i = (ln(s_i^k), \, ln(s_i^h), ln(n_i + g + \delta)).$

A negative value for $-(1-e^{-\lambda_i\tau})\frac{\alpha+\gamma}{1-\alpha-\gamma}$ in the constrained regression or for β in the unconstrained regression has been taken as evidence of convergence, corresponding to the intuition that convergence occurs when low per capita output economies grow more quickly than high per capita output economies.

A number of new growth models are based on the idea that there exists a range of human or physical capital levels over which the aggregate production function is not concave, which will lead to different long run steady states for different initial conditions. For example, Azariadis and Drazen (1990) argue that there exist human or physical capital accumulation thresholds which induce shifts in aggregate productivity. One version of the Azariadis-Drazen model replaces (1) with a production function embodying a physical capital threshold $\widetilde{K}(t)$, and a human capital threshold $\widetilde{H}(t)$, which may depend on time, such that

$$Y_{i,t} = \phi K_{i,t}^{\alpha_j} H_{i,t}^{\gamma_j} (A_t L_{i,t})^{1 - \alpha_j - \gamma_j}$$

$$\tag{4}$$

where

$$\alpha_{j} = \alpha_{1} \text{ if } K_{i,t} < \widetilde{K}(t), \ \alpha_{2} \text{ otherwise; } \gamma_{j} = \gamma_{1} \text{ if } H_{i,t} < \widetilde{H}(t), \ \gamma_{2} \text{ otherwise.}$$
 (5)

This type of nonconvexity will, for some values of the thresholds $\widetilde{H}(t)$ and $\widetilde{K}(t)$, generate multiple steady state equilibria with an associated cross-section law of motion

$$ln(Y/L)_{i,T+\tau} - ln(Y/L)_{i,T} = g\tau + (1 - e^{-\lambda_i \tau}) \left(\Theta_j + \frac{\alpha_j}{1 - \alpha_j - \gamma_j} ln(s_i^k) + \frac{\gamma_j}{1 - \alpha_j - \gamma_j} ln(s_i^h) - \frac{\alpha_j + \gamma_j}{1 - \alpha_j - \gamma_j} ln(n_i + g + \delta) - ln(Y/L)_{i,T}\right)$$

$$(6)$$

$$\text{where } \lambda_i = (1-\alpha_j - \gamma_j)(n_i + g + \delta), \text{ and } \Theta_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j \text{ and } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with } \alpha_j = \frac{1}{1-\alpha_j - \gamma_j}ln(\phi) - ln(A_0) - gT, \text{ with$$

¹Models such as Murphy, Shleifer, and Vishny (1989) and Durlauf (1993) in which economies exhibit multiple steady states due to coordination failure produce similar multiple regime implications for the data.

²We allow for these thresholds to depend on time in order to account for factors such as technical change or population growth which might produce steady state capital growth without causing a country to undergo the sort of industrial transformation envisioned by models such as Azariadis and Drazen (1990).

 γ_i determined by (5).

A country possessing this technology will follow one of four distinct Solow-type laws of motion, depending on the relationship between $(K_{i,t},H_{i,t})$ and $(\widetilde{K}(t),\widetilde{H}(t))$. As a result, the cross-section regressions (2) and (3) are correctly specified for subsets of countries when the aggregate technology obeys (4) and (5). The testable implications of (1) versus (4) and (5) are summarized in the requirement that the cross-section data are generated by a common linear law of motion whose coefficients obey the constraints embedded in (2). Conversely, Bernard and Durlauf (1993) show how a negative initial output coefficient can occur when (2) or (3) is estimated from data generated by (4) and (5), so that the standard convergence test cannot differentiate between the two models.

This example motivates our empirical strategy for analyzing cross-country growth behavior by determining whether the data obey a single Solow-type growth equation or whether the data exhibit multiple regimes in the sense that subgroups of countries identified by initial conditions obey distinct Solow-type regressions.

2. Data

All cross-country growth rates we employ are based upon the Summers-Heston (1988) international output estimates; the sample of countries and a number of associated data series are contained in the data appendix.⁴ The variables are:

 $(Y/L)_{i,t}$ = real GDP per member of the population aged 15-64, country i at t.

 $(I/Y)_i$ = fraction of real GDP devoted to investment (including government investment), country i, annual average for 1960-1985.

 n_i = growth rate of the working-age population, country i, annual average 1960-1985.

 $\frac{SCHOOL_i}{^3 \mathrm{Quah}}$ = fraction of the working-age population enrolled in secondary school, country of the initial output coefficient.

⁴Besides Summers and Heston (1988), the primary sources for the data set are the World Bank's World Tables and World Development Report.

i, annual average 1960-1985.

 $LR_{i,1960}$ = adult literacy rate, fraction of the population aged 15 and over that is able to read and write, country i, in 1960.⁵

We follow M-R-W in assuming that g=0.02 (implying that $g\tau=0.5$, a value that we impose in estimation) and $\delta=0.03$, figures that are approximately true for the United States. We also follow these authors in using $(I/Y)_i$ to represent s_i^k and $SCHOOL_i$ to represent s_i^k .

3. Specification tests for multiple regimes

In this section we attempt to identify the presence of multiple regimes in the data through the use of specification tests which take a single regime model as the null hypothesis. We do this by mechanically splitting the data into subgroups based upon different control variables and examining whether model parameters are equal across groups. We consider two estimating equations. First, we fit

$$ln(Y/L)_{i, 1985} - ln(Y/L)_{i, 1960} =$$

$$\zeta + \beta ln(Y/L)_{i, 1960} + \pi_1 ln(I/Y)_i + \pi_2 ln(n_i + g + \delta) + \pi_3 ln(SCHOOL)_i + \epsilon_i$$
(7)

by least squares over each subgroup. This estimate represents the unconstrained version of the Solow model. We separately estimate a constrained version of the model by imposing cross-coefficient restrictions defined by (2).

We consider two different control variables to group countries with initial conditions.⁶ The first variable we employ is per capita output at the beginning of the

⁵For some countries the 1960 literacy rate is unavailable so the 1975 rate is used instead. As most of these have literacy rates of 90% or greater this has little effect on our results. In addition, for many countries, the "1960" literacy rate is actually calculated for some (unknown) year between 1958 and 1962. It seems unlikely that literacy changes by much in a two year period so the resultant error is probably small. Two countries studied by M-R-W, Botswana and Mauritius, are omitted due to lack of data on literacy.

