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marginscontplot: Plotting the marginal effects of continuous predictors

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Abstract. I provide a new tool (marginscontplot) for plotting the marginal effect of continuous covariates in regression models. The plots may be univariate or according to levels or user-selected values of a second covariate. Nonlinear relationships involving transformed covariates may be plotted on the original scale.

Keywords: gr0056, marginscontplot, mcp, regression models, continuous covariates, margins, graphing marginal effects, interactions

1 Introduction

The developers of Stata 11 and 12 have clearly put much effort into creating the margins and marginsplot commands. Their work appears to have been well received by users. However, margins and marginsplot are naturally focused on margins for categorical (factor) variables, and continuous predictors are arguably rather neglected. In this article, I present a new command, marginscontplot, which provides facilities to plot the marginal effect of a continuous predictor in a meaningful way for a wide range of regression models. In principle, it can handle any regression command for which margins is applicable and makes sense. This includes all the familiar commands such as regress, logit, probit, poisson, glm, stcox, streg, and xtreg.

marginscontplot is also known as mcp for those who dislike typing the full command name. You may use marginscontplot and mcp interchangeably.

2 Comments on margins

To the beginner, the meaning of the term "margin" may be somewhat elusive. It certainly was for me. Beginners may find useful a recent article by Williams (2012). The author concentrates on using the margins command with categorical covariates. Here we are concerned more with continuous covariates, although categorical covariates are also supported.

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Consider the simple but illustrative example of a regression in the iconic auto.dta of mpg on foreign and weight. We use the modern approach and specify foreign as a factor variable, letting Stata take care of any dummy variables that are needed:

. sysuse auto (1978 Automob:	ile Data)							
. regress mpg	i.foreign wei	ght						
Source	SS	df		MS		Number of obs	=	74
						F(2, 71)	=	69.75
Model	1619.2877	2	809	.643849		Prob > F	=	0.0000
Residual	824.171761	71	11	.608053		R-squared	=	0.6627
						Adj R-squared	=	0.6532
Total	2443.45946	73	33.4	4720474		Root MSE	=	3.4071
mpg	Coef.	Std.	Err.	t	P> t	[95% Conf.	In	terval]
1.foreign	-1.650029	1.075	5994	-1.53	0.130	-3.7955		4954422
weight	0065879	.0006	5371	-10.34	0.000	0078583		0053175
_cons	41.6797	2.16	5547	19.25	0.000	37.36172	4	5.99768

We apply the margins command to get the marginal effect of foreign manufacture, adjusting for vehicle weight:

```
. margins foreign
Predictive margins
                                                    Number of obs
                                                                               74
                                                                     =
Model VCE
             : OLS
Expression
             : Linear prediction, predict()
                           Delta-method
                                                  P>|z|
                                                            [95% Conf. Interval]
                             Std. Err.
                   Margin
                                             z
     foreign
                                                                         22.78569
          0
                  21.78785
                             .5091123
                                          42.80
                                                  0.000
                                                                20.79
          1
                  20.13782
                             .8535566
                                         23.59
                                                  0.000
                                                            18.46488
                                                                         21.81076
```

We see that weight for weight, the marginal means (in miles per gallon) are 21.79 (0.51) for domestic cars and 20.14 (0.85) for foreign cars. For clarification, we now demonstrate how the same estimates (without standard errors) can be obtained by manipulating predictions from the regression model directly:

. preserve					
. replace fore (22 real chang	0				
. predict marg (option xb as:		d values)			
. summarize ma	argin0				
Variable	Obs	Mean	Std. Dev.	Min	Max
margin0	74	21.78785	5.120063	9.794333	30.08502
. restore					
. preserve					

. replace forei (52 real change	0				
. predict margin (option xb assumed		values)			
. summarize mar	gin1				
Variable	Obs	Mean	Std. Dev.	Min	Max
margin1	74	20.13782	5.120063	8.144303	28.43499
. restore					

We see that the mean prediction for foreign set to 0 for the entire sample is identical to the margin for foreign = 0 and similarly for foreign = 1. The estimated margin is essentially an out-of-sample prediction: we pretend that the weights of the vehicles do not change when we pretend that all of them were domestic or all were foreign.

