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## AGRICULTURAL DEVELOPMENT SYSTEMS EGYPT PROJECT UNIVERSITY OF/CALIFORNLA, DAVIS

REGRESSION ANALYSIS OF GRAPE, POTATO, AND TOMATO PRICESATEL NOZHA MARKET, ALEXANDRIA, MONTHLY DATA, 1972-1981
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REGRESSION ANALYSIS OF GRAPE, POTATO, AND TOMATO PRICES AT EL NOZHA MARKET, ALEXANDRIA, MONTHLY DATA, 1972-19811

By Jerry Foytik and Nabil Habashy

Price-quantity relationships for grapes, potatoes, and tomatoes sold at the El Nozha market are determined by regressional analysis of monthly data for 1972-1981. Several equations with price as the dependent variable were formulated to describe meaningful relationships presumed to exist on this market. All factors considered to have an important effect on price could not be included because the needed quantitative data were not available. Nevertheless, the computed equations do fit the empirical data well and do indicate how the price-making mechanism operates in response to changes in the variables used in the models formulated.

In brief, the results computed for the various equations indicate a negative price-quantity function and an upward trend in prices during 1972-1981. Furthermore, this function shifts considerably on a monthly basis. These monthly shifts form an orderly movement during the year rather than representing mere random fluctuations.

METHOD
Techniques of ordinary least squares (OLS) are used for relating price at the El Nozha market to the quantity sold (Q), trend (T), and monthly dummy variables $\left(X_{i}\right)$. The $X_{i}$ variables determine shifts in monthly levels of the price-quantity function. Only linear functions are formulated and computed.
$1_{\text {An analysis of weekly prices for potatoes and tomatoes sold at the Rod }}$ E1 Farag market, Cairo, is reported in Working Paper No. 172 of this series.

These are fitted in pairs--with the median price ( $Y$ ) and the minimum price ( $P$ ) of the monthly range of prices as alternate dependent variables. For example, one equation for each commodity is expressed by

$$
P=A+B_{1} Q+B_{2} T+C_{1} X_{1}+C_{2} X_{2}+\cdots+C_{n} X_{n}
$$

The Durbin-Watson test indicates definite positive autocorrelation among successive observations for both potatoes and tomatoes, but not for grapes. Hence, first order autoregressive equations are fitted only for potatoes and tomatoes.

## DATA USED

The monthly prices collected by the Egyptian Ministry of Agriculture give the price range separately for each month. These data provide the two price series used for the dependent variable. One is the low end of this monthly range, i.e., the minimum monthly price ( P ). The other is the median or average ( $Y$ ) of the range.

Three principal independent variables are used. Quantity is represented by monthly sales as reported by the Ministry. Dummy variables are introduced for determining the month-to-month shifts in the level of the price-quantity function. Thirdly, a trend factor serves as a proxy for the average net effect of omitted variables.

Per capita income data for urban areas were supplied only on an annual basis when this analysis was made. They were used in equations for grapes, but not for potatoes and tomatoes. Since underlying conditions can change
$2_{\text {For each such equation, a companion is computed using } Y \text { as the dependent }}$ variable. And, of course, a third equation for each set could have been fitted using the high prices of the monthly range. This is not done for no particular reason except to avoid increasing the number of equations fitted.
substantially during ten years, some equations are computed for subperiods of 1972-1981.

The monthly data used in the analyses are given in Tables A, B, and C which are placed at the end of the report. Monthly averages of the ten yearly values (for each month) are in the last column of each table. Averages at the foot of each column are annual averages for the months.

## RESULTS FOR GRAPES

Table 1 summarizes the computed values for ten equations. Results for each equation relate price negatively to quantity ( $Q$ ) and positively to per capita income (I) and to the time trend (T). The other results differ, sometimes markedly, depending on which price series represents the dependent variable. When $Y$ is used, somewhat higher (and better) values are secured for $R^{2}$ and DW. Also, the price-quantity function declines as the season advances from June to September. If, on the other hand, the minimum price ( $P$ ) is used, the price-quantity function is at a low point in June and increases to a higher level maintained during July-August-September.

Four of the equations include another shift variable to compare the levels of the net price-quantity function during 1972-1977 and 1978-1981. Its inclusion changes the net regression coefficients for the other independent variables without materially improving the fits as measured by $R^{2}$ values. Furthermore, the average levels are shifted in opposite directions depending on whether price is represented by $Y$ or $P$. It may be desirable, therefore, to not consider these equations further.

TABLE 1: Grape Prices at El Nozha Market in Alexandria Regression Analysis of Monthly Data, 1972-1981

