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# SURVIVAL OF THE SMALL FIRM AND THE ENTREPRENEUR UNDER DEMAND AND EFFICIENCY UNCERTAINTY

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No 700

## WARWICK ECONOMIC RESEARCH PAPERS

**DEPARTMENT OF ECONOMICS** 



# Survival of the Small Firm and the Entrepreneur under Demand and E¢ciency Uncertainty<sup>®</sup>

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#### **Abstract**

The objective of this paper is to oxer an answer to the question: why do some entrepreneurs wish to own another ...rm in the future after having closed an unsuccessful one? We ...rst show this question is relevant because making use of a sample of entrepreneurs in the UK who have experienced a business closure, we show that 45% of them have the desire to own another ...rm in the future, despite having an unsuccessful experience in small ...rm ownership. To tackle our question we develop a model where the pro...ts of the small ...rm depend on two ...rm-speci...c parameters: the e⊄ciency parameter, which represents the skills of the entrepreneur to manage and cope ecciently with the everyday tasks of the small ...rm, and the demand parameter, which denotes the success of the ...rm's product to attract demand or capture a market niche. It is found that our model answers our initial question by revealing the existence of a mechanism of entrepreneurial self-selection. Under such mechanism, skilful entrepreneurs are the only ones who wish to own another ...rm in the future, regardless of the degree of success in their previous venture, whereas unskilful entrepreneurs prefer to go to wage work. We show this mechanism accounts not only for the empirical evidence relevant to our initial question, but also for the rest of cases of entrepreneurs' attitudes after experiencing a business closure.

Keywords: Small Firm, Entrepreneur, Survival, Entrepreneurial Skills

JEL Classi...cation: J23, L11, L25, M13

<sup>&</sup>quot;I want to thank my supervisors Michael Waterson and Keith Cowling for their guidance and help, and to seminar participants at the University of Warwick for their comments. I am also grateful to David Storey for his help. The data was kindly provided by Robert Blackburn from Kingston University to whom I am indebted. Funding from CONACYT Mexico is also acknowledged. Errors in this document are my exclusive responsibility.

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#### 1 Introduction

Why do some small ...rm owners wish to start a new ...rm after having closed one that was not successful? In this paper we try to answer this question. Why is this question relevant? Firstly, because straightforward intuition provides two con‡icting hypotheses as answers. On one hand, we can argue that the small ...rm owner has learned from his mistakes and believes that in the following venture he can do better. This suggests the entrepreneur believes he has the potential talent to run successful ...rms, he was just unlucky in his previous venture. On the other hand, we can argue that the lack of success in his previous venture is a retection of the fact that he does not have the skills to run a successful ...rm. If he does not have what it takes, why would he want to start a new ...rm? Secondly, because we show that the desire of opening a new ...rm after having closed an unsuccessful one is a rather common occurrence amongst entrepreneurs. Utilising a survey of entrepreneurs in the United Kingdom who have recently experienced a business closure, we show that 45% of these entrepreneurs wish to start a new ...rm, despite the lack of success in their previous venture. Do these entrepreneurs have the talent to run successful ...rms?, or are they being irrational by hoping they will do better the next time given that it has been proved they do not have the necessary entrepreneurial skills? Both questions cannot be answered a¢rmatively. In any case, we believe an answer in one way or another will constitute ...ndings which should be considered by policy makers interested in the promotion and encouragement of start-ups and entrepreneurial activity. Hence, the importance of tackling our initial question.

Our question is also relevant in the context of research on small ...rms. In the Economics literature, the interest in research on small ...rms has been increasing in recent years. This can be regarded as a consequence of the recognition during the 80's and onwards that small ...rms account for a considerable share of economic activity (Acs and Audretsch, 1990; Braunerhjelm, 2000). In spite of the growing importance of small ...rms in the economy, it has been found that small ...rms consistently have lower likelihood of survival than larger ...rms do, a ...nding which is now regarded as an stylised result in small ...rm research (Geroski, 1995; Storey and Wynarczyk, 1996). In the light of these results, exorts have been directed to unravel the determinants of small ...rm survival (Bates, 1990; Audretsch, 1991; Kalleberg and Leicht, 1991; Mata and Portugal, 1994; Storey and Wynarczyk, 1996). Despite the fact that in some of these research the role the entrepreneur plays as owner and manager has been acknowledged to some degree, none of them look at the survival of the entrepreneur, in other words, at the outcome of the decision between keeping in entrepreneurialism by starting another ...rm after having closed the previous one, or going to wage work. Glad-

stone and Lee (1995, p. 27) on discussing the impact of the insolvency system in the UK on entrepreneurialism assert that '...there is still little or no concomitant recognition of, or accompanying policy, to rehabilitate entrepreneurs forced out of entrepreneurialism (...rm owners whose ...rms did not survive, my brackets), even though they are a vital part of the competitive cycle. The impact of failure on the individual entrepreneur has been of minimal interest to most theorists...' Therefore, by trying to answer why some small ...rm owners wish to start a new ...rm after having closed an unsuccessful one, we also contribute to the exorts aimed to understand the processes which determine the survival of small ...rms, and we also attempt to reduce the gap in the study of the forces which in‡uence the survival of the entrepreneur¹.

The paper has the following structure. In the next section, after specifying the de...nition of entrepreneur to be used throughout our analysis, we present empirical evidence on entrepreneurial survival which shows the relevance of our initial question. Such empirical evidence also reveals the whole spectrum of entrepreneurs' attitudes, which derive from the combination of having or not the desire to own another ...rm in the future, after having the experience of running successful ...rms or unsuccessful ones. In Section 3 the model and the assumptions we use to try to answer our initial question are introduced. In contrast to current literature, in our model we specify that the pro...ts of the small ...rms depend on two ...rm-speci...c determinants: the ecciency parameter, which represents the skills of the entrepreneur to manage and cope ecciently with the everyday tasks of the small ...rm, and the demand parameter, which denotes the success of the ...rm's product to attract demand or capture a market niche. We assume such parameters are independent of each other. In Section 4 we introduce an alternative model in which we assume the entrepreneur's ability are not restricted to skills to manage, but that they represent some type of "overall" skills. The purpose of this is to provide a benchmark case for the predictions obtained by our general model. In this section we also present the predictions oxered by our general model and by the alternative one, and we discuss the answers both models oxer to our initial question. It is found that our general model establishes that those entrepreneurs who start or have the desire to start a new ...rm after having closed an unsuccessful one, have skills to manage as large as those who are running successful ...rms. Contrary to this, the alternative model gives the explanation that such entrepreneurs should not exist, because the fact that the

<sup>&</sup>lt;sup>1</sup>Interestingly, in Labour Economics, research on the survival of individuals as self-employed has attracted a lot of attention (for a survey article see Le, 1999). However, such studies concentrate only on the outcome of staying in or exiting self-employment by the individual, without considering the fact that these individuals may or may not have owned several ...rms in the process. That is, that they may have decided to close a ...rm and have started a new one, which is our main concern.

small ...rm did not survive is simply the result that they do not have the necessary skills to run a successful ...rm. We believe our general model provides a more sensible answer to our initial question. However, to determine which model oxers more credible results, we state that such model should provide an explanation not only to our initial question, but also to the whole empirical evidence contained in Section 2.

In Section 5 we discuss which model is able to explain the empirical evidence. We found that our general model is successful in this task, whilst the alternative model fails. By means of revealing the existence of a mechanism of entrepreneurial self-selection, our general model is able to account for the empirical evidence on entrepreneurial survival. Under the mechanism of entrepreneurial self-selection, skilful entrepreneurs are the only ones who wish to own another ...rm in the future after having closed one, regardless of the degree of success in their previous venture, whereas unskilful entrepreneurs prefer to go to wage work. In this section, given that the alternative model, which uses the assumption that entrepreneurs have some type of "overall" skills, is unable to explain the empirical evidence, we also reach the following conclusion: when undertaking research on entrepreneurship if we consider data comprising small ...rm owners without any other discriminatory criterion, it is reasonable to suppose that the skills of such business owners are limited to skills to manage, and that they do not comprise skills to innovate or to spot pro...table opportunities. In Section 6 we address the robustness of some of our assumptions and the implications of alternative ones. Finally, Section 7 summarises our ...ndings and mentions paths for future research.

In summary, our paper answers our initial question by saying that the reason why some small ...rm owners wish to start a new ...rm after having closed an unsuccessful one is because they have the skills to run potentially successful ...rms. In fact, our ...ndings state that such behaviour is part of a mechanism of entrepreneurial self-selection. Under such mechanism, skilful entrepreneurs are the only ones who wish to own another ...rm in the future, regardless of the degree of success in their previous venture, whereas unskilful entrepreneurs prefer to go to wage work. Although this mechanism accounts for the empirical evidence on entrepreneurial survival in Section 2, we recognise that further research is needed to reject or fail to reject the prediction that those entrepreneurs who have the desire to start another ...rm, have indeed higher skills than those who prefer to go to wage work. In any case, we believe the ...ndings of this paper are a ...rst step in a research agenda aimed at the study of the survival of the entrepreneur.

#### 2 Preliminaries

#### 2.1 The De...nition of Entrepreneur

Despite being a fertile and growing area of research, there is no agreement amongst academics on the de...nition of entrepreneur. Across the literature, one article may use entrepreneur to refer to those who simply own and manage a ...rm, whereas others may include more characteristics, for instance, capacity of innovation or risk taking. Moreover, in some cases these de...nitions have been used interchangeably. Holtz-Eakin (2000) on addressing the question "Are small businesses entrepreneurial or just small?" points to the problem. He argues that 'The research literature to date, however, has not provided a clear resolution to this question. In part, this question has been avoided; the entrepreneurial virtues of new business are often assumed rather than examined' (p. 284).

Contrary to this, we restrict the de...nition of entrepreneur to be used in this article. To accomplish this we resort to one of the few articles which distinguishes and groups the di¤erent de...nitions of entrepreneurship. Tyson et al (1994) o¤ers four categories to classify the di¤erent de...nitions. The ...rst one is "Entrepreneurship as innovation". They include in this category those de...nitions built upon the schumpeterian view of entrepreneurs as agents of innovation, in terms of developing new products or methods of productions, identifying new markets or sources of supply, or developing new organisational forms. The second category is "Entrepreneurship as risk-taking". They group in this category those de...nitions which view entrepreneurs as having relatively low aversion risk, which enables them to undertake an innovation that others are not willing to attempt. The third category is "Entrepreneurship as stabilising force". The de...nitions included here are those which regard entrepreneurs as taking advantage of the state of disequilibrium of the economy, where the ine¢cient allocation of resources generates the opportunity for pro...table activities. The ...nal category they suggest is "Entrepreneurship as founding or owning and managing a small business". They assert that '...this view surfaces quite often as the empiricist's de...nition - understandably, given the practical di¢culties of identifying the population of "Schumpeterian innovators" or "risk takers" in an economy' (Tyson et al, 1994, p. 167).

This paper adheres to the de...nition used more by the empiricists and regards entrepreneurs simply as those who start or own and manage a small ...rm. Several reasons account for this decision. Firstly, me make use of empirical data to show why our initial question "why do some small ...rm owners wish to start a new ...rm after having closed one that was not successful?" is relevant, in the sense that starting a business after having closed

an unsuccessful one is a rather common occurrence amongst small ...rm owners. Clearly, the database we use focuses on individuals who own and manage their ...rms. Accordingly, we are bound to adopt the de...nition of entrepreneurship as founding or owning and managing a business. Our decision gains strength when we acknowledge the growing interest in the measurement of entrepreneurship amongst researchers and institutions, which in general implicitly or explicitly de...ne an entrepreneur as an individual who manages his own business<sup>2</sup>. Secondly, in order to try to answer our initial question, this paper proposes that the entrepreneurial skills of the small ...rm owners are in general of a restricted nature. Speci...cally we will argue that small ...rms owners have an endowment of skills to manage the business, that is, to deal ecciently with the day to day activities of the business<sup>3</sup>. This endowment varies from individual to individual. We argue that these managerial skills are in general not related with the ability to generate revenue for the ...rm, in other words, with the ability to select a product or service for which there is enough demand or there is a market niche. In summary, this paper will suggest that the entrepreneurial skills of small ...rm owners are in general restricted to managerial skills. Note that by no means we state that it is impossible for some small ...rm owners to have more than one type of skills. As will be shown, our argument states that when we de...ne entrepreneur as a small ...rm owner, then it is more sensible to assume that their skills are limited to managerial tasks in the sense de...ned later on in this paper, and that in general this managerial skills are not correlated with the ability to select and oxer an attractive product. Finally, it must be added that as a consequence of our de...nition of entrepreneur, we use the terms "...rm owner", "business owner", and "owner-manager" as synonyms of entrepreneur.

### 2.2 Empirical Evidence on Entrepreneurial Survival: Entrepreneurs who Re-enter and Obstinate Entrepreneurs

The study by Stokes and Blackburn (2001) "Opening up Business Closures: a Study of Businesses that Close and Owners' Exit Routes" is one in a kind. It is, perhaps, the only research which has addressed the question of what happens to the entrepreneur once his ...rm has not survived. The study was carried out in the United Kingdom. It comprised, as a ...rst stage, the elaboration of the questionnaire to be used to interview the small ...rm

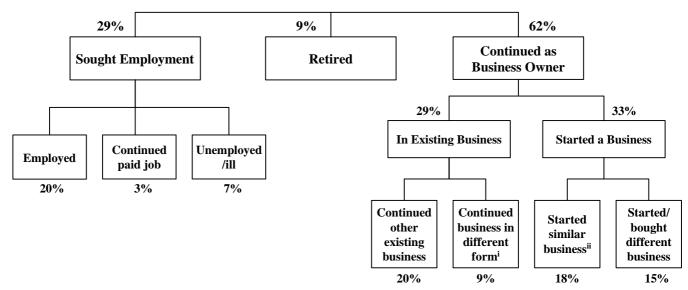
<sup>&</sup>lt;sup>2</sup>For instance, in the project "Global Entrepreneurship Monitor" where one of the principal objectives is to measure the level of entrepreneurial activity across several countries, entrepreneurship is de...ned as 'Any attempt at new business or new venture creation, such as self-employment, a new business organization, or the expansion of an existing business, by an individual, a team of individuals, or an established business' (Reynolds et al, 1999, p. 3).

<sup>&</sup>lt;sup>3</sup>A more extended exposition of what these skills might embody is contained in the next section.

owners. This questionnaire was built from interviews with 20 organisations of dizerent type, including private organizations (e.g. banks, accountants), non-pro...t organisations, and government consultants, which had experience in advising small business. In a second stage, the questionnaire was sent to a sample of 2719 owner-managers who had recently closed their businesses, from which 388 usable observations were obtained. The study collects a rich set of variables, which includes information on the ...rm (e.g. size, age), the owner-manager (e.g. reasons to start ...rm), ...nancial situation of the business at the time of closure, path followed by the business owner, attitudes to the experience of closing a business, learning experience, amongst others. The results of the study are impressive inasmuch as they provide the existing picture of the entrepreneurs' decision between sticking with entrepreneurialism or other alternatives, once the experience of business closure has occurred. As Stokes and Blackburn state, SB henceforth, 'The research has considerable implications for business educationalists, policy makers and ...nanciers. Those who have closed a business are strong candidates to become involved in a new venture, and should therefore be a prime target for those seeking to advise or ...nance new business' (p. ii). In this sense, the ...ndings by SB are subject to provide support on the relevance of our initial question. We will proceed as follows. As introduction, we ...rst provide evidence that some entrepreneurs start new ...rms after having closed one, that is, evidence on entrepreneurial re-entry. However, our question concentrates on those entrepreneurs who wish to start new ...rms, after having closed unsuccessful ones, that is, on the obstinate entrepreneurs. The SB study is also helpful in this respect, as it provides evidence that these entrepreneurs do exist, and that they might represent a considerable share of the population of small ...rm owners. Thus, in a second stage, we reproduce this evidence.

