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# Department of Economics UNIVERSITY OF CANTERBURY <br> CHRISTCHURCH, NEW ZEALAND 



# BOUNDS ON THE EFFECT OF HETEROSCEDASTICITY ON THE CHOW TEST FOR STRUCTURAL CHANGE 

David Giles and Offer Lieberman

## Discussion Paper

No. 9101

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David Giles*<br>and<br>Offer Lieberman<br>Department of Economics, University of Canterbury

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#### Abstract

This paper considers the effect of heteroscedastic regression errors on the size of the Chow test for structural stability. We show that bounds can be placed on the true size of this test in the light of such misspecification, and on the true critical value needed to achieve any desired significance level when using the test under various degrees of heteroscedasticity. These bounds are data-independent, and some cases are tabulated. An example is given to illustrate the practical application of the critical value bounds.


[^0]
## I. Introduction

The Chow (1960) test for the constancy of the regression coefficient vector over the sample is one of the most widely used diagnostic tests in applied econometrics. In its various forms, this test amounts to one of the validity of particular exact restrictions on the regression coefficients (e.g., Fisher (1970)).

It is well known that the statistics associated with the various forms of the Chow test are F-distributed under the null hypothesis of parameter stability (and non-central $F$ under the alternative hypothesis), provided that certain conditions are satisfied. The usual assumption of normal errors can be relaxed to one of spherical symmetry (provided that the errors are homoscedastic) without affecting the null distributions of these statistics, but their distributions under the alternative (and hence their power) are sensitive to this relaxation (e.g., Ullah and Phillips (1986), Giles (1991)). The assumption of homoscedastic disturbances over the full sample cannot be relaxed without distorting both the null and alternative distributions of the test statistics even with normal errors. In the face of heteroscedasticity, we have a form of the Behrens-Fisher problem.

Several studies have considered the effect of this misspecification of the model on the Chow test. For example, Toyoda (1974) approximates the distribution of the test statistic in this case, and Schmidt and Sickles (1977) provide exact evidence. Other authors have proposed alternative tests which might be robust to heteroscedasticity or which allow for its presence in some way. For example Jayatissa (1977) suggests a finite-sample test which has been criticised by Honda (1982) and others. Watt (1979) proposes an asymptotic Wald test whose exact distribution is discussed by ohtani and Toyoda (1985), and finite-sample bounds for which are described by Ohtani and Kobayashi (1986). A further test is suggested by Weerahandi (1987).

MacKinnon (1989) derives heteroscedasticity-robust variants of the Chow test which have asymptotic validity, but whose finite-sample properties are rather mixed.

Given its ease of construction, the Chow test continues to be used widely in favour of the proposed alternatives, even in situations where the homoscedasticity assumption is unreasonable. Following Schmidt and Sickles (1977) it is quite straightforward to determine the true (as oppposed to nominal) size of the Chow test for any specific data matrix and known actual level of heteroscedasticity, by using the techniques of Imhof (1961) or Davies (1980). This is somewhat analogous to computing an exact Durbin-Watson test rather than using the tabulated bounds on the critical values, and can be undertaken with the SHAZAM package (White et al. (1990)). However, the size distortion is data-specific, and most applied researchers (who may not have easy access to software for computing the distribution of ratios of quadratic forms in normal random vectors) are unlikely to proceed in this way, even given an estimate of the degree of heteroscedasticity.

Instead, it is common for the Chow test to be applied without allowance for possible heteroscedasticity despite its well known inadequacy in this case. Accordingly, for different degrees of heteroscedasticity, it would be helpful to have bounds on the true critical values for the test (or, equivalently, bounds on its true size) which are independent of the data values in the sample. In this paper we use the results of Kiviet (1980) to construct such bounds. The problem and notation are formalised in the next section. Section III details the construction of the bounds, and Section IV reports our results. Some concluding comments appear in Section V.

## II. Model and Notation

Consider a sample of $T=T_{1}+T_{2}$ observations and the model

$$
\begin{equation*}
y_{i}=X_{i} \beta_{i}+u_{i} ; \quad i=1,2 \tag{1}
\end{equation*}
$$

where $y_{i}$ is $\left(T_{i} \times 1\right) ; X_{i}$ is $\left(T_{i} \times K\right)$, non-stochastic and of $\operatorname{rank} K\left(<T_{i}\right)$; and $\beta_{i}$ is $(K \times 1) ; i=1,2$. The same variables enter the model in each sub-sample but (typically) with different values.