| Eqn. | Constant | Regression Coefficient |  |  |  |  |  |  | Supplemental Measure |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Q | T | I | S | $\mathrm{X}_{1}$ | $\mathrm{X}_{2}$ | $\mathrm{X}_{3}$ | $\mathrm{R}^{2}$ | SE | DW |
| Y as dependent variable $\quad$ ¢ |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 23.946 | $\begin{array}{r} -8.526 \\ (1.3) \end{array}$ | $\begin{aligned} & 19.96 \\ & (11.9) \end{aligned}$ |  |  | $\begin{aligned} & 36.04 \\ & (1.9) \end{aligned}$ | $\begin{aligned} & 23.48 \\ & (1.6) \end{aligned}$ | $\begin{aligned} & 15.81 \\ & (1.1) \end{aligned}$ | . 8128 | 28.49 | 1.63 |
| 2 | 47.417 | $\begin{array}{r} -13.079 \\ (3.9) \end{array}$ | $\begin{aligned} & 11.95 \\ & (2.4) \end{aligned}$ | $\begin{aligned} & .2164 \\ & (1.8) \end{aligned}$ |  |  | - |  | . 8095 | 28.74 | 1.82 |
| 3 | 22.215 | $\begin{array}{r} -8.600 \\ (1.4) \end{array}$ | $\begin{aligned} & 12.46 \\ & (2.6) \end{aligned}$ | $\begin{aligned} & .1900 \\ & (1.6) \end{aligned}$ |  | $\begin{aligned} & 34.03 \\ & (1.8) \end{aligned}$ | $\begin{aligned} & 21.68 \\ & (1.6) \end{aligned}$ | $\begin{aligned} & 14.00 \\ & (1.0) \end{aligned}$ | . 8221 | 27.78 | 1.63 |
| 4 | 38.573 | $\begin{array}{r} -12.947 \\ (3.9) \end{array}$ | $\begin{aligned} & 13.36 \\ & (2.6) \end{aligned}$ | $\begin{aligned} & .2533 \\ & (2.1) \end{aligned}$ | $\begin{array}{r} -19.72 \\ (1.1) \end{array}$ |  |  |  | . 8102 | 28.69 | 1.82 |
| 5 | 13.222 | $\begin{array}{r} 8.129 \\ (1.3) \end{array}$ | $\begin{aligned} & 13.79 \\ & (2.8) \end{aligned}$ | $\begin{aligned} & .2264 \\ & (1.9) \end{aligned}$ | $\begin{array}{r} -19.10 \\ (1.1) \end{array}$ | $\begin{aligned} & 34.54 \\ & (1.9) \end{aligned}$ | $\begin{aligned} & 20.80 \\ & (1.5) \end{aligned}$ | $\begin{aligned} & 13.19 \\ & (1.0) \end{aligned}$ | . 8228 | 27.72 | 1.61 |
| $\underline{P}$ as dependent variable |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 41.001 | $\begin{array}{r} -11.496 \\ (2.1) \end{array}$ | $\begin{aligned} & 15.52 \\ & (11.0) \end{aligned}$ |  |  | $\begin{array}{r} -24.02 \\ (1.5) \end{array}$ | $\begin{array}{r} 2.37 \\ (0.2) \end{array}$ | $\begin{array}{r} 3.00 \\ (0.3) \end{array}$ | . 7546 | 24.00 | 1.31 |
| 7 | 19.499 | -4.513 $(1.7)$ | $\begin{array}{r} 8.46 \\ (2.1) \end{array}$ | $\begin{aligned} & .1656 \\ & (1.7) \end{aligned}$ |  |  |  |  | . 7713 | 23.18 | 1.30 |
| 8 | 39.415 | $\begin{array}{r} -11.56 \\ (2.2) \end{array}$ | $\begin{array}{r} 8.64 \\ (2.1) \end{array}$ | $\begin{aligned} & .1741 \\ & (1.8) \end{aligned}$ |  | $\begin{array}{r} -25.86 \\ (1.7) \end{array}$ | $\begin{array}{r} 0.73 \\ (0.1) \end{array}$ | $\begin{aligned} & 1.34 \\ & (0.1) \end{aligned}$ | . 7704 | 23.22 | 1.42 |
| 9 | 30.576 | $\begin{array}{r} -4.68 \\ (1.8) \end{array}$ | $\begin{array}{r} 6.70 \\ (1.7) \end{array}$ | $\begin{aligned} & .1192 \\ & (1.2) \end{aligned}$ | $\begin{aligned} & 24.70 \\ & (1.7) \end{aligned}$ |  |  |  | . 7829 | 22.58 | 1.59 |
| 10 | 51.534 | $\begin{array}{r} -12.20 \\ (2.4) \\ \hline \end{array}$ | $\begin{array}{r} 6.85 \\ (1.7) \\ \hline \end{array}$ | $\begin{aligned} & .1252 \\ & (1.3) \end{aligned}$ | $\begin{aligned} & 25.73 \\ & (1.8) \\ & \hline \end{aligned}$ | $\begin{array}{r} -26.55 \\ (1.8) \\ \hline \end{array}$ | $\begin{array}{r} 1.91 \\ (0.2) \\ \hline \end{array}$ | $\begin{array}{r} 2.44 \\ (0.2) \\ \hline \end{array}$ | . 7848 | 22.48 | 1.77 |

Figures in parentheses are t-statistics for regression coefficients.
Measures $\mathrm{R}^{2}$ and SE are adjusted for degrees of freedom.
Symbols used:
P - low of high-low range of monthly prices, LE per ton.
$Y$ - middle of this range, LE per ton.
Q - monthly sales, in 1,000 tons.
T - time measured in years from 1971.
I - per capita urban income, LE per year.
S - shift variable indicating average level for 1978-1981 relative to 1972-1977 level.
$X_{1}, X_{2}, X_{3}-$ shift in level for June, July, and August, respectively, relative to September level.

Equation (3) is selected for added discussion. Separate monthly equations are specified by making appropriate changes in the constant term. ${ }^{3}$ These equations are

$$
\begin{aligned}
& Y=56.25-8.60 Q+12.46 T+0.19 I \text { for June } \\
& Y=43.90-8.60 Q+12.46 T+0.19 I \text { for July } \\
& Y=36.22-8.60 Q+12.46 T+0.19 I \text { for August } \\
& Y=22.22-8.60 Q+12.46 T+0.19 I \text { for September }
\end{aligned}
$$

Thus price is related negatively to sales and positively to income. Also the function shifts upward over time and declines as the season advances over the four-month period when grapes are marketed in large volume. About 82 percent of the variance in monthly prices during $1972-1981$ is accounted for by fluctuations in sales and changes in the other variables in the formulation.

## OLS RESULTS FOR POTATOES AND TOMATOES

Income is omitted as an independent variable because only annual data were available when the study was made. Hence the income effect is reflected indirectly, and possibly inaccurately, by the trend factor. This situation must be considered when the results are interpreted.

Only nine of the regression equations computed for potatoes are listed in Table 2. The equations relate price to different combinations of $Q, T, S$, and $X_{i}$. The first three fit $P$ for the entire $1972-1981$ period. The other six fit Y first for the entire period and then for only 1972-1979. Many comparisons can be made among results for these equations.
$3_{\text {This }}$ is done by substituting values for the dummy variables: $X_{1}=1$ for June, $X_{2}=1$ for July, $X_{3}=1$ for August, and $X_{1}, X_{2}, X_{3}=0$ otherwise.