In this paper we make use of two ...gures from SB. The ...rst one, Figure 1, reproduces the ...gure "Business owner exits - what they did next" (SB, p. 17), except for the notes (i) and (ii) which were added for explanatory purposes. Figure 1 displays the answers by the owner-managers, and the percentage which answered in this way, to the question "What did you do after leaving the business?" Therefore, Figure 1 exectively provides evidence on entrepreneurial re-entry. The relevance of the ...ndings from Figure 1 is that, to the best of my knowledge, a serious research on entrepreneurial re-entry had not been undertaken, until the SB study. Figure 1 speaks for itself, although some features are worth pointing out. Firstly, the ...gure shows that 62% of the entrepreneurs in the sample remained in entrepreneurialism after having experienced a business closure, as opposed to 29% who opted for paid employment. Thus, we can exectively say that 29% of entrepreneurs in the sample

#### Fate of the business owner



<sup>&</sup>lt;sup>i</sup> It refers to a different organisational-legal form

Figure 1: "Business owner exits - what they did next" from Stokes and Blackburn (2001, p. 17)

did not "survive". The percentage of surviving entrepreneurs is further classi...ed into those who started a new business, 33%, and those who continued in an existing business, 29%. One point is worth noting. Looking at the ...nal sub-category "Continued business in di¤erent legal form", it does not seem to ...t in the de...nition of closing a business as understood for economic purposes. That is, this sub-category refers to those entrepreneurs who did a legal change to their businesses, but from an economic point of view it is still the same ...rm o¤ering the same product. As a consequence, the observations in this sub-category should be ignored. This is not the case with the sub-category "Started a similar business in a di¤erent location", because location itself is a source of product di¤erentiation. Hence, it can be argued that these entrepreneurs indeed started a new ...rm. Finally, the sub-category "Continued other existing business" reveals that at least 20% of the sample were entrepreneurs that were running more than one ...rm at the same time. This is consistent with the term "Portfolio owners" suggested by Storey (1994), on referring to the ...ndings of Storey et al (1987) that it is not uncommon for some entrepreneurs to have ownership interests in more than one ...rm. Overall, removing the observations in the ...nal sub-category "Continued business in

ii It refers to start a similar business in a different location

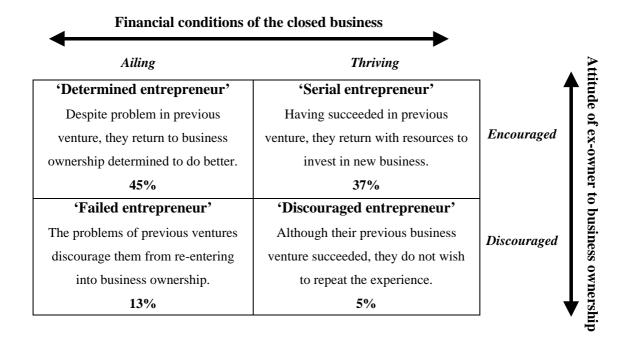


Figure 2: "A matrix of owners' responses to business closure" from Stokes and Blackburn (2001, p.29)

di¤erent legal form", Figure 1 reveals that 58% percent of the owner-managers in the SB study were entrepreneurs who re-entered with a new ...rm or continued as business owners, despite having closed a previous business.

These ...gures on entrepreneurial re-entry do not oxer any information on whether the closed business was successful or not. Furthermore, they only show those entrepreneurs which in fact started a new ...rm, and not those who wished to do so but did not re-enter. To amend this situation Figure 2 reproduces the ...gure "A matrix of owners' responses to business closure" from SB (p. 29). It classi...es the entrepreneurs in four quadrants, depending on the owner's view whether the business was ...nancially ailing or thriving at the time of closure, and on whether the owner felt encouraged or discouraged to own a business in the future given the experience of closure. Each quadrant also shows the percentage of owners which ...t into the category. It is important to add that when answering these questions the owners had the option of choosing from 1 to 5, where 5 meant thriving (encouraged) and 1 ailing (discouraged). Thus, Figure 2 should be seen as having in the axis the scale 1 to 5. Given the nature of the questions, we can state that the top row of Figure 2 includes

those entrepreneurs who wish to start a new ...rm, as opposed to those in the bottom row who want to leave entrepreneurialism. On the other hand, the left column comprises those entrepreneurs who saw their ...rms as ...nancially ailing at the time of closure. Common sense would suggest that ...rm's success is related to its ...nancial performance. We can argue then that the left column shows those entrepreneurs who were running unsuccessful ...rms, contrary to those in the left column who regarded their ...rms as successful. In this sense, the top-left quadrant represents the obstinate entrepreneurs, i.e., those entrepreneurs who wish to start a new ...rm, even though their previous ventures were unsuccessful. According to SB, these are the "determined entrepreneurs", who represent 45% of the sample, and in fact they are the single largest group of the four. Figure 2 also shows the other three possibilities: those who had successful ...rms and wish to start a new ...rm, the "serial entrepreneurs"; those who despite having successful ...rms do not want to remain in entrepreneurialism, the "discouraged entrepreneurs"; and those who were running unsuccessful ...rms and do not want to own a business in the future, the "failed entrepreneurs". Interestingly, the group of "discouraged entrepreneurs" represents the antagonistic case to the one we try to explain. Why do these individuals want to leave entrepreneurialism if they had the experience of running a successful business? Is not this proof enough that they are skilful entrepreneurs? As will be shown, in our attempt to explain the reasons which drive the "determined entrepreneurs" to start a new ...rm despite not being successful in the previous one, we also try to explain the other three possibilities included in Figure 2.

Regarding Figure 2, an issue must be addressed. The right column of Figure 2 may reveal an apparent inconsistency: why would some entrepreneurs close their ...rms despite being ...nancially thriving? Although not the only ones, two possibilities can explain this situation. Firstly, it is hard to imagine a small ...rm which was ...nancially thriving throughout its life span. Thus, it could be possible that by answering thriving or ailing the owners tended to describe the recent average performance of their ...rms. Consequently, it is not unlikely to suppose that some entrepreneurs in the right column of Figure 2 had ...rms who were meeting their expectations once, i.e., that were successful, but its performance started to decline. Secondly, for those ...rms in the right column of Figure 2 which were indeed ...nancially thriving, it can be the case that such performance might have attracted the attention of other entrepreneurs. In this sense, it is not unlikely that if a price large enough was oxered to the owners of these successful ...rms, some of them might have accepted to sell their ...rms. Under these views, the apparent inconsistency between success and closure reduces.

The most important point from Figure 2 is that it reveals that 45% of entrepreneurs in the

sample have the desire of keeping in entrepreneurialism, even though they did not succeed in their previous venture. We have no grounds to assert that the sample in the SB study is not fully representative of the populations of entrepreneurs who have experienced a business closure in the UK<sup>4</sup>. Nevertheless, we believe that this rather high percentage indicates the relevance of the question we try to tackle. We now introduce the model which might help us to explain this evidence.

#### 3 The Model

The model assumes the objective of the individual is to maximise his lifetime utility. He will do so by choosing between working in a paid job or setting up and running a ...rm. Here we are invoking the so called "income choice model" which can be traced back to Knight (1921). The individual obtains utility U=W when he is an employee and  $U= + \xi$  when he is running his own ...rm, where W is the wage from the paid job and  $+ \xi$  or denotes the extra satisfaction to the individual for being his own boss, which we assume as non-constant across individuals. We also de...ne  $\xi$  as the "entrepreneurial spirit" of the individual. The individual discounts the future with rate  $0 < \delta \cdot 1$  over his life span T. Thus, the problem for the individual is max  $\frac{T}{t=1} \delta^{t_1} U_t$  by deciding between a paid job or running his own ...rm.

The individual knows his own  $\xi$ , which is constant over time, and has perfect foresight on future values of W. For the sake of simplicity we assume W remains constant. If the individual decides to run a ...rm, he will enter an industry characterised by monopolistic competition where the technological conditions of such industry and the phase of the product life cycle suggest incumbent ...rms are not axected by economies of scale, and as a result they do not need to grow to survive. The purpose of these assumptions is to simplify the analysis by allowing the ...rm to ignore its competitors<sup>5</sup> and by eliminating the requirement to grow to survive found as empirical regularity for small ...rms in the manufacturing sector<sup>6</sup>. We

<sup>&</sup>lt;sup>4</sup>According to SB, the 388 usable responses were obtained from HSBC bank customers who closed a business account (36%), from Dun and Bradstreet lists of existing business (5%), and from closures identi…ed during research on other projects by the Small Business Research Centre, Kingston University (59%).

<sup>&</sup>lt;sup>5</sup>We use the de...nition of monopolistic competition proposed by Hart (1985). He points out, in the spirit of Chamberlin (1933), that monopolistic competition might be de...ned as one where there are many ...rms producing di¤erentiated commodities, each ...rm is negligible so it can ignore its impact and reactions from other ...rms, and each ...rms faces a downward sloping demand curve.

<sup>&</sup>lt;sup>6</sup>There is an abundant literature which provides empirical support to the fact that small ...rms' presence and survival in the manufacturing sector depend on the technological conditions of the industry, suggesting that economies of scale play a role. See, for instance, White (1982), Acs and Audretsch (1989), Audretsch

now discuss the nature of the entrepreneurial skills to be used in this paper.

On the small ...rm and entrepreneurship literature there is now a tradition to assume that the pro...ts of the small ...rm depend on the talent or skills of its owner. Lucas (1978) was the ...rst who put forward the notion that ...rm's pro...ts depend on the talent of the managers. In his model he shows how variations in talent across managers lead to a size distribution of ...rms. Jovanovic (1982) proposed that ecciency was the ...rm-speci...c determinant of pro...ts. In his model, ...rms start small and those which discover they are e⊄cient grow and survive. Later on, Frank (1988) merged the two ideas by assuming that the skills or talent of the entrepreneur determines the ecciency of the small ...rm, and thereby its pro...ts and survival. Further theoretical and empirical studies show that it became rather common to assume that small ...rm pro...ts depend on the skills of the entrepreneur<sup>7</sup>. The points to highlight in these papers are that they assume the skills of the entrepreneur are the only ...rm-speci...c determinant of pro...ts, and that they do not discuss what these skills entail. Contrary to the models such as the ones in Jovanovic (1982) and Frank (1988), we assume the pro...ts of the small ...rm depend on two ...rm-speci...c determinants, which we call the e⊄ciency and the demand parameters, and we restrict the nature of the entrepreneurial skills of the small ...rm owner. More speci...cally, we assume a pro...t function for the small ...rm of the following form

$$+^{ij} = pQ^{i}p, \alpha^{ij}^{\phantom{ij}} + \frac{1}{\alpha^{j}}cQ^{i}p, \alpha^{ij}^{\phantom{ij}}. \tag{1}$$

These are the pro...ts for entrepreneur j 2 J running ...rm i 2 I, where  $I \setminus J = \ref{n}$ , and where p is the price of the good/service oxered or to be oxered by the ...rm, and Q ( $\mathfrak t$ ) represents the demand function. The demand parameter is represented by  $\alpha$ . It denotes how successful the ...rm's product is in attracting customers or in capturing a market niche. A high value in  $\alpha^{ij}$  would mean that entrepreneur j is running the small ...rm i which is oxering a product or service that is very appealing to customers, which in turn is generating relatively large volumes of revenue to the small ...rm. The e $\mathfrak t$ ciency parameter is represented by  $\theta$ . It denotes the skills of the entrepreneur to run a business, which are directly translated as the e $\mathfrak t$ ciency of the ...rm. A skilful entrepreneur would be represented by a high value in  $\theta^j$ ,

<sup>(1991),</sup> Mata and Portugal (1994), Geroski (1995). Interestingly, the very few studies that have looked at the service sector (e.g. Audretsch et al, 1999), or at industries in the mature phase of the product life cycle (Agarwal and Audretsch, 1999 and 2001; Agarwal and Gort, 1996) have found that small ...rms in these circumstances do not need to grow survive. This can be explained by accounting for the small size of the minimum eccient scale in these industries.

<sup>&</sup>lt;sup>7</sup>See, for instance, Evans and Jovanovic (1989), Bates (1990), Holtz-Eakin et al (1994), Cressy (1996), Storey and Wynarczyk (1996).

which in turns means he is able to run his own ...rm more e $\$ ciently<sup>8</sup>. We further assume that these parameters are a source of uncertainty for the entrepreneur because they are unknown to him. He only knows that his "true" skills and "true" demand for his ...rm's product are random draws from some distributions. The only way the entrepreneur can learn the parameters  $\alpha^{ij}$  and  $\theta^j$  is by running a ...rm. Speci...cally, we assume that

A.1  $\alpha$  is an i.i.d. stochastic variable with cumulative distribution function (CDF)  $A(\mathfrak{k})$ , with support [0,1).  $A(\mathfrak{k})$  is continuous and twice dimerentiable.  $A(\mathfrak{k})$  is known by the individual.

A.2  $\theta$  is an i.i.d. stochastic variable. It has a CDF  $G(\mathfrak{k})$  with support (0, 1).  $G(\mathfrak{k})$  is continuous and twice di¤erentiable. The individual knows the form of  $G(\mathfrak{k})$ .

One consequence of these assumptions is that the parameters  $\alpha$  and  $\theta$  are uncorrelated with each other. Furthermore, note that by assuming the pro...ts of the small ...rm depend on these two uncorrelated ...rm-speci...c determinants, and by assuming that the ...rm's demand function is only axected by the parameter  $\alpha^{ij}$ , we restrict the nature of the entrepreneurial skills of the small ...rm owner. In other words, our framework supposes that the entrepreneurial skills  $\theta^{j}$  are limited to skills to manage the ...rm, and do not include the ability to select and oxer an attractive product, as represented by  $\alpha^{ij}$ , which might guarantee large revenue to the ...rm. Without attempting an exhaustive lists, our de...nition of the parameter  $\theta^{j}$ , include the entrepreneur's ability to organise and assume the responsibility of the activities of the small ...rm, to select the cheapest inputs given a desire level of quality, to deal with suppliers and, perhaps, employees, to ensure that the production of goods or services in the ...rm is done in the best possible way using the resources available, amongst others. In general, they represent the skills to undertake ecciently the everyday activities of the ...rm and to tackle the problems that might arise. As can be seen, our de...nition of entrepreneurial skills do not includes the notion of "Schumpeterian" innovators, but is closer to the de...nition of the entrepreneur's "general ability" put forward by Marshall<sup>9</sup>.

<sup>&</sup>lt;sup>8</sup>Two other important dimensions of entrepreneurship which might a¤ect the pro…ts of the small …rm are the entrepreneur's degree of risk aversion and the entrepreneur's degree of disutility of e¤ort. To keep our model simple, we omit them in the present analysis. In a later section we discuss the likely impact of their inclusion.

<sup>&</sup>lt;sup>9</sup>He de...nes the entrepreneur's "general ability" as the one which allows him 'to be able to bear in mind many things at a time, to have everything ready when wanted, to act promptly and show resource when anything goes wrong, to accommodate oneself quickly to changes, to be steady and trustworthy, to have always a reserve of force...' Marshall (1930, pp. 206 - 207).

Similarly, this paper follows those which have explicitly acknowledge the possibility that the entrepreneur may have skills which are restricted to speci...c activities<sup>10</sup>.

