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Stata tip 115: How to properly estimate the multinomial probit model with heteroskedastic errors

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Models for multinomial outcomes are frequently used to analyze individual decision making in consumer research, labor market research, voting, and other areas. The multinomial probit model provides a flexible approach to analyzing decisions in these fields because it does not impose some of the restrictive assumptions inherent in the often used conditional logit approach. In particular, multinomial probit relaxes 1) the assumption of independent error terms, allowing for correlation in individual choices across alternatives, and 2) it does not impose the assumption of identically distributed errors, allowing unobserved factors to affect the choice of some alternatives more strongly than others (that is, heteroskedasticity).

By default, `asmprobit` relaxes both the assumptions of independence and homoskedasticity. To avoid overfitting, however, the researcher may sometimes wish to relax these assumptions one at a time.¹ A seemingly straightforward solution would be to rely on the options `stddev()` and `correlation()`, which allow the user to set the structure for the error variances and their covariances, respectively (see [R] `asmprobit`).

When doing so, however, the user should be aware that specifying `std(het)` and `corr(ind)` does not actually fit a pure heteroskedastic multinomial probit model. With J outcome categories, if errors are independent, $J - 1$ error variances are identified (see below). Instead, Stata estimates $J - 2$ error variances and, hence, imposes an additional constraint, which causes the model to be overidentified. As a result, the estimated model is not invariant to the choice of base and scale outcomes; that is, changing the base or scale outcome leads to different values of the likelihood function.

To properly estimate a pure heteroskedastic model, the user needs to define the structure of the error variances manually. This is easy to accomplish using the `pattern` or `fixed` option. The following example illustrates the problem and shows how to estimate the model correctly.

1. Another reason to relax them one at a time is that heteroskedasticity and error correlation cannot be distinguished from each other in the default specification. That is, one cannot simply look at the estimated covariance matrix of the errors and see whether the errors are heteroskedastic, correlated, or both. What Stata estimates is the normalized covariance matrix of error differences whose elements do not allow one to draw any conclusions on the covariance structure of the errors themselves.

Consider an individual's choice of travel mode with the alternatives being air, train, bus, and car and predictor variables, including general cost of travel, terminal time, household income, and traveling group size. One might suspect the choice of some alternatives to be driven more by unobserved factors than the choice of others. For example, there might be more unobserved reasons related to an individual's decision to travel by plane than by train, bus, or car. Allowing the error variances associated with the alternatives to differ, we fit the following model:

```
. use http://www.stata-press.com/data/r12/travel
. asmpbchoice travelcost termtime, casevars(income partysize)
> case(id) alternatives(mode) std(het) corr(ind) nolog

Alternative-specific multinomial probit      Number of obs      =      840
Case variable: id                          Number of cases     =      210
Alternative variable: mode                  Alts per case: min  =       4
                                              avg                =      4.0
                                              max                =       4

Integration sequence:      Hammersley
Integration points:        200
Log simulated-likelihood = -181.81521      Wald chi2(8)        =      71.57
                                              Prob > chi2         =      0.0000
```

choice	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
mode						
travelcost	-.012028	.0030838	-3.90	0.000	-.0180723	-.0059838
termtime	-.050713	.0071117	-7.13	0.000	-.0646517	-.0367743
air	(base alternative)					
train						
income	-.03859	.0093287	-4.14	0.000	-.0568739	-.0203062
partysize	.7590228	.190438	3.99	0.000	.3857711	1.132274
_cons	-.9960951	.4750053	-2.10	0.036	-1.927088	-.0651019
bus						
income	-.0119789	.0081057	-1.48	0.139	-.0278658	.003908
partysize	.5876645	.1751734	3.35	0.001	.2443309	.930998
_cons	-1.629348	.4803384	-3.39	0.001	-2.570794	-.6879016
car						
income	-.004147	.0078971	-0.53	0.599	-.019625	.011331
partysize	.5737318	.163719	3.50	0.000	.2528485	.8946151
_cons	-3.903084	.750675	-5.20	0.000	-5.37438	-2.431788
/lnsigmaP1	-1.097572	.7967201	-1.38	0.168	-2.659115	.4639704
/lnsigmaP2	-.3906271	.3468426	-1.13	0.260	-1.070426	.2891719
sigma1	1	(base alternative)				
sigma2	1	(scale alternative)				
sigma3	.3336802	.2658497			.0700102	1.590376
sigma4	.6766324	.2346849			.3428624	1.335321

(mode=air is the alternative normalizing location)

(mode=train is the alternative normalizing scale)

As can be seen, two of the four error variances are set to one. These are the base and scale alternatives. While choosing a base and scale alternative is necessary to identify the model, the problem here is that because errors are uncorrelated, fixing the variance of the base alternative is not necessary to identify the model. As a result, an additional constraint is imposed, which leads to a different model structure depending on the choice of base and scale alternatives. For example, changing the base alternative to car produces a different log likelihood:

```
. quietly asmprobit choice travelcost termtime, casevars(income partysize)
> case(id) alternatives(mode) std(het) corr(ind) nolog base(4)
. display e(11)
-181.58795
```