TABLE 2: Potato Prices at El Nozha Market in Alexandria Regression Analysis of Monthly Data, 1972-1981

| Eqn: | Constant | Regression Coefficient |  |  |  | Supplemental Measure |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Q | T | S | X | $\mathrm{R}^{2}$ | SE | DW |
| P as dependent variable, 1972-1981 |  |  |  |  |  |  |  |  |
| 1 | 25.346 | $\begin{array}{r} -.2571 \\ (2.3) \end{array}$ | $\begin{aligned} & .5772 \\ & (15.6) \end{aligned}$ |  | a/ | . 7710 | 13.06 | 1.07 |
| 2 | 25.854 | $\begin{array}{r} -.2551 \\ (2.3) \end{array}$ | $\begin{aligned} & .5561 \\ & (8.1) \end{aligned}$ | $\begin{aligned} & 1.726 \\ & (0.4) \end{aligned}$ | a/ | . 7692 | 13.11 | 1.07 |
| 3 | 17.834 | $\begin{array}{r} -.1349 \\ (2.2) \end{array}$ | $\begin{aligned} & 6470 \\ & (7.0) \end{aligned}$ | $\begin{array}{r} -4.527 \\ (0.7) \end{array}$ |  | . 5449 | 18.41 | 0.70 |
| $\underline{Y}$ as dependent variable, 1972-1981 |  |  |  |  |  |  |  |  |
| 4 | 34.297 | $\begin{array}{r} -.3154 \\ (3.6) \end{array}$ | $\begin{aligned} & .7206 \\ & (24.2) \end{aligned}$ |  | a/ | . 8790 | 10.49 | 0.85 |
| 5 | 34.473 | $\begin{array}{r} -.3148 \\ (3.5) \end{array}$ | $\begin{aligned} & .7133 \\ & (13.0) \end{aligned}$ | $\begin{array}{r} .597 \\ (0.2) \end{array}$ | a/ | . 8779 | 10.54 | 0.85 |
| 6 | 24.228 | $\begin{array}{r} -.1281 \\ (2.3) \end{array}$ | $\begin{array}{r} .7942 \\ (9.2) \end{array}$ | $\begin{array}{r} -5.490 \\ (0.9) \end{array}$ |  | . 6794 | 17.08 | 0.56 |
| $\underline{\mathrm{Y}}$ as dependent variable, 1972-1979 |  |  |  |  |  |  |  |  |
| 7 | 30.167 | $\begin{gathered} -.1885 \\ (1.7) \end{gathered}$ | $\begin{gathered} .7007 \\ (17.0) \end{gathered}$ |  | a/ | . 8332 | 10.31 | 0.73 |
| 8 | 30.534 | $\begin{gathered} -.1840 \\ (1.7) \end{gathered}$ | $\begin{aligned} & .6812 \\ & (11.0) \end{aligned}$ | $\begin{aligned} & 1.588 \\ & (0.4) \end{aligned}$ | a/ | . 8316 | 10.36 | 0.73 |
| 9 | 24.356 | $\begin{array}{r} -.0982 \\ (1.7) \\ \hline \end{array}$ | $\begin{array}{r} .7586 \\ (8.6) \\ \hline \end{array}$ | $\begin{array}{r} -2.591 \\ (0.5) \\ \hline \end{array}$ |  | . 6167 | 15.63 | 0.53 |

Figures in parentheses are t-statistics for regression coefficients. Measures $R^{2}$ and $S E$ are adjusted for degrees of freedom. Q - monthly sales, in 100 tons.
$\mathrm{P}, \mathrm{Y}, \mathrm{S}$ - have same meanings as indicated for Table 1.
$X$ - shifts in monthly levels from average annual level.
a/ - Monthly shifts were computed for these equations. The following values for equations (1) and (4) are similar to those for other equations.

| Month | Equation 1 | Equation 4 | Month | Equation 1 | Equation 4 |
| :--- | :--- | :--- | :--- | ---: | ---: |
|  |  |  |  |  |  |
| Jan | -7.79 | -11.20 | July | -3.81 | -0.64 |
| Feb | -14.73 | -14.64 | Aug | 6.14 | 3.54 |
| Mar | -12.83 | -10.59 | Sept | 19.44 | 14.29 |
| Apr | -12.07 | -10.46 | Oct. | 20.09 | 24.08 |
| May | -14.11 | -14.09 | Nov | 24.61 | 30.41 |
| June | -8.05 | -10.82 | Dec | 3.11 | 0.07 |

Examination of the tabulation leads to several conclusions. The shift variable $S$ is not significant statistically since values for its t-statistic vary from 0.2 to 0.9. Hence, adding $S$ to the formulation does not change very much the net regression coefficients for $Q$ and $T$. It reduces slightly the adjusted value of $R^{2}$. On the other hand, introducing dummy variables for the months improves the fit considerably. Comparing the last two equations in each group of three shows that the $R^{2}$ value is raised by a third. Also, values for regression coefficients are doubled for $Q$ and decreased 10 percent for $T$.

The monthly shifts in the price-quantity function are large and form a definite pattern. These shifts for equations (1) and (4) are shown in the footnote to Table 2. The shift is down by about LE 13 per ton during February-May and up by about LE 22 for September-November.

Table 3 lists results for the same nine equations fitted to the tomato data. Generally, the changes are similar, though smaller in magnitude, to those computed for potatoes. Using the shift variable $S$ is more significant, particularly in equations (2) and (8). In these two equations, its inclusion increases the net regression coefficient of $T$ by 14 percent but changes the coefficient of $Q$ and the $R^{2}$ value only slightly.

Monthly shifts in the price-quantity function are substantial as for potatoes. However, for tomatoes they do not reveal a strong seasonal pattern. Also, they are not consistent for the two equations listed in the footnote to Table 3.