The most common form of the "Chow test" for parameter stability considers $H_{0}: \beta_{1}=\beta_{2}$ vs. $H_{A}: \beta_{1} \neq \beta_{2}$. This may be expressed as a standard test of linear restrictions by writing (1) as

$$
\begin{aligned}
y & \equiv\binom{y_{1}}{y_{2}}=\left(\begin{array}{ll}
X_{1} & 0 \\
0 & X_{2}
\end{array}\right)\binom{\beta_{1}}{\beta_{2}}+\binom{u_{1}}{u_{2}} \\
& \equiv x \beta+u
\end{aligned}
$$

and the null hypothesis as $H_{0}: R \beta=r$, where $R=\left(I_{K},-I_{K}\right)$ and $r=0$. The Chow test statistic is

$$
f=\left(\frac{T-2 K}{K}\right)(R \hat{\beta}-r)^{\prime}\left[R\left(X^{\prime} X\right)^{-1} R^{\prime}\right]^{-1}(R \hat{\beta}-r) / e^{\prime} e
$$

where $\hat{\beta}=\left(X^{\prime} X\right)^{-1} X^{\prime} y$ and $e=y-X \hat{\beta}$.
If $u \sim N\left(0, \sigma^{2} I_{T}\right)$ then $f$ is $F$-distributed with $K$ and ( $T-2 K$ ) degrees of freedom if $H_{0}$ is true, and it is non-central $F$ with these degrees of freedom and non-centrality parameter $\phi=(R \beta-r)^{\prime}\left[R\left(X^{\prime} X\right)^{-1} R^{\prime}\right]^{-1}(R \beta-r) / 2 \sigma^{2}$ under $H_{A}$. It is readily verified that under $\mathrm{H}_{\underline{\mathrm{O}}}$,

$$
\begin{equation*}
f=\left(\frac{T-2 K}{K}\right) u^{\prime} A u / u^{\prime} M u \tag{2}
\end{equation*}
$$

where

$$
\begin{aligned}
& M=I_{T}-X\left(X^{\prime} X\right)^{-1} X^{\prime} \\
& A=X\left(X^{\prime} X\right)^{-1} R^{\prime}\left[R\left(X^{\prime} X\right)^{-1} R^{\prime}\right]^{-1} R\left(X^{\prime} X\right)^{-1} X^{\prime}
\end{aligned}
$$

and both $M$ and $A$ are idempotent. If $u \sim N\left(0, \sigma^{2} \Omega\right)$, for arbitrary positive definite symmetric $\Omega \neq \mathrm{I}_{\mathrm{T}}$, then the above distributional results no longer hold, though (2) is still valid.

As the Chow test is a special case of the usual test of $h$ linear restrictions on $\beta$, the results of Kiviet (1980) can be used to derive bounds on $f$ when $u \sim N\left(0, \sigma^{2} \Omega\right)$. The bounds on $f$ can be used to construct bounds on its critical value for any chosen significance level, or on the true significance level of the test constructed by rejecting $H_{0}$ if $f>F^{c}(\alpha)$, where $\mathrm{F}^{\mathrm{C}}(\alpha)$ is the $100 \alpha 7$ critical value based on the (wrongly) assumed $\mathrm{F}_{\mathrm{K}, \mathrm{T}-2 \mathrm{~K}}$ null distribution. All of these bounds depend on $T, K$ and $\Omega$, but they are independent of X .

As noted in the Introduction, the assumption that $u \sim N\left(0, \sigma^{2} I_{T}\right)$ is often unreasonable when applying the Chow test. A more realistic assumption is that $u_{i} \sim N\left(0, \sigma_{i}^{2} T_{1}\right)$, or $u \sim N\left(0, \sigma_{1}^{2} \Omega\right)$ where $\Omega=\operatorname{diag} .\left(\omega_{i}\right)$ and

$$
\omega_{i}=\left\{\begin{array}{l}
1 \quad ; \quad i=1, \ldots, T_{1} \\
\theta=\sigma_{2}^{2} / \sigma_{1}^{2} ; \quad i=T_{1}+1, \ldots, T
\end{array}\right.
$$

As $\Omega$ depends on $T_{1}$ and $T_{2}$ here, these separate values partially determine the various bounds.

## III. Calculation of the Bounds

Recalling the form of $f$ in (2) and applying the principal theorem of Kiviet (1980, p.354), it follows that under the null hypothesis $f_{L} \leq f \leq f_{u}$, where

$$
\begin{align*}
& f_{L}=\left(\frac{T-2 K}{K}\right)\left(\sum_{i=1}^{K} \lambda_{i} x_{i}^{2} / \sum_{i=2 K+1}^{T} \lambda_{i} x_{i}^{2}\right)  \tag{3}\\
& f_{u}=\left(\frac{T-2 K}{K}\right)\left(\sum_{i=1}^{K} \lambda_{T-K+i} \chi_{i}^{2} / \sum_{i=2 K+1}^{T} \lambda_{i-2 K} \chi_{i}^{2}\right) . \tag{4}
\end{align*}
$$

The $\chi_{i}^{2}$ are independent central Chi square variates, each with one degree of freedom and $\lambda_{1} \leq \lambda_{2} \leq \ldots \leq \lambda_{\mathrm{T}}$ are the eigenvalues of $\Omega$. As $\Omega$ is diagonal here, the $\lambda_{i}$ 's are its (appropriately ordered) diagonal elements.