margins handles the presence of interaction terms in the model with aplomb:

```
. regress mpg i.foreign##c.weight
  (output omitted)
. margins foreign
                                                                               74
Predictive margins
                                                    Number of obs
Model VCE
             : OLS
Expression
             : Linear prediction, predict()
                           Delta-method
                            Std. Err.
                                                  P>|z|
                                                            [95% Conf. Interval]
                   Margin
                                             z
     foreign
                 21.60544
                             .4967815
                                         43.49
                                                  0.000
                                                            20.63177
                                                                         22.57912
          0
```

Let us return to the simpler model (regress mpg i.foreign weight). Suppose we want the marginal effects of weight on mpg. We could type, for example,

12.82

0.000

14.77108

20.104

1.360464

```
. margins, at(weight=3000)
```

1

or

```
. margins foreign, at(weight=3000)
```

17.43754

to get the miles per gallon predicted at a roughly central value of a car weight of 3,000 pounds, without or with distinguishing the effect of foreign. However, there are no fewer than 64 distinct values of weight. We cannot validly type margins weight to get its marginal effect, because weight is a continuous variable and Stata does not allow this syntax; weight would have to be a categorical variable for this to work. Even if we could type it, it would not be much help to see a table of the estimated margins for the 64 values of weight.

We would really like to create a visual assessment, for example, a plot of the margins against weight. The ado-file marginscontplot is designed to help us do just that.

3 A simple example of marginscontplot

We continue with the auto.dta example. The following code uses standard Stata commands, margins followed by marginsplot, to give a plot with 95% pointwise confidence intervals of the marginal effect of weight on mpg, adjusting for foreign:

```
. quietly regress mpg i.foreign weight
```

. quietly margins, at(weight = (1760(100)4840))

```
. marginsplot
```

Variables that uniquely identify margins: weight

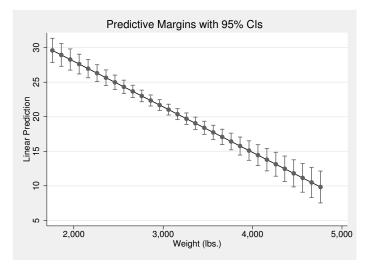


Figure 1. Marginal effect of weight on mpg with a pointwise 95% confidence interval, from a linear regression model. Produced by using margins and marginsplot.

The plot is shown in figure 1. The appearance could be improved by using a more appropriate rendition of the confidence intervals, but the required information is basically all there.

Figure 2 shows a similar plot, this time produced by a single marginscontplot command:

. quietly regress mpg i.foreign weight

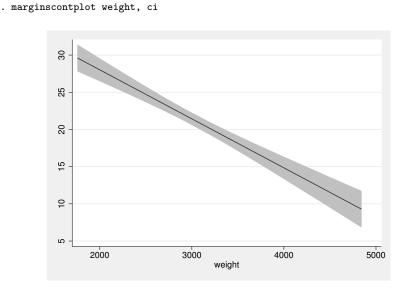


Figure 2. Marginal effect of weight on mpg with a pointwise 95% confidence interval, from a linear regression model. Produced by using marginscontplot.

Although you do not see it, marginscontplot is working behind the scenes to generate such plots. Let x be the covariate that is used. By default, marginscontplot extracts the unique values of x observed in the sample and evaluates the margin at each unique value, together with a pointwise confidence interval if the ci option has been specified. To do this, it calls the margins command with a suitably constructed at() option that defines the plotting values. The constructed at() option resembles the margins option at(weight = (1760(100)4840)) we have already seen, except that all 64 unique values of weight are spelled out. marginscontplot saves the resulting estimates to a separate, temporary file, which it loads, manipulates if necessary, and plots.