⁶The use of split variables which are known at the beginning of the sample under study is necessary to avoid the selection bias problem noted by DeLong (1986).

Table 1
Specification Tests for Different Regimes

Subsamples defined by	Unconstrained Regressions	Constrained Regressions
2 Way Calit based on		
2-Way Split based on	0.000	0.040
$(Y/L)_{i,1960}$	0.009	0.218
$LR_{i,1960}$	0.011	0.112
3–Way Split based on $(Y/L)_{i,1960} \\ LR_{i,1960}$	$0.029 \\ 0.404$	0.011 0.000
4-Way Split based on both	${f h}$	
$\stackrel{\circ}{L}R_{i,1960}$ and $(Y/L)_i$		0.000

This table shows the marginal significance levels for the Wald tests of the null hypothesis that the parameters of the indicated models are constant across the indicated subsamples. Splits are described in the text.

sample period, $(Y/L)_{i,1960}$. Most models of multiple steady states predict that if economies are concentrated around several steady states, then their initial per capita output levels will fall into nonoverlapping categories. Second, we examine sample splits based upon the adult literacy rate of each country in 1960. The use of literacy as a segregating variable makes sense if one thinks of the potential regimes in the data as stemming from differences in the level of social and economic development rather than the current level of economic activity. Alternatively, these variables may be interpreted as proxies for identifying threshold effects associated with the unobserved physical and human capital stocks.

Table 1 reports the results for several different data splits. Each entry represents the significance level of a Wald test of the null hypothesis that all parameters are equal across the subsamples under analysis. The first panel of the Table divides countries into two equal sized groups by segregating high and low initial output and initial literacy countries into separate categories. Each subgroup thus consists of 48 countries. The second panel divides countries into three equal groups of 32 using each of these variables. The third panel allows interactions between the variables. In this case, we divide the countries according to whether they lie in the high or low half of the sample according to the two controls. This segregation results in four categories: high output/high literacy (42 countries), high output/low literacy (6 countries), low output/high literacy (6 countries) and low output/low literacy (42 countries).

 $^{^{7}}$ This distinction is also relevant for coordination-based models with multiple regimes.

⁸Following Barro (1991) and others, we employ heteroskedasticity-corrected test statistics and standard error estimates based on White (1980), in order to permit error variances to differ across countries. White's heteroskedasticity test reveals some evidence against a homoskedastic null. Assuming homoskedasticity in the calculation of the Wald statistics increases the number of rejections of the single regime model.

 $^{^9{\}rm The}$ two-way output splits are based on $(Y/L)_{i,1960} < \$1950$ and $\$1950 \le (Y/L)_{i,1960};$ the three way splits are based on $(Y/L)_{i,1960} < \$1150,$ $\$1150 \le (Y/L)_{i,1960} \le \2750 and $\$2750 < (Y/L)_{i,1960}.$ For initial literacy, the two-way splits are based on $LR_{i,1960} < 54\%$ and $54\% \le LR_{i,1960};$ the three way splits are based on $LR_{i,1960} < 26\%, \ 26\% \le LR_{i,1960} \le 72\%$ and $72\% < LR_{i,1960}.$ The data appendix records the three way splits for various countries by identifying each as falling into a high (H), intermediate (I) or low (L) output or literacy class.

Table 2 Cross-Section Regressions Initial Output and Literacy-Based Sample Breaks Dependent Variable: $ln(Y/L)_{i,\,1985} - ln(Y/L)_{i,\,1960}$

		$(Y/L)_{i,1960} < 1950$	$1950 \le (Y/L)_{i, 1960}$
	M-R-W	and $LR_{i, 1960} < 54\%$	and $54\% \le LR_{i,1960}$
Observations	98	42 Unconstrained Regressions	42
constant	$3.04^{\dagger} \ (0.831)$	1.40 (1.85)	$0.450 \\ (0.723)$
$ln(Y/L)_{i,1960}$	-0.289^{\dagger} (0.062)	$^{-0.444}^{\dagger}_{(0.157)}$	$^{-0.434}^{\dagger}_{} \ (0.085)$
$ln(I/Y)_i$	$0.524^{\dagger} \ (0.087)$	$0.310^{\dagger} \\ (0.114)$	$0.689^{\dagger} \ (0.170)$
$ln(n+g+\delta)_i$	-0.505 (0.288)	-0.379 (0.468)	-0.545 (0.283)
$ln(SCHOOL)_i$	$0.233^{\dagger} \ (0.060)$	$0.209^{\dagger} \\ (0.094)$	0.114 (0.164)
\bar{R}^2	0.46	0.27	0.48
σ_ϵ	0.33	0.34	0.30
		Constrained Regressions	
Θ	$-2.56^{\dagger \ddagger}$ (1.14)	2.29 (1.17)	-0.395 (1.24)
α	$0.431^{\dagger} \ (0.061)$	$0.275^{\dagger} \ (0.097)$	$0.509^{\dagger} \ (0.098)$
γ	$0.241^{\dagger} \ (0.046)$	$0.217^{\dagger} \\ (0.061)$	$0.108 \\ (0.094)$
$ar{R}^2$	0.42	0.28	0.50
σ_ϵ	0.34	0.34	0.29

[†] denotes significance at asymptotic 5% level

[‡] This equation has been reestimated under the restriction $\lambda_i = (1 - \alpha - \gamma)(n_i + g + \delta)$, where λ_i is the rate of convergence toward the steady state. This restriction was not imposed by M-R-W. Their estimates are constant = 2.46 (0.48); $\alpha = 0.48$ (0.07); $\gamma = 0.23$ (0.05); $\bar{R}^2 = 0.46$; and, $\sigma_{\epsilon} = 0.33$.

As the Table indicates, there is substantial evidence that the laws of motion for growth within each subgroup are different. For three of the four initial output splits, equality of coefficients across the groups is rejected at the 3% level. When initial literacy represents the control variable, we reject in two of the four cases at about 1%. Further, we strongly reject coefficient equality across splits for both the unconstrained and constrained regressions in the interactive four regime specification. This change in the significance level indicates the importance of both variables in identifying data regimes.