Among the OLS linear regressions computed, the best fits for both potatoes and tomatoes are the equations relating price to sales, a time trend, and monthly shifts. However, as already mentioned, the monthly changes determined for tomatoes form a somewhat erratic pattern and hence may be

TABLE 3: Tomato Prices at El Nozha Market in Alexandria Regression Analysis of Monthly Data, 1972-1981

| Eqn. | Constant | Regression Coefficient |  |  |  | Supplemental Measure |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Q | T | S | X | $\mathrm{R}^{2}$ | SE | DW |
| $\underline{P}$ as dependent variable, ${ }^{\text {1972-1981 }}$ |  |  |  |  |  |  |  |  |
| 1 | 52.215 | $\begin{aligned} & -5.753 \\ & (7.4) \end{aligned}$ | $\begin{aligned} & .5216 \\ & (14.5) \end{aligned}$ |  | a/ | . 7438 | 13.36 | 1.48 |
| 2 | 49.367 | $\begin{gathered} -5.702 \\ (7.4) \end{gathered}$ | $\begin{aligned} & .6114 \\ & (9.1) \end{aligned}$ | $\begin{aligned} & -7.444 \\ & (1.6) \end{aligned}$ | a/ | . 7473 | 13.23 | 1.50 |
| 3 | 62.247 | $\begin{array}{r} 7.306 \\ (12.8) \end{array}$ | $\begin{aligned} & .5924 \\ & (8.6) \end{aligned}$ | $\begin{aligned} & -5.317 \\ & (1.1) \end{aligned}$ |  | . 7261 | 13.81 | 1.57 |
| $\underline{Y}$ as dependent variable, 1972-1981 |  |  |  |  |  |  |  |  |
| 4 | 100.847 | $\begin{gathered} -11.069 \\ (7.8) \end{gathered}$ | $\begin{aligned} & .8267 \\ & (12.5) \end{aligned}$ |  | a/ | . 6764 | 24.50 | 1.18 |
| 5 | 100.462 | $\begin{gathered} -11.061 \\ (7.7) \end{gathered}$ | $\begin{aligned} & 8409 \\ & (6.7) \end{aligned}$ | $\begin{aligned} & -1.175 \\ & (0.1) \end{aligned}$ | a/ | . 6734 | 24.61 | 1.18 |
| 6 | 101.217 | $\begin{array}{r} -11.020 \\ (10.2) \end{array}$ | $\begin{aligned} & .8117 \\ & (6.2) \end{aligned}$ | $\begin{aligned} & 0.553 \\ & (0.1) \end{aligned}$ |  | . 6338 | 26.06 | 1.34 |
| $\underline{Y}$ as dependent variable, 1972-1979 |  |  |  |  |  |  |  |  |
| 7 | 78.684 | $\begin{gathered} -7.126 \\ (9.2) \end{gathered}$ | $\begin{aligned} & .6010 \\ & (13.1) \end{aligned}$ |  | a/ | . 7551 | 10.92 | 1.28 |
| 8 | 76.382 | $\begin{gathered} -7.067 \\ (9.2) \end{gathered}$ | $\begin{gathered} .6690 \\ (10.4) \end{gathered}$ | $\begin{aligned} & -5.848 \\ & (1.5) \end{aligned}$ |  | . 7588 | 10.84 | 1.30 |
| 9 | 77.924 | $\begin{array}{r} -7.239 \\ (12.1) \\ \hline \end{array}$ | $\begin{array}{r} .6626 \\ (9.5) \\ \hline \end{array}$ | $\begin{aligned} & -5.291 \\ & (1.2) \end{aligned}$ |  | . 6978 | 12.13 | 1.59 |

Figures in parentheses are t-statistics for regression coefficients.
Measures $\mathrm{R}^{2}$ and $S E$ are adjusted for degrees of freedom.
Q - monthly sales, in 100 tons.
$\mathrm{P}, \mathrm{Y}, \mathrm{S}$ - have same meanings as indicated for Table 1.
$X$ - shifts in monthly levels from average annual level.
a/ - Monthly shifts were computed for these equations. The following values for equations (1) and (4) are representative of shifts for other equations.

| Month | Equation 1 | Equation 4 | Month | Equation 1 | Equation 4 |
| :--- | ---: | ---: | :--- | ---: | ---: |
|  |  |  |  |  |  |
| Jan | 2.79 | 1.47 | July | -5.91 | -3.86 |
| Feb | -0.35 | -10.41 | Aug | -2.52 | 0.47 |
| Mar | 11.20 | 1.23 | Sept | -5.63 | -8.31 |
| Apr | 13.90 | 9.16 | Oct | 0.08 | 3.94 |
| May | -1.69 | 30.94 | Nov | -7.23 | -13.66 |
| June | -5.45 | -8.49 | Dec | 0.81 | -2.48 |

difficult to interpret. Values for the Durbin-Watson statistic are low for all 18 equations. Therefore, autoregressive equations are computed in order to obtain more efficient estimators for the structural parameters.

## AUTOREGRESSION

A first order autoregressive model is used to correct for the high autocorrelation remaining among the residuals for all equations given in Tables 2 and 3. Examination of the input data presented in Tables $B$ and $C$ reveals substantially higher prices during the later years of 1972-1981. Hence, the decade is divided into two subperiods of four years: 1972-1975 and 1978-1981.4 The same linear equation, with $Y$ as the dependent variable, is fitted for each period:

$$
Y=A+B_{1} Q+B_{2} T+\sum C_{i} X_{i}
$$

This formulation is selected because $Q, T$, and $X_{i}$ are the most important variables in the OLS equations. Each OLS equation is recomputed after adding the autoregressive coefficient rho. Thus, there are four equations for potatoes and four for tomatoes. The computed results appear in Table 4.