Because (3) and (4) hold only under $H_{0}$, it follows that the true $100 \alpha \%$ upper critical value, $C(\alpha)$, of $f$ satisfies $C_{L}(\alpha) \leq C(\alpha) \leq C_{u}(\alpha)$, where

$$
\begin{align*}
& \operatorname{Pr} \cdot\left(f_{L} \geq C_{L}(\alpha)\right)=\alpha  \tag{5}\\
& \operatorname{Pr} \cdot\left(f_{u} \geq C_{u}(\alpha)\right)=\alpha \tag{6}
\end{align*}
$$

Using (3) and (4), $C_{L}(\alpha)$ and $C_{u}(\alpha)$ may be computed by noting they are values satisfying

$$
\begin{equation*}
\operatorname{Pr} \cdot\left(\sum_{i=1}^{T} w_{i} x_{i}^{2} \leq 0\right)=1-\alpha \tag{7}
\end{equation*}
$$

and

$$
\begin{equation*}
\operatorname{Pr} \cdot\left(\sum_{i=1}^{T} \dot{z}_{i} x_{i}^{2} \leq 0\right)=1-\alpha \tag{8}
\end{equation*}
$$

where

$$
\begin{aligned}
& w_{i}= \begin{cases}\lambda_{1}(T-2 K) / K & i=1, \ldots, K \\
-\lambda_{1} C_{L}(\alpha) & i=2 K+1, \ldots, T \\
0 & \text { otherwise }\end{cases} \\
& z_{i}= \begin{cases}\lambda_{T-K+1}(T-2 K) / K & i=1, \ldots, K \\
-\lambda_{1-2 K} C_{u}(\alpha) & i=2 K+1, \ldots, T \\
0 & \text { otherwise }\end{cases}
\end{aligned}
$$

The calculation of (7) and (8) is a standard problem. We use a FORTRAN version of Davies' (1980) algorithm to calculate these probabilities, searching over $C_{L}(\alpha)$ and $C_{u}(\alpha)$ to satisfy (7) and (8).

Similarly, the true size $\left(\alpha_{0}\right)$ of the test which is constructed by rejecting $H_{0}$ if $f>F^{c}(\alpha)$, satisfies $\alpha_{L} \leq \alpha_{0} \leq \alpha_{u}$, where

$$
\begin{align*}
& \alpha_{L}=\operatorname{Pr} \cdot\left(f_{L} \geq F^{c}(\alpha)\right)  \tag{9}\\
& \alpha_{u}=\operatorname{Pr} \cdot\left(f_{u} \geq F^{c}(\alpha)\right) . \tag{10}
\end{align*}
$$

Using (3) and (4),

$$
\begin{align*}
& \alpha_{L}=1-\operatorname{Pr} \cdot\left(\sum_{i=1}^{T} w_{i}^{*} x_{i}^{2} \leq 0\right)  \tag{11}\\
& \alpha_{u}=1-\operatorname{Pr} \cdot\left(\sum_{i=1}^{T} z_{i}^{*} x_{i}^{2} \leq 0\right) \tag{12}
\end{align*}
$$

where the $w_{i}^{* \prime} s$ and $z_{i}^{* \prime} s$ equal the $w_{i}$ 's and $z_{i}^{\prime}$ 's respectively, but with $F^{c}(\alpha)$ replacing both $C_{L}(\alpha)$ and $C_{u}(\alpha)$. Davies' routine facilitates the direct calculation of $\alpha_{L}$ and $\alpha_{u}$.

The usefulness of the above bounds is that they are independent of the data - they depend only ${ }^{1}$ on $\alpha, K, T_{1}, T_{2}$ and $\theta$. Finally, if the errors are homoscedastic, $\lambda_{i}=1$ for all $i$. Then recalling the additivity properties of independent Chi square variates, it follows that $f_{L}=f=f_{u}, C_{L}(\alpha)=F^{c}(\alpha)=$ $C_{u}(\alpha)$, and $\alpha_{L}=\alpha=\alpha_{u}$.

## IV. RESULTS

Given the form of $\Omega$, the bounds will obviously exhibit certain symmetries. For example, if $\mathrm{T}_{1}=\mathrm{T}_{2}$, the results for $\theta=0.1$ are identical to those for $\theta=10$, etc. Similarly, those for $T_{1}=10$ and $T_{2}=20$ when $\theta=0.1$ are identical to those for $T_{2}=10$ and $T_{1}=20$ when $\theta=10$, etc.

Table 1 illustrates the bounds on $C(\alpha)$ and $\alpha_{0}$ for $\alpha=0.05$ and the values of $T_{1}, T_{2}, K$ and $\theta$ considered in Table $I$ of Schmidt and Sickles (1977, p. 1295). Their results provide exact values of $\alpha_{0}$ for certain specific $X$ matrices. It can be verified that $\alpha_{L}$ and $\alpha_{u}$ in Table 1 bound all of their reported $\alpha_{0}$ 's (and the nominal $\alpha=0.05$ ). Also, for fixed $T_{1}, T_{2}$ and $K$, as $\theta$ departs from unity (and $H_{0}$ becomes increasingly false), the values of ( $C_{u}(\alpha)-$