If we complicate the model by adding an interaction term, no difficulty accrues (figure not shown):

- . regress mpg i.foreign##c.weight
- . marginscontplot weight, ci

In the case of a linear function (as here), we only actually need two values, for example, the minimum and maximum of observed x, to define the line. However, this would not display the confidence interval accurately. A practical suggestion is 10 to 20

values, equally spaced over the range of x. The number of such values is controlled by the var1() and var2() options of marginscontplot. Alternatively, you can supply your own choice of x values by including them directly in the at1() or at2() option, for example,

. marginscontplot weight, ci var1(20)
. marginscontplot weight, ci at1(2000(500)4500)

Here we are working with univariate plots (just one variable), and we need only the at1() or var1() option to specify the range of x values for plotting. Later, we shall see how the at2() and var2() options are used for plotting at values of a second covariate.

4 An example from survival analysis

We use the German breast cancer dataset to illustrate two issues:

- 1. How marginscontplot handles margins in nonlinear regression models such as stcox.
- 2. The use of the percentile feature of the at1() option to limit the range of plotting values.

We load the data by using the webuse command, and we stset it for use as survival data:

```
. webuse brcancer
(German breast cancer data)
. stset rectime, failure(censrec)
     failure event: censrec != 0 & censrec < .</pre>
obs. time interval: (0, rectime]
 exit on or before: failure
      686 total obs.
        0 exclusions
      686 obs. remaining, representing
      299 failures in single record/single failure data
                                                                  0
  771400 total analysis time at risk, at risk from t =
                                                                  0
                             earliest observed entry t =
                                  last observed exit t =
                                                               2659
```

Suppose we fit a Cox proportional hazards model on the continuous covariates x5e and x6. We wish to see the effect of x6 on the relative hazard of an event:

- . quietly stcox x5e x6
- . marginscontplot x6, ci

The result is shown in figure 3(a).

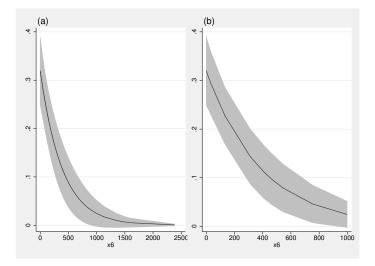


Figure 3. Marginal effect of x6 on the relative hazard in a Cox model, with pointwise 95% confidence intervals. (a) Full range of x6; (b) range restricted to (1,99) centiles.

It appears that larger values of x6 are associated with a (dramatically) lower relative hazard. Note that although we have fit x6 as a linear term in the Cox model, its marginal effect appears as a curve rather than a straight line. The reason is that by default, predict for stcox predicts the relative hazard, whereas the regression coefficient, $_b[x6]$, and hence, the linear predictor xb, acts on the log relative-hazard scale. If we wanted to see the effect of x6 on the log relative-hazard, we would use the margopts() option with predict(xb) to specify the linear predictor (figure not shown):

```
. marginscontplot x6, ci margopts(predict(xb))
```

The observed distribution of x6 is markedly skewed (coefficient of skewness = 4.8), having a concentration of values at 0 and a small number of large values. For example, the 99th centile is 998 fmol/l, whereas the range extends out to 2,380 fmol/l. We can limit the plotting values according to chosen centiles of x6 by using the % prefix in the at1() option, for example,

. marginscontplot x6, ci at1(%1 10 25 50 75 90 95(1)99)

This restricts the range of the plot [see figure 3(b)].

5 Examples with transformed x

5.1 Log transformation

Suppose the relationship between the response variable, y, and x is log linear. Such a situation is not uncommon. We wish to model E(y) as a linear function of log x, and we want to graph the relationship on the original scale of x, not the scale of log x. Let us return to auto.dta for an example that achieves the aim. We model mpg as a log-linear function of weight:

- . quietly generate logwt = ln(weight)
- . quietly regress mpg logwt

Suppose we decide to plot at 20 values of weight equally spaced between the observed lowest and the highest weights. Stata's range command can conveniently be used to create a new variable (say, w) containing such values:

```
. summarize weight
. range w r(min) r(max) 20
```

Next we log-transform w, and use w and the transformed values in the var1() option of marginscontplot:

```
. quietly generate logw = ln(w)
```

```
. marginscontplot weight(logwt), var1(w(logw)) ci
```

The result is shown in figure 4.