The last column in the table indicates a sharp increase in Durbin-Watson values, to almost 2.0 for the autoregressive equations. This means that the existence of positive autocorrelation among residuals in OLS equations can be replaced by the assumption of zero autocorrelation.
${ }^{4}$ For the major variables, 1972-1975 and 1978-1981 averages are:

| Average | Potatoes |  |  | Tomatoes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | P | Y | Q | P | Y | Q |
| 1978-1982 | 69.58 | 89.52 | 4568.23 | 54.06 | 89.54 | 821.71 |
| 1972-1975 | 30.10 | 39.08 | 3720.10 | 23.77 | 41.90 | 680.10 |

TABLE 4: OLS and Autoregressive Results for Potatoes and Tomatoes El Nozha Market, Alexandria, Monthly Data 1972-1975 and 1978-1981 Median price (Y) as dependent variable

| Eqn.a Constant | Regression Coefficient ${ }^{\text {b }}$ |  |  | Supplemental Measures |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Q | T | $\rho$ | $\mathrm{R}^{2}$ | SE | DW |
| Potatoes, 1972-1975 |  |  |  |  |  |  |
| $11 \quad 41.102$ | $-\begin{array}{r} .4169 \\ (2.4) \end{array}$ | $\begin{aligned} & 0.566 \\ & (6.6) \end{aligned}$ |  | . 7565 | 7.55 | 0.82 |
| $11 \mathrm{~A} \quad 25.680$ | $-\quad .0466$ | $\begin{aligned} & 0.584 \\ & (2.4) \end{aligned}$ | $\begin{aligned} & 0.773 \\ & (8.4) \end{aligned}$ | . 6309 | 4.98 | 1.80 |
| Potatoes, 1978-1981 |  |  |  |  |  |  |
| $12 \quad 31.697$ | $-\quad .4378$ | $\begin{aligned} & 0.806 \\ & (7.5) \end{aligned}$ |  | . 8332 | 9.94 | 1.18 |
| 12A 25.376 | $\begin{array}{r} -\quad .3709 \\ (3.2) \end{array}$ | $\begin{aligned} & 0.849 \\ & (4.8) \end{aligned}$ | $\begin{aligned} & 0.420 \\ & (3.2) \end{aligned}$ | . 7338 | 9.12 | 1.99 |
| Tomatoes, 1972-1975 |  |  |  |  |  |  |
| $11 \quad 63.896$ | $\begin{array}{r} -5.2313 \\ (4.2) \end{array}$ | $\begin{aligned} & 0.661 \\ & (5.8) \end{aligned}$ |  | . 7496 | 9.84 | 1.29 |
| 11A 59.995 | $\begin{array}{r} -4.3777 \\ (3.7) \end{array}$ | $\begin{aligned} & 0.584 \\ & (3.5) \end{aligned}$ | $\begin{aligned} & 0.366 \\ & (2.7) \end{aligned}$ | . 7205 | 9.13 | 1.96 |
| Tomatoes, 1978-1981 |  |  |  |  |  |  |
| $12 \quad 169.198$ | $\begin{array}{r} -17.2980 \\ (4.1) \end{array}$ | $\begin{aligned} & 0.751 \\ & (1.7) \end{aligned}$ |  | . 6131 | 33.81 | 1.21 |
| $12 \mathrm{~A} \quad 143.21$ | $\begin{array}{r} -16.1340 \\ (4.1) \\ \hline \end{array}$ | $\begin{aligned} & 0.820 \\ & (1.3) \end{aligned}$ | $\begin{aligned} & 0.401 \\ & (3.0) \\ & \hline \end{aligned}$ | . 5525 | 31.46 | 1.90 |

Note: See Tables 2 and 3 for symbols used.
$a_{\text {Equations ( }}$ (11) and (12) are OLS; equations (11A) and (12A) are for the autoregressive model.
$b_{\text {All }}$ equations include dummy variables to indicate monthly shifts from annual levels. Shifts for equations (12) and (12A) are:

|  | Potatoes |  | Tomatoes |  |
| :---: | :---: | :---: | :---: | ---: |
| Month | Equation 12 | Equation 12A | Equation 12 | Equation 12A |
| Jan | -14.14 | -15.49 | 5.65 | -15.06 |
| Feb | -22.50 | -22.96 | -14.21 |  |
| Mar | -13.53 | -13.31 | -11.23 | -9.28 |
| Apr | -12.37 | -12.19 | 13.81 | 19.23 |
| May | -19.47 | -19.36 | 59.08 | 57.49 |
| June | -11.21 | -9.46 | 4.44 | 2.09 |
| July | 1.47 | 3.69 | 3.33 | 0.80 |
| Aug | -3.73 | -1.24 | -2.62 | -3.93 |
| Sept | 16.45 | 19.21 | -17.36 | -17.38 |
| Oct | 34.16 | 32.65 | -13.40 | -13.12 |
| Nov | 42.33 | 37.30 | -23.19 | -23.36 |
| Dec | 2.54 | 1.16 | -2.45 | -3.60 |

Introducing the coefficient rho into the formulation also reduces the standard error--sharply for the first equation pair and much less for the other three pairs. This means that the predictive accuracy is improved. However, the tabulated $\mathrm{R}^{2}$ values are lower in each case. How can this be the case? This apparent contradiction is due to the method used for computing the values.

The equation pairs for tomatoes is used to illustrate the computation of the $R^{2}$ listed in the table to a possible alternative method. The three $R^{2}$ values are determined similarly. The variance unexplained by the equation is compared with the variance in the dependent variable. The latter variance may be computed with reference to the actual values of Y for (11) or with reference to the rho-transformed values of $Y$ for (11A). Then, of course, $R^{2}$ values differ. Specifically, the three values for tomatoes are determined as follows:

|  | Equation (11) | Equation (11A) | Alternative |
| :--- | :---: | :---: | :---: |
| Original $\mathrm{SD}^{2}$ | 386.44 |  | 386.44 |
| Transformed $\mathrm{SD}^{2}$ |  | 298.22 |  |
| $\mathrm{SE}^{2}$ | 96.68 | 83.36 | 83.36 |
| Difference | 289.66 | 214.86 | 303.08 |
| $\mathrm{R}^{2}$ | .7496 | .7205 | .7843 |

Which of the latter two values is appropriate depends on how the researcher will interpret and use the results. The two $R^{2}$ values from Table 4 together with $\mathrm{R}^{2}$ computed in the alternate way are as follows:.

|  | Potatoes |  | Tomatoes |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $1972-1977$ | $1978-1982$ | $1972-1977$ | $1978-1982$ |
| OLS | .7565 | .8332 | .7496 | .6131 |
| Autoregressive | .6309 | .7338 | .7205 | .5525 |
| Alternative | .8942 | .8585 | .7843 | .6682 |

Of course, the alterative $R^{2}$ is greater than $R^{2}$ for the OLS equation because the standard error is reduced by the introduction of rho into the formulation.

The monthly shifts in the price-quantity function for the 1978-1981 period are listed in the footnote to Table 4. For both potatoes and for tomatoes, the shifts in equation (12) follow a definite pattern and are similar to those in equation (12A). The average shift for potatoes is down LE 17 per ton in February-May and up LE 30 during September-November. For tomatoes, the shift ranges from plus LE 37 per ton in April-May to minus LE 18 during September-November.

## CONCLUS ION

The computed linear OLS regressions are good fits to the monthly data. Several have $\mathrm{R}^{2}$ values in the 0.75 to 0.88 range. They clearly indicate an empirical price-quantity relationship which is subject to parallel shifts on a month-to-month basis and to an upward trend over time. These results say something about how the price mechanism operates on the El Nozha market. They provide unbiased estimates for net regression coefficients. These OLS equations are satisfactory for making predictions providing the underlying market conditions do not change materially.

Residuals from the OLS equations computed for potatoes and tomatoes have high positive autocorrelation. More efficient estimators of the structural
parameters are determined by using a first order autoregressive model. These values are better than the OLS estimates for some purposes--e.g., for computing elasticity coefficients. The OLS equations for grapes do not give evidence of autocorrelation. Hence, autoregressive equations are not needed.

Results might be improved by modifying the formulations. For example, introducing consumer income as a variable in equations for grapes reduces substantially the trend effect. This factor is omitted from equations for potatoes and tomatoes merely because only annual information was available for this analysis. It would be better to include income explicitly as a separate variable, rather than have its effect enter indirectly by the trend factor. Monthly estimates should be used if they can be derived from available data.

Values for monthly shifts in the price-quantity function indicate definite seasonal patterns. These may be related to short-time changes in consumer preferences, in varieties or qualities marketed, or in other factors. If so, the net influence of sales, trend, etc. may be different for various subperiods of a year. This could be tested by computing separate equations for two or three periods of months, e.g., for January-June and July-December in the case of potatoes. Possibly temporal markets are interrelated. That is, the influence of quantity on price may be due both to current sales and the quantity sold during the preceding month. In that case, lagged sales should appear as a separate independent variable in the formulation.

Some researchers prefer to determine equations with quantity as the dependent variable instead of price as used in this study. This can be done. The results will be different and better for some purposes, such as computing the elasticity of demand. However, care must be exercised to avoid introducing multicollinearity if income and price are highly correlated.

Theoretically, some economic relationships are curvilinear. Linear functions are used for all equations to indicate first approximations to the actual relationships. Introducing curvilinearity into the formulation might reveal whether it is reasonable to use linear functions. For example, some equations might be fitted with a logarithmic or parabolic relationship between price and quantity.

TABLE A: Monthly Input Data for Analysis of Grape Prices E1 Nozha Market, Alexandria, 1972-1981

| Month | 1972 | 1973 | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | Average ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P - Minimum actual price, LE per ton ${ }^{\text {b }}$ |  |  |  |  |  |  |  |  |  |  |  |
| June | 45 | 50 | 60 | 50 | 90 | 100 | 80 | 100 | 200 | 200 | 97.5 |
| July | 40 | 40 | 50 | 70 | 70 | 70 | 100 | 150 | 190 | 120 | 90.0 |
| Aug | 45 | 52 | 50 | 70 | 55 | 70 | 120 | 150 | 190 | 120 | 92.2 |
| Sept | 50 | 55 | 50 | 70 | 55 | 120 | 120 | 140 | 150 |  | 90.0 |
| Aver. | 45.0 | 49.2 | 52.5 | 65.0 | 67.5 | 90.0 | 105.0 | 135.0 | 182.5 | 146.7 | 92.49 |
| Y - Median actual price, LE per ton ${ }^{\text {b }}$ |  |  |  |  |  |  |  |  |  |  |  |
| June | 72 | 85 | 90 | 100 | 145 | 175 | 165 | 200 | 300 | 330 | 166.2 |
| July | 55 | 75 | 85 | 80 | 120 | 160 | 126 | 166 | 208 | 210 | 128.5 |
| Aug | 58 | 61 | 80 | 80 | 78 | 195 | 136 | 166 | 208 | 158 | 122.0 |
| Sept | 60 | 55 | 68 | 80 | 78 | 135 | 120 | 145 | 172 |  | 101.4 |
| Aver. | 61.2 | 69.0 | 80.8 | 85.0 | 105.2 | 166.2 | 136.8 | 169.2 | 222.0 | 236.7 | 130.26 |
| Q - Quantity, sales in tons |  |  |  |  |  |  |  |  |  |  |  |
| June | 272 | 279 | 304 | 334 | 289 | 206 | 353 | 914 | 538 | 731 | 422.0 |
| July | 3418 | 2722 | 4035 | 4095 | 4028 | 3867 | 3906 | 2931 | 2175 | 2523 | 3370.0 |
| Aug | 3224 | 2261 | 3535 | 2607 | 3387 | 3478 | 3836 | 2256 | 2384 | 5360 | 3232.8 |
| Sept | 2007 | 1913 | 2065 | 1792 | 1891 | 1740 | 3834 | 2995 | 4139 |  | 2486.2 |
| Aver. | 2230 | 1794 | 2485 | 2207 | 2399 | 2323 | 2982 | 2274 | 2309 | 2871 | 2374.97 |
| I - Per capita urban income, LE per year |  |  |  |  |  |  |  |  |  |  |  |
| Annual | 107 | 109 | 141 | 160 | 177 | 212 | 253 | 316 | 393 | 503 | 237.1 |

aThe last average in each block is the average of the 39 actual observations average of monthly averages.
$\mathrm{b}_{\mathrm{P}}$ is the low of the high-1ow range of monthly prices; Y is the middle of this range.
Source: Data supplied by Ministry of Agriculture, Egypt.