Table 2 reports the original M-R-W regression along with estimates of the regressions associated with the high initial output/high initial literacy and low initial output/low initial literacy splits described above. (The high initial output/low initial literacy and low initial output/high initial literacy splits are omitted due to lack of degrees of freedom.) Several of the subsample coefficients are substantially different from both one another and from the M-R-W regression. For the unconstrained regressions, the coefficient on initial output, $ln(Y/L)_{i,1960}$, is approximately equal for the high output/high literacy and low output/low literacy groups at -0.434 and -0.444 respectively; these estimates are much larger than the -0.289 estimate for the whole sample. This difference reveals a faster convergence rate for the subsamples than for the single regime. Further, the $ln(I/Y)_i$ coefficient for high output/high literacy countries is 0.689, which is over twice as large as the 0.310 estimate for the low output/low literacy countries and over 25% higher than the 0.524 estimate for the whole sample. Similarly, the implied physical capital share in output for the constrained regressions, α , is far larger for the high output/high literacy countries at 0.509 than for the low literacy/low output countries at 0.275, and somewhat larger than the 0.431 share for the whole sample. Conversely, the low output/low literacy countries exhibit a much larger coefficient for the human capital investment measure ln(SCHOOL), as well as the associated human capital output share γ than high output/high literacy countries, although both subsample estimates are below those for the whole sample. These estimates suggest that the aggregate production function differs substantially across subsamples.

¹⁰See Rauch (1989) for corroborating evidence of literacy-based regime differences.

One explanation of these results is that the set of control variables dictated by the Solow model is too small to account for some important differences in growth performance so that our evidence of multiple regimes is actually due to omitted variables. In this case, inclusion of these variables among the X_i would render the specification correct and eliminate the statistical significance of the sample splits. Barro (1991) uses a broader set of control variables than M-R-W in an attempt to model a wide variety of potential influences on growth. We therefore investigate whether our rejection of the single regime model is robust to the addition of Barro's variables to those dictated by the strict Solow model. The variables we used are:¹¹

 $AFRICA_i = 1$ if country i is in sub-Saharan Africa;

 $ASSASS_{i}$ = number of assassinations per million population per year, country i;

 $(G^c/Y)_i$ = average ratio of government consumption (exclusive of defense and education) to GDP, country i;

 $LATAMER_i = 1$ if country i is in Latin America;

 $LIT60_i = \text{adult literacy rate in 1960, country } i;^{12}$

 $MIXED_i = 1$ if country i has a mixed free enterprise/socialistic economic system;

 $PPI60DEV_i = \text{deviation from sample mean of the 1960 purchasing power parity value for the investment deflator, country <math>i$;

 $PRIM60_i$ = primary-school enrollment rate, country i, 1960.

 REV_i = number of revolutions and coups per year, country i;

 $SEC60_i = \text{secondary-school enrollment rate, country } i, 1960.$

 $SOC_i = 1$ if country i has a socialist economic system;

¹¹ All of the data are from Barro and Wolf (1989).

 $^{^{12}}$ This variable is measured differently from the variable $LR_{i,\,1960}$ that we use to split up the sample but, for the 94 countries for which there are data on both, the correlation coefficient between them is 0.96.

 $^{^{13}}SEC60_i$ differs from $SCHOOL_i$ as it measures the ratio of secondary students to the population between 12-17 rather than to all working age persons and because it equals a point estimate for 1960 rather than an average over 1960-1985.

Table 3
Specification Tests: Robustness Check

Additional Control Variables	Marginal Significance Value
None	0.001
Equation 1	0.002
Equation 11	0.000
Equation 12	0.000
Equation 13	0.000
Equation 14	0.000

This table shows the marginal significance levels for the Wald tests of null hypothesis that the coefficients on the variables dictated by the Solow model are the same in the low output/low literacy and high output/high literacy groups described in the text when the indicated sets of Barro control variables are added to the model. The sets of controls are:

Equation $1 - SEC60_i$, $PRIM60_i$, $(G^c/Y)_i$, REV_i , $ASSASS_i$, $PPI60DEV_i$;

Equation 11 - STTEAPRI_i, STTEASEC_i, (G^c/Y)_i, REV_i, ASSASS_i, PPI60DEV_i;

 $\texttt{Equation 12} - SEC60_i, \ PRIM60_i, \ LIT60_i, \ (G^c/Y)_i, \ REV_i, \ ASSASS_i, \ PPI60DEV_i;$

Equation $13 - SEC60_i$, $PRIM60_i$, $(G^c/Y)_i$, REV_i , $ASSASS_i$, $PPI60DEV_i$, SOC_i , $MIXED_i$; and,

 $\text{Equation } 14-SEC60_i,\ PRIM60_i,\ (G^c/Y)_i,\ REV_i,\ ASSASS_i,\ PPI60DEV_i,\ AFRICA_i,\ LATAMER_i.$

 $STTEAPRI_i = 1960$ primary school student-teacher ratio, country i; and, $STTEASEC_i = 1960$ secondary school student-teacher ratio, country i.

We focus on the differences between the low output/low literacy and the high output/high literacy groups of countries identified above. Specifically, we reestimate equations (2) and (3) for these groups after adding subsets of the Barro variables corresponding to the different combinations of regressors reported in Barro (1991), again testing the significance of the differences in the estimated coefficients between groups.

Table 3 gives the results. The first line establishes the significance of the differences between the two groups with no additional control variables. The remainder of the Table shows the results when the controls are the regressors from equations 1 and 11 through 14 in Barro's Table 1. In no case does the marginal significance value exceed 0.002. The evidence of multiple regimes thus appears to be robust to the addition of these additional control variables.¹⁵

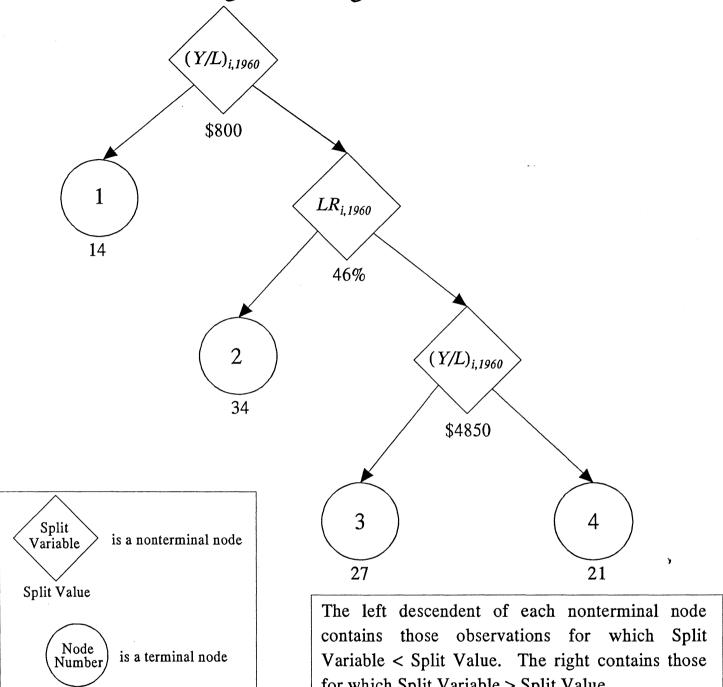
4. Regression tree estimates of country groups