The following additional assumption are made about the pro...t function and about the industry the small ...rm would operate in:

A.3  $Q(p, \alpha^{ij}) = D(\alpha^{ij})_i$  bp is the demand function the small ...rm faces, where b>0 and p is the price of the good/service. Since the industry is subject to monopolistic competition, elasticities of substitution between any ...rm's good and the rest are assumed to be zero, and only the price of the ...rm's own good axects the ...rm's demand. The demand function has the following properties:

$$\partial D^{\mathbf{i}} \alpha^{ij} \mathcal{L}^{\pm} \partial \alpha > 0, \ \partial^2 D^{\mathbf{i}} \alpha^{ij} \mathcal{L}^{\pm} \partial \alpha^2 < 0.$$
 (2)

A.4 All operating ...rms have the same cost structure which they acquire after paying the exogenous sunk cost k > 0, which is the same for every ...rm.

A.5 The cost function  $\frac{1}{\theta^j}cQ$   $(p,\alpha^{ij})$  presents constant marginal costs, where c>0. We also assume that there exist a  $Q^{\max}$  such that for any  $Q>Q^{\max}$ , c=1.

These assumptions serve dixerent purposes. Conditions A.4 and A.5 together imply all ...rms can potentially produce the same amount of output. Note that, due to the assumption of monopolistic competition, all ...rms are by de...nition small, which means that should the size of ...rms be measured by production levels,  $Q^{\text{max}}$  is small enough for all ...rms to ...t in the small size category. Condition A.5 also tells us that marginal cost is constant over the feasible production range. Intuitively, this captures the assumption that ...rms are not axected by economies of scale, since the average cost is constant over the production range. Thus, growing to reach the minimum excient scale is not a requisite for the ...rms to remain competitive.

Prior to owning a ...rm, the individual ignores his entrepreneurial skills and whether or not the product/service he is planning to oxer will attract enough demand, i.e., he ignores his endowment of  $\alpha^{ij}$  and  $\theta^j$ . Once the individual runs a ...rm for the ...rst time, nature

<sup>&</sup>lt;sup>10</sup>Our model is similar to the ones in Holmes and Schmitz (1990) and Gi¤ord (1993) where it is assumed there are two types of entrepreneurial abilities: talent to manage and talent to develop new products. However, our model di¤ers from theirs in we are interested in the study of small ...rm and entrepreneurial survival, whilst Holmes and Schmitz (1990) concentrate on the sale and buy of business, and Gi¤ord (1993) focuses on the distribution of ...rm sizes and the choice of specialisation as innovative entrepreneur or managerial entrepreneur.

determines these values from the CDFs A ( $\mathfrak{t}$ ) and G ( $\mathfrak{t}$ ), respectively. Additionally, when the individual is running a ...rm, he does not observe these values directly, but indirectly through realisations in every period. This process is represented by

$$\varphi_t^{ij} = \alpha^{ij} + \omega_t ,$$

$$\eta_t^j = \theta^j + \omega_t ,$$
(3)

where  $\omega$  is an i.i.d. normal random variable with mean zero and variance  $\sigma^2$ . Once the ...rm is in operation, the entrepreneur learns about its own e $\Phi$ ciency and demand by observing the realisations  $\varphi_t^{ij}$  and  $\eta_t^j$  in every period. We assume that the learning process, or in other words, the method the entrepreneur uses to estimate and update his beliefs about  $\alpha^{ij}$  and  $\theta^j$  in every period is a bayesian method.

#### Pro...t Maximisation

The objective of the individual when he is running a ...rm is pro...t maximisation. Since pro...ts depend on the parameters  $\alpha$  and  $\theta$ , the maximised value of pro...ts will depend on the speci...c parameters the individual is endowed with. The maximisation problem is represented as

where  $p_t$  represents the price the monopolistic ...rm chooses to apply, and  $\alpha_B^{ij}$  and  $\theta_B^j$  denotes the bayesian estimator of  $\alpha^{ij}$  and  $\theta^j$ , respectively. We also assume the individual starts a ...rm in period e. Since the expected value of future values of a bayesian estimator is equal to the current bayesian estimator, i.e.,  $E\left[\alpha_B\right]_{t+z} = \left[\alpha_B\right]_t$  for any z>0, where  $E\left[\ell\right]$  denotes the expectation operator<sup>11</sup>, the problem reduces to calculate the maximisation problem just for the period t=e. The ...rst order conditions give

$$p \, \mathfrak{t} \, \frac{\partial Q}{\partial p} + Q^{\mathbf{i}} p, \alpha_B^{ij} \, \mathfrak{t}_{\mathbf{i}} \, \frac{c}{\theta_B^j} \frac{\partial Q}{\partial p} = 0 , \qquad (4)$$

which rearranged provides the standard mark-up rule

$$\frac{p_i \frac{1}{\theta_B^j} c}{p} = \frac{1}{\varepsilon \alpha_B^{ij}} , \qquad (5)$$

<sup>&</sup>lt;sup>11</sup>See Winkler (1972, p. 204).

Equation (5) spells out the exect the demand and e $\Phi$ ciency parameters have on the pricing strategy of the ...rm and, ultimately, on the pro...ts of the ...rm. The more skilful the entrepreneur is, i.e., the higher  $\theta^j$ , the higher the mark-up is. Likewise, the higher the demand parameter, the more inelastic the price elasticity  $\varepsilon^i \alpha_B^{ij}$  is, and the higher the mark-up is.

Let the optimum price and quantity be expressed as

$$p^{\mathbf{m}} \stackrel{\mathbf{i}}{\sim} p \stackrel{\mathbf{i}}{\mathbf{i}} \alpha_{B}^{ij}, \theta_{B}^{j} \mathbf{t}$$
 
$$Q^{\mathbf{m}} \stackrel{\mathbf{i}}{\sim} Q \stackrel{\mathbf{i}}{\mathbf{i}} \alpha_{B}^{ij}, \theta_{B}^{j} \mathbf{t}$$

and the solution to the maximisation problem as

$$\max_{p_t} \mathbf{P}_{\substack{T_{\mathbf{i}} \ 1 \ e}}^{T_{\mathbf{i}} \ 1} \delta^{t_{\mathbf{i}} \ e} \mathbf{i}_{\mid ij} + \xi^{j} \mathbf{t}_{t} \quad \mathbf{i}_{\mid a} \mathbf{i}_{\alpha_B^{ij}, \theta_B^{j}} \mathbf{t}_{t} + \xi^{j} \mathbf{t}_{t} \quad \mathbf{i}_{\mid a} \mathbf{i}_{\alpha_B^{ij}, \theta_B^{j}} \mathbf{t}_{t} + \xi^{j} \mathbf{t}_{t} \quad \mathbf{i}_{\mid a} \delta^{T_{\mathbf{i}} \ e} \mathbf{t}_{t}$$
s.t.  $\alpha_B^{ij}$  and  $\theta_B^{ij}$ . (6)

This is the discounted value of the maximum expected utility from running a ...rm. It can be shown that the second order conditions for a maximum are satis...ed. As can be seen, the maximum expected pro...ts  $\mid \overset{\mathbf{i}}{\alpha} \overset{ij}{B}, \theta^j_B$ , from now on simply pro...ts, are a function of the parameters  $\alpha^{ij}$  and  $\theta^j$  which are updated in a bayesian fashion every period. The next lemmas are presented for mathematical rigorousity and establish the properties of the pro...ts with respect to the demand and ecciency parameters. To save on notation we drop the superscripts i, and j, and the subscripts t and B.

Lemma 1. The pro...ts are an increasing function of e $\diamondsuit$ ciency:  $\frac{\partial \mid "(\alpha,\theta)}{\partial \theta} > 0$ .

Proof. The ...rst order conditions (4) are expressed as  $\mathbf{j}$   $bp + D\left(\alpha\right)\mathbf{j}$   $bp + \frac{cb}{\theta} = 0$ , thus  $p\left(\alpha,\theta\right) = \frac{D(\alpha)}{2b} + \frac{c}{2\theta}$ . The demand function is  $Q\left(p,\alpha\right) = D\left(\alpha\right) + bp$ . Hence,  $Q\left(\alpha,\theta\right) = \frac{D(\alpha)}{2}\mathbf{j}\mathbf{j}$  and  $\mathbf{j}^{\parallel}\left(\alpha,\theta\right) = \frac{(bc_{\mathbf{j}}\theta D(\alpha))^2}{4b\theta^2}\mathbf{j}$ . From here it follows that  $\frac{\partial\mathbf{j}^{\parallel}\left(\alpha,\theta\right)}{\partial\theta} = \frac{c}{2\theta^3}\left(\theta D\left(\alpha\right)\mathbf{j}\right)$ , which rearranged yields  $\frac{\partial\mathbf{j}^{\parallel}\left(\alpha,\theta\right)}{\partial\theta} = \frac{c}{\theta^2}\frac{D(\alpha)}{2}\mathbf{j}\mathbf{j}$ . Now, the terms inside the brackets in the right-hand-side are equivalent to  $Q\left(\alpha,\theta\right)$ . In this way we can write  $\frac{\partial\mathbf{j}^{\parallel}\left(\alpha,\theta\right)}{\partial\theta} = \frac{c}{\theta^2}Q\left(\alpha,\theta\right)$  and thus  $\frac{\partial\mathbf{j}^{\parallel}\left(\alpha,\theta\right)}{\partial\theta} > 0$ .  $\mathbf{\xi}$ 

Lemma 2. The pro…ts are a function of the demand parameter in the following way: whenever  $p\left(\alpha,\theta\right)>MC$  we have  $\frac{\partial_{+}^{\parallel n}(\alpha,\theta)}{\partial\alpha}>0$ , and for  $p\left(\alpha,\theta\right)>MC+\frac{1}{2b}\left(\frac{\partial D(\alpha)}{\partial\alpha}\right)^{2}$  i  $\frac{\partial^{2}D(\alpha)}{\partial\alpha^{2}}$  we have  $\frac{\partial_{-}^{2}^{\parallel n}(\alpha,\theta)}{\partial\alpha^{2}}<0$ , where  $MC=\frac{c}{\theta}$  is the marginal cost.

Proof. From the proof of Lemma 1 we obtain  $\frac{\partial_{+}^{+}{}^{\pi}(\alpha,\theta)}{\partial \alpha} = \frac{\partial D(\alpha)}{\partial \alpha} \frac{D(\alpha)}{2b}_{i} \frac{c}{2\theta}$ . From the value of  $p(\alpha,\theta)$  we have  $\frac{D(\alpha)}{2b} = p(\alpha,\theta)_{i} \frac{c}{2\theta}$ , which inserted in the term in brackets renders

 $\frac{\partial_{+}^{\mathbf{n}}(\alpha,\theta)}{\partial\alpha} = \frac{\partial D(\alpha)}{\partial\alpha} \stackrel{\mathbf{i}}{p} (\alpha,\theta) \stackrel{\mathbf{c}}{\mathbf{i}} \stackrel{\mathbf{c}}{\mathbf{f}}. \text{ The sign of this expression is positive whenever } p(\alpha,\theta) > \frac{c}{\theta}.$  Regarding the second part, we calculate  $\frac{\partial^{2}_{+}^{\mathbf{n}}(\alpha,\theta)}{\partial\alpha^{2}} = \frac{1}{2b} \frac{\partial D(\alpha)}{\partial\alpha} \stackrel{\mathbf{c}}{\mathbf{g}} + \frac{\partial^{2}D(\alpha)}{\partial\alpha^{2}} \stackrel{\mathbf{i}}{\mathbf{g}} p(\alpha,\theta) \stackrel{\mathbf{c}}{\mathbf{g}}. \text{ We require } \frac{\partial^{2}_{+}^{\mathbf{n}}(\alpha,\theta)}{\partial\alpha^{2}} < 0 \text{ , so we evaluate under which conditions } \frac{1}{2b} \frac{\partial D(\alpha)}{\partial\alpha} \stackrel{\mathbf{c}}{\mathbf{g}} + \frac{\partial^{2}D(\alpha)}{\partial\alpha^{2}} \stackrel{\mathbf{i}}{\mathbf{g}} p(\alpha,\theta) \stackrel{\mathbf{c}}{\mathbf{g}} < 0.$  Rearranging for  $p(\alpha,\theta)$  we ...nd that  $\frac{\partial^{2}_{+}^{\mathbf{n}}(\alpha,\theta)}{\partial\alpha^{2}} < 0 \text{ takes place whenever } p(\alpha_{B},\theta_{B}) > \frac{c}{\theta} + \frac{1}{2b} \frac{\partial D(\alpha)}{\partial\alpha} \stackrel{\mathbf{c}}{\mathbf{g}} \stackrel{\mathbf{c}}{\mathbf{g}} > \frac{\partial^{2}D(\alpha)}{\partial\alpha^{2}} \stackrel{\mathbf{c}}{\mathbf{g}} \stackrel{\mathbf{c}}{\mathbf{g}} > \frac{\partial^{2}D(\alpha)}{\partial\alpha^{2}} \stackrel{\mathbf{c}}{\mathbf{g}} \stackrel{\mathbf{c}}{\mathbf{g}} > \frac{\partial^{2}D(\alpha)}{\partial\alpha^{2}} \stackrel{\mathbf{c}}{\mathbf{g}} > \frac{\partial^{2}$ 

#### 3.1 The Decision to Start a Firm

The individual will choose to work in a paid job or to set up and run a ...rm depending on whether or not the expected utility in one state is larger than it is in the other. When the individual has not started a ...rm before, the only information he has available to calculate the expected pro...ts from running a ...rm is the distribution of the parameters  $\alpha$  and  $\theta$ . At this stage the only two alternative states are to start a ...rm or to work in a paid job. Under this situation, the maximisation problem for the individual can be expressed as choosing

arg max 
$$W^j$$
,  $E \max_{p} \mathbf{i} \mid ^{ij} + \xi^j$ , (7)

where  $\mid^{ij}$  is speci...ed by (1), and E [4] denotes the expectation operator. At this stage, the individual is constrained to rely on the expected value of the maximum pro...ts as he has no other way to infer better estimators for his true parameters. This expression is rewritten as

arg max 
$$W^j$$
,  $E_{\alpha,\theta}[ \mid ^{\pi}(\alpha,\theta)] + \xi^j$  (8)

where we de...ne  $+ (\alpha, \theta)$  as the value of maximised pro...ts, and therefore

$$E_{\alpha,\theta}[ \mid (\alpha,\theta)] \quad (\alpha,\theta) \quad dA \quad (\alpha,\theta) \quad dG \quad (\alpha,\theta) \quad dG \quad (\beta) \quad (\beta)$$

as its expected value. Rearranging expression (8) we obtain

We are now in position to state that whenever the following expression is true, the individual has an incentive to turn down paid job and start a ...rm

$$E_{\alpha,\theta}[ \mid {}^{\mathfrak{m}}(\alpha,\theta)] , W^{j} \mid \xi^{j} . \tag{11}$$

Note that the above inequality does not state that individual j will enter the industry in case it is ful...lled. To enter the industry the individual requires funds to set up the ...rm and cover the sunk costs. The process whereby individuals gather these funds and the di¢culties they may face are issues not included in the scope of this paper<sup>12</sup> 13.

Note that the assumptions of our model are consistent with the de...nition of entrepreneur we use in this paper as those who started or own and manage his ...rm. Firstly, by assuming that the individual seeks to maximise utility by choosing between running his own ...rm or being an employee, we eliminate any possibility that entrepreneurs would start a ...rm because they have generated any kind of innovation or because they have spotted a pro...table opportunity. This is reinforced with the fact that we assume the demand parameter  $\alpha$  to be a random draw and that the entrepreneur is not able to provide a better forecast apart from the mean of the parameter's distribution. Additionally, as has been already discussed, by assuming that  $\alpha$  and  $\theta$  are independent random variables no correlated with each other, we restrict the skills of the entrepreneurs to manage. Secondly, by making no speci...c assumptions about those individuals who start and run a ...rm, our model implies all entrepreneurs have the same degree of risk aversion. We now turn to the predictions this model oxers to answer our initial question.