TABLE B: Monthly Input Data for Analysis of Potato Prices El Nozha Market, Alexandria, 1972-1981

| Month | 1972 | 1973 | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | Average |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | $\underline{P}-\underline{M}$ | mum a | 1 pric | LE per | $\mathrm{n}^{\text {a }}$ |  | . |  |  |  |  |
| Jan | 20 | 13 | 20 | 28 | 30 | 60 | 50 | 65 | 50 | 50 | 38.6 |
| Feb | 18 | 20 | 18 | 20 | 25 | 40 | 25 | 50 | 50 | 50 | 31.6 |
| Mar | 16 | 20 | 15 | 25 | 30 | 30 | 40 | 60 | 50 | 60 | 34.6 |
| Apr | 20 | 18 | 18 | 30 | 40 | 20 | 45 | 50 | 45 | 70 | 35.6 |
| May | 15 | 15 | 15 | 23 | 35 | 25 | 40 | 50 | 40 | 70 | 32.8 |
| June | 18 | 15 | 20 | 25 | 50 | 25 | 80 | 75 | 80 | 70 | 45.8 |
| July | 40 | 15 | 35 | 60 | 50 | 35 | 30 | 100 | 80 | 80 | 52.5 |
| Aug | 45 | 28 | 45 | 68 | 80 | 50 | 30 | 100 | 90 | 100 | 63.6 |
| Sept | 50 | 28 | 55 | 70 | 85 | 50 | 90 | 110 | 120 | 130 | 78.8 |
| Oct | 35 | 40 | 50 | 65 | 60 | 80 | 80 | 85 | 70 | 130 | 69.5 |
| Nov | 20 | 30 | 35 | 50 | 50 | 80 | 70 | 60 | 80 | 110 | 58.5 |
| Dec | 23 | 25 | 35 | 33 | 60 | 70 | 70 | 55 | 75 | 80 | 52.6 |
| Aver. | 26.7 | 22.2 | 30.1 | 41.4 | 49.6 | 47.1 | 54.2 | 71.7 | 69.2 | 83.3 | 49.54 |
|  | Y - | n act | price | per |  |  |  |  |  |  |  |
| Jan | 25 | 23 | 27 | 34 | 35 | 70 | 62 | 78 | 70 | 72 | 49.6 |
| Feb | 26 | 29 | 26 | 28 | 42 | 60 | 38 | 72 | 70 | 70 | 46.1 |
| Mar | 27 | 29 | 24 | 40 | 50 | 48 | 55 | 82 | 80 | 80 | 51.5 |
| Apr | 29 | 28 | 24 | 48 | 55 | 36 | 62 | 75 | 78 | 85 | 52.0 |
| May | 24 | 24 | 24 | 39 | 52 | 39 | 60 | 65 | 65 | 82 | 47.4 |
| June | 30 | 24 | 32 | 45 | 68 | 42 | 85 | 88 | 90 | 88 | 59.2 |
| July | 44 | 26 | 41 | 65 | 68 | 62 | 75 | 105 | 100 | 138 | 72.4 |
| Aug | 48 | 32 | 52 | 73 | 92 | 75 | 75 | 105 | 108 | 120 | 78.0 |
| Sept | 58 | 42 | 61 | 80 | 95 | 75 | 105 | 120 | 130 | 145 | 91.1 |
| Oct | 50 | 52 | 60 | 72 | 100 | 90 | 105 | 108 | 105 | 145 | 88.7 |
| Nov | 34 | 38 | 50 | 65 | 70 | 95 | 98 | 85 | 85 | 140 | 76.0 |
| Dec | 26 | 31 | 42 | 44 | 72 | 85 | 85 | 68 | 90 | 105 | 64.8 |
| Aver. | 35.1 | 31.5 | 38.6 | 52.7 | 66.6 | 64.8 | 75.4 | 87.6 | 89.2 | 105.8 | 64.73 |
|  | 1-9 | 1ty, | $s$ in |  |  |  |  |  |  |  |  |
| Jan | 3304 | 3493 | 3475 | 4438 | 4029 | 4201 | 4627 | 4429 | 4892 | 4730 | 4162 |
| Feb | 3393 | 3414 | 4884 | 4279 | 4386 | 4643 | 5416 | 3836 | 4749 | 5090 | 4409 |
| Mar | 3208 | 3748 | 4788 | 4509 | 3896 | 4652 | 4059 | 3752 | 4530 | 4943 | 4208 |
| Apr | 3153 | 4397 | 4833 | 3983 | 4037 | 4582 | 3735 | 5257 | 4982 | 4419 | 4338 |
| May | 4091 | 4868 | 5285 | 4467 | 5766 | 5066 | 4591 | 5433 | 4735 | 4282 | 4858 |
| June | 1609 | 2265 | 2594. | 2536 | 2022 | 3511 | 1204 | 2279 | 2677 | 3123 | 2382 |
| July | 1420 | 2197 | 1998 | 1552 | 1007 | 2041 | 448 | 2083 | 2167 | 1603 | 1652 |
| Aug | 1282 | 2269 | 1549 | 1435 | 1230 | 1977 | 713 | 1204 | 1220 | 1433 | 1431 |
| Sept | 654 | 1421 | 1285 | 1085 | 755 | 1205 | 290 | 758 | 697 | 982 | 913 |
| Oct | 4519 | 2196 | 1542 | 3220 | 4451 | 6059 | 3742 | 10248 | 9357 | 4750 | 5008 |
| Nov | 7560 | 11203 | 9956 | 10602 | 12757 | 11763 | 12387 | 12722 | 15583 | 8166 | 11270 |
| Dec | 4815 | 4909 | 4516 | 4366 | 3951 | 4772 | 6753 | 6754 | 6630 | 6815 | 5428 |
| Aver. | 3251 | 3865 | 3892 | 3873 | 4024 | 4539 | 3997 | 4896 | 5185 | 4195 | 4171.7 |

ap is the low of the high-low range of monthly prices; $Y$ is the middle of this range.
Source: Data supplied by Ministry of Agriculture, Egypt.

TABLE C: Monthly Input Data for Analysis of Tomato Prices El Nozha Market, Alexandria, 1972-1981

| Month | 1972 | 1973 | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | Average |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | P- Minimum actual price, LE per ton ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |  |  |
| Jan | 15 | 25 | 40 | 35 | 25 | 50 | 20 | 40 | 50 | 70 | 37.0 |
| Feb | 15 | 20 | 30 | 40 | 25 | 35 | 20 | 60 | 60 | 90 | 39.5 |
| Mar | 20 | 60 | 30 | 40 | 45 | 30 | 35 | 85 | 100 | 100 | 54.5 |
| Apr | 35 | 55 | 70 | 50 | 70 | 45 | 70 | 60 | 130 | 180 | 76.5 |
| May | 10 | 15 | 20 | 8 | 25 | 30 | 20 | 50 | 40 | 60 | 27.8 |
| June | 10 | 15 | 20 | 20 | 40 | 25 | 20 | 30 | 40 | 60 | 28.0 |
| July | 10 | 15 | 20 | 15 | 20 | 30 | 20 | 25 | 50 | 40 | 24.5 |
| Aug | 10 | 13 | 20 | 10 | 30 | 60 | 50 | 30 | 30 | 35 | 28.8 |
| Sept | 13 | 25 | 25 | 20 | 20 | 80 | 25 | 50 | 40 | 60 | 35.8 |
| Oct | 15 | 7 | 20 | 25 | 20 | 50 | 20 | 50 | 50 | 100 | 35.7 |
| Nov | 10 | 10 | 25 | 20 | 25 | 30 | 40 | 50 | 40 | 80 | 33.0 |
| Dec | 20 | 30 | 40 | 25 | 50 | 40 | 30 | 50 | 60 | 80 | 42.5 |
| Aver. | 15.2 | 24.2 | 30.0 | 25.7 | 32.9 | 42.1 | 30.8 | 48.3 | 57.5 | 79.6 | 38.63 . |
|  | $\underline{\text { - Median actual price, LE per ton }}$ |  |  |  |  |  |  |  |  |  |  |
| Jan | 22 | 52 | 52 | 52 | 40 | 67 | 50 | 60 | 85 | 100 | 58.0 |
| Feb | 22 | 42 | 55 | 60 | 45 | 52 | 35 | 72 | 70 | 115 | 56.8 |
| Mar | 30 | 80 | 65 | 60 | 60 | 52 | 52 | 95 | 115 | 140 | 74.9 |
| Apr | 60 | 90 | 98 | 75 | 90 | 60 | 102 | 88 | 315 | 220 | 119.8 |
| May | 32 | 32 | 72 | 19 | 72 | 50 | 50 | 75 | 270 | 105 | 77.7 |
| June | 19 | 22 | 34 | 35 | 62 | 40 | 40 | 50 | 60 | 95 | 45.7 |
| July | 16 | 22 | 32 | 38 | 40 | 58 | 35 | 32 | 110 | 60 | 44.3 |
| Aug | 16 | 18 | 35 | 20 | 40 | 80 | 75 | 50 | 90 | 78 | 50.2 |
| Sept | 30 | 45 | 44 | 40 | 35 | 95 | 58 | 90 | 75 | 95 | 60.7 |
| Oct | 38 | 24 | 40 | 48 | 25 | 82 | 32 | 105 | 100 | 122 | 61.6 |
| Nov | 20 | 30 | 40 | 42 | 40 | 55 | 55 | 75 | 60 | 110 | 52.7 |
| Dec | 35 | 50 | 60 | 48 | 82 | 58 | 55 | 85 | 82 | 110 | 66.5 |
| Aver. | 28.3 | 42.2 | 52.2 | 44.8 | 52.6 | 62.4 | 53.2 | 73.1 | 119.3 | 112.5 | 64.08 |
|  | Q- Quantity, sales in tons |  |  |  |  |  |  |  |  |  |  |
| Jan | 674 | 537 | 586 | 792 | 999 | 865 | 953 | 948 | 951 | 812 | 811.7 |
| Feb | 692 | 467 | 433 | 744 | 880 | 768 | 919 | 768 | 760 | 796 | 722.7 |
| Mar | 672 | 397 | 600 | 625 | 838 | 873 | 647 | 740 | 672 | 654 | 671.8 |
| Apr | 295 | 199 | 299 | 217 | 303 | 698 | 416 | 832 | 95 | 99 | 345.3 |
| May | 1040 | 1073 | 713 | 990 | 666 | 1010 | 1157 | 1183 | 761 | 706 | 929.9 |
| June | 656 | 881 | 784 | 972 | 600 | 774 | 1242 | 940 | 961 | 892 | 870.2 |
| July | 742 | 904 | 882 | 960 | 877 | 884 | 1114 | 1144 | 867 | 948 | 932.2 |
| Aug | 775 | 925 | 834 | 1161 | 1058 | 872 | 929 | 983 | 922 | 795 | 925.4 |
| Sept | 529 | 658 | 809 | 877 | 1064 | 489 | 988 | 747 | 825 | 601 | 758.7 |
| Oct | 810 | 1275 | 885 | 853 | 1089 | 743 | 1079 | 642 | 692 | 620 | 868.8 |
| Nov | 752 | 683 | 726 | 839 | 867 | 944 | 742 | 874 | 890 | 659 | 797.6 |
| Dec | 640 | 622 | 642 | 924 | 586 | 923 | 878 | 836 | 944 | 819 | 781.4 |
| Aver. | 689.8 | 718.4 | 682.8 | 829.5 | 818.9 | 820.2 | 922.0 | 886.4 | 778.3 | 700.1 | 784.64 |

ap is the low of the high-low range of monthly prices; $Y$ is the middle of this range.
Source: Data supplied by Ministry of Agriculture, Egypt.