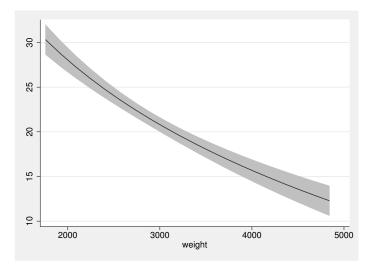


Figure 4. Plot of the marginal effect of weight on mpg in auto.dta when log(weight) is fit.

5.2 Fractional polynomials

What if the relationship between the response variable, y, and x is more complex? A simple class of functions for modeling quite a wide range of nonlinear functions is fractional polynomials (FPs) (Royston and Altman 1994). These are essentially extensions of ordinary polynomials that allow noninteger and negative values of the polynomial power transformations. This greatly increases their flexibility. For example, a quadratic $\beta_0 + \beta_1 x^1 + \beta_2 x^2$ generalizes to the FP2 function $\beta_0 + \beta_1 x^{p_1} + \beta_2 x^{p_2}$, where p_1 and p_2 are powers belonging to the restricted set $S = \{-2, -1, -0.5, 0, 0, 5, 1, 2, 3\}$. By convention, x^0 means $\ln(x)$. Also included are "repeated powers" models of the form $\beta_0 + \beta_1 x^{p_1} + \beta_2 x^{p_1} \ln(x)$. FP1 functions have the simple form $\beta_0 + \beta_1 x^{p_1}$ for p_1 in S.

Many details of FPs and their modeling, both in a univariate and in a multivariable context, are provided in Royston and Sauerbrei (2008). In Stata, univariate FPs are implemented in the command fracpoly, and multivariable FPs (models) in mfp. In Stata 13, mfp is unchanged, but fracpoly has been superseded by a new command, fp (although fracpoly continues to work). marginsconplot works properly with fp. For example, the information carried by FP-transformed variables created by fp or fp generate is used appropriately by marginscontplot.

Consider extending the auto.dta example to allow an FP function of weight:

<pre>. fracpoly: regress mpg weight foreign -> gen double Iweig1 = X^-21096835742 if e(sample) -> gen double Iweig2 = X^-2*ln(X)121208886 if e(sample) (where: X = weight/1000)</pre>								
Source	SS	df		MS		Number of obs		
Model Residual	1696.05946 747.400002	3 70		353152 771429		F(3, 70) Prob > F R-squared	= 0.0000 = 0.6943	
Total	2443.45946	73	33.4	720474		Adj R-squared Root MSE	= 0.6810 = 3.2676	
mpg	Coef.	Std.	Err.	t	P> t	[95% Conf.	Interval	
Iweig1 Iweig2 foreign _cons	15.88527 127.9349 -2.222516 20.95519	20.60 47.53 1.053 .569	8106 8782	0.77 2.69 -2.11 36.79	0.443 0.009 0.039 0.000	-25.2067 33.13723 -4.324218 19.81923	56.97724 222.7327 1208133 22.09115	

Deviance: 381.13. Best powers of weight among 44 models fit: -2 -2.

fracpoly has determined that the best-fitting FP2 model has powers (-2, -2) for weight; that is, a function of the form $\beta_1 x^{-2} + \beta_2 x^{-2} \ln(x)$ has been selected. How do we produce a margins plot of the fitted function of weight? We need to tell the software the weight values at which we want to plot the fit and the corresponding FP-transformed values on which the regression model has been fit. Suppose we decide to plot at 20 values of weight equally spaced between the observed lowest and the highest weights. We take the approach described above in the log-linear example to create a new variable (say, w1) containing such values:

- . quietly summarize weight
- . range w1 r(min) r(max) 20

Now we compute the required FP transformation of w1, namely, x^{-2} and $x^{-2} \ln (x)$. Some care is needed. We see from the fracpoly output given above that for each new variable fracpoly created, namely, Iweig_1 and Iweig_2, it has actually scaled weight by dividing by 1,000 before creating each transformation, and then added a constant. For the regression parameters to be valid for out-of-sample prediction at new variables, say, w1a and w1b, derived from w1, we must mimic that process precisely:

```
. generate w1a = (w1/1000)^-2-.1096835742
```

. generate w1b = $(w1/1000)^{-2} * \ln(w1/1000)^{-.121208886}$

To create the margins plot, including a pointwise 95% confidence interval for the fit, we run marginscontplot with the var1() and ci options. The var1() option provides a look-up table between our plotting positions (stored in w1) and their FP transformations (stored in w1a and w1b):

```
. marginscontplot weight (Iweig__1 Iweig__2), var1(w1 (w1a w1b)) ci
```

The syntax weight (Iweig_1 Iweig_2) has a flavor similar to var1(w1 (w1a w1b)). The original predictor is weight, and Iweig_1 Iweig_2 expresses how weight appears in the regression model. The resulting graph is shown in figure 5.