TABLE 1.-BOUNDS ON TRUE CRITICAL VALUES AND SIZES OF CHOW TEST WHEN THE NOMINAL SIGNIFICANCE LEVEL IS 5\%

| $\mathrm{T}_{1}$ | $\mathrm{T}_{2}$ | k | $\theta$ | $C_{L}$ | $\mathrm{C}_{\mathbf{u}}$ | $\alpha$ | $\alpha_{u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 10 | 2 | 0.01 | 0.065 | 13.134 | 0.000 | 0.318 |
|  |  |  | 0.1 | 0.595 | 9.884 | 0.000 | 0.260 |
|  |  |  | 1 | 3.634 | 3.634 | 0.050 | 0.050 |
| 25 | 25 | 2 | 0.01 | 0.062 | 7.476 | 0.000 | 0.250 |
|  |  |  | 0.1 | 0.564 | 6.583 | 0.000 | 0.214 |
|  |  |  | 1 | 3.200 | 3.200 | 0.050 | 0.050 |
| 20 | 30 | 2 | 0.01 | 0.079 | 10.171 | 0.000 | 0.345 |
|  |  |  | 0.1 | 0.687 | 8.297 | 0.000 | 0.287 |
|  |  |  | 1 | 3.200 | 3.200 | 0.050 | 0.050 |
|  |  |  | 10 | 0.478 | 5.444 | 0.000 | 0.160 |
|  |  |  | 100 | 0.050 | 5.904 | 0.000 | 0.181 |
| 40 | 10 | 2 | 0.01 | 0.037 | 4.151 | 0.000 | 0.095 |
|  |  |  | 0.1 | 0.365 | 4.034 | 0.000 | 0.089 |
|  |  |  | 1 | 3.200 | 3.200 | 0.050 | 0.050 |
|  |  |  | 10 | 1.191 | 16.422 | 0.001 | 0.513 |
|  |  |  | 100 | 0.177 | 33.667 | 0.000 | 0.658 |

$\left.C_{L}(\alpha)\right)$ and ( $\alpha_{u}-\alpha_{L}$ ) increase, as expected. This is consistent with the results in Tables 4-6 of Kiviet (1980, pp.356-7) for the general F-test in the case of AR(1) or MA(1) errors ${ }^{2}$.

The effects on the bounds of varying $T_{1}, T_{2}$ and $K$ are best seen by considering Table 1 in conjunction with the Appendix tables. The latter provide bounds on $\mathrm{C}(0.05)$ for a range of situations likely to be encountered in the applied work. In practice, having computed the Chow test statistic, we require a critical value in order to implement the test. In the face of possible heteroscedasticity, the Appendix provides bounds on such critical values. ${ }^{3}$

For $\theta<1$, increasing $T_{1}$ (ceteris paribus) leads to decreases in $C_{L}(0.05), C_{u}(0.05)$ and their difference. The converse result emerges if $\theta>$ 1. For increasing $T_{2}$, these results are reversed in general. Exceptions ${ }^{4}$ can be seen for $C_{u}(0.05)$ for $\theta=10$ or 100 in Table A4. Changing the value of $K$, ceteris paribus, produces less clear patterns in the results. This is to be expected as $K$ determines both the numerator and denominator degrees of freedom of $f$, and so its effect on $F^{c}(0.05)$ and the bounds depends on $T_{1}$ and $T_{2}$.

The usefulness of Tables A1 - A4 is best seen with an example. Gujarati (1972) discusses ${ }^{5}$ a structural shift in the relationship between unemployment (UN) and vacancies (VAC) in Great Britain in 1966. Using the quarterly data given by Gujarati (1988, p.465) we have fitted the model $U N_{i}=\beta_{1}+\beta_{2} V A C_{i}+$ $u_{i}$ over the periods 1959(2) - 1970(2), 1959(2) - 1966(3) and 1966(4) 1970(2). The corresponding olS sums of squared residuals are 2.72600, 0.22581 and 0.35241 . As $T_{1}=30, T_{2}=15$ and $K=2$, the Chow test statistic takes the value 76.147. The corresponding $5 \%$ tabulated $F$-value (for 2 and 4 degrees of freedom) is 3.226 , so we would reject the null hypothesis of structural stability. However, dividing the sub-sample sums of squared residuals by their respective degrees of freedom, and taking their ratio, gives an estimate
of $\hat{\theta}=0.297$. This suggests that the regression errors are moderately heteroscedastic. From Table $A 1$, when $\theta=0.1, C_{L}(0.05)=0.434$ and $C_{u}(0.05)=$ 4.959. As $76.147>4.959$ we can reject the null hypothesis when $0.1<\theta<1$, given the patterns in the bounds. In this case, the outcome of the test is not affected by the heteroscedasticity.

## V. CONCLUSIONS

While it is widely recognised that the Chow test for structural stability is invalid in the face of heteroscedastic regression errors, it continues to be used widely. To compensate for this, our tabulated critical value bounds should help applied researchers. However, they also illustrate that the appropriate choice of critical value in this case can be dramatically different from the assumed one. This highlights the extent to which a conventional application of the Chow test can be distortive, regardless of the data matrix, when the errors are heteroscedastic.

These bounds apply only to that form of the test which allows for a structural shift in the full coefficient vector, and where there are positive degrees of freedom in each sub-sample. The methods we have described can also be used if these requirements are relaxed, but this would necessitate a very extensive set of tables.