Although the exogenously imposed data splits of the previous section permit straightforward specification testing, they do not address the problem of identifying economies with common laws of motion. In order to identify economies whose growth behavior obeys a common statistical model, it is necessary to allow the data to determine the location of the different regimes. At the same time, mechanically splitting the data by initial conditions in order to produce multiple regimes will quickly eliminate all degrees of freedom; for example, a three-way split by output and literacy creates 9

¹⁴We do not consider the high output/low literacy and low output/high literacy groups because of the small number of observations in each.

¹⁵We omit the variables in the subsequent analysis in order to highlight the differences between the single and multiple regime versions of the Solow growth model, since 1) inclusion of the variables has no qualitative effect on the results and 2) these control variables are *ad hoc* additions to the standard Solow model.

Figure 1: Regression Tree



Number of Countries

for which Split Variable ≥ Split Value.

Table 4

Regression Tree Sample Breaks

Country Classification

Terminal Node Number

1	2	3	4
Burkina Faso	Algeria	Madagascar	Austria
Burundi	Angola	South Africa	Belgium
Ethiopia	Benin	Hong Kong	Denmark
Malawi	$\operatorname{Cameroon}$	Israel	Finland
Mali	Central African Rep.	Japan	France
Mauritania	Chad	Korea	Federal Republic of Germany
Niger	Congo, People's Rep.	Malaysia	Italy
Rwanda	Egypt	Philippines	The Netherlands
Sierra Leone	Ghana	Singapore	Norway
Tanzania	Ivory Coast	Sri Lanka	Sweden
Togo	Kenya	Thailand	Switzerland
Uganda	Liberia	Greece	United Kingdom
Zaire	Morocco	Ireland	Canada
Burma	Mozambique	Portugal	Trinidad and Tobago
	Nigeria	Spain	United States of America
	Senegal	Costa Rica	Argentina
	Somalia	Dominican Republic	Chile
	Sudan	El Salvador	Uruguay
	Tunisia	Jamaica	Venezuela
	Zambia	Mexico	Australia
	Zimbabwe	Nicaragua	New Zealand
	$\operatorname{Bangladesh}$	Panama	
	India	Brazil	
	f Jordan	Columbia	
	Nepal	Ecuador	
	Pakistan	Paraguay	
	Syria	Peru	
	Turkey		
	Guatemala		
	Haiti		
	Honduras		
	Bolivia		
	Indonesia	•	
	Papua New Guinea		

categories for only 96 observations. Further, economic theory provides no prior guidance as to either the number of regimes or as to the way in which the different variables defining initial conditions interact in determining regimes. Therefore, it is desirable to employ a data sorting method which allows the data to endogenously select these features.

Regime identification is performed based on regression tree analysis.¹⁶ This technique, described in Breiman et al (1984), provides a general nonparametric way of identifying multiple data regimes from a set of control variables. The technique allows one to search for an unknown number of sample splits using multiple control variables. Intuitively, the procedure approximates the growth process as a union of piecewise linear functions, where observations are grouped by initial conditions. The actual sorting algorithm is quite complicated and is described in the technical appendix. No asymptotic theory exists to test the statistical significance of the number of regimes uncovered by the regression tree. The virtue of the procedure lies in its ability to uncover multidimensional data splits.

The result of this procedure is the regression tree shown in Figure 1. Squares in this figure indicate the splitting criteria for the sample; circles represent terminal nodes which contain different subsamples. The subsamples are: 1) $(Y/L)_{i,1960} < \$800$, 2) $\$800 \le (Y/L)_{i,1960} \le \4850 and $LR_{i,1960} < 46\%$, 3) $\$800 \le (Y/L)_{i,1960} \le \4850 and $46\% \le LR_{i,1960}$, and 4) $\$4850 < (Y/L)_{i,1960}$. The regression tree partitions the sample into low, intermediate and high output countries and then further partitions the intermediate output countries into low and high literacy countries. The fact that, given the opportunity to split the sample by either output or literacy, the regression tree shows a preference for output splits suggests that output dominates literacy as a variable useful in identifying multiple regimes in the data.

Table 4 details the countries in each subsample. The Table indicates that there is substantial geographic homogeneity within each group. The low output/low literacy

¹⁶We have also examined endogenous data splitting in which the number of different regimes is set *a priori* with break points chosen to maximize a quasi-log likelihood function. Setting the number of regimes at three and using each of initial output or initial literacy to order the data produced statistically significant splits.

Table 5 Cross-Section Regressions Regression Tree Sample Breaks Dependent Variable: $ln(Y/L)_{i,\,1985} - ln(Y/L)_{i,\,1960}$

Terminal Node Number

	Tollinda Ivanisei			
	1	2	3	4
Observations	14	34	27	21
		Unconstrained Reg	gressions	
constant	3.46 (2.27)	-0.915 (1.79)	0.277 (1.42)	-7.26^{\dagger} (1.59)
$ln(Y/L)_{i,1960}$	$-0.791^{\dagger} \\ (0.269)$	-0.086 (0.131)	$-0.316^{\dagger} \ (0.123)$	$0.069 \\ (0.139)$
$ln(I/Y)_i$	$0.314^{\dagger} \ (0.109)$	$0.129 \ (0.159)$	$1.110^{\dagger} \\ (0.165)$	$0.475^{\dagger} \\ (0.119)$
$ln(n+g+\delta)_i$	-0.429 (0.678)	-0.390 (0.489)	$0.059 \\ (0.451)$	$^{-1.75}^{\dagger}$ (0.270)
$ln(SCHOOL)_i$	-0.028 (0.073)	$0.469^{\dagger} \ (0.095)$	-0.114 (0.167)	$0.341^{\dagger} \\ (0.141)$
$ar{R}^2$	0.57	0.52	0.57	0.82
σ_{ϵ}	0.16	0.28	0.28	0.12
		Constrained Regr	ressions	
Θ	$4.107^{\dagger} \ (0.552)$	$0.539 \ (1.809)$	-3.95 (2.67)	-11.0 (7.64)
α	$0.306^{\dagger} \\ (0.083)$	$0.186 \ (0.123)$	$0.758^{\dagger} \ (0.095)$	$0.333^{\dagger} \\ (0.100)$
γ	-0.034 (0.083)	$0.416^{\dagger} \ (0.080)$	-0.073 (0.114)	$0.455^{\dagger} \\ (0.103)$
$ar{R}^2$	0.64	0.40	0.55	0.71
σ_ϵ	0.19	0.32	0.30	0.18

 $[\]dagger$ denotes significance at asymptotic 5% level

group is composed almost exclusively of poor African countries. The intermediate output/low literacy group is largely made up of relatively resource rich African countries and subcontinental Asian countries. Far eastern Asian and Latin American countries dominate the intermediate output/high literacy group. North American and European countries dominate the high output group.¹⁷

Table 5 presents estimates for each of the subsamples. In terms of overall fit, we find some improvement over the single regime specification. Whereas M-R-W found that they could explain 46% of overall growth variation in the unconstrained model, we find that for the poorest economies, we explain 57%, for intermediate output economies with low literacy rates 52%, for the intermediate output economies with high literacy rates 57%, and for high output economies fully 82% of the total growth variation. Similar results hold for the constrained regressions.

Perhaps the most striking feature of these estimates is how much they differ across subsamples. For example, the estimated coefficient on $ln(Y/L)_{i,\,1960}$ is -0.791 and significant for the first group while it is 0.069 but insignificant for the fourth group. This failure to find evidence of convergence among the high output economies parallels the results of DeLong (1988) who rejected convergence over a much longer time span when studying economies with similar high initial outputs. The point estimates for the second and third subsamples, -0.086 and -0.316, are both negative although only the latter is significant. The regression tree thus identifies a convergent subgroup within the intermediate output countries.

Similar heterogeneity holds for other variables. The coefficient on $ln(I/Y)_i$ is significant in the first, third, and fourth subsamples, but the subsample estimates vary greatly, ranging from 0.314 in the first subsample to 1.110 in the third subsample. The estimated coefficient on $ln(SCHOOL)_i$ is insignificant for the first and third subsamples, and is over a third larger in the second subsample (0.469) than in the fourth (0.341).

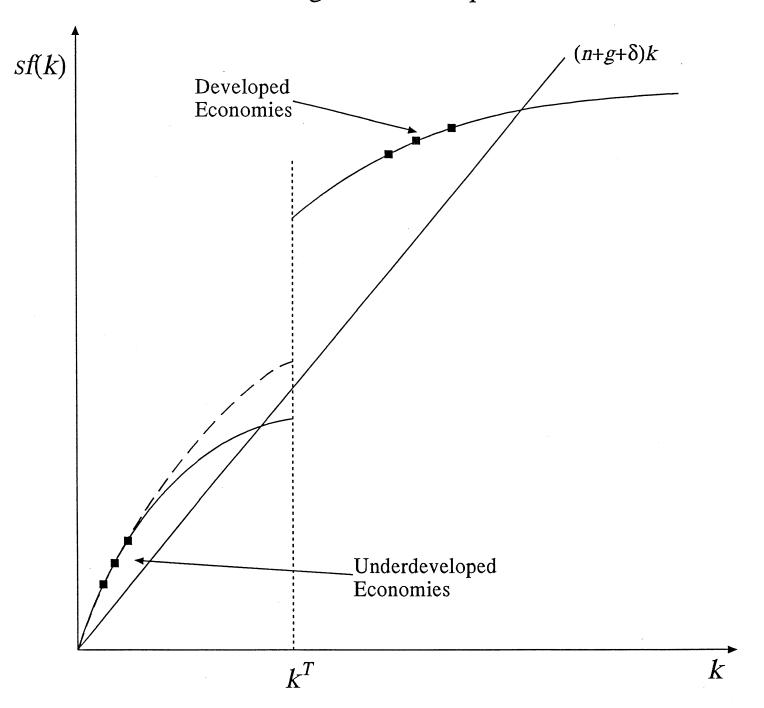
¹⁷We performed several specification tests on the regression tree splits to see if there is any residual nonlinearity. Tests based on the addition of quadratic or cubic terms to the within-group linear regressions or based on additional data splits as determined by initial conditions produced little evidence of within-group nonlinearity.

Estimation of the constrained model produces vastly different estimates of both the physical and human capital shares across regimes. The estimated physical capital share in the third subsample (.758) is more than twice that in the first (.306) and fourth (.333) and is not statistically significant in the second (.186). The estimated human capital shares are near zero for the first and third subsamples and are approximately equal for the second and fourth subsamples at 0.416 and 0.455. The fourth subsample is the only case where both shares are significant. Our estimates are strongly consistent with the view that different economies have access to different aggregate technologies.

The striking differences in the human capital share can be interpreted in different ways. One possibility is that economies go through production regimes which are indexed by different thresholds of human capital formation, in a way similar to Azariadis and Drazen (1990). Suppose that certain forms of organization of production within a firm or industry are constrained by the educational level of the labor force. constraints no longer bind, then marginal increases in human capital will appear to have low marginal product, until an economy grows to the point where production is reorganized, creating a need for more human capital. In this case, the second and fourth nodes may represent regimes where human capital accumulation augments the utilized technology. Alternatively, the different estimates might also reflect the weakness of the human capital variable, $ln(SCHOOL)_i$. This variable only measures secondary school enrollment. If primary, secondary and college human capital formation have regimespecific output shares, then this variable may simply perform poorly in some cases. general, if the magnitude of measurement error for any of the right hand side variables correlates with the initial conditions we use for sample splitting, spurious production function differences could be identified.