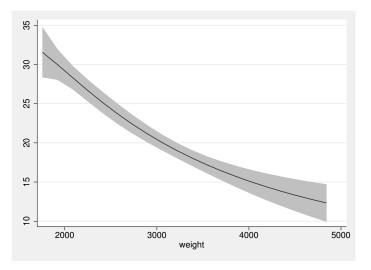


Figure 5. Marginal effect of weight on mpg with a pointwise 95% confidence interval, from a two-term fractional polynomial regression model.

The fitted function shows curvature in the functional form (cf. figure 4).

We can easily elaborate the plot to show the effect of weight according to foreign status as follows (see figure 6):

```
foreign = Domestic
                                                             foreign = Foreign
                                                4
35
8
                                                8
ŝ
20
                                                20
15
                                                9
5
     2000
                 3000
                             4000
                                        5000
                                                     2000
                                                                3000
                                                                            4000
                                                                                        5000
                     weight
                                                                    weight
```

. marginscontplot weight (Iweig__1 Iweig__2) foreign, var1(w1 (w1a w1b)) ci

Figure 6. Marginal effect of weight on mpg by the two values of foreign with a pointwise 95% confidence interval, from a fractional polynomial regression model.

Note that the *x* dimension for the plot is always the first-mentioned variable, and the "by-variable" is the second, namely, **foreign**. The program figures out that margins for **weight** at the two distinct values of **foreign** are needed. If the **ci** option is omitted, the same two lines are plotted on the same graph, making them easier to compare directly but sacrificing information on their precision.

The program **fracpoly** stores in characteristics the details of the rather complicated FP transformations it performed:

. char list Iweig1[fp]	
<pre>Iweig1[fp]:</pre>	X^-21096835742: X = weight/1000
. char list Iweig2[fp]	
<pre>Iweig2[fp]:</pre>	X^-2*ln(X)121208886: X = weight/1000

To make the plotting process easier, marginscontplot can use this information internally to transform user-specified values of weight to the values it needs to compute the margins:

```
. marginscontplot weight (Iweig__1 Iweig__2), var1(20) ci
```

In this context, the option var1(20) says "plot the fit at 20 values of weight equally spaced between the minimum and maximum".

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A third way to achieve the same result is to generate the FP-transformed variables for weight yourself by using fracgen, run the regression, and finally run marginscontplot:

```
. fracgen weight -2 -2
. local fp2_weight `r(names)`
. display "`fp2_weight'"
weight_1 weight_2
. regress mpg i.foreign `fp2_weight`
. marginscontplot weight (`fp2_weight`), var1(20) ci
```

fracgen creates FP-transformed variables, here called weight_1 and weight_2, silently storing their details in characteristics. For convenience, I have stored these names in a local macro called fp2_weight. By default, fracgen omits the constants -0.1096835742 and -0.121208886, but this has no effect on marginscontplot.

6 A more complex example

6.1 Analysis with fractional polynomials

We move from auto.dta to data from a biomedical survey, nhanes2f.dta. The dataset is available via the command webuse nhanes2f.

The dataset comprises observations of 10,337 individuals: 4,909 males and 5,428 females. We concentrate on modeling blood pressure in the males (sex==1). There are two measures of blood pressure in the dataset: bpsystol (systolic blood pressure) and bpdiast (diastolic blood pressure). Because they are physiologically and statistically highly correlated, we model a composite measure known as mean arterial pressure (MAP):

. generate map = (bpsystol + 2 * bpdiast)/3

Known predictors of blood pressure are age and body mass index (BMI, equal to weight in kg divided by the square of height in m). Modeling MAP with mfp shows that hemoglobin (hgb) and race (race, coded 1 = white, 2 = black, and 3 = other) are also significant predictors of MAP in a multivariable context. Age needs an FP2 model with powers (-2, -1), whereas BMI and hemoglobin seem to have linear effects.