The same approach is not fruitful as a means of bounding the power of the test. It is easily shown that under the alternative hypothesis, the bounds are no longer independent of the data, so they are of little value. However, Kiviet's approach can be used on a wide range of other testing problems of importance to applied econometricians, and work in progress considers some other such cases for various forms of model misspecification.

* We are grateful to Judy Giles and John Small for their helpful comments, and to Robert Davies for supplying the FORTRAN code for his algorithm.

1. As $f$ in (2) is invariant to scale, the bounds are independent of the separate values of $\sigma_{1}^{2}$ and $\sigma_{2}^{2}$.
2. A glimpse of some bounds for the critical value of the form of the Chow test considered here, when the errors are $\operatorname{AR}(1)$ can be obtained from the entries for (his) $k=4, h=2$ in Kiviet's Table 5.
3. Corresponding tables of bounds on $\alpha_{0}$ are available from the authors on request. The $\alpha_{0}$ values reported in Table II of Schmidt and Sickles (1977, p.1296) lie within the appropriate bounds in our table.
4. Similar exceptions arise for critical value upper bounds reported for the F-test with ARMA ( 1,1 ) errors in Table 7 of Kiviet (1980, p.357).
5. See, also, Gujarati (1988, pp.449-450).

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## APPENDIX

Bounds on Chow Test Critical Values When Errors Are Heteroscedastic

TABLE A1. -NOMINAL SIGNIFICANCE LEVEL $=5 \% ; \mathrm{k}=2$


| 10 | 10 | 3.634 | 0.065 | 13.134 | 0.595 | 9.884 | 0.595 | 9.884 | 0.065 | 13.134 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 15 | 10 | 3.467 | 0.051 | 7.486 | 0.487 | 6.624 | 0.726 | 11.486 | 0.084 | 16.887 |
| 20 | 10 | 3.369 | 0.045 | 5.852 | 0.436 | 5.428 | 0.841 | 12.802 | 0.104 | 20.494 |
| 25 | 10 | 3.305 | 0.042 | 5.085 | 0.407 | 4.819 | 0.943 | 13.910 | 0.123 | 23.967 |
| 30 | 10 | 3.259 | 0.040 | 4.642 | 0.388 | 4.453 | 1.034 | 14.861 | 0.141 | 27.314 |
| 35 | 10 | 3.226 | 0.039 | 4.354 | 0.375 | 4.208 | 1.117 | 15.690 | 0.159 | 30.545 |
| 40 | 10 | 3.200 | 0.037 | 4.151 | 0.365 | 4.034 | 1.191 | 16.422 | 0.177 | 33.667 |
| 15 | 15 | 3.369 | 0.063 | 9.198 | 0.578 | 7.718 | 0.577 | 7.718 | 0.063 | 9.198 |
| 20 | 15 | 3.305 | 0.053 | 6.946 | 0.505 | 6.224 | 0.660 | 8.698 | 0.075 | 10.885 |
| 25 | 15 | 3.259 | 0.048 | 5.887 | 0.462 | 5.439 | 0.737 | 9.582 | 0.087 | 12.547 |
| 30 | 15 | 3.226 | 0.045 | 5.274 | 0.434 | 4.959 | 0.808 | 10.386 | 0.098 | 14.185 |
| 35 | 15 | 3.200 | 0.043 | 4.875 | 0.414 | 4.636 | 0.875 | 11.121 | 0.110 | 15.799 |
| 40 | 15 | 3.179 | 0.041 | 4.595 | 0.399 | 4.403 | 0.937 | 11.797 | 0.121 | 17.390 |
| 20 | 20 | 3.259 | 0.061 | 8.031 | 0.569 | 6.963 | 0.569 | 6.963 | 0.061 | 8.031 |
| 25 | 20 | 3.226 | 0.055 | 6.684 | 0.514 | 6.026 | 0.630 | 7.652 | 0.071 | 9.106 |
| 30 | 20 | 3.200 | 0.050 | 5.904 | 0.478 | 5.444 | 0.687 | 8.297 | 0.079 | 10.171 |
| 35 | 20 | 3.179 | 0.047 | 5.395 | 0.452 | 5.048 | 0.742 | 8.901 | 0.087 | 11.228 |
| 40 | 20 | 3.162 | 0.045 | 5.037 | 0.433 | 4.762 | 0.790 | 9.469 | 0.095 | 12.275 |
| 25 | 25 | 3.200 | 0.061 | 7.476 | 0.564 | 6.583 | 0.564 | 6.583 | 0.061 | 7.476 |
| 30 | 25 | 3.179 | 0.056 | 6.530 | 0.520 | 5.909 | 0.612 | 7.112 | 0.068 | 8.263 |
| 35 | 25 | 3.162 | 0.052 | 5.912 | 0.488 | 5.446 | 0.657 | 7.616 | 0.075 | 9.045 |
| 40 | 25 | 3.148 | 0.049 | 5.478 | 0.465 | 5.110 | 0.701 | 8.096 | 0.081 | 9.822 |
| 30 | 30 | 3.162 | 0.061 | 7.153 | 0.561 | 6.355 | 0.561 | 6.355 | 0.061 | 7.153 |
| 35 | 30 | 3.148 | 0.056 | 6.428 | 0.524 | 5.831 | 0.600 | 6.784 | 0.067 | 7.773 |
| 40 | 30 | 3.136 | 0.053 | 5.918 | 0.496 | 5.447 | 0.638 | 7.196 | 0.072 | 8.390 |
| 35 | 35 | 3.136 | 0.061 | 6.941 | 0.558 | 6.203 | 0.558 | 6.203 | 0.061 | 6.941 |
| 40 | 35 | 3.126 | 0.057 | 6.356 | 0.527 | 5.776 | 0.592 | 6.563 | 0.065 | 7.453 |
| 40 | 40 | 3.117 | 0.061 | 6.792 | 0.557 | 6.095 | 0.557 | 6.095 | 0.061 | 6.792 |

TABLE A2.-NOMINAL SIGNIFICANCE LEVEL $=5 \% ; \mathrm{k}=3$

## $\theta$

|  | 1 | 0.01 |  | 0.1 |  | 10 |  | 100 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{T}_{1} \quad \mathrm{~T}_{2}$ |  | $\mathrm{C}_{\mathrm{L}}$ | $\mathrm{C}_{u}$ | $C_{L}$ | $\mathrm{C}_{u}$ | $c_{L}$ | $\mathrm{c}_{\mathrm{u}}$ |  | $\mathrm{C}_{u}$ |


| 10 | 10 | 3.344 | 0.052 | 20.713 | 0.484 | 12.131 | 0.484 | 12.131 | 0.052 | 20.713 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 15 | 10 | 3.127 | 0.041 | 7.973 | 0.401 | 6.736 | 0.607 | 13.591 | 0.069 | 26.795 |
| 20 | 10 | 3.009 | 0.037 | 5.668 | 0.362 | 5.167 | 0.713 | 14.705 | 0.087 | 32.367 |
| 25 | 10 | 2.934 | 0.035 | 4.738 | 0.340 | 4.450 | 0.807 | 15.596 | 0.104 | 37.506 |
| 30 | 10 | 2.883 | 0.033 | 4.239 | 0.326 | 4.044 | 0.890 | 16.334 | 0.121 | 42.273 |
| 35 | 10 | 2.845 | 0.032 | 3.929 | 0.316 | 3.784 | 0.964 | 16.958 | 0.137 | 46.718 |
| 40 | 10 | 2.816 | 0.031 | 3.718 | 0.309 | 3.603 | 1.032 | 17.496 | 0.153 | 50.879 |
| 15 | 15 | 3.009 | 0.052 | 9.962 | 0.483 | 7.853 | 0.483 | 7.853 | 0.052 | 9.962 |
| 20 | 15 | 2.934 | 0.045 | 6.810 | 0.423 | 5.954 | 0.558 | 8.823 | 0.063 | 11.909 |
| 25 | 15 | 2.883 | 0.041 | 5.535 | 0.389 | 5.049 | 0.628 | 9.677 | 0.073 | 13.815 |
| 30 | 15 | 2.845 | 0.038 | 4.849 | 0.366 | 4.524 | 0.692 | 10.437 | 0.083 | 15.681 |
| 35 | 15 | 2.816 | 0.036 | 4.423 | 0.351 | 4.184 | 0.751 | 11.119 | 0.094 | 17.511 |
| 40 | 15 | 2.794 | 0.035 | 4.132 | 0.339 | 3.945 | 0.807 | 11.735 | 0.104 | 19.304 |
| 20 | 20 | 2.883 | 0.052 | 7.940 | 0.481 | 6.676 | 0.481 | 6.676 | 0.052 | 7.940 |
| 25 | 20 | 2.845 | 0.046 | 6.325 | 0.435 | 5.611 | 0.536 | 7.340 | 0.060 | 9.058 |
| 30 | 20 | 2.816 | 0.043 | 5.456 | 0.405 | 4.982 | 0.587 | 7.954 | 0.067 | 10.164 |
| 35 | 20 | 2.794 | 0.040 | 4.915 | 0.384 | 4.568 | 0.635 | 8.524 | 0.074 | 11.257 |
| 40 | 20 | 2.776 | 0.038 | 4.546 | 0.368 | 4.277 | 0.681 | 9.055 | 0.082 | 12.339 |
| 25 | 25 | 2.816 | 0.053 | 7.110 | 0.480 | 6.140 | 0.480 | 6.140 | 0.052 | 7.110 |
| 30 | 25 | 2.794 | 0.047 | 6.060 | 0.443 | 5.405 | 0.522 | 6.639 | 0.058 | 7.889 |
| 35 | 25 | 2.776 | 0.044 | 5.405 | 0.416 | 4.938 | 0.563 | 7.111 | 0.064 | 8.663 |
| 40 | 25 | 2.761 | 0.042 | 4.958 | 0.397 | 4.597 | 0.602 | 7.559 | 0.069 | 9.431 |
| 30 | 30 | 2.775 | 0.052 | 6.660 | 0.479 | 5.835 | 0.479 | 5.835 | 0.052 | 6.660 |
| 35 | 30 | 2.761 | 0.048 | 5.893 | 0.448 | 5.295 | 0.514 | 6.233 | 0.057 | 7.257 |
| 40 | 30 | 2.748 | 0.045 | 5.368 | 0.424 | 4.908 | 0.548 | 6.615 | 0.061 | 7.851 |
| 35 | 35 | 2.748 | 0.052 | 6.378 | 0.478 | 5.638 | 0.478 | 5.638 | 0.052 | 6.378 |
| 40 | 35 | 2.737 | 0.049 | 5.778 | 0.451 | 5.209 | 0.508 | 5.970 | 0.056 | 6.862 |
| 40 | 40 | 2.728 | 0.052 | 6.185 | 0.478 | 5.501 | 0.478 | 5.501 | 0.052 | 6.185 |

TABLE A3. -NOMINAL SIGNIFICANCE LEVEL $=5 \% ; k=4$

## $\theta$



| 10 | 10 | 3.259 | 0.041 | 62.560 | 0.402 | 18.127 | 0.402 | 18.127 | 0.041 | 62.560 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 15 | 10 | 2.965 | 0.035 | 9.652 | 0.339 | 7.518 | 0.523 | 18.610 | 0.058 | 73.853 |
| 20 | 10 | 2.817 | 0.031 | 5.888 | 0.311 | 5.237 | 0.626 | 19.020 | 0.071 | 82.573 |
| 25 | 10 | 2.728 | 0.030 | 4.667 | 0.295 | 4.335 | 0.717 | 19.367 | 0.091 | 89.669 |
| 30 | 10 | 2.668 | 0.029 | 4.071 | 0.285 | 3.860 | 0.796 | 19.662 | 0.107 | 95.646 |
| 35 | 10 | 2.626 | 0.028 | 3.720 | 0.277 | 3.569 | 0.867 | 19.916 | 0.122 | 100.840 |
| 40 | 10 | 2.594 | 0.027 | 3.489 | 0.272 | 3.372 | 0.931 | 20.138 | 0.138 | 105.339 |
| 15 | 15 | 2.817 | 0.044 | 12.276 | 0.418 | 8.707 | 0.418 | 8.707 | 0.044 | 12.276 |
| 20 | 15 | 2.728 | 0.039 | 7.174 | 0.369 | 6.062 | 0.490 | 9.695 | 0.054 | 14.812 |
| 25 | 15 | 2.668 | 0.035 | 5.507 | 0.341 | 4.944 | 0.556 | 10.535 | 0.064 | 17.266 |
| 30 | 15 | 2.626 | 0.033 | 4.693 | 0.322 | 4.338 | 0.617 | 11.262 | 0.074 | 19.644 |
| 35 | 15 | 2.594 | 0.032 | 4.213 | 0.309 | 3.962 | 0.673 | 11.900 | 0.083 | 21.948 |
| 40 | 15 | 2.570 | 0.031 | 3.896 | 0.300 | 3.705 | 0.725 | 12.465 | 0.093 | 24.183 |
| 20 | 20 | 2.668 | 0.045 | 8.442 | 0.423 | 6.804 | 0.423 | 6.804 | 0.045 | 8.442 |
| 25 | 20 | 2.626 | 0.041 | 6.340 | 0.384 | 5.510 | 0.474 | 7.476 | 0.052 | 9.692 |
| 30 | 20 | 2.594 | 0.037 | 5.311 | 0.359 | 4.792 | 0.523 | 8.088 | 0.059 | 10.924 |
| 35 | 20 | 2.570 | 0.035 | 4.703 | 0.341 | 4.338 | 0.568 | 8.649 | 0.066 | 12.140 |
| 40 | 20 | 2.550 | 0.034 | 4.303 | 0.327 | 4.026 | 0.611 | 9.165 | 0.073 | 13.339 |
| 25 | 25 | 2.594 | 0.046 | 7.165 | 0.426 | 6.039 | 0.426 | 6.039 | 0.046 | 7.165 |
| 30 | 25 | 2.570 | 0.042 | 5.924 | 0.394 | 5.222 | 0.465 | 6.534 | 0.051 | 7.984 |
| 35 | 25 | 2.550 | 0.039 | 5.191 | 0.371 | 4.699 | 0.503 | 6.998 | 0.056 | 8.795 |
| 40 | 25 | 2.534 | 0.037 | 4.707 | 0.354 | 4.336 | 0.540 | 7.435 | 0.062 | 9.600 |
| 30 | 30 | 2.550 | 0.046 | 6.535 | 0.427 | 5.631 | 0.427 | 5.631 | 0.046 | 6.535 |
| 35 | 30 | 2.534 | 0.043 | 5.676 | 0.400 | 5.045 | 0.460 | 6.020 | 0.051 | 7.141 |
| 40 | 30 | 2.520 | 0.040 | 5.110 | 0.379 | 4.636 | 0.491 | 6.391 | 0.055 | 7.444 |
| 35 | 35 | 2.520 | 0.046 | 6.160 | 0.428 | 5.378 | 0.428 | 5.378 | 0.046 | 6.160 |
| 40 | 35 | 2.509 | 0.043 | 5.512 | 0.404 | 4.925 | 0.455 | 5.698 | 0.050 | 6.641 |
| 40 | 40 | 2.499 | 0.046 | 5.911 | 0.429 | 5.206 | 0.429 | 5.206 | 0.046 | 5.911 |