Finally, it is interesting to compute the pattern of labor shares across country groups: 0.728 for node 1, 0.398 for node 2, 0.315 for node 3, and 0.212 for node 4. These figures illustrate how the labor share declines as an economy becomes more developed in terms of literacy and production. This path for the evolution of the aggregate production function suggests that the high productivity of advanced economies is due not only to capital deepening, but also to the way in which capital per worker is converted into

Figure 2: Multiple Steady States versus Stages of Development



output per worker.¹⁸ The idea that high output economies more effectively utilize capital relative to low output economies is a feature of many multiple steady state models, and is one way to interpret either the Azariadis and Drazen (1990) model of threshold externalities or the Durlauf (1993) model of local technological spillovers, and is consistent with the finding in Dowrick and Gemmell (1991) of capital productivity differences between rich and poor countries.¹⁹

5. Caveats

We raise three caveats in the interpretation of our results.

i. Identification

While our results illustrate how the standard cross-section growth regression is misspecified and how a nonlinear generalization of the standard regression exists which is compatible with a multiple steady state alternative, it is important to emphasize a sense in which the presence or absence of convergence is not identified by the analysis. Simply put, the contrasting behavior of economies with different initial conditions is compatible both with model in which economies pass through distinct phases of development towards a unique steady state as well as one in which multiple steady states exist. This basic identification problem in interpreting the long run implications of multiple growth regimes is illustrated in Figure 2, where a single capital type is assumed. If the production function follows the solid line for all capital/labor ratios k, then developed and underdeveloped economies will fail to converge. Alternatively, if the broken line represents the aggregate production function for capital/labor ratios between the capital levels of the underdeveloped economies and k^T , then convergence holds. Cross-section

 $^{^{18}\}mathrm{Recall}$ that for the two factor Cobb-Douglas technology, output per worker increases monotonically with the capital share.

¹⁹At the same time, the pattern of human and physical capital coefficients is not a specific implication of any growth model we are aware of.

data combining developed and undeveloped economies does not discriminate between the two candidate production functions.

Therefore, while our results show the compatibility of cross-country growth patterns with multiple steady states, they cannot be interpreted as a formal rejection of a single steady state model. On the other hand, our evidence of multiple regimes is consistent with the notion that cross-country growth rates are affected by the way capital is converted on the margin into output regardless of whether one interprets our regimes as stages of development or as multiple steady states.

ii. Residual heterogeneity

One way to interpret our empirical procedure is to observe that while the standard linear growth regression rules out any heterogeneity in the growth process across countries, we allow for such heterogeneity across country groups. The regression tree procedure assumes all heterogeneity disappears once one sorts the economies into subgroups. While this assumption is justifiable in the context of certain multiple steady state models, the assumption is nevertheless extreme as it rules out any country-specific differences. It is possible that each country obeys a regression of the form (2) with different coefficients. In this case, the regression tree procedure diminishes but does not eliminate heterogeneity in the cross-section regressions as it groups countries with similar laws of motion. As discussed in Pesaran and Smith (1994), this means that the withingroup regression coefficients represent averages of the underlying individual coefficients for each country. As a result, our evidence of within-group convergence is compatible with some long run differences between countries within a group.

iii. Omitted initial conditions

While the use of initial income and literacy as conditioning variables produces country groupings which seem overall quite reasonable, there are some clear anomalies in

the estimated regression tree. For example, Japan and Korea are assigned to group 3 along with El Salvador whereas Trinidad and Tobago and Uruguay are assigned to group 4 along with the United States. These anomalies would seem most plausibly explained by the existence of additional initial conditions beyond those we study which are relevant for determining long run growth patterns. One obvious candidate for such an omitted initial condition is "social capital" (see Coleman (1990) for a detailed discussion) which captures the role of cultural norms and values concerning interactions between individuals, which may range from attitudes towards work to respect for property rights, in economic growth. One obvious difficulty with a concept such as social capital is its lack of quantifiability, which indicates how econometric studies of the sort we have developed may be usefully augmented by country-specific studies.²⁰

6. Summary and conclusions

Taking as a starting place the work of Mankiw, Romer and Weil (1992), we have reexamined the Summers-Heston data set to see whether the cross-country growth process exhibits multiple regimes in which subgroups of countries defined by initial conditions obey separate linear models. Our results are twofold. First, we reject the cross-country linear model specification which underlies most empirical work on growth. Second, we use regression tree methods to identify groups of countries which obey a common model. This analysis reveals substantial differences between the aggregate production functions of economies with different initial conditions. These features illustrate the compatibility of growth rate behavior with a multiple steady state perspective.

One important extension of our work is to see whether the multiple regimes we identify can be shown to arise from some of the production or demand complementarities which have been proposed as explanations for long run divergence. The identification of these complementarities, in turn, will require a more careful understanding of within-country growth processes and thus seems likely to depend on the explicit analysis of a

²⁰Some evidence of the role of such factors may be found in Barro (1994), who finds correlations between different subjective measures of political freedom and growth.

dynamic panel of countries. This line of research has been initiated in Quah (1992a,b); see also Pesaran and Smith (1994) for analysis of many of the relevant econometric issues.

Data Appendix

Number	Country	(Y/L) _{i,1960}	LR _{i,1960}	Growth Rate	Income Class	Literacy Class
1	Algeria	2485	10.0	4.8	I	L
2	Angola	1588	5.0*	0.8	I	L
3	Benin	1116	5.0*	2.2	I	L
4	Botswana	959	na	8.6	I	na
5	Burkina Faso	529	2.0*	2.9	L	L
6	Burundi	755	14.0*	1.2	L	L
7	Cameroon	889	19.0*	5.7	I	L
8	Central African Republic	838	7.0*	1.5	I	L
9	Chad	908	6.0	-0.9	· I	L
10	People's Republic of the Congo	1009	16.0*	6.2	I	L
11	Egypt	907	26.0	6.0	I	L
12	Ethiopia	533	15.0†*	2.8	L	I
15	Ghana	1009	27.0*	1.0	I	L
17	Ivory Coast	1386	5.0*	5.1	I	L
18	Kenya	944	20.0*	4.8	I	L
20	Liberia	863	9.0*	3.3	I	L
21	Madagascar	1194	50.0†*	1.4	Ī	Ī
22	Malawi	455	25.0†*	4.8	Ĺ	L
23	Mali	737	2.0	2.1	L	L
24	Mauritania	777	5.0	3.3	L	L
25	Mauritius	1973	na	4.2	Ī	na
26	Morocco	1030	14.0	5.8	Ī	L
27	Mozambique	1420	8	1.4	Ī	L
28	Niger	539	1.0	4.4	L	Ĺ
29	Nigeria	1055	15.0*	2.8	Ī	L ·
30	Rwanda	460	16.0*	4.5	Ĺ	Ĺ
31	Senegal	1392	6.0*	2.5	Ī	Ĺ
32	Sierra Leone	511	7.0*	3.4	Ĺ	Ĺ
33	Somalia	901	2.0	1.8	Ī	L
34	South Africa	4768	57.0	3.9	Ī	Ī
35	Sudan	1254	13.0*	1.8	Ī	Ĺ
37	Tanzania	383	10.0	5.3	Ĺ	Ĺ
38	Togo	777	10.0	3.4	L	L
39	Tunisia	1623	16.0*	5.6	Ī	L
40	Uganda	601	35.0*	3.5	L	L
41	Zaire	594	31.0	0.9	Ĺ	Ĺ
42	Zambia	1410	29.0	2.1	Ī	L
43	Zimbabwe	1187	39.0*	5.1	Ī	L
46	Bangladesh	846	22.0*	4.0	Ī	L
47	Burma	517	60.0*	4.5	Ĺ	I
48	Hong Kong	3085	70.0	8.9	Ī	H
49	India	978	28.0*	3.6	Ï	L
52	Israel	4802	84.0*	5.9	Ï	H
53	Japan	3493	98.0*	6.8	I	H
54	Jordan	2183	32.0*	5.4	İ	L
55	Republic of Korea	1285	71.0	7.9	Ï	H
57	Malaysia	2154	53.0	7.1	Ī	I
58	Nepal	833			-	-