There are six possible two-way multiplicative interactions between the four predictors. Of these, three are highly significant (P < 0.001) in a model that includes all the main effects and interactions: $FP2(age) \times race$, $FP2(age) \times BMI$, and $FP2(age) \times$ hemoglobin. (In these expressions, we include two variables to represent the FP2 transformation of age.) We thus arrive at a rather complex model that includes four main effects and three interactions, all of which involve a nonlinear transformation of age:

<pre>. fracgen age -2 -1 -> gen double age_1 = X^-2 -> gen double age_2 = X^-1 (where: X = age/10)</pre>										
. regress map age_1 age_2 i.race bmi hgb race#c.(age_1 age_2) > c.bmi#c.(age_1 age_2) c.hgb#c.(age_1 age_2)										
Source	SS	df	MS		Number of obs F(14, 4894)					
Model Residual	204564.182 756201.129		1.7273 515964		Prob > F R-squared Adj R-squared	= 0.0000 = 0.2129				
Total	960765.311	4908 195.	754953		Root MSE	= 12.43				
map	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]				
age_1 age_2	777.3663 -583.2943	275.0243 160.1266	2.83 -3.64	0.005 0.000	238.1953 -897.2143	1316.537 -269.3742				
race		4 444470				10 1050				
2 3	1.062011 24.75007	4.643472 9.477148	0.23 2.61	0.819 0.009		10.1653 43.32953				
bmi hgb	.0241705 -1.907729	.35309 1.248318	0.07 -1.53	0.945 0.127	6680443 -4.354992	.7163853 .5395346				
race#c.age_1 2 3	-77.04519 155.6329	60.46379 118.9581	-1.27 1.31	0.203 0.191	-195.5814 -77.5783	41.49096 388.8441				
race#c.age_2										
2 3	30.53207 -135.8852	35.9084 71.43399	0.85 -1.90	0.395 0.057	-39.8645 -275.9278	100.9286 4.157523				
c.bmi#c.age_1	-11.19275	4.635915	-2.41	0.016	-20.28122	-2.104274				
c.bmi#c.age_2	7.566864	2.732302	2.77	0.006	2.210326	12.9234				
c.hgb#c.age_1	-22.17118	17.11388	-1.30	0.195	-55.72206	11.37971				
c.hgb#c.age_2	17.56146	9.997191	1.76	0.079	-2.037522	37.16044				
_cons	147.2989	19.92625	7.39	0.000	108.2345	186.3633				

The table of estimates looks pretty complicated. How do we interpret the results? To gain understanding, we work with graphs created by marginscontplot. We start with the marginal effect of age alone, and then we explore the three age interactions. Figure 7(a) shows the marginal relationship between MAP and age.

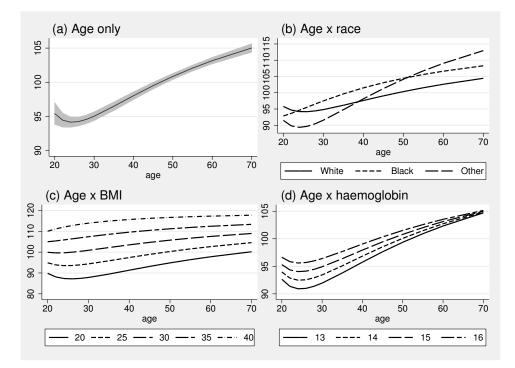


Figure 7. Marginal plots of the effect of age on map in nhanes2f.dta. a) Age alone; b) age by race; c) age by BMI at five selected values of BMI; d) age by hemoglobin at four selected values of hemoglobin. The model includes three interactions with FP2 transformations of age.

Mean MAP shows a clear increase with age. (The inflection point at about 25 years may be an artifact of the FP2 model. It seems more plausible that the underlying curve is roughly "flat" between about 20 and 30 years, but the FP2 family is not flexible enough to mimic this behavior.)

The remaining three plots show the interactions with age. In figure 7(b), we see somewhat different shapes of the functions across races, against a generally increasing trend. Figure 7(c) shows there is a strong effect of BMI at all ages, which is a little stronger in younger people. Comparing it with figure 7(a), we see that the effect of age adjusted for BMI is noticeably smaller than the marginal effect of age. Finally, figure 7(d) suggests that higher hemoglobin is associated with higher blood pressure at young ages but not in older people. An example of the marginscontplot command needed to produce such plots is given below for panel (c):

```
. marginscontplot age (age_1 age_2) bmi, at1(20(2)30 35(5)60 70) at2(20(5)40)
> plotopts(lpattern(1 - _ - -.) lwidth(medthick ..) name(g3, replace)
> title("(c) Age x BMI", placement(west)) legend(label(1 "20") label(2 "25")
> label(3 "30") label(4 "35") label(5 "40") row(1)))
```

Much of the code here is needed in plotopts() to produce a satisfying plot appearance.

6.2 Analysis with spline models

The techniques described above for plotting results from FP models can be applied in a similar fashion to spline models or indeed to any model involving nonlinear transformations of continuous predictors. Space limitation prevents me from giving full details. In principle, the steps for spline modeling are as follows:

- 1. Determine a suitable spline model for the data.
- 2. Create the required spline basis variables for all continuous covariates with a nonlinear effect. (This is analogous to the **fracgen** operations described above. You can, for example, use Stata's **mkspline** command.)
- 3. Fit the selected model, including the spline basis variables and, if necessary, any important interactions.
- 4. For a given continuous predictor whose marginal effect is to be plotted, create a variable holding a limited number of plotting positions.
- 5. Transform the plotting-positions variable into the requisite number of spline basis variables, using the same knot numbers and positions as in the main analysis. These transformed variables provide the "look-up table" for plotting the fit on the original scale of the predictor (for example, plotting at actual ages rather than at meaningless transformed values).
- 6. Run marginscontplot with an appropriate syntax.

Of course, this simple schema hides many issues connected with spline model selection. These issues are beyond the present scope. However, I am happy to provide an example file on request suggesting how to produce the spline model equivalent of figure 7.

7 The marginscontplot command

7.1 Syntax

The syntax of marginscontplot is as follows:

```
{marginscontplot | mcp} xvar1 [ (xvar1a [xvar1b ...]) ] [xvar2 [ (xvar2a [xvar2b
...])]] [if] [in] [, at(at_list) at1([%]at1_list) at2([%]at2_list) ci
margopts(string) nograph plotopts(twoway_options) saving(filename[,
replace]) showmarginscmd var1(#|var1_spec) var2(#|var2_spec)]
```

The options are described below.

7.2 Description

marginscontplot provides a graph of the marginal effect of a continuous predictor on the response variable in the most recently fit regression model. When only *xvar1* is provided, the plot of marginal effects is univariate at values of *xvar1* specified by the at1() or var1() option. When both *xvar1* and *xvar2* are provided, the plot of marginal effects is against values of *xvar1* specified by the at1() or var1() option for fixed values of *xvar2* specified by the at2() or var2() option. A line is plotted for each specified value of *xvar2*.

marginscontplot has the distinctive ability to plot marginal effects on the original scale of *xvar1* or *xvar2*, even when the model includes transformed values of *xvar1* or *xvar2* but not *xvar1* or *xvar2* themselves. Such a situation arises in FP or spline modeling, for example, where nonlinear relationships with continuous predictors are to be approximated, and transformed covariates are included in the model to achieve this.

mcp is a synonym for marginscontplot for those who prefer to type less.