#### 4 Results

Once the individual has decided to set up and run a ...rm at the end of a given period, it is assumed that the ...rm is formally in operation in the next one. As de...ned before, the problem for the individual is to maximise his lifetime utility. Therefore, when he is running a ...rm he has to determine which state provides the largest utility. What are these states? It is straightforward to see that one possibility is to keep his current ...rm running. A second possibility is the wage worker state. This would imply to close the current ...rm and go to paid job. Furthermore, a third possibility is the option of running a di¤erent ...rm. In other words, the possibility of closing the current ...rm and starting a new one. Why is this last

<sup>&</sup>lt;sup>12</sup> For research on the topic see, for instance, Evans and Jovanovic (1989), Blanch‡ower and Oswald (1998), Taylor (2001).

here, we can de...ne when the individual is risk averse  $(R^j>0)$ , risk neutral  $(R^j=0)$ , or a risk lover  $(R^j<0)$ . Thus, in this paper we are assuming that the individual is risk neutral. A more extended discussion on the reasons why it is more sensible to include the entrepreneur's degree of risk aversion on the decision between employment and self-employment, and not as a parameter a ecting the pro...ts of the small ...rm, is contained in a subsequent section.

possibility relevant? In line with monopolistic competition markets, the situation we are looking at is, for example, one where the entrepreneur was running a Chinese take away and is deciding to move to Mexican food, or to open a sport clothes retail outlet. In this sense, by new ...rm we refer to one where the good or service to be oxered by such ...rm is dixerent from the one oxered by the previous ...rm. Therefore, once the entrepreneur is running a ...rm, to maximise his utility he must decide whether keeping his current ...rm is the best choice, or if closing and starting a new ...rm provides the largest utility, or whether he is better ox by closing and going to a paid job.

Let e represent the period in the individual's life span when he started a …rm. At the end of every period e, e+1, ..., T the individual evaluates which state provides the largest utility. Let  $s \ 2 \ f1, 2, ..., T_i \ eg$  represent the number of periods the individual has been running a …rm. Thus, the utility from keeping the current …rm running is calculated by

$$\max_{p_t} \sum_{t=s}^{\mathbf{X}^1} \delta^{t_i s} \mid_{t}^{ij} \text{ s.t. } \alpha_B^{ij} \text{ and } \theta_B^j . \quad \mid \overset{\mathbf{i}}{=} \alpha_B^{ij}, \theta_B^j \overset{\mathbf{t}}{=} \frac{\mathbf{1}_{i} \delta^{T_i s} \overset{\mathbf{t}}{=} 0}{\mathbf{1}_{i} \delta} . \tag{12}$$

This is the same expression as in (6), in which the entrepreneur uses the bayesian method to calculate his expectations about the parameters  $\alpha^{ij}$  and  $\theta^j$ .

Given the nature of the parameters  $\alpha^{ij}$  and  $\theta^j$ , the procedure to calculate the pro...ts the entrepreneur would obtain for starting a new ...rm is dimerent from the one shown by the previous expression. Recall that  $\theta^j$  represents the skills of the entrepreneur to manage the ...rm e¢ciently. These skills are time invariant, that is, talented entrepreneurs are always talented, whereas unskillful entrepreneur are not able to enhance such skills<sup>14</sup>. Therefore, once the entrepreneur has started a ...rm for the ...rst time and has learned his "true" value of e¢ciency, he is constrained to this value in the future. This means every time he starts a new ...rm, his e¢ciency parameter remains the same. However, this is not true for the case of the demand parameter, for we allow dimerent products to face dimerent levels of demand. In other words, every time the entrepreneurs runs a new ...rm, he receives a dimerent value of  $\alpha$ . In the context of the above example, it is easy to think that the new Mexican food outlet or the new sport clothes retail outlet the entrepreneur is planning to set up might not

 $<sup>^{14}</sup>$ This assumption may seem very restrictive at ...rst glance, since it eliminates any possibility for the improvement of skills to manage as a result of learning. However, in our model this is not the case because we assume the parameter  $\theta^j$  embodies the endowment of potential skills, which can be regarded as time invariant. In this sense, entrepreneurs with low e¢ciency may improve the way they manage their ...rms over time, but they have a very limited space to improve these skills because by de...nition they have low potential.

attract enough demand, regardless of the fact that the Chinese take away was a successor not. In terms of our model, this implies the expected pro...ts of a new ...rm are calculated as follows:

$$E \max_{\alpha} \max_{p_t} \delta^{t_i s} |_{t}^{j} \text{ s.t. } \theta_B^{j} |_{0}^{t} \alpha, \theta_B^{j} dA (\mathfrak{c}) \frac{\mathbf{i}_{1_i} \delta^{T_i s}}{\mathbf{1}_i \delta}.$$
 (13)

Note the dixerence between expression (9) and (13). Expression (9) represents the expected pro...ts for a de novo entrepreneur, that is, for an entrepreneur which does not have any experience in running a ...rm. This means that a de novo entrepreneur ignores his endowment of both parameters  $\alpha$  and  $\theta$ , and as a consequence he would calculate expected pro...ts by applying expectation over both parameters. In contrast, in our model an incumbent entrepreneur, i.e. one which has experience in running a ...rm, has already discovered his e $\Phi$ ciency parameter. Therefore, if he is to start a new ...rm the unique uncertainty is the demand parameter. Hence, the fact that the expected pro...ts of a new ...rm as shown by (13) are calculated by applying expectation only over the demand parameter. To save on notation we de...ne

$$E_{\alpha}^{\mathbf{f}_{|\alpha|}} \mathbf{i}_{\alpha,\theta_{B}^{j}} \mathbf{f}^{\alpha} \cdot \mathbf{Z}_{1} + \alpha,\theta_{B}^{j} \mathbf{f}_{\alpha,\theta_{B}^{j}} dA (\mathbf{f}) .$$

Finally, the third alternative for the entrepreneur is to close his current ...rm and go to employment. Given that expression (11) was the decision rule to enter the market, we set

to indicate the reservation level of pro...ts. Additionally, we assume that once the entrepreneur is running his ...rm, the value of the alternative of returning to wage work starts to depreciate. This can be regarded as the increase in satisfaction the individual receives for being his own boss. This is indicated by  $\gamma^s \downarrow_R^j$ , where  $0 < \gamma < 1$  is the rate of depreciation and s is the number of periods the individual has been running a ...rm as de...ned before. The purpose of this is to adhere to the stylised result that the probability of dropping from self-employment decreases the more time the individual spends as self-employed (Evans and Leighton, 1989; Blanch‡ower and Meyer, 1994). The utility from the employment state are thus expressed as

$$\begin{array}{c}
\mathbf{X}^{1} \\
 & \gamma^{t} \delta^{t_{\mathbf{i}} s} \mid_{R}^{j} = \gamma^{s} \mid_{R}^{j} \frac{\mathbf{1}_{\mathbf{i}} (\gamma \delta)^{T_{\mathbf{i}} s}}{\mathbf{1}_{\mathbf{i}} \gamma \delta}
\end{array}.$$

In this sense the problem for the entrepreneur is written as

$$\underset{\text{arg max}}{\text{n}} \mid_{\alpha_{B}^{ij}, \theta_{B}^{j}}, \underset{\alpha}{E} \mid_{\alpha} \mid_{\alpha, \theta_{B}^{j}} \uparrow_{\alpha}, \mid_{R} \mid_{\alpha} \mid_{\alpha} (\gamma, \delta, T, s) \qquad (15)$$

where  $d\left(\gamma,\delta,T,s\right)=\frac{\gamma^s(\mathbf{1}_i\ \delta)(\mathbf{1}_i\ (\gamma\delta)^{T_i\ s})}{(\mathbf{1}_i\ \gamma\delta)\left(\mathbf{1}_i\ \delta^{T_i\ s}\right)}$ , and the ...rst argument stands for the pro...ts of the current ...rm, the second argument for the pro...ts of a new ...rm, and the third one for the value of going to wage work. Before proceeding with the predictions o¤ered by expression (15) we will look ...rst at the predictions obtained from an alternative model, which will provide a benchmark for our general model, and will provide a case in support of the de...nition we have given to the parameter  $\theta^j$ .

#### 4.1 The Alternative Model

In Subsection 2.1 we mention that there is a lack of consistency in the de...nition of entrepreneur used by academics across the research literature. To surmount this problem we also state that the de...nition of entrepreneur to be used throughout this paper refers to those individuals who started or own and manage his own business. In agreement with this de...nition we specify that the e $\Phi$ ciency parameter  $\theta^j$  denotes the ability of the entrepreneur, which we restrict to skills to manage and deal ecciently with the everyday activities of the ...rm. In this context, the objective of this subsection is to build an alternative model where this assumption is relaxed, and to try to provide an answer to our initial question using such alternative model. In turn, the predictions of both the alternative model and the general one will be confronted. The justi...cation to do this is simple: if in the specilised literature on business and economics there is no agreement on the de...nition of entrepreneur, in the nonspecilised literature like newspapers and magazines and in the popular knowledge the feeling is that an entrepreneur is or should rather be an individual which possesses many qualities: good management skills, vision, discipline, innovative ideas, willingness to take risks, amongst others. Hence, the attractiveness of modifying the de...nition of our parameter  $\theta^j$ to encompass one or more of these characteristics.

To this end consider the pro...t function

$$\begin{vmatrix} j & & \\ & a \\ \end{vmatrix}^{\sharp} . \tag{16}$$

Let  $^{a\,j}$  represents some sort of "overall" entrepreneur skills for individual j. Accordingly, we assume that the pro…ts are a strictly increasing function of  $^a$ , i.e.,  $\partial_+^i/\partial_-^a>0$ . This function generalises the pro…t function that can be found in Jovanovic (1982) and Frank

(1988), and in fact, in terms of the assumptions of our general model, it would imply that the parameters  $\alpha^{ij}$  and  $\theta^j$  are perfectly correlated. To appreciate this consider a pro...t function of the form revenue function minus cost function

$$= R(\mathfrak{l}) \in C(\mathfrak{l})$$

where the technology of production is included in the latter and the demand function in the former. Recall that this is the form of the pro...t function we consider in our model as shown by expression (1), where the demand parameter  $\alpha^{ij}$  axis the revenue function directly, and the eciency parameter  $\theta^{j}$  in tuences the cost function. Jovanovic (1982) assumes the small ...rm produces in an industry with homogeneous product and perfect competition. Hence, he eliminates the need for the existence of a parameter like  $\alpha^{ij}$  and concentrates on the cost function. In his model the ecciency parameter axects the cost function and is the only ...rm-speci...c determinant. Frank (1988) assumes that the talent of the entrepreneur is the only ...rm-speci...c determinant and that it axects the technology of production as well. He does not make any assumption on the type of competition the small ...rm faces. His model is equivalent to Jovanovic's in the sense that it discards the existence of a parameter like  $\alpha^{ij}$  by implicitly assuming homogeneous product and concentrates in the technology of production. We believe our general model oxers a more realistic case by assuming monopolistic competition and hence the existence of dixerentiated products, than by simply assuming small ...rms compete in markets with homogeneous products. Under our general model, if we assume the pro...ts of the small ...rm depend on a single parameter which embodies the overall entrepreneurial skills of the owner, then it must be the case that such skills axect both the revenue function and the cost function. Hence, our argument that under such scenario, it is as though the parameters  $\alpha^{ij}$  and  $\theta^j$  were perfectly correlated.

Note that the parameter <sup>a j</sup> therefore represents more than one characteristic of entrepreneurial skills, because under the form of a pro...t function like (16), the implications is that the entrepreneur has talent to generate revenue for the small ...rm, as he does to manage the ...rm e¢ciently. In other words, it implies that if the entrepreneur is a skilful manager, then he also has the ability to identify or develop products which are very appealing to customers, in other words, he also has skills to innovate or to spot pro...table opportunities. Under this assumptions, a skilful entrepreneur running a small restaurant would be as successful as he would in running a small video shop, because having a high value on the parameter <sup>a j</sup> implies that he is a skilful managers and skilful in distinguishing pro...table opportunities.

Following a similar procedure as in Subsection 3.1, assume <sup>a</sup> is an i.i.d. stochastic variable which follows a speci...c cumulative distribution function, and let

$$E\left[\begin{smallmatrix} & \mathbf{x} & \mathbf{a} \\ & & \end{bmatrix} \right] = \begin{smallmatrix} & & j \\ & & B \end{smallmatrix}$$
 (17)

represent the entry decision, where  $\frac{1}{R} = W^j$  i  $\xi^j$ . If inequality (17) is satis...ed, the entrepreneur has an incentive to turn down paid job and start a ...rm. Once the entrepreneur is running a ...rm, the entrepreneur evaluates which state provides the largest utility. Thus, he has the option of keeping his current ...rm, or closing down and going to wage work, which is represented by the following expression

$$\max_{p_t}\max_{t=s}^{\infty} \delta^{t_{\parallel}s} \mid j \text{ (a )}_t \text{ s.t. } \text{a } j \text{ } \\ \sum_{t=s}^{\infty} \gamma^t \delta^{t_{\parallel}s} \mid j \text{ } \\ \sum_{t=s}^{s} \gamma^t \delta^{t_{\parallel}s} \mid j \text{ }$$

This expression is equivalent to

$$\arg\max \left( \prod_{a} \mathbf{i}_{a} \int_{B}^{\mathbf{c}} \mathbf{f} d \left( \gamma, \delta, T, s \right) \right) , \tag{18}$$

where  $| ^{\text{m}} i_{a} j_{B}^{\text{c}}$  are the maximum pro...ts given the bayesian estimation of  $^{a} j$ . The ...rst argument represents the value for the entrepreneur of keeping his current ...rm, and the second denotes the value of the alternative of returning to wage work for an entrepreneur who has been running a ...rm for s periods.

Note that the dixerence between expression (18) and (15) is that the pro...ts of a possible new ...rm are not included in (18), because these pro...ts would be the same as the pro...ts of the current ...rm. In other words, given that the small ...rm pro...ts depend only on the "overall" skills of the entrepreneur as denoted by  $^{a}j$ , and since these skills do not change from running one ...rm to another, the entrepreneur would expect the performance in the new ...rm to be the same as the one he experiences in the current ...rm: the same success in the small restaurant as in the video shop<sup>15</sup>. This means it would not make sense for the entrepreneur to shut the current ...rm and try to start a new one because he will not do any better in the new venture.

From expression (18) whenever the ...rst argument is at least as large as the ...rst one the individual decides to keep running his ...rm, i.e., the ...rm survives. Therefore, for the ...rm

<sup>&</sup>lt;sup>15</sup>As in the case of  $\theta^j$  in our genereal model, we assume <sup>a j</sup> entails the endowment of potential skills, so entrepreneurs with low values of <sup>a</sup> will always perform poorly.

to survive, the problem for the entrepreneur reduces to obtain pro...ts satisfying the weak inequality

From here we obtain the next proposition.

Proof. Let  ${}^a{}_F$  solve  ${}^j{}_R = {}^j{}^a{}^a{}({}^a{}_F)$ . Since  $\partial{}^j{}(\mathfrak{k})/\partial{}^a{}>0$ , any  ${}^a{}^j{}>{}^a{}_F$  would satisfy (17) Let  ${}^a{}_{min}$  solve expression (19),  ${}^j{}^a{}({}^a{}_{min})={}^j{}^a{}^a{}(d(\gamma,\delta,T,s))$ . Thus, we rewrite this expression as  ${}^j{}^a{}({}^a{}_{min})={}^j{}^a{}({}^a{}_F){}^a{}(d(\gamma,\delta,T,s))$ . Since the term in square brackets is smaller than one for  $\gamma<1$ , this implies  ${}^a{}_{min}<{}^a{}_F$ . If for the subgroup H expression (19) is not satis...ed and since  $\partial{}^j{}({}^a{}(\ell)/\partial{}^a{}>0$ , then it must be the case that 8j 2 H,  ${}^a{}^j{}_B<{}^a{}_{min}<{}^a{}_F$ . Given that the value  ${}^a{}^j{}$  does not vary overtime, the second argument of expression (18), which represent the reward in the wage work state, will always be the largest for subgroup H.

Proposition 1 states that when the only ...rm-speci...c determinant of the pro...ts of the small ...rm are the overall entrepreneurial skills of the owner-manager, those entrepreneurs whose ...rms do not survive have skills lower than they expected and lower than the ones required to run a ...rm, therefore, it is optimal for them not to try to start another ...rm in the future. In other words, this framework unambiguously implies that for every failed ...rm there is a failed entrepreneur. As a consequence, not only the ...rm will not survive, but also the entrepreneur will not attempt to start another ...rm again.

Figure 3 presents graphically the arguments contained in Proposition 1. Recall that  $\downarrow_R^j$  represents the value of the wage worker state, and we refer to  $\downarrow_R^j \ell d$  ( $\gamma, \delta, T, s$ ) as the updated reservation level, that is, once the individual has started a ...rm<sup>16</sup>. An individual would start a ...rm provided he believes he will receive pro...ts larger than the reservation level. In Figure

<sup>&</sup>lt;sup>16</sup> In Figure 3 we are further assuming  $\frac{1}{B}$  (0) = 0 and  $\frac{\partial^2 \frac{1}{B}}{\partial \theta^2}$  < 0. None of these assumptions are central to the results in Proposition 1.

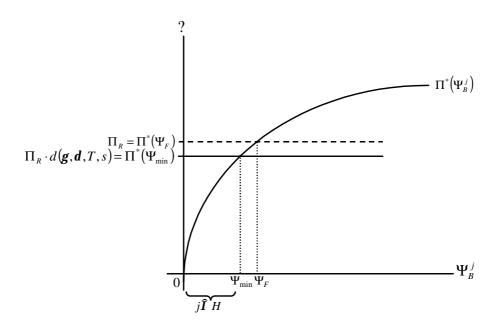


Figure 3: When the pro...ts of the small ...rm depend only on the overall entrepreneurial skills of the owner-manager.

3 this is depicted as anticipating pro...ts over or above the horizontal dotted line, which involves that the entrepreneur expects to have skills no smaller than  ${}^a{}_F$ . Once the ...rm is running, the entrepreneur will keep the ...rm and refuse to become a wage worker whenever the expected pro...ts are larger than the updated reservation level, i.e., whenever the expected pro...ts are above the horizontal solid line. This suggest the entrepreneur must have skills larger than or equal to  ${}^a{}_{min}$ , where we interpret this last parameter as the minimum skills to run a ...rm. The ...rst fact to note is that  ${}^a{}_{min} < {}^a{}_F$ . In other words, the entrepreneur can a¤ord to have skills smaller than the ones which would draw him into the market, and still opt for running a ...rm. This result is a direct consequence of including the depreciation rate  $\gamma$ . Focusing on Figure 3, it is easy to see that a ...rm that did not survive means the owner-manager estimated the expected pro...ts to be lower than the rewards in the wage worker state. In turn, this unequivocally means the entrepreneur has skills to run a ...rm below  ${}^a{}_{min}$ . Given that the entrepreneur is con...ned to this level of skills, he will ...nd optimal not to start another ...rm in the future.

More speci...cally, when the pro...ts of the small ...rm depend only on the overall entrepreneurial skills of the owner, Proposition 1 indicates two points. Firstly, if the small ...rm does not survive, it means the entrepreneur has skills lower than he required. In other words,

he is not good in running ...rms. Secondly, under this scenario, this failed entrepreneur would ...nd it optimal not to own another ...rm in the future, because having low entrepreneurial skills means he will receive higher rewards from the wage worker state. As it stands, this alternative model does not seem to provide an intuitive answer to our initial question as to why some small ...rm owners wish to start a new ...rm after having closed one that was not successful. According to Proposition 1 such entrepreneurs should not exist, because the fact that the small ...rm did not survive is simply the result that the entrepreneur does not have the necessary skills to run a successful ...rm, and therefore it is not rational for him to own another ...rm in the future since the wage work state provides higher rewards. However, the empirical evidence provided in Section 2 shows that a rather high share of entrepreneurs who close a ...rm wish to own another one in the future, despite the lack of success in their previous venture. We conclude that a model wherein the pro...ts of the small ...rm depend only on the overall entrepreneurial skills of the small ...rm owner, which implicitly assumes the owner has the same level of skills to select an attractive product which generates high revenue for the small ...rm as he does to manage the ...rm ecciently, does not help us to answer our initial question and to explain the empirical evidence. In the following subsection we present and evaluate the predictions of our general model, which provide a better explanation. Finally, note that another implication of the alternative model is that the terms "survival of the ...rm" and "survival of the entrepreneur" are equivalent, event though they have dizerent meanings. We can roughly de...ne "survival of the ...rm" as the term which refers to the situation when the small ...rm continues trading, and "survival of the entrepreneur" as the one which denotes when the entrepreneur keeps running ...rms instead of going to wage work. According to the alternative model, failure by the entrepreneur to keep a small ...rm trading -the non survival of the small ...rm- indicates that he does not have the necessary entrepreneurial skills and therefore he is better ox in a paid job -the non survival of the entrepreneur-.

#### 4.2 The General Model

When the pro...ts of the small ...rm depend on the demand parameter  $\alpha^{ij}$  and the e $\mathbb{C}$ ciency parameters  $\theta^j$  as shown by (1), where the former denotes how successful the ...rm's product is in attracting customers and the latter represents the skills of the owner to manage the ...rm e $\mathbb{C}$ ciently, and under assumptions A.1 trough A.5, the problem for the entrepreneur is

$$\underset{\text{arg max}}{\text{n}} \stackrel{\mathbf{i}}{\underset{\alpha}{ij}} \alpha_{B}^{ij}, \theta_{B}^{j}, E_{\alpha}^{\mathbf{f}} \stackrel{\mathbf{i}}{\underset{\alpha}{i}} \alpha, \theta_{B}^{j} \stackrel{\mathbf{f}}{\underset{\beta}{i}}, \stackrel{j}{\underset{R}{i}} d(\gamma, \delta, T, s) \qquad (20)$$

which is a repetition of expression (15), where the ...rst argument stands for the pro...ts of the current ...rm, the second one for the expected pro...ts of a new ...rm, and the third one for the

value of going to wage work. The important feature to keep in mind is that the e $\Phi$ ciency parameter is the same in the ...rst and second arguments, whilst the parameter for demand changes. Depending on the value of the parameters  $\alpha^{ij}$  and  $\theta^j$ , the entrepreneur will decide whether keeping the current ...rm, opening a new one, or going to wage work, provides the highest rewards.

The entrepreneur's current ...rm will survive whenever the ...rst argument is the largest. Therefore, su¢cient conditions for the current ...rm to survive are

$$| \overset{\mathbf{i}}{\alpha} \overset{ij}{\alpha_B}, \theta_B^j > E \overset{\mathbf{f}}{\alpha} | \overset{\mathbf{i}}{\alpha}, \theta_B^j \overset{\mathbf{f}^{\mathbf{x}}}{\alpha}$$
 (21)

and

$$E_{\alpha}^{\mathbf{f}} \mid {}^{\mathbf{n}} \mathbf{i}_{\alpha}, \theta_{B}^{j} {}^{\mathbf{f}\mathbf{n}} > \mid {}^{j}_{R} {}^{\mathbf{f}} d (\gamma, \delta, T, s) .$$
 (22)

Our interest is to provide an explanation as to why some entrepreneurs wish to start a new ...rm after having closed a previous one that was not successful. In terms of our model, it is as though the second term in (20) had the largest value. In other words, the situation is similar to one where inequality (21) is not satis...ed, i.e., when the current ...rm does not survive, whilst inequality (22) is satis...ed, or in other words, whilst the entrepreneur wishes to start another ...rm. This paves the way to our next proposition.

Proposition 2 Let the pro...t function be the one shown by (1). The maximisation problem is the one in (20). De...ne  $\theta_{\min}$  as the minimum level of entrepreneurial skills which satis...es the su $\Phi$ cient conditions for the current ...rm to survive (21) and (22). Let  $D \ 1/2 \ J$  be the subgroup for which the second term in (20) is the largest. Therefore,  $8j \ 2 \ D$ ,  $\theta_B^j > \theta_{\min}$ . As consequence, the wage worker state will always provide the smallest rewards to subgroup D.

Proof. Let  $\overline{\alpha}$  solve expression (21) as an equality. Lemma 3 in Appendix A establish the conditions under which  $\overline{\alpha}$  exist. Utilising Lemma 2 and assuming p>MC, expression (21) is satis...ed whenever  $\alpha_B^{ij}>\overline{\alpha}$ , where i 2 I, j 2 J, and  $I\setminus J=$ ?. From expression (11) let  $\theta_F$  solve  $|{}^j_R=E[|{}^{\sharp}(\alpha,\theta_F)]$ , and from expression (22) let  $\theta_{\min}$  solve  $E[|{}^{\sharp}(\alpha,\theta_{\min})]=|{}^j_R d(\gamma,\delta,T,s)$ . Lemma 4 in Appendix A establish under which conditions  $\theta_F$  and  $\theta_{\min}$  exist. Thus,  $E[|{}^{\sharp}(\alpha,\theta_{\min})]=E[|{}^{\sharp}(\alpha,\theta_F)]d(\gamma,\delta,T,s)$ . Making use of Lemma 1, any  $\theta_B^j>\theta_{\min}$  satis...es (22). If for subgroup D expression (21) is not satis...ed, but expression (22) is, we must therefore have  $\alpha_B^{ij}<\overline{\alpha}$  and  $\theta_B^j>\theta_{\min}$ ,  $\theta_B^j$ 

a new draw for the demand parameter. De...ne the new draw as  $\alpha_B^{lj}$ , where  $i \in l \ 2 \ I$ ,  $j \ 2 \ D$ . It can be the case that  $\alpha_B^{lj} \ \mathbf{R} \ \overline{\alpha}$ . Under any of these situations, either the ...rst argument or the second one in (20) are the largest. This implies the third argument in expression (20), which represents the wage working state, has always the smallest value for subgroup D.

Proposition 2 says that when the pro...ts of the small ...rm depend on the e¢ciency and demand parameters, those entrepreneurs whose ...rms do not survive, but wish to start a new one, have skills to manage the ...rm at least as large as the ones required to run a potentially successful ...rm. This implies that every time their ...rms fail to survive, the optimal action for them is to start another one, rather than becoming a wage worker. Note that this is the opposite result to the one obtained from Proposition 1, namely, that under the alternative model failure by the entrepreneur to keep his ...rm a‡oat implies he does not have the necessary skills, whereas under our general model, the fact that the entrepreneur wishes to own another ...rm is a re‡ection that he is skilful, the only thing his ...rm lacked was a more appealing product. Additionally, Proposition 2 establishes that such a skilful entrepreneur will always ...nd that the prospects of starting another ...rm render a higher value to him than the alternative of going to wage work does.

Regarding our initial question as to why some entrepreneurs wish to own another ...rm after having closed an unsuccessful one, the answer by Proposition 2 is: because these entrepreneurs have enough skills to run potentially successful ...rms, assuming such skills are restricted to managerial skills; the other condition to run a successful ...rm is to ...nd a product or service which is appealing to customers or for which there is a market niche. Two important questions to ask are: how plausible these assumptions are and hence, how reliable the prediction oxered by our general model by means of Proposition 2 is. We provide the following arguments to tackle such questions. Firstly, such assumptions are consistent with the view suggested by Audretsch (1995), who asserts that entrepreneurs are always in the process of discovering whether they possess the "the right stu" in terms of the product they oxer for which succient demand exists and whether they can produce it more e¢ciently than their rivals. More speci...cally he states that 'when a new ...rm is launched, its prospects are shrouded in uncertainty. If the new ...rm is built around a new idea, it is uncertain whether there is succient demand or if some competitor will have the same or even superior idea. Even if the new ...rm is a clone, there is the question whether there is enough demand' (p. 67) He further asserts that 'an additional layer of uncertainty is how competent the new ...rm really is' (p. 67), which in terms of our model this last statement can be easily translated as referring to how skilful the owner-manager is. Storey (1990)

acknowledges a possibility which is also in line with our assumptions. He declares that 'the creation and subsequent closure of a ...rm may merely be part of the small entrepreneurs way of searching out pro...table opportunities...' (p. 47). Secondly, we believe the predictions of our model will gain strength if they account for all the possibilities as provided by the empirical evidence in Figure 2. That is, whilst Proposition 2 oxers an explanation as to why the "determined entrepreneurs" in Figure 2 have the desire to own another ...rm in the future, such explanation does not involve the other three cases. The following proposition present the complete results of our general model, which we believe suggests an explanation for all the empirical evidence contained in Figure 2.

Proposition 3 Let the pro...t function be the one shown by (1). The maximisation problem is the one in (20). De...ne  $\theta_{\min}$  as the minimum level of entrepreneurial skills which satis...es the su $\Phi$ cient conditions for the current ...rm to survive (21) and (22), and de...ne the group R as the one which contain the diæerent combinations of  $\alpha^{ij}$  and  $\theta^j$  such that  $\{(\alpha^r, \theta^r) = \{(\alpha, \theta, \theta), (T, s)\}, (\alpha^r, \theta^r)\}$  2.R

- (i) Let M ½ J be the subgroup for which the ...rst term in (20) is the largest. Therefore  $\alpha_B^{ij} > \overline{\alpha}$  8j 2 M,  $\theta_B^j > \theta_{\min}$  8j 2  $M_1$ ,  $\theta_{\min} > \theta_B^j > \theta^r$  8j 2  $M_2$ , i 2 I, r 2 R, where  $M_1$  [  $M_2 = M$  and  $M_1 \setminus M_2 =$  ?.
- (ii) Let  $D \not\!\!\! 2 J$  be the subgroup for which the second term in (20) is the largest. Therefore  $\alpha_B^{ij} < \overline{\alpha}$ ,  $\theta_B^j > \theta_{\min}$ , 8j 2 D, i 2 I.
- (iii) Let Z ½ J be the subgroup for which the third term in (20) is the largest. Therefore  $\alpha_B^{ij}<\overline{\alpha}$  and  $\theta_B^j<\theta_{\min}$  8j 2  $Z_1$ ,  $\alpha_B^{ij}>\overline{\alpha}$  and  $\theta_B^j<\theta_{\min}$  8j 2  $Z_2$ , i 2 I, r 2 R where  $Z_1$  [  $Z_2=Z$ , and  $Z_1\setminus Z_2=$ ?.
- (iv) For subgroups  $M_1$  and  $M_2$  the sale of their ...rms or any shock which makes  $\alpha_B^{ij} < \overline{\alpha}$ ,  $j \ 2 \ M$ ,  $i \ 2 \ I$ , assuming  $\alpha_B^{ij}$  is exposed to unforeseen shocks, has the exect of making the second argument in (20) the largest for subgroup  $M_1$ , and the third argument in (20) the largest for subgroup  $M_2$ .