60	Pakistan	1077	15.0*	5.8	I	L
61	Philippines	1668	72.0	4.5	I	H
63	Singapore	2793	75.0†*	9.2	I	Н
64	Sri Lanka	1794	75.0*	3.7	I	Н
65	Syrian Arab Republic	2382	30.0	6.7	I	L
67	Thailand	1308	68.0	6.7	I	Н
70	Austria	5939	99.0	3.6	Н	Н
71	Belgium	6789	99.0†	3.5	Н	Н
73	Denmark	8551	99.0†	3.2	Н	Н
74	Finland	6527	99.0*	3.7	Н	Н
75	France	7215	99.0†	3.9	Н	Н
76	Federal Republic of Germany	7695	99.0†	3.3	Н	Н
77	Greece	2257	81.0	5.1	I	Н
79	Ireland	4411	97.0*	3.8	I	Н
80	Italy	4913	91.0*	3.8	I	Н
83	Netherlands	7689	99.0†	3.6	Н	Н
84	Norway	7938	99.0†*	4.3	Н	Н
85	Portugal	2272	62.0	4.4	I	I
86	Spain	3766	87.0	4.9	I	Н
87	Sweden	7802	99.0†*	3.1	Н	Н
88	Switzerland	10308	99.0†	2.5	Н	Н
89	Turkey	2274	38.0	5.2	I	L
90	United Kingdom	7634	99.0†	2.5	Н	Н
92	Canada	10286	99.0†	4.2	Н	Н
93	Costa Rica	3360	90.0†	4.7	I	Н
94	Dominican Republic	1939	65.0	5.1	I	I
95	El Salvador	2042	49.0*	3.3	I	L
96	Guatemala	2481	32.0	3.9	I	L
97	Haiti	1096	15.0	1.8	I	L
98	Honduras	1430	45.0*	4.0	I	L
99	Jamaica	2729	82.0	2.1	I	Н
100	Mexico	4229	65.0	5.5	I	I
101	Nicaragua	3195	57.0†	4.1	I	I
102	Panama	2423	73.0	5.9	I	H
103	Trinidad and Tobago	9253	93.0*	2.7	H	Н
104	United States of America	12362	98.0*	3.2	Н	Н
105	Argentina	4852	91.0	2.1	H	Н
106	Bolivia	1618	39.0	3.3	I	L
107	Brazil	1842	61.0	7.3	I	I
108	Chile	5189	84.0	2.6	H	Н
109	Columbia	2672	63.0*	5.0	I	I
110	Ecuador	2198	68.0*	5.7	I	Н
112	Paraguay	1951	75.0*	5.5	I	Н
113	Peru	3310	61.0	3.5	I	I
115	Uruguay	5119	94.0*	0.9	H	Н
116	Venezuela	10367	63.0*	1.9	H	I
117	Australia	8440	100.0†	3.8	H	Н
119	Indonesia	879	39.0*	5.5	I	L
120	New Zealand	9523	99.0†	2.7	H	H
121	Papua New Guinea	1781	29.0	3.5	I	L

[&]quot;Number" is the number given the country in the Summers and Heston [1988] data set.

na = not available.

† indicates that the Literacy Rate is for 1975 rather than 1960 as this is the next earliest available year.

* indicates that the Literacy Rate is for a year different, though no more than 2 years distant, from the specified year.

Technical Appendix: Regression tree analysis

This appendix describes the construction of a regression tree. The method can uncover general forms of nonlinearity in data; Breiman et al (1984) show that the regression tree method is consistent in the sense that, under suitable regularity conditions, the estimated piecewise linear regression function converges to the best nonlinear predictor (in a mean squared error sense) of the dependent variable of interest.

Suppose that the optimal predictor of y_j given the vector $X_j = (x_{1,\,j},...,x_{r,\,j})$ is, in a mean squared error sense, the function $f(X_j)$. The estimation issue is the determination of f(X) with little prior information on its form. One way of solving this problem is the following. Rewrite the support of each $x_{i,\,j}$ as the union of M intervals, $a_{i,\,0} \leq x_{i,\,j} < a_{i,\,1},...,a_{i,\,M-1} \leq x_{i,\,j} < a_{i,\,M}$. The support of X, X, can be expressed as the union of sets X_i , X_i , X_i , X_i as the union of sets X_i , X_i ,

$$f(X) \approx \sum_{m=1}^{M^r} \delta_m(X) X \beta_{S_m} \tag{A.1}$$

where $\delta_m(X)=1$ if $X\in S_m$, 0 otherwise and β_{S_m} is a constant vector. As the edges of each of the hyper-rectangles S_m are made small, this approximation can generally be made arbitrarily accurate.²¹

While the idea of estimating a piecewise linear approximation to f(X) is appealing, one quickly runs into a curse of dimensionality problem if one were simply to search over the possible hyper-rectangle partitions of S so as to choose a particular piecewise linear approximation of f(X). The problem is that the number of observations will quickly become very small relative to the number of hyper-rectangles in multiple dimensions, even for a small number of splits per individual variable. (See Härdle (1990)

²¹Notice that one can a priori set any of the elements of β_S equal to zero if one wants to use some variables for splitting without using them to predict within subgroups. We in fact do this for $LR_{i,1960}$.

for a discussion of this point.) Regression tree methods circumvent the curse of dimensionality by searching sequentially over the possible partitions of S.