7.3 Options

- at(at_list) fixes values of model covariates other than xvar1 and xvar2. at_list has syntax varname1 = # [varname2 = # ...]. By default, predictions for such covariates are made at the observed values and averaged across observations.
- at1([%] at1_list) defines the plotting positions for xvar1 through the numlist at1_list. If the prefix % is included, at1_list is interpreted as percentiles of the distribution of xvar1. If at1() is omitted, all the observed values of xvar1 are used if feasible. Note that xvar1 is always treated as the primary plotting variable on the x dimension.
- at2([%] at2_list) defines the plotting positions for xvar2 through the numlist at2_list. If the prefix % is included, at2_list is interpreted as percentiles of the distribution of xvar2. If at2() is omitted, all the observed values of xvar2 are used if feasible. Note that xvar2 is always treated as the secondary "by-variable" for plotting purposes.

- ci displays pointwise confidence intervals for the fitted values on the margins plot. For legibility, if more than one line is specified, each line is plotted on a separate graph.
- margopts(string) supplies options to the margins command. The option most likely
 to be needed is predict(xb), which means that predicted values and, hence, margins are on the scale of the linear predictor. For example, in a logistic regression
 model, the default predictions are of the event probabilities. Specifying the option
 margopts(predict(xb)) gives margins on the scale of the linear predictor, that is,
 the predicted log odds of an event.

Note that the margins are calculated with the default setting, asobserved, for margins. See help margins for further information.

nograph suppresses the graph of marginal effects.

- plotopts(*twoway_options*) are options of graph twoway; see [G-3] *twoway_options*.
- saving(filename[, replace]) saves the calculated margins and their confidence intervals to a file (filename.dta). This can be useful for fine-tuning the plot or tabulating the results.
- showmarginscmd displays the margins command that marginscontplot creates and issues to Stata to do the calculations necessary for constructing the plot. This information can be helpful in fine-tuning the command or identifying problems.
- var1(#|var1_spec) specifies plotting values of xvar1. If var1(#) is specified, then
 # equally spaced values of xvar1 are used as plotting positions, encompassing the
 observed range of xvar1. Alternatively, var1_spec may be used to specify transformed
 plotting values of xvar1. The syntax of var1_spec is var1 [(var1a [var1b ...])].
 var1 is a variable holding user-specified plotting values of xvar1. var1a is a variable
 holding transformed values of var1 and similarly for var1b ... if required.
- var2(#|var2_spec) specifies plotting values of xvar2. If var2(#) is specified, then
 # equally spaced values of xvar2 are used as plotting positions, encompassing the
 observed range of xvar2. Alternatively, var2_spec may be used to specify transformed
 plotting values of xvar2. The syntax of var2_spec is var2 [(var2a [var2b ...])].
 var2 is a variable holding user-specified plotting values of xvar2. var2a is a variable
 holding transformed values of var2 and similarly for var2b ... if required.

7.4 Remarks

The version of var1() with var1_spec is appropriate for use after any covariate transformation is used in the model and you want a plot with the original (untransformed) covariate on the horizontal axis. This includes simple transformations such as logs and more complicated situations. For example, the model may involve an FP model in xvar1 using fracpoly or mfp. Alternatively, FP transformations of xvar1 may be calculated using fracgen, and the required model fit to the transformed variables before applying marginscontplot. The same facility is also available for the var2() option. It works in the same way but with xvar2 instead of xvar1. marginscontplot has been designed to handle quite high-dimensional cases, that is, cases where many margins must be estimated. Be aware, however, that the number of margins is limited by the maximum matrix size; see help matsize. This can be increased if necessary by using the set matsize # command. marginscontplot tells you the smallest value of # needed to accommodate the case in question.

8 Concluding comments

When continuous variables are modeled, especially in a nonlinear fashion, plotting plays a vital role in understanding the nature of their association with the response variable. This is particularly true when interactions are involved because tables of regression coefficients are inadequate tools for understanding relationships. I hope that marginscontplot will continue the good work started by margins and marginsplot in understanding outputs from such models.

9 Acknowledgment

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10 References

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About the author

Patrick Royston is a medical statistician with more than 30 years of experience and with a strong interest in biostatistical methods and in statistical computing and algorithms. He works largely in methodological issues in the design and analysis of clinical trials and observational studies. He is currently focusing on alternative outcome measures in trials with a time-to-event outcome; on problems of model building and validation with survival data, including prognostic factor studies and treatment-covariate interactions; on parametric modeling of survival data; and on novel clinical trial designs.