TABLE A4.-NOMINAL SIGNIFICANCE LEVEI $=5 \% ; k=5$


| 10 | 10 | 3.326 | 0.033 | 332.582 | 0.333 | 33.258 | 0.333 | 33.258 | 0.033 | 332.582 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 15 | 10 | 2.901 | 0.029 | 14.108 | 0.290 | 9.292 | 0.455 | 29.013 | 0.049 | 290.130 |
| 20 | 10 | 2.711 | 0.027 | 6.519 | 0.271 | 5.587 | 0.559 | 27.109 | 0.065 | 271.090 |
| 25 | 10 | 2.603 | 0.026 | 4.783 | 0.260 | 4.377 | 0.648 | 26.030 | 0.081 | 260.299 |
| 30 | 10 | 2.534 | 0.025 | 4.037 | 0.253 | 3.797 | 0.727 | 25.336 | 0.096 | 253.356 |
| 35 | 10 | 2.485 | 0.025 | 3.625 | 0.249 | 3.460 | 0.796 | 24.851 | 0.111 | 248.515 |
| 40 | 10 | 2.449 | 0.025 | 3.364 | 0.245 | 3.241 | 0.858 | 24.495 | 0.125 | 244.947 |
|  |  |  |  |  |  |  |  |  |  |  |
| 15 | 15 | 2.711 | 0.038 | 18.196 | 0.367 | 10.516 | 0.367 | 10.516 | 0.038 | 18.196 |
| 20 | 15 | 2.603 | 0.034 | 8.069 | 0.327 | 6.482 | 0.438 | 11.470 | 0.048 | 22.034 |
| 25 | 15 | 2.534 | 0.031 | 5.710 | 0.304 | 5.019 | 0.502 | 12.244 | 0.057 | 25.647 |
| 30 | 15 | 2.485 | 0.030 | 4.693 | 0.289 | 4.290 | 0.561 | 12.891 | 0.066 | 29.059 |
| 35 | 15 | 2.449 | 0.028 | 4.131 | 0.279 | 3.858 | 0.615 | 13.443 | 0.075 | 32.289 |
| 40 | 15 | 2.422 | 0.028 | 3.776 | 0.272 | 3.574 | 0.665 | 13.922 | 0.084 | 35.354 |
| 20 | 20 | 2.534 | 0.040 | 9.589 | 0.380 | 7.266 | 0.380 | 7.266 | 0.040 | 9.589 |
| 25 | 20 | 2.485 | 0.036 | 6.626 | 0.346 | 5.608 | 0.429 | 7.960 | 0.046 | 11.080 |
| 30 | 20 | 2.449 | 0.034 | 5.344 | 0.324 | 4.753 | 0.475 | 8.581 | 0.053 | 12.544 |
| 35 | 20 | 2.422 | 0.032 | 4.635 | 0.309 | 4.237 | 0.519 | 9.141 | 0.060 | 13.980 |
| 40 | 20 | 2.400 | 0.031 | 4.187 | 0.297 | 3.894 | 0.560 | 9.649 | 0.066 | 15.391 |
| 25 | 25 | 2.449 | 0.041 | 7.532 | 0.386 | 6.151 | 0.386 | 6.152 | 0.041 | 7.532 |
| 30 | 25 | 2.422 | 0.038 | 5.991 | 0.357 | 5.190 | 0.424 | 6.656 | 0.046 | 8.430 |
| 35 | 25 | 2.401 | 0.035 | 5.136 | 0.337 | 4.599 | 0.460 | 7.125 | 0.051 | 9.318 |
| 40 | 25 | 2.383 | 0.034 | 4.595 | 0.322 | 4.202 | 0.495 | 7.562 | 0.056 | 10.197 |
| 30 | 30 | 2.400 | 0.042 | 6.633 | 0.389 | 5.602 | 0.389 | 5.602 | 0.042 | 6.633 |
| 35 | 30 | 2.383 | 0.039 | 5.635 | 0.365 | 4.946 | 0.420 | 5.993 | 0.046 | 7.270 |
| 40 | 30 | 2.363 | 0.037 | 5.003 | 0.347 | 4.499 | 0.450 | 6.363 | 0.050 | 7.903 |
| 35 | 35 | 2.368 | 0.042 | 6.131 | 0.392 | 5.277 | 0.392 | 5.277 | 0.042 | 6.131 |
| 40 | 35 | 2.356 | 0.040 | 5.408 | 0.370 | 4.786 | 0.418 | 5.594 | 0.046 | 6.624 |

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[^0]:    Address for Correspondence: Professor David Giles, Department of Economics, University of Canterbury, Christchurch, NEW ZEALAND.