The regression tree algorithm is as follows:

1. For each of the variables x_i , i=1...r, consider an initial split of the data into two subgroups according to the rule: assign observation j to $S_{(a,i)}$ if $x_{i,j} < a$, otherwise assign to $S_{(a^c,i)}$. Allowing a to range across the support of x_i traces out all possible binary splits of the data when x_i is the control. Repeating this for all i from 1 to r identifies all such binary splits. Let $\widehat{\beta}_{(a,i)}$ denote the OLS estimate for the regression of y_j onto X_j using observations assigned to $S_{(a,i)}$; $\widehat{\beta}_{(a^c,i)}$ is defined analogously. Some split variable x_i and some value a will minimize the sum of squared residuals (SSR)

$$\sum_{j \in S_{(a,i)}} (y_j - X_j \widehat{\beta}_{(a,i)})^2 + \sum_{j \in S_{(a^c,i)}} (y_j - X_j \widehat{\beta}_{(a^c,i)})^2$$
(A.2)

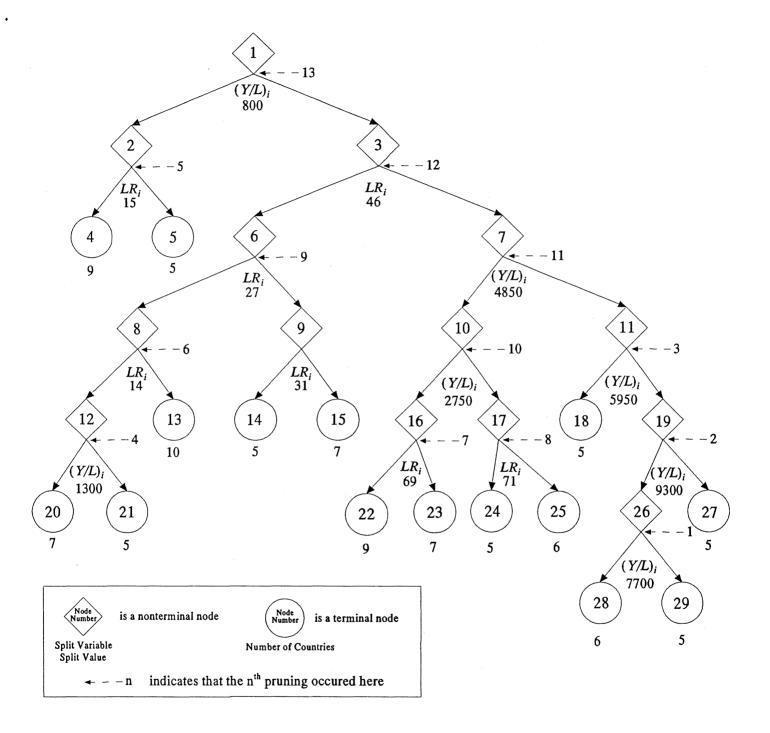
over all possible two-way splits. The x_i and a that minimize (A.2) define the initial split of the data into two subgroups which we call S_1 and S_2 ; denote this set of splits as T_1 .

2. Repeat step 1 on each of the two subsets S_1 and S_2 . The SSR minimizing split for observations in S_1 will define two new groups S_3 and S_4 ; S_5 and S_6 are constructed for observations in S_2 . Notice that these new splits may occur on different variables, i.e. $j \neq k$. Denote this new set of splits $S_3...S_6$ as T_2 . Repeat again for each of these new subsets and generate a new set of splits T_3 . As before, the splits in T_3 define disjoint subgroups of data. Sequential splitting of each subset terminates either when there is no SSR reduction from splitting or when the number of observations in the cell is less than or equal to twice the number of regressors. Figure 3 illustrates this splitting for the Heston-Summers data. Let T_L denote the set of subsets S_k which are not further split; these terminal splits lie at the "bottom" of the tree. The SSR for T_L equals

$$\sum_{S_m \in T_L} \sum_{j \in S_m} (y_j - X_j \widehat{\beta}_{S_m})^2 \tag{A.3}$$

3. The piecewise linear model generated by step 2 is most likely overparameterized as the data splits were costless. We now "prune" the tree which

Figure 3: Unpruned Regression Tree



produced T_L by incorporating a cost to data splits. Let the cost of splitting equal $\alpha \cdot (\#(N) - 1)$, where #(N) is the number of terminal nodes in a tree. For each α , one determines which set of terminal nodes minimizes

$$SSR + \alpha \cdot (\#(N) - 1), \tag{A.4}$$

working backwards from T_L . First, remove any terminal splits in T_L whose elimination reduces the value of (A.4), producing a new tree. Removal means the replacement of a pair of terminal nodes with a new terminal node which contains the set of observations whose split in the construction of T_L produced them. Next, remove all terminal splits of this new tree which, as before, are justified on the basis of minimizing (A.4). Continue this sequential elimination of terminal nodes until no further removals will reduce (A.4). This produces a tree with terminal nodes $T^*(\alpha)$. Constructing $T^*(\alpha)$ for all $0 \le \alpha \le \infty$ produces a series of trees and associated sets of terminal nodes starting with $T^*(0)=T_L$ that sequentially eliminates terminal splits so that $T^*(\infty)$ equals a single node which contains all observations. Figure 3 contains the tree used to produce our estimates in the text. Starting with an unpruned tree, increasing α from 0 first eliminates nodes 28 and 29, combining them to make node 26 terminal; further increasing α next combines nodes 27 and 28 to make node 19 terminal, etc.

4. Calculate a cross-validated estimate of the SSR for each $T^*(\alpha)$. For each observation in the terminal splits of a given tree, form the predictor $\widehat{\beta}_{-i,S_m}X_i$ for y_i where $\widehat{\beta}_{-i,S_m}$ is the OLS estimate of β within subgroup S_m when the *i*'th observation is omitted. Summing $(y_i - \widehat{\beta}_{-i,S_m}X_i)^2$ over all observations produces the cross-validated SSR. The $T^*(\alpha)$ with the smallest cross-validated SSR produces the piecewise linear approximation which converges to the best nonlinear predictor.

The regression tree method resembles one which chooses among different splits using the Akaike information criterion. The key features of the tree approach are 1) splits are sequential, so that only a subset of all possible splits is examined, 2) cross-validation is used to assess model fit, 3) no penalty value is assigned a priori; rather, all possible penalties are considered.

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