#### Proof. See Appendix A. ■

Proposition 3 is represented graphically in Figure 4. It shows under which conditions, in terms of combinations of the parameters  $\alpha$  and  $\theta$ , it is optimal for the entrepreneur to keep his current ...rm, start a new ...rm, or go to wage work. More speci...cally, Figure 4 is an isopro...t map in the space  $(\alpha, \theta)$ , where every point in its surface entails speci...c coordinates which form part of an isopro...t curve. In turn, every isopro...t curve is associated with a single

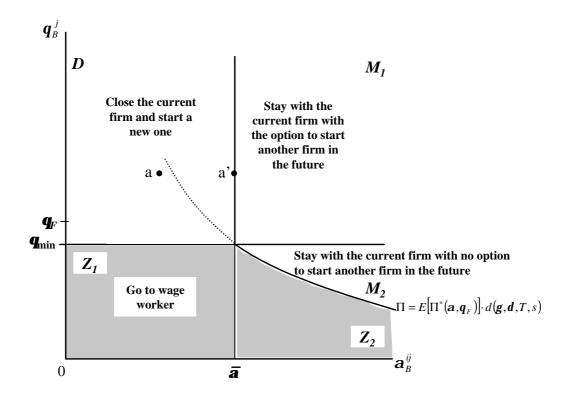


Figure 4: Optimal decision for the entrepreneur when the pro...ts of the small ...rm depend on the e¢ciency and demand parameters

value of pro...ts for di¤erent combinations of  $\alpha$  and  $\theta$ . Lemma 5 in Appendix A establishes that such isopro...ts curves have negative slope and are convex with respect to the origin. The farther to the north-east the isopro...t is placed, the higher the associated value of pro...ts.

Figure 4 is divided in ...ve areas. Areas  $M_1$  and  $M_2$  contain the combinations of parameters  $\alpha_B^{ij}$  and  $\theta_B^j$  such that the best option for the entrepreneur is to keep his current ...rm, because it is providing pro...ts larger than the updated reservation level  $E \ [ \ \ \ \ \ \ ] (\alpha, \theta_F) ] (d(\gamma, \delta, T, s))$ , which is represented by the isopro...t curve that divides areas  $M_2$  and  $M_2$  and once it crosses the coordinates  $(\overline{\alpha}, \theta_{\min})$  continues upward as a dotted line. Recall that such updated reservation level represents the rewards in the wage working state. Therefore, any point to the right of its associated isopro...t curve represents pro...ts that exceed such rewards. This explains why entrepreneurs placed in areas  $M_1$  and  $M_2$  are better ox keeping his current ...rm, whilst those in areas  $M_1$  and  $M_2$  are better ox keeping his current ...rm, but instead of becoming wage workers, they are better ox by starting a new ...rm. Note that area  $M_1$  comprises

some combinations of  $\alpha_B^{ij}$  and  $\theta_B^j$  which are placed to the right of the isopro...t curve of the updated reservation level, and some combinations located to the left of it. However, according to Proposition 3 the best course of action for entrepreneurs in area D is not to keep the current ...rm or close down and go to wage work, but to shut their current ...rm and start a new one. The reason is because by starting a new ...rm these entrepreneurs have the option of oxering a dixerent product in the hope of drawing a higher  $\alpha$ : closing the Chinese take away and opening a sport clothes retail outlet. Take for example an entrepreneur who ...nds himself in a situation where his coordinates of parameters are represented by point a in Figure 4. His current ...rm's pro...ts are smaller than the reservation level. However, by starting a new ...rm his expectations are to reach a point like a' which is placed in an isopro...t to the right of the reservation level. As a result, this entrepreneur does not ...nd optimal to go to wage work, but to keep in entrepreneurialism by starting a new ...rm. The key point is that Proposition 3 states that all entrepreneurs in area D have skills above the cutox point  $\theta_{\min}$ , contrary to those in area  $Z_1$  who do not. In this sense, what entrepreneurs in areas Dand  $M_1$  have in common is that all of them have skills above the cutox point  $\theta_{min}$ . Notice from Figure 4 that we can say that entrepreneurs in area  $M_1$  are the ones who are running successful ...rms because their ...rms' demand is above average. Therefore, it is fair to say the only thing an entrepreneur in area D lacked was to oxer a more appealing product, but his skills to manage the ...rm ecciently are as good as the ones of those entrepreneurs who run successful ...rm. This is the case previously pointed out by Proposition 2.

Proposition 3 also establishes that the dixerence between entrepreneurs in areas  $M_1$  and  $M_2$  is that, in case their current ...rms do not survive or in case they sell them, the former have the option of keeping in entrepreneurialism by starting a new ...rm, whereas the latter do not and have to go to wage work. The intuition is as follows. Suppose an entrepreneur in area  $M_1$  sells his ...rm. He has the option of starting a new ...rm or going to wage work. If he plans to start a new ...rm, his expectation about his new ...rm's demand is  $\overline{\alpha}$ . Given that he has skills above  $\theta_{\min}$ , his expectation with a new ...rm in term of Figure 4 is to reach a point over the vertical line which starts from the coordinates  $(\overline{\alpha}, \theta_{\min})$  and goes upward. As can be seen, any point in this line above the point  $(\overline{\alpha}, \theta_{\min})$  renders pro...ts higher than the updated reservation level. Therefore, it is optimal for an entrepreneur in  $M_1$  to start a new ...rm. This is not the case for an entrepreneur in area  $M_2$ , since this entrepreneur has skills lower than  $\theta_{\min}$ . In other words, by starting a new ...rm he expects to be placed in area Z, which means he would receive pro...ts lower than the reservation level. Therefore, entrepreneurs in area  $M_2$  ...nd optimal to go to wage work after having sold their ...rms. This intuition is equivalent to the one where there is a shock in demand and the ...rm does not

survive. For instance, the shock can represent a downturn in demand because another ...rm entered the market and is o $\alpha$ ering a product similar enough to impinge in the demand of the original ...rm. If the shock is big enough, the small ...rm's demand may fall below  $\alpha$ . Thus, it is as if entrepreneurs in area  $M_1$  were "moved" to area D, where according to Proposition 3, these entrepreneurs are better o $\alpha$  by closing their current ...rms and starting a new one. On the other hand, entrepreneurs in area  $M_2$  would be placed in area Z after the shock, where they are better o $\alpha$  by going to wage work.

Notice that Proposition 3 predicts that only entrepreneurs with skills above  $\theta_{\min}$  have the option of starting new ...rms, that is, only those in areas  $M_1$  and D. This is regardless of whether they were previously running ...rms with high demand or low demand. In this sense, Proposition 3 suggests the existence of a mechanism of entrepreneurial self-selection whereby skilful entrepreneurs self-select themselves by starting new ...rms after having closed one, regardless of the degree of success on the previous ...rm, whereas unskilful entrepreneurs go to paid employment. We are now in position to discuss whether or not this mechanism of entrepreneurial self-selection explains the empirical evidence in Section 2 and thereby, whether or not there is support for our general model. Before proceeding, note that unlike the alternative model our general model does dixerentiate between survival of the small ...rm and survival of the entrepreneur. According to Figure 4, survival of the small ...rm takes place under the conditions described by areas  $M_1$  and  $M_2$ , whereas survival of the entrepreneur occurs under the conditions described by areas D and D0.

### 5 Explaining the Evidence

Why do some entrepreneurs wish to start new ...rms after having closed one that was not successful? This is the question which the present paper tries to tackle. We showed the relevance of such question by means of the empirical evidence in Figure 2 in page 9. By doing so, we not only revealed there is potentially a large share of entrepreneurs who have closed a ...rm that was not successful and still want to own another ...rm in the future, but that there also exist, amongst other cases, some entrepreneurs that despite having successful ...rms do not have the desire to run their own ...rms again. In order to o¤er an explanation to our initial question and to the empirical evidence in general, we proposed and developed a model whose principal assumption is that the pro...ts of the small ...rm depend on two ...rmspeci...c parameters: the ...rst one captures the success of the ...rm's product in attracting demand, and the second the skills of the owner to manage the ...rm e¢ciently, that is, to deal

e¢ciently with the day-to-day activities. We assume such parameters are not correlated, i.e., we assume the entrepreneur's skills to manage are not correlated with the ability to select and o¤er an appealing product. On the contrary, we suppose the demand parameter varies every time the entrepreneur starts a new ...rm. From our model we obtained Propositions 2 and 3. To compare such results with the ones from an alternative model wherein the entrepreneur has some type of overall skills which includes skills to manage and skills to innovate or spot pro...table opportunities, we also obtained Proposition 1.

As regards our initial question, Proposition 2 and 3 establish that those entrepreneurs who start or have the desire to start a new ...rm after having closed an unsuccessful one have skills to manage as great as those who are running successful ...rms. Our model goes further by suggesting the existence of a mechanism of entrepreneurial self-selection. Under such mechanism, entrepreneurs who are skilful are the only ones who start or have the desire to start another ...rm in the future after having closed a previous one. Such desire is independent of whether or not the previous experience of running a ...rm is regarded as a success or failure. This is not true of unskilful entrepreneurs, who prefer to go to employment. Does this mechanism oxer an explanation to the empirical evidence provided in Figure 2? We believe it does. By means of Figure 4 our theory argues that the reason why the "determined entrepreneurs" and the "serial entrepreneurs" in Figure 2 have the intention to own another ...rm in the future is because they are skilful entrepreneurs. They would be placed in areas D and  $M_1$  in Figure 2, respectively. Our theory interprets skilful entrepreneurs as those who have managerial skills at least as large as those needed to run potentially successful small ...rms, i.e., ...rms which would provide larger economic and noneconomic rewards than the wage worker state would. In fact our model states that the "determined entrepreneurs" are as skilful as the "serial entrepreneurs". The latter were just "luckier" with their ...rms in the sense that they were running a ...rm with a very appealing product or service. Similarly, the mechanism of entrepreneurial self-selection also accounts for the cases of "failed entrepreneurs" and "discouraged entrepreneurs" shown by Figure 4. The former would be placed in area Z in Figure 4 and the latter in area  $M_2$ . According to our general model, the fact that a "discouraged entrepreneur" wishes to leave entrepreneurialism despite having owned a ...rm that was successful, can be explained by saying that he was "lucky" in running a ...rm with a very attractive product or service, whose success indeed compensated for his low skill to manage the ...rm. However, this unskilful entrepreneur does not expect to "hit the jackpot" again, so he prefers to go to a paid job after having closed his current ...rm<sup>17</sup>.

<sup>&</sup>lt;sup>17</sup>We believe the closest interpretation to the demand parameter  $\alpha^{ij}$  in our model is luck. This is because

To oxer such explanations our model relies on the assumption that the skills of the small ...rm owners are restricted to skills to manage the ...rm ecciently, and that such skills are not related with the ability to oxer an attractive and appealing product. Let us assume the entrepreneur has both abilities. Thus, an entrepreneur who deals ecciently with the day-today activities of the small ...rm is also good at innovating or spotting pro...table opportunities. This is the case of the model discussed in Subsection 4.1, from which Proposition 1 was obtained. Such proposition establishes that those entrepreneurs whose ...rms do not survive have skills lower than required, and that it is optimal for them to not attempt to own another ...rm in the future. This means that for those entrepreneurs who run successful ...rms, they are better ox starting new ...rms. In other words, under such model only the "serial entrepreneurs" and the "failed entrepreneurs" in Figure 2 exist. As can be seen, the alternative model fails to explain the whole spectrum of empirical evidence, whereas our general model does not. Therefore, we can state that in general, the empirical evidence supports our assumption that the skills of the small ...rm owners are restricted to skills to manage the ...rm ecciently. The present discussion should be placed in its correct context. Firstly, we do not suggest that it is impossible for some entrepreneurs to have both high skills to manage and high skills to innovate or spot pro...table opportunities. Secondly, regardless of the de...nition of entrepreneurship, our conclusion supports the view that when undertaking research on entrepreneurship if we consider data comprising small ...rm owners without any other discriminatory criterion, it is reasonable to suppose that the ability to manage and the ability to innovate or spot pro...table opportunities are in general not correlated amongst small ...rm owners.

Therefore, given that the assumptions of our general model seem plausible, the mechanism of entrepreneurial self-selection gains strength. After all, the central argument of such mechanism is analogous to the idea of survival of the ...ttest: only the skilful entrepreneurs survive, whilst the unskilful do not. However, by skills and entrepreneurial survival such mechanism refers, in the case of the former, to skills to manage de...ned in this paper as skills to undertake e¢ciently the responsibilities of the everyday activities of the small ...rm, and in the case of the latter, to the entrepreneur's desire to own another ...rm, which should not be mistaken for the survival of the small ...rm.

we specify it as a random variable which the entrepreneur is unable to predict every time he starts a new ...rm, even if he has experience in running previous businesses.

## 6 Extensions and Discussion

# 6.1 Robustness and Alternative Assumptions

In this subsection we discuss the robustness of some of the assumptions in our model, and we address some alternatives hypotheses which might also explain the empirical evidence shown in Section 2.

#### Transferability of Skills

In our model we de...ne the parameter  $\theta^j$  as the one which embodies the entrepreneur's skills to manage his own ...rm ecciently. As we developed our model and de...ned the maximisation problem the entrepreneur faces once he is running a ...rm, which is shown by expression (??), one underlying assumption is that the entrepreneur can perfectly transfer his skills from his old ...rm to the new one. In our model a new ...rm is de...ned as one where the product or service is dimerent from the one omered by the previous ...rm. Given that in our model we do not restrict the nature of product or services oxered by small ...rms, one can argue the assumption of perfect transferability of skills seems not plausible when we contemplate the hypothetical example of an entrepreneur who was running a small restaurant and is planning to close and start a small manufacturing ...rm to produce computer microchips. Although we agree that such assumption is rather strong whenever we look at the possibility of an entrepreneur moving across small ...rms with very dixerent activities, we point out two arguments which we think lessen the severity of such assumption. Firstly, we believe our de...nition of skills to manage included in Section 3 is general enough to make the assumption of transferability of skills across dizerent ...rm activities more palatable. We de...ned such skills as the '...ability to organise and assume the responsibility of the activities of the small ...rm, to select the cheapest inputs given a desire level of quality, to deal with suppliers and, perhaps, employees, to ensure that the production of goods or services in the ...rm is done in the best possible way using the resources available, amongst others. In general, they represent the skills to undertake ecciently the everyday activities of the ...rm and to tackle the problems that might arise'. In this sense, it is not hard to think of a restaurateur or bed and breakfast owner opening a retail shop or vice versa. Secondly, we believe situations similar to the example mentioned above are rather unlikely. Figure 1 in page 8 provides some hints to support our argument. Amongst those who closed a ...rm but continued as business owners, Figure 1 shows that 34% started a similar business in a dixerent location, compared to 28% who started or bought a dixerent business<sup>18</sup>. As can be seen the ...rst group

<sup>&</sup>lt;sup>18</sup>In Figure 1, ignoring those who continued business in a di¤erent legal form, the results were obtained

would have no problems in transferring his skills to manage as the activities of the old and new ...rms are similar, whilst the fact that the new ...rm is placed in a di¤erent location ...ts into the de...nition of di¤erentiated product. Ideally, information on the old and new ...rm's activities for the group of entrepreneurs who starter or bought a di¤erent business in Figure 1 would provide us with stronger evidence to accept or refute our second argument. We lack such information. However, the fact that the empirical evidence shows that a larger share of entrepreneurs are owning new ...rms with activities similar to the old ones', compared to those who are running ...rms with di¤erent activities, suggests that cases where entrepreneurs move across small ...rms with very di¤erent activities might be minimal. After all, it makes sense for the entrepreneur to own ...rms where he can make use of the skills he has acquired in previous experiences.

#### Low Risk Aversion and Exort

In this part we ask ourselves to what extent the entrepreneur's attitudes towards risk and towards exort, in place of our original assumptions or additional to them, can explain the empirical evidence contained in Section 2 and, hence, answer our initial question. Consider the degree of risk aversion of entrepreneurs. Most of the classic economists who re‡ected on entrepreneurship converged on the notion that a speci...c characteristic of entrepreneurs is that they shoulder the risks of the economic activities they undertake. On overviewing historical contributions to entrepreneurship research, van Praag (1999, pp. 327-328) declares that '[Richard] Cantillon's entrepreneur bears the risks as a consequence of selling (buying) at a certain price and buying (selling) at an uncertain price. [Jean-Baptiste] Say's entrepreneur bears the risk of losing capital and reputation due to experimenting and the chance of failure. The Marshallian entrepreneur is responsible for undertaking the business risk associated with the activities of his ...rm. ...[Frank] Knight...de...nes the entrepreneur as the decision maker whenever uncertainty is involved, where the square brackets are mine. In modern economic research this idea has been translated as the entrepreneur's decision between receiving a risk-free wage from employment, or engaging in self-employment, which includes owning and running a ...rm, with the inherent risks involved. In turn, the entrepreneurs' low risk aversion is a force which drives them to join self-employment<sup>19</sup>. Moreover, taking advantage of recent development on databases, some authors have been able to prove empirically that entrepreneurs indeed experience a lower degree of risk aversion<sup>20</sup>.

from the calculations 0.18/(0.62-0.09) and 0.15/(0.62-0.09), respectively.

<sup>&</sup>lt;sup>19</sup> For instance, see Kihlstrom and La¤ont (1979).

<sup>&</sup>lt;sup>20</sup>Uusitalo (2001), van Praag and Cramer (2001).

What the above deliberation suggests is that, in terms of our model, the entrepreneur's degree of risk aversion has to do more with the decision to start a ...rm in the ...rst place, and less with the desire of starting a new ...rm after having closed one, which is our main concern. Therefore, it is sensible to say that it is unlikely that a model to investigate the survival of small ...rms and entrepreneurs based solely on the entrepreneur's degree of risk aversion, would explain the empirical evidence in Section 2.

With respect to the entrepreneur's attitude towards exort, popular knowledge and anecdotal evidence would assert that entrepreneurs, de...ned as owners and managers of their ...rms, exert more exort whilst working at their ...rms than an employee working for somebody else would. Moreover, it is often regarded that to run successful ...rms, the entrepreneur, compared to a common employee, must be willing to sacri...ce more leisure in favour of hours of work<sup>21</sup>. This suggests that the entrepreneur's attitude towards exort is an important element to be considered in any research theorising on the behaviour of small ...rms and entrepreneurs. Surprisingly, very limited studies in research in Economics have incorporated such element<sup>22</sup>. van Praag (1999) compares the determinants of successful entrepreneurship as discussed by some classic economists. None of them seem to refer to the entrepreneur's exort as an important element to success, at least not directly<sup>23</sup>. The standard consumption-leisure model which captures the notion that individuals value leisure, i.e., that they dislike work exort, and which has had a signi...cant impact in particular areas of Economics<sup>24</sup>, has been almost ignored when it comes to models of small ...rms or entrepreneurship. This is

<sup>&</sup>lt;sup>21</sup>The empirical evidence contained in Blanch‡ower (2004) supports these beliefs. Using a survey which contains information for more than 35 countries he shows that self-employed work longer hours than employees. Similarly, using di¤erent surveys and through econometric estimation he arrives to the conclusion that self-employed place more weight on work than they do on leisure, which can be interpreted as self-employed experiencing less disutility of e¤ort.

<sup>&</sup>lt;sup>22</sup>This is not the case in our sister disciplines Sociology, Psychology and Business Studies. Douglas and Shepherd (2002) and Gatewood et al (2002) are cases in context for Business Studies. The latter also surveys some relevant articles to our topic in the discipline of Sociology and Psychology.

<sup>&</sup>lt;sup>23</sup>Amongst other determinants of successful entrepreneurship, Jean Baptiste Say refers to "perseverance", Schumpeter to "willingness", Knight to "willingness and motivation" (van Praag, 1999, p. 329). It can be argued that in these and some other characteristics speci...ed by these economists, it is implied, to various degrees, that the entrepreneur requires to apply considerably exort in his tasks to be successful.

<sup>&</sup>lt;sup>24</sup>Since in the consumption-leisure model work e¤ort is a bad, it asserts that individuals are willing to "endure" work e¤ort in exchange for a wage which would enable them to consume other goods, hence generating labour supply. This model is the basis of an entire branch of Economics: Labour Economics. It also spurred the research on the Principal-Agent problem, which in the beginning looked into the relationship employer-employee and how ine⊄ciencies arise given the incentive by the employee to shirk in the job due to his disutility of e¤ort (some early relevant articles are Alchian and Demsetz, 1972; Jensen and Meckling, 1976). In Macroeconomics, this idea of incentive to shirk also gave way to theories of unemployment, through the development of the e⊄ciency-wage models (see Romer, 1996).

particularly relevant because, as discussed above, one would expect entrepreneurs to be more willing to forego leisure, thereby in uencing the decision to join self-employment and, perhaps, the success in entrepreneurship. Three notably exceptions are Frank (1988), De Fraja (1996), and Douglas and Shepherd (2000). Although published in a business journal, Douglas and Shepherd (2000) use an economic model in essence. Amongst other results, they show that employees who generate less disutility of exort have a greater incentive to join self-employment, other things being equal (e.g. ability, attitude towards risk and independence). De Fraja (1996) speci...es a model where the entrepreneur has the choice of carrying out a project by himself, or selling it to an outside investor and work as manager, where he explicitly acknowledges that the entrepreneur experiences disutility of expression of expressions. The product or service generated by the project can have either high or low demand, which is unknown before undertaking the project. De Fraja's model reveals that under conditions of high (low) demand, the entrepreneur exerts less (more) exort, in other words, that the entrepreneur has a more "laid back" attitude during good times. He declares this is ineccient because '...e Cciency requires higher exorts in good times, when higher returns can be reaped' (De Fraja, 1996, p. 90). However, he shows that this result is exactly the opposite when the entrepreneur sells his project and acts as manager. Frank (1988) also takes into account the aversion to exort by the individual. His model focuses in the entrepreneur's decision to continue running a ...rm or exit self-employment. In his model he shows more explicitly that the optimal decision by the entrepreneur is one which is essentially based on the criterion marginal bene...t of entrepreneurship must be equal to marginal cost of entrepreneurship. In his model, the former is equal to the entrepreneur's ability, and the former to the disutility of exort<sup>25</sup>. Consequently, Frank reaches the conclusion that more able entrepreneurs exert more exort, whereas less able entrepreneurs act more lazily.

The models by Frank (1988) and De Fraja (1996), although with rather strong restrictions<sup>26</sup>, suggest that in our model, if the entrepreneur's exort and his attitude towards it are considered, the structure of our model itself make it unclear what to expect in terms of the intensity of the entrepreneur's exort. In other words, De Fraja's model ignores the role of the entrepreneur's ability - in our model this is the e¢ciency parameter  $\theta^j$ -, but he does considers the project's demand -the demand parameter  $\alpha^{ij}$  in our model-. In turn, he ...nds that high values of  $\alpha^{ij}$  mean low exort from the entrepreneurs. On the other hand,

<sup>&</sup>lt;sup>25</sup>In the model by De Fraja (1996), once the entrepreneur has decided to run the project by himself, the maximisation problem basically entails the same criterion.

<sup>&</sup>lt;sup>26</sup>One of De Fraja's assumptions is that the entrepreneur is the only one capable of carrying out the project, constraining any potential outside buyer of the project to hire him as manager. Regarding Frank's model, we have already mentioned that he implicitly assumes the entrepreneur enters a market of homogeneous goods.

Frank ignores the demand parameter  $\alpha^{ij}$  and ...nds that more skilful entrepreneurs, i.e., those with higher values of  $\theta^j$ , work harder. Assuming such results hold when both parameters are considered, like in our model, the ...nal results are ambiguous or counter-intuitive. For instance, considering the four areas in Figure 4 in page 30, those entrepreneurs in area  $M_1$ who have high skills and run ...rms with high demand would have, on one hand, the incentive to exert greater exort, but on the other, the incentive to not. The ...nal result is ambiguous. This is not the case with entrepreneur in area D, who are also skilful but owning ...rms with low demand. If the results of the models of Frank (1988) and De Fraja (1996) hold, it means these entrepreneurs apply greater exort, even greater than those in area  $M_1$ . If these results were to be used to explain the empirical evidence in Figure 2 in page 9, the implications would be that the determined entrepreneurs work harder than the serial entrepreneurs do, and yet the ...rms of the former are not successful. The intuition in this sense is hard to swallow. In any case, to disentangle the role of the entrepreneur's attitude towards exort in the survival of the small ...rm and the entrepreneur, and to conclude whether or not such new element changes our results and helps to explain the evidence in Section 2, a more formal model has to be developed. We believe this is material for a dixerent paper.

Finally, notice that in the heart of Frank's and De Fraja's models and in ours, lies the assumption that the entrepreneur's exort does not alter the demand or the ecciency parameter. They are ...xed parameters determined by nature, whose values intuence the optimal decision by the entrepreneur to stay with his ...rm or as entrepreneur, and how hard to work. This makes a call for the development of models where the causality is assumed to be the other way around, e.g., models where the entrepreneur's exorts may improve his ...rm's demand. We conclude by recognising the importance of considering the value entrepreneurs allocate to exort whenever research in small ...rm or entrepreneurship is undertaken. We also recognise that including such element in our model may render more insights into the determinants of the survival of the small ...rm and the entrepreneur. We believe this task is relevant enough to be considered in an alternative paper.

# 7 Conclusions and Final Remarks

This paper oxers and addition to the theories aimed at disentangling the forces and processes which determine the survival of the small ...rm and the entrepreneur. The principal objective of this paper is to provide an answer to the question: why do some small ...rm owners wish to start a new ...rm after having closed one that was not successful? By attempting to do

so, the paper also tries to explain some empirical evidence on small ...rm and entrepreneurial survival. The paper speci...es and develops a model, based on speci...c assumptions, which provides an explanation to the empirical evidence and, hence, proposes an answer to our initial question. The paper also discusses alternative assumptions to the ones used in our model. It is found that such assumptions do not help to explain the empirical evidence. Our ...ndings and the implications which derive from them can be summarised as follows.

Firstly, to answer our initial question our model proposes the following explanation. The reason why some small ...rm owners wish to start a new ...rm after having closed an unsuccessful one is because they the have the skills to run potentially successful ...rms, that is, ...rms which would provide larger economic and non-economic rewards to the entrepreneur than those from being an employee. In fact, our theory states that such behaviour is part of a mechanism of entrepreneurial self-selection. Under such mechanism, skilful entrepreneurs, where entrepreneurs are de...ned as small ...rm owners, are the only ones who wish to own another ...rm in the future after having closed one, regardless of the degree of success in their previous venture, whereas unskilful entrepreneurs prefer to go to wage work. We showed this mechanism accounts for the empirical evidence on entrepreneurial survival provided at the outset of this paper. All in all, we believe this ...ndings are a contribution to the exorts aimed to change the view that failure to keep a small ...rm atoat implies a failed entrepreneur. In other words, through the mechanism of entrepreneurial self-selection, this paper suggests that those entrepreneurs who wish to own another ...rm, even if they have had unsuccessful experiences, should not be regarded with suspicion. On the contrary, our ...ndings argue these entrepreneurs have the talent to run successful ...rms. Clearly, one disadvantage of the present paper with relation to the mechanism of entrepreneurial self-selection is that it predicts only skilful entrepreneurs survive, without oxering any supporting evidence. That is, even though such mechanism accounts for the empirical evidence on entrepreneurial survival included in this paper, it is still necessary to undertake further research to accept or reject the prediction that those entrepreneurs who started another ...rm or have the desire to start another ...rm, after having closed one, have indeed higher skills than those who prefer to go to wage work. We believe this is a task for a separate paper. In the same way, we believe that any possible policy implications should be addressed once such research has been carried out and its results obtained. In this sense, the ...ndings of this paper are a ...rst step in a research agenda aimed at the study of the survival of the entrepreneur.

To reach the above result, our model relies on the assumption that the skills of the small ...rm owner are restricted to skills to manage, de...ned as skills to undertake ecciently the

everyday tasks of the small ...rm. Speci...cally, we assume that such skills do not include the ability to develop and o¤er a successful product or for which there is a market niche, that is, that they do not include skills to innovate or to spot pro...table opportunities. We assumed that the success of the small ...rm's product depends more on luck. This assumption is put to the test by specifying that entrepreneurs has some type of overall skills which incorporates skills to manage and skills to innovate or to spot pro...table opportunities. We found that by making use of such alternative assumption we fail to explain the empirical evidence. This leads us to our second important result: regardless of the de...nition of entrepreneurship, our ...ndings support the view that when undertaking research on entrepreneurship if we consider data comprising small ...rm owners without any other discriminatory criterion, it is reasonable to suppose that the skills of such business owners are limited to skills to manage, and that they do not comprise skills to innovate or to spot pro...table opportunities.

Thirdly, the paper emphasises the need to di¤erentiate between survival of the small ...rm and survival of the entrepreneur. Small ...rms are run by entrepreneurs. We say a small ...rm has not survived when it has stopped trading, though such an event does not necessarily mean the entrepreneur has not survived. The survival of the entrepreneur is the outcome of the decision between going to wage work or owning another ...rm, after having closed the previous one.

Finally, one may argue that the present paper does not oxer any suggestion on how the survival of small ...rms could be improved. However, it does hint that perhaps we have been looking at the wrong problem in the sense that the survival of the entrepreneur might be of more signi...cance. After all, as mentioned above, entrepreneurs are the ones who start and run the small ...rms.

# **Appendix**

# Α

Lemma 3. Let  $M^{\alpha} = {\bf R}_{0}^{1} D(\alpha) dA(\alpha)$  and  $N^{\alpha} = {\bf R}_{0}^{1} D(\alpha)^{2} dA(\alpha)$ . Assume both  $M^{\alpha}$  and  $N^{\alpha}$  are positive constants. Thus, under the condition  $M^{\alpha} = (N^{\alpha})^{1/2}$  there exist a value of  $\alpha^{ij}$ , call it  $\overline{\alpha}$ , which solves  $|{\bf r}^{i} \overline{\alpha}, \theta^{j}_{B}| = E^{i} |{\bf r}^{i} \alpha, \theta^{j}_{B}|$ .

Proof. From Lemma 1  $\mid {}^{\mathtt{x}}(\alpha,\theta) = \frac{(bc_{1}\theta D(\alpha))^{2}}{4b(\theta)^{2}}$ , which we re-write as

$$| ^{\pi} (\alpha, \theta) = \frac{bc^2}{4(\theta)^2} | \frac{cD(\alpha)}{2\theta} + \frac{D(\alpha)^2}{4b} .$$

Thus,

$$E_{\alpha}^{\mathbf{f}} \mid {}^{\mathbf{n}} \mathbf{i}_{\alpha}, \theta_{B}^{j} = \frac{bc^{2}}{4(\theta_{B}^{j})^{2}} \mathbf{i} \quad \frac{c}{2\theta_{B}^{j}} \quad D(\alpha) dA(\alpha) + \frac{1}{4b} \int_{0}^{\mathbf{T}} D(\alpha)^{2} dA(\alpha) ,$$

SO

$$E_{\alpha}^{\mathbf{f}} \mid {}^{\mathbf{n}} \mathbf{i}_{\alpha}, \theta_{B}^{j} {}^{\mathbf{f}\mathbf{n}} = \frac{bc^{2}}{4(\theta_{B}^{j})^{2}} \mid \frac{c}{2\theta_{B}^{j}} M^{\alpha} + \frac{1}{4b} N^{\alpha}.$$

If  $\overline{\alpha}$  solves  $| \overset{\mathbf{i}}{\alpha}, \theta_B^j = E \underbrace{\overset{\mathbf{f}}{\alpha}}_{\alpha} | \overset{\mathbf{i}}{\alpha}, \theta_B^j$ , then it solves the equation

$$\frac{bc^2}{4(\theta_B^j)^2} i \frac{cD(\overline{\alpha})}{2\theta_B^j} + \frac{D(\overline{\alpha})^2}{4b} = \frac{bc^2}{4(\theta_B^j)^2} i \frac{c}{2\theta_B^j} M^{\alpha} + \frac{1}{4b} N^{\alpha},$$

or

$$\frac{1}{4b} {}^{\mathbf{i}} D (\overline{\alpha})^{2} {}_{\mathbf{i}} N^{\alpha} {}^{\mathbf{c}} {}_{\mathbf{i}} \frac{c}{2\theta_{B}^{j}} (D (\overline{\alpha}) {}_{\mathbf{i}} M^{\alpha}) = 0.$$

Hence we require  $D(\overline{\alpha}) = (N^{\alpha})^{1/2}$  and  $D(\overline{\alpha}) = M^{\alpha}$ . By virtue of the inverse-function theorem<sup>27</sup> we get  $\overline{\alpha} = D^{\text{i-1}}((N^{\alpha})^{1/2})$  and  $\overline{\alpha} = D^{\text{i-1}}(M^{\alpha})$ . Since  $D(\overline{\alpha})$  is an increasing function we must therefore have  $M^{\alpha} = (N^{\alpha})^{1/2}$ .  $\mathbf{Y}$ 

Lemma 4. Let  $M^{\alpha}= {\bf R}_{\bf 0} \ D\left(\alpha\right) dA\left(\alpha\right)$  and  $N^{\alpha}= {\bf R}_{\bf 0} \ D\left(\alpha\right)^2 dA\left(\alpha\right)$ . Assume both  $M^{\alpha}$  and  $N^{\alpha}$  are positive constants.. Suppose that  $N^{\alpha}$  i  $4\mid_{R}^{j}>0$  and  $(M^{\alpha})^2>N^{\alpha}$  i  $4\mid_{R}^{j}$ . Thus,

<sup>&</sup>lt;sup>27</sup>De la Fuente (2000, p. 181).

under these conditions there exist values of  $\theta^j$ , which we name as  $\theta_F$  and  $\theta_{\min}$ , which solve  $E\left[ \left| \begin{array}{c} \mathbf{x} \\ \alpha \end{array} \right| \left( \alpha, \theta_F \right) \right] = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_{\min} \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_F \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_{\min} \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_F \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_F \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_F \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_F \right) = \left| \begin{array}{c} \mathbf{j} \\ R \end{array} \right| \left( \alpha, \theta_F \right) 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Proof. From Lemma 3 we know that

$$E\left[ \left| {^{\mathbf{n}}} (\alpha, \theta_F) \right] = \frac{bc^2}{4(\theta_F)^2} \left| {\mathbf{i}} \frac{c}{2\theta_F} M^{\alpha} + \frac{1}{4b} N^{\alpha} \right|.$$

If  $\theta_F$  solves  $E\left[ \mid \overset{\mathbf{r}}{\alpha} (\alpha, \theta_F) \right] = \mid \overset{j}{R}$ , then it solves the equation

$$\frac{bc^2}{4(\theta_E)^2} i \frac{c}{2\theta_E} M^\alpha + \frac{1}{4b} N^\alpha i \mid_R^j = 0 .$$

The positive root which we obtain from here is

$$\theta_F = \frac{1}{N^{\alpha} \mathbf{i} \mathbf{4} \stackrel{j}{\downarrow}_{R}^{B}} bcM^{\alpha} + bc^{\mathbf{i}} (M^{\alpha})^{2} \mathbf{i} N^{\alpha} + 4b \stackrel{j}{\downarrow}_{R}^{\mathbf{t}_{1/2}} ,$$

where  $\theta_F$  will be a positive constant as long as  $N^{\alpha}_{i}$  4 $^{i}_{R}$  > 0 and  $(M^{\alpha})^{2}$  >  $N^{\alpha}_{i}$  4 $^{i}_{R}$ . Similarly,  $\theta_{\min}$  solves the equation

$$\frac{bc^2}{4(\theta_{\min})^2} i \frac{c}{2\theta_{\min}} M^{\alpha} + \frac{1}{4b} N^{\alpha} i \mid_{R}^{j} d(\gamma, \delta, T, s) = 0.$$

The positive root which solves this equation is

$$\theta_{\min} = \frac{1}{N^{\alpha} \mathbf{i} 4b \begin{bmatrix} j \\ R \end{bmatrix} d(\gamma, \delta, T, s)} bcM^{\alpha} + bc \mathbf{i} (M^{\alpha})^{2} \mathbf{i} N^{\alpha} + 4b \begin{bmatrix} j \\ R \end{bmatrix} d(\gamma, \delta, T, s)^{\mathbf{c}_{1/2}}.$$

It can be shown that  $d(\gamma, \delta, T, s) \cdot 1$  for  $\gamma \cdot 1$  and  $s \cdot T$ . Thus the conditions mentioned above are su $\varphi$ cient for  $\theta_{\min}$  to be a positive constant.  $\mathbf{Y}$ 

Proof of Proposition 3. Su¢cient and necessary conditions which make the ...rst term in (20) to be the largest are

$$| {}^{\mathbf{i}}\alpha_{B}^{ij}, \theta_{B}^{j} > E \underset{\alpha}{\overset{\mathbf{f}}{=}} | {}^{\mathbf{i}}\alpha, \theta_{B}^{j}$$
 (23)

and

$$| |^{\mathbf{a}} \alpha_B^{ij}, \theta_B^{j} |^{\mathbf{c}} > |_{R}^{j} |^{\mathbf{c}} d (\gamma, \delta, T, s) .$$
 (24)

Whenever the following inequality is true

$$E \mid {}^{\mathbf{f}} \mid {}^{\mathbf{n}} \mathbf{i} \alpha, \theta_B^j \downarrow {}^{\mathbf{f}\mathbf{n}} > \mid {}^{j}_R \mathfrak{k} d (\gamma, \delta, T, s)$$
 (25)

such conditions are satis...ed. However we can have

$$E_{\alpha}^{\mathbf{f}} \mid {}^{\mathbf{n}} \mathbf{i}_{\alpha}, \theta_{B}^{j} \stackrel{\mathbf{f}^{\mathbf{n}}}{=} < \mid {}^{j}_{R} \mathfrak{f} d (\gamma, \delta, T, s)$$
 (26)

and still satisfy them. From the two last expression and using Lemma 4 let  $\theta_F$  solve  $E[\mid \ (\alpha, \theta_F)] = \mid \ _R^j$  and let  $\theta_{\min}$  solve  $E[\mid \ (\alpha, \theta_{\min})] = \mid \ _R^j \ (\alpha, \delta, T, s)$ . We obtain

$$E\left[ \left| \left| \left| \left| \left( \alpha, \theta_{\mathsf{min}} \right) \right| \right. \right] = E\left[ \left| \left| \left| \left| \left| \left( \alpha, \theta_F \right) \right| \right| \right| \right] \left( \left| \left( \gamma, \delta, T, s \right) \right| \right). \tag{27}$$

If for subgroup M the ...rst term in (20) is the largest, then from (23) and Lemma 1 and Lemma 3 we must have  $\alpha_B^{ij} > \overline{\alpha}$  8j 2 M. From (27) and Lemma 2, any  $\theta_B^j > \theta_{\min}$  satis...es (25) and consequently (24). We de...ne  $M_1$  such that  $\theta_B^j > \theta_{\min}$ , 8j 2  $M_1$ . Note that the left hand side of equation (27) contains the rewards in the wage worker state, i.e., it is the updated reservation level. Therefore, there must be an isopro...t curve representing this updated reservation level. As de...ned, let R represent the subgroup which contain the dimerent combinations of  $\alpha^{ij}$  and  $\theta^j$ , respectively, which account for such isopro...t curve. That is they satisfy

$$\mid (\alpha^r, \theta^r) = E[\mid \alpha(\alpha, \theta_F)] d(\gamma, \delta, T, s), 8(\alpha^r, \theta^r) 2R.$$
 (28)

Thus, for some  $(\alpha^r, \theta^r)$  2 R, say  $(\alpha_i, \theta_i)$  we have

$$\mid (\alpha_i, \theta_i) = E[\mid \pi(\alpha, \theta_F)] d(\gamma, \delta, T, s)$$
,

then from (27) we have that

$$\mid (\alpha_i, \theta_i) = E[\mid \alpha(\alpha, \theta_{min})]$$

SO

$$\frac{bc^2}{4(\theta_{\rm i})^2} \; \mathrm{i} \; \; \frac{cD\left(\alpha_{\rm i}\right)}{2\theta_{\rm i}} + \frac{D\left(\alpha_{\rm i}\right)^2}{4b} = \frac{bc^2}{4(\theta_{\rm min})^2} \; \mathrm{i} \; \; \frac{c}{2\theta_{\rm min}} M^\alpha + \frac{1}{4b} N^\alpha \; ,$$

or

$$\frac{bc^2}{4} \frac{\mu}{(\theta_i)^2} \mathbf{i} \quad \frac{1}{(\theta_{\min})^2} \mathbf{i} \quad \frac{c}{2} \frac{\mu}{\theta_i} \frac{D(\alpha_i)}{\theta_i} \mathbf{i} \quad \frac{M^{\alpha}}{\theta_{\min}} \mathbf{1} + \frac{1}{4b} \mathbf{i} D(\alpha_i)^2 \mathbf{i} \quad N^{\alpha} = 0 ,$$

which will be satis...ed if  $\theta_i = \theta_{\min}$ , and  $D(\alpha_i) = M^{\alpha}$  and  $D(\alpha_i)^2 = N^{\alpha}$ . Using Lemma 3 we know the last two equalities hold for  $\alpha_i = \overline{\alpha}$ . This means that the isopro...t curve represented by (28) crosses through the point  $(\overline{\alpha}, \theta_{\min})$ . Lemma 3 below establishes that this isopro...t curve has negative slope and is convex to the origin. By means of (23), we

have the restriction  $\alpha_B^{ij} > \overline{\alpha}$  and given that the isopro...t curve (28) has negative slope, is convex to the origin, and crosses through  $(\overline{\alpha}, \theta_{\min})$ , (26) and (24) are satis...ed if and only if  $\theta_{\min} > \theta_B^j > \theta^r$ . We de...ne  $M_2$  such that  $\theta_{\min} > \theta_B^j > \theta^r$ , 8j 2  $M_2$ . Note that  $M_1 \setminus M_2 = ?$  and  $M_1$  [  $M_2 = M$ . This accounts for (i).

For subgroup Z the third argument is the largest. Thus, the following are su $\Phi$ cient and necessary conditions for such situation to take place

$$+ {}^{\sharp} {}^{i} \alpha_{B}^{ij}, \theta_{B}^{j} {}^{\xi} < + {}^{j}_{B} {}^{\xi} d (\gamma, \delta, T, s)$$
 (29)

and

$$E = \lim_{\alpha \to \infty} (\alpha, \theta_B^j)^{\text{tx}} < \lim_{\alpha \to \infty} (\alpha, \delta, T, s)$$
(30)

where we can either have

$$| \overset{\mathbf{i}}{\alpha} \overset{ij}{\alpha} \overset{j}{\beta} + \overset{\mathbf{f}}{\beta} | \overset{\mathbf{f}}{\alpha} \overset{\mathbf{f}}{\beta} | \overset{\mathbf{f}}{\alpha} \overset{\mathbf{f}}{\beta}$$
 (31)

or

$$| {}^{\mathbf{n}} {}^{\mathbf{i}} \alpha_B^{ij}, \theta_B^{j} {}^{\mathbf{t}} < E {}^{\mathbf{f}} | {}^{\mathbf{n}} {}^{\mathbf{i}} \alpha, \theta_B^{j} {}^{\mathbf{t}\mathbf{n}}.$$
 (32)

Using Lemma 2 and equation (27), condition (30) is satis...ed whenever  $\theta_B^j < \theta_{\min}$ . Additionally, If (32) is met, then condition (29) is also satis...ed. This is accomplished by means of Lemma 1 and Lemma 3 whenever  $\alpha_B^{ij} < \overline{\alpha}$ . We de...ne  $Z_1$  such that  $8j \ 2 \ Z_1$ ,  $\alpha_B^{ij} < \overline{\alpha}$  and  $\theta_B^j < \theta_{\min}$ . If (31) is met, then condition (30) is satis...ed, provided (29) is also satis...ed. Thus, (31) is true whenever  $\alpha_B^{ij} > \overline{\alpha}$ . Given this restriction and since the left-hand-side term of (29) represent a level of pro...ts equivalent to the isopro...t curve depicted by (28), which in turn is characterised by Lemma 5, condition (29) is satis...ed if and only if  $\theta_B^j < \theta^r < \theta_{\min}$ . We de...ne  $Z_2$  such that  $8j \ 2 \ Z_2$ ,  $\alpha_B^{ij} > \overline{\alpha}$  and  $\theta_B^j < \theta^r < \theta_{\min}$ . Note that  $Z_1 \setminus Z_2 = \overline{Z}$ , and  $Z_1 \ Z_2 = \overline{Z}$ . This accounts for (iii).

An entrepreneur in subgroup M will be willing to sell his current ...rm if and only if the oxered price is higher than the sum of expected discounted pro...ts. That is, if the price is

larger that the ...rst term in expression (20). Thus, the problem for entrepreneurs in subgroup M becomes

$$\underset{\alpha}{\operatorname{arg \, max}} \stackrel{\mathbf{f}}{\underset{\alpha}{E}} \stackrel{\mathbf{f}}{\underset{\alpha}{\vdash}} \stackrel{\mathbf{f}}{\underset{\alpha}{\vdash}} \stackrel{\mathbf{f}}{\underset{\alpha}{\vdash}} \stackrel{\mathbf{f}}{\underset{\beta}{\vdash}} \stackrel{\mathbf{f}}{\underset{\alpha}{\vdash}} \stackrel{$$

where the ...rst argument are the expected pro...ts from starting a new ...rm, and the second the value of going to wage work. The entrepreneur will start another ...rm if  $E \mid_{\alpha}^{\mathbf{r}} \mid_{\alpha}^{\mathbf{r}} \mid_{\alpha}^{\beta} \mid_{\beta}^{\beta} \mid_{\beta$ 

Lemma 5. The isopro...ts curves of the (maximum expected) pro...ts function in the space  $(\alpha, \theta)$  have negative slope and are convex to the origin.

**Proof.** For simplicity all superscripts and subscripts are dropped. The slope of the isopro...ts is determined by

$$\frac{\partial \theta}{\partial \alpha} = i \frac{\partial \left( (\alpha, \theta) / \partial \alpha \right)}{\partial \left( (\alpha, \theta) / \partial \theta \right)}.$$

From the proof of Lemma 1 and Lemma 2 we obtain,

$$\frac{\partial \theta}{\partial \alpha} = i \frac{\theta^2}{bc} \, \frac{\partial D(\alpha)}{\partial \alpha} .$$

From assumption A.3 we have that  $\frac{\partial D(\alpha)}{\partial \alpha} > 0$ , therefore  $\frac{\partial \theta}{\partial \alpha} < 0$ . The convexity of the curves is established by

$$\frac{\partial^2 \theta}{\partial \alpha^2} = i \frac{\theta^2}{bc} \, \frac{\partial^2 D(\alpha)}{\partial \alpha^2} .$$

From assumption A.3 we have that  $\frac{\partial^2 D(\alpha)}{\partial \alpha^2} < 0$ . Therefore,  $\frac{\partial^2 \theta}{\partial \alpha^2} > 0$  and the isopro…ts are convex to the origin.  $\mathbf{Y}$ 

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