To properly estimate an unconstrained heteroskedastic model, one needs to define a vector of variance terms in which one element (the scale alternative) is fixed and pass this vector on to the estimation command. For example, to set the error variance of the second alternative to unity, define a vector of missing values, `stdpat`, whose second element is 1, and then call this vector from inside `asmprobit` using the option `std(fixed)` (see [R] `asmprobit` for details):

```

. matrix define stdpat = (.,1,...)
. asmprobit choice travelcost termtime, casevars(income partysize)
> case(id) alternatives(mode) std(fixed stdpat) corr(ind) nolog base(1)

Alternative-specific multinomial probit      Number of obs      =      840
Case variable: id                          Number of cases      =      210
Alternative variable: mode                  Alts per case: min   =        4
                                           avg                 =       4.0
                                           max                 =        4

Integration sequence:      Hammersley
Integration points:        200
Log simulated-likelihood = -180.01839      Wald chi2(8)         =      26.84
                                           Prob > chi2          =      0.0008

```

choice	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]		
mode							
travelcost	-.0196389	.0067143	-2.92	0.003	-.0327988	-.006479	
termtime	-.0664153	.0140353	-4.73	0.000	-.093924	-.0389065	
air							
(base alternative)							
train							
income	-.0498732	.0154884	-3.22	0.001	-.08023	-.0195165	
partysize	1.126922	.3651321	3.09	0.002	.4112761	1.842568	
_cons	-1.072849	.680711	-1.58	0.115	-2.407018	.2613198	
bus							
income	-.0210642	.0139892	-1.51	0.132	-.0484826	.0063542	
partysize	.8678651	.3179559	2.73	0.006	.244683	1.491047	
_cons	-1.831363	.7345686	-2.49	0.013	-3.271091	-.3916349	
car							
income	-.010205	.0131711	-0.77	0.438	-.0360199	.01561	
partysize	.8708577	.3202671	2.72	0.007	.2431458	1.49857	
_cons	-4.971594	1.261002	-3.94	0.000	-7.443112	-2.500075	
/lnsigmaP1	.558377	.3076004	1.82	0.069	-.0445087	1.161263	
/lnsigmaP2	-1.0078	1.116358	-0.90	0.367	-3.195822	1.180223	
/lnsigmaP3	-.0158072	.3593511	-0.04	0.965	-.7201225	.6885081	
sigma1	1.747833	.5376342			.9564673	3.193964	
sigma2	1	(scale alternative)					
sigma3	.3650213	.4074946			.0409329	3.255099	
sigma4	.9843171	.3537155			.4866926	1.990743	

(mode=air is the alternative normalizing location)

(mode=train is the alternative normalizing scale)

Now the model is properly normalized, and the user may verify that changing either the scale alternative (that is, changing the location of the 1 in `stdpat`) or the base alternative leaves results unchanged. Note that while, in theory, the only restriction necessary to identify the heteroskedastic probit model is to fix one of the variance terms, in the Stata implementation of the model, the base and scale outcomes must be different. That is, Stata does not allow the same alternative to be the base outcome and the scale outcome. However, this is more of an inconvenience than a restriction: such a model would be equivalent to one in which the base and scale outcomes differed.

Finally, to show that independence of errors indeed implies $J - 1$ estimable error variances, we must verify that the error variances can be calculated directly from the variance and covariance parameters of the normalized error differences. Only the latter are identified and, hence, estimable (Train 2009). Suppose, without loss of generality, $J = 3$, and let $j = 1$ be the base outcome.

Following the normalization approach advocated by Train (2009, 100f.), the normalized covariance matrix of error differences is given by

$$\tilde{\Omega}_1^* = \begin{pmatrix} 1 & \theta_{23}^* \\ & \theta_{33}^* \end{pmatrix}$$

with elements θ^* relating to the actual error variances σ_{jj} and covariances σ_{ij} as follows:

$$\begin{aligned} \theta_{23}^* &= \frac{\sigma_{23} + \sigma_{11} - \sigma_{12} - \sigma_{13}}{\sigma_{22} + \sigma_{11} - 2\sigma_{12}} \\ \theta_{33}^* &= \frac{\sigma_{33} + \sigma_{11} - 2\sigma_{13}}{\sigma_{22} + \sigma_{11} - 2\sigma_{12}} \end{aligned}$$

Under independence, $\sigma_{ij} = 0$. Fixing $\sigma_{22} = 1$ (that is, choosing $j = 2$ as the scale outcome) yields $\theta_{23}^* = \sigma_{11}/(1 + \sigma_{11})$ and $\theta_{33}^* = (\sigma_{33} + \sigma_{11})/(1 + \sigma_{11})$. Obviously, σ_{11} can be calculated from θ_{23}^* , and subsequent substitution produces σ_{33} from θ_{33}^* . The same is true if we choose to fix either σ_{11} or σ_{33} because in each case, we would obtain two equations in two unknowns. Similar conclusions follow when there are four or more outcome categories. Thus, with independent errors, $J - 1$ variance parameters are estimable.

Reference

Train, K. E. 2009. *Discrete Choice Methods with Simulation*. 2nd ed. Cambridge: Cambridge University Press.