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**Resilient Provision of Ecosystem Services from Agricultural Landscapes: Tradeoffs  
Involving Means and Variances of Water Quality Improvements**

**ABSTRACT**

We assess the tradeoffs and synergies involved in reducing agriculture-generated nutrient loads with different levels of resilience. We optimize the selection of least-cost patterns of agricultural conservation practices for both the expected performance of the conservation actions and its variance. Securing nutrient loads with a higher level of resilience is costly, with marginal costs of resilience generally declining with lower loads. We find that the main tradeoff dimension is between cost of conservation investments and ecosystem service objectives, as opposed to pronounced mean-variance or between- nutrient objectives tradeoffs. We find relative synergies in agricultural conservation investments aimed at nutrient reductions.

**Keywords:** *agricultural conservation practices, agricultural nonpoint-source pollution, ecosystem services tradeoffs; multiobjective optimization; evolutionary algorithms, safety-first; resilience*

**JEL Codes:** Q25, C63

**Suggested running head:** Resilient Provision of Water Quality from Agriculture

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62 **Resilient Provision of Ecosystem Services from Agricultural Landscapes: Tradeoffs**

63 **Involving Means and Variances of Water Quality Improvements**

64 **Longer abstract**

65 Many ecosystem services are rival and important tradeoffs exist in their production process,  
66 while some jointness in production (synergies) are also postulated to exist. We assess the  
67 strength of tradeoffs and synergies involved in reducing agriculture-generated watershed nutrient  
68 loads with different levels of resilience. We define resilience as the simulated probability of  
69 attaining the desired level of nutrient load. We spatially optimize the selection of least-cost  
70 patterns of agricultural conservation practices or both the expected performance of the  
71 conservation actions and its variance. The modeling framework is applied to the Boone River  
72 Watershed in Iowa. The empirical results confirm that securing nutrient loads with a higher level  
73 of resilience is costly. However, the marginal cost is not necessarily increasing: focusing on  
74 larger nutrient reductions allows one to obtain resilience at a smaller additional cost than if one is  
75 seeking only modest nutrient reductions. In our model, this is due to the ability of perennial  
76 grassland to buffer against exogenous shocks and to drastically reduce variability in nutrient  
77 loads. In extending the model to two nutrients, nitrogen and phosphorus, we find that the main  
78 tradeoff dimension is between cost of conservation investments and ecosystem service  
79 objectives, as opposed to pronounced mean-variance tradeoffs or strong tradeoffs between the  
80 two nutrient objectives. While some meaningful tradeoffs exist between nutrient objectives, our  
81 findings highlight the presence of relative synergies in agricultural conservation investments  
82 aimed at nutrient reductions. However, while *relative* synergies exist, controlling risk of nutrient  
83 loads is once again shown to have high opportunity costs, and resilience comes at a significant  
84 premium.

85 In recent years, the concept of ecosystem services and natural capital has garnered significant  
86 attention from the research, policy, and conservation community (see, e.g., Heal and Small  
87 (2002), Boyd and Banzhaf (2007), Polasky and Segerson (2009), Barbier (2015), and a Special  
88 Feature in the *Proceedings of National Academy of Sciences* devoted to the topic). For  
89 intensively managed agriculture-dominated landscapes, there can be both complementarities and  
90 competition between ecosystem services including the provisioning services of food, feed, fuel,  
91 and clean water, the regulating service of waste processing (provided by streams), and the  
92 cultural ecosystem services tied to the presence of wildlife for hunting or recreation. The  
93 diminution of ecosystem services related to environmental externalities is, of course, a generally  
94 expected outcome of a market system. Given the signals provided by agricultural markets, it is  
95 not surprising that the agricultural system heavily favors production of private ecosystem  
96 services (food, feed, and fuel) (Lichtenberg 2002, p. 1254). The US Midwest, for example, has  
97 the highest rates of crop growth in the world, to the point that agriculture affects regional climate  
98 (Mueller et al. 2015). At the same time, heavy reliance on fertilizer use, has caused some  
99 scientists to suggest that humanity has exceeded its “safe operating space” with respect to  
100 nutrient fluxes (Steffen et al. 2015).

101 The recognition of these issues has led to extensive agri-environmental policy efforts in  
102 the US and elsewhere as well as a literature identifying approaches for incorporating ecological  
103 objectives in policy (Lichtenberg 2002; Lankoski and Ollikainen 2003, Bateman et al. 2013).  
104 While these efforts have found some success, most scientific assessments of environmental  
105 impacts of U.S. agriculture indicate many remaining concerns including fish and wildlife habitat  
106 (USDA-CEAP, Wildlife National Assessment 2015), air pollution (Mueller and Mendelsohn  
107 2011), nutrient pollution (US EPA 2015), and other environmental endpoints.

108 Elucidating the nature of tradeoffs between different ecosystem services requires  
109 understanding natural system processes and evaluating *counterfactual* scenarios to determine  
110 where tradeoffs exist, where synergies occur (e.g., Karp et al. 2015), and how other ecosystem  
111 services can be improved at the lowest sacrifice to marketed agricultural goods. Understanding  
112 tradeoffs or potential synergies<sup>1</sup> requires two things. First is the quantifiable understanding of the  
113 underlying ecosystem service production process and of the economic inputs that go into their  
114 production.<sup>2</sup> The ecological production functions themselves, however, are often poorly  
115 understood, may exhibit complex nonlinear dynamics with thresholds (e.g., Carpenter et al.  
116 2015; Barbier et al. 2008), or, even in the best case of relatively small scientific uncertainty, may  
117 be represented by computer simulation programs that do not correspond to traditional economics  
118 understanding of a production function (e.g., Heal and Small 2002).

119 While tradeoffs in ecosystem services may be unavoidable, it is desirable to limit  
120 consideration to those that are on a Pareto-efficient frontier. This is particularly important when  
121 considering the exact magnitudes (marginal costs or marginal rates of product transformation) of  
122 tradeoffs between ecosystem services. Yet another dimension to the question of tradeoffs  
123 between different classes of ecosystem services is uncertainty in the provision of a particular  
124 joint product from an ecosystem. In addition to having different opportunity costs of private  
125 goods, alternative ecosystem service bundle can differ in terms of the risk associated with their  
126 provision. That is, some conservation investments may consistently yield a given bundle of  
127 ecosystem services while others may on average a higher level of services, but with a wider

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<sup>1</sup> Heal et al. (2001) called the presence of synergies a “conservation umbrella.”

<sup>2</sup> See Heal and Small (2002) for an interesting distinction between economic and non-economic inputs into the ecosystem services production function. Economic inputs have opportunity costs, while others, like sunlight needed for agricultural production, while essential, are non-economic. In our application, economic inputs include foregoing crop production entirely and planting perennial grass or bringing machinery, expertise, and labor inputs for the adoption of “working land” conservation practices.

128 variability of provision over time. The mean-variance tradeoff for a particular cost of  
129 conservation investment may be relevant in choosing across services.

130           Consideration of tradeoffs between mean and variance of provision of services is  
131 consistent with the literature on resilience in ecosystem service provision. The notion of  
132 resilience is nuanced and complex, but for this work we adopt a definition similar to one used in  
133 Gren (2010) —namely, the reliability of ecosystem service provision under exogenous shocks,  
134 specifically weather risk.<sup>3</sup> In this paper, we explore tradeoffs for the expected provision level and  
135 for different levels of reliability (specified as simulated probability of attaining the desired  
136 provision level) for the case of a single non-market ecosystem service, and then expand the  
137 notion of tradeoffs to multiple dimensions of aquatic ecosystem services, where we focus on the  
138 joint probability of meeting desired ecological targets.<sup>4</sup> To do so, we adopt a multiobjective  
139 optimization approach with the objectives specified as means and standard deviations of desired  
140 ecosystem outputs. For this application, we focus on a heavily agricultural watershed in Iowa and  
141 use nutrient loads as inputs into aquatic ecosystem services. This approach can will be relevant to  
142 any situation where the connection between human actions on the landscape and ecosystem  
143 services is characterized by a complex relationship involving nonlinearities, nonconvexities and  
144 nonseparabilities (for example, conservation network design as in Parkhurst and Shogren 2008).

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<sup>3</sup> Social preference for reliability of goal attainment is reflected in the required “margin of safety” in the TMDL regulations, requiring either to explicitly reduce allowable pollutant loads in a watershed based on modeled uncertainty or to employ conservative modeling assumptions

(<http://water.epa.gov/lawsregs/lawsguidance/cwa/tmdl/TMDL-ch3.cfm>)

<sup>4</sup> However, as Heal and Small (2002) point out “We are powerfully ignorant about the technology that produces ecosystem services.” While true, ignorance should not be a reason to explore the implications of existing levels of understanding of some dimensions of ecosystem services production process, embodied, in our case, in the ecohydrologic model. See Kling (2011) for a call to action while acknowledging the deep uncertainties involved and importance of learning and adaptive management.

146 **Resilience in ecosystem services provision**

147 The concept of resilience has been used extensively by many disciplines, each approaching the  
148 concept from somewhat different perspectives and providing different definitions. We refer the  
149 reader to Longstaff et al.'s (2013) typology and to translate the concept among different  
150 disciplines. Intuitively, the notion of resilience deals with the ability of a system to perform  
151 desired functions under most, if not all, possible external shocks. Within their typology, we adopt  
152 the definition referred to as Type I resilience: the capacity of a system "to rebound and recover."  
153 Simply put, we seek to spatially optimize the selection of agricultural conservation practices  
154 which optimize both the expected performance of the conservation actions and their variance  
155 (Shortle and Horan (2013) suggest a similar approach). Longstaff et al.'s (2013) typology  
156 distinguishes approaches to resilience based on level of complexity (low/reductionist approach to  
157 high/holism/emergent properties) of the studied system as well as based on degree of normativity  
158 (on the scale from descriptive/positive to normative). Our work fits in the low complexity/low  
159 normativity category, as our studied system deals with quantifiable uncertainty (risk) and  
160 employs a deterministic, reductionist approach to quantifying the costs and ecosystem service  
161 outputs of evaluated scenarios.<sup>5</sup> This definition of resilience can be equivalently thought of as  
162 the reliability of meeting ecosystem service provision targets.

163 Next, we briefly sketch a simple model to aid in conceptual framing of our work.

164 Suppose one possesses a quantified joint ecological-economic production function

165  $S(\mathbf{x}; \boldsymbol{\varepsilon}): \mathbb{R}^m \rightarrow \mathbb{R}^k$ , where  $\mathbf{x}$  is an  $m \times 1$  vector of controllable economic inputs into the

166 production of ecosystem services (e.g., land, machinery, labor, fertilizer input, conservation

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<sup>5</sup> Were we to adopt a specific form for an economic damage function associated with ecosystem service degradation, our work would align with type II resilience definition of Longstaff et al. (2013), and would involve objectives of net benefit optimization (see Polasky and Segerson (2009) and Shortle and Horan (2013) for discussion of the relationship between outcomes obtained under physically defined goals and economically efficient outcomes).



167 practices) being combined, over the relevant spatial and temporal scale, to produce a  $k \times$   
168 1 vector of monetized benefits/costs and nonmonetized final ecosystem services, and  $\boldsymbol{\varepsilon}$   
169 representing exogenous factors (e.g., non-economic inputs into production of ecosystem services  
170 such as rainfall, solar radiation, soil quality, as well as exogenous economic factors such as  
171 commodity prices or government policy) treated as random. One of the components of the output  
172 vector serves to monetize the choices made with respect to human actions  $\boldsymbol{x}$  in the form of net  
173 social benefits. Depending on the availability of data and models, this can range from a full  
174 accounting of net social benefits measuring welfare impacts of marketed ecosystem services and  
175 non-market values of some non-market ecosystem services to simply measuring estimated  
176 engineering costs associated with  $\boldsymbol{x}$ . With this resilience measure, it is assumed that decision-  
177 makers can specify a set of desirable performance targets  $\bar{S}$ . Appropriately scaling outputs so that  
178 they are all desirable, the problem of resilience can be written as  $\max_{\boldsymbol{x}} P(S(\boldsymbol{x}; \boldsymbol{\varepsilon}) \geq \bar{S})$ , that is, the  
179 most resilient set of actions are those that maximize the probability of meeting a desired level of  
180 monetized and non-monetized ecosystem services.

181 This is a version of Roy's (1952) safety-first criterion.<sup>6</sup> Safety-first approaches have  
182 found numerous applications in many fields, including agricultural and environmental  
183 economics. Of many past efforts, examples include Paris (1979), Beavis and Walker (1983),  
184 Lichtenberg and Zilberman (1988), McSweeney and Shortle (1990), Bigman (1996), Willis and  
185 Whittlesey (1998), Horan and Shortle (2011), Eloffson (2003), Gren (2008), Kampas and White  
186 (2003), Rabotyagov (2010). As highlighted by Shortle and Horan (2013), the Total Maximum  
187 Daily Load rules adopts safety-first approach through the requirement of a "margin of safety"

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<sup>6</sup> More broadly, this kind of formulation can be described as a P-model of Chance-Constrained Programming (CCP) of Charnes and Cooper (1959), and CCP can be described as a class of anticipative (non-adaptive) stochastic programming approaches (Poojari and Varghese 2008)

188 constraint on the allowable watershed pollution loads. Another example is that the government of  
189 Canada was at one point explicitly favoring climate change policy requiring 95% certainty in  
190 agricultural carbon sequestration credits (Rabotyagov 2010).

191 In many applications, the tradeoffs embedded in resilience can be appropriately  
192 formulated by minimizing the (non-stochastic) cost of achieving a single stochastic ecosystem  
193 service objective with a given probability. The resilience objective is typically written as a  
194 constraint  $P(S_i(\mathbf{x}; \boldsymbol{\varepsilon}) \geq \bar{S}_i) \geq \alpha$ , where  $\alpha$  is level of resilience (or reliability) of the system.  
195 Rewriting the probabilistic constraint in a deterministic form can be accomplished when the  
196 distribution of the random term is known. In this case, a deterministic constraint involving the  
197 critical value of the standardized distribution of  $S_i$ , the controlled mean and variance of  
198 ecosystem service provision can be written as  $E_{\boldsymbol{\varepsilon}}(S_i(\mathbf{x})) + F_z^{-1}(1 - \alpha)Var(S_i(\mathbf{x}))^{0.5} \geq \bar{S}_i$ .  
199 For high desired levels of confidence  $\alpha$  (so that  $F_z^{-1}(1 - \alpha) < 0$ ), the term  $(F_z^{-1}(1 -$   
200  $\alpha)Var(S_i(\mathbf{x}))^{0.5})$  has the standard interpretation of a “margin of safety” or of an “uncertainty  
201 discount”. Tradeoffs between costs and the resilience of providing non-monetized ecosystem  
202 services are then seen by increasing cost of attaining higher reliability. This is a standard finding,  
203 although the costs of resilience have varied from single-digit percentage uncertainty discounts  
204 for soil carbon sequestration (Rabotyagov 2010), to almost doubling the costs of pollution  
205 reduction when required confidence in pollution reduction goes from 50 to 90-95% (Björstom,  
206 Andersson, Gren (2000); Elofsson (2003)) to finding a seven-fold increase in costs of controlling  
207 N runoff (McSweeney and Shortle, 1990). Resilience is costly, but the exact tradeoffs involved in  
208 achieving higher resilience depends on the particular situation.<sup>7</sup>

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<sup>7</sup> An obvious source of affecting costs of resilience lies with the choice of the critical value  $F_z^{-1}(1 - \alpha)$ . Under uncertainty about the form of the controlled distribution, one can purchase resilience with respect to distributional

209 The simple case of no uncertainty in the opportunity costs of ecosystem services  
 210 provision allows for a particularly convenient inversion of the probability statement and for  
 211 dealing with “resilient” levels of provision. If  $\mathbf{x}$  is costly, the constraint will be binding and  
 212  $E_{\varepsilon}(S_i(\mathbf{x}^*)) + F_z^{-1}(1 - \alpha)Var(S_i(\mathbf{x}^*))^{0.5} = \bar{S}_i$  represents the  $\alpha$ -quantile of the controlled  
 213 provision distribution (also sometimes referred to as a claimable amount (Kurkalova 2005)) and  
 214  $\mathbf{x}^*$  denotes choices leading to resilient provision. When multiple objectives are brought under the  
 215 joint probabilistic constraint, such an inversion from joint probabilities to unique quantiles is no  
 216 longer possible, except for the case of statistically independent objectives, where the jointly  $\alpha^n$ -  
 217 resilient set is constructed of individual (marginal)  $\alpha$ -resilient provision levels. Instead,  
 218 combinations of individual provision levels which jointly produce the desired  $\alpha$ -level resilience  
 219 will be required. This is akin to confidence ellipses encountered in joint significance testing of  
 220 regression parameters (for the introduction to the issues encountered in joint chance constraints,  
 221 see Bawa (1973), Prekopa (1970), Willis and Whittlesey (1998) for an applied agricultural  
 222 economics example or Hong, Yang, and Zhang (2011) for the modern operations research  
 223 perspective). In short, a simple interpretation of results as producing unique “resilient”  $\bar{S}_i, \bar{S}_k$  no  
 224 longer applies.

225 Fortunately, if we ask “what is the joint resilience associated with a particular solution  $\mathbf{x}$   
 226 and specified objectives,  $\bar{S}$ ?”, the answer, expressed as a joint probability, is easy to understand  
 227 (if not necessarily compute). Namely, the probability is  $P(\mathbf{x}) = \int I[S(\mathbf{x}; \varepsilon) \geq \bar{S}]dF(\varepsilon)$ . In some  
 228 simpler cases, where a single stochastic objective is encountered, and a particular distribution for  
 229 the random factor (e.g., normal) is assumed, the probability can be retrieved from existing tables.

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uncertainty by relying on the Chebyshev Inequality (e.g., Gren (2010)). This, however, appears unnecessarily  
 conservative for most practical applications.

230 In other cases of intermediate difficulty, in which a low-dimension economic-ecological  
231 production process may be assumed to be linear and separable ( $S(\mathbf{x}; \boldsymbol{\varepsilon}) \equiv \mathbf{s}(\boldsymbol{\varepsilon})' \mathbf{x}$ ), analytical  
232 expressions can be constructed (e.g., (Kampas and White 2003). However, even for a single  
233 dimension of ecosystem service output, where the production process may take place over  $K$   
234 locations, and where multiple actions ( $J$ ) are available in  $\mathbf{x}$ , construction of (conditional on  $\mathbf{x}$ )  
235 variance to arrive at the standardized ecosystem output involves estimating  $\frac{KJ(KJ-1)}{2}$  terms of the  
236 variance-covariance matrix, which would account for all the spatial and action-related  
237 covariances. This is a common problem that arises in risk management, and analytical techniques  
238 such as copula estimation exist to aid researchers and decision-makers (Cherubini, Luciano, and  
239 Vecchiato, 2004).

240 Gren (2010) considered several abatement actions and the implied abatement correlations  
241 across actions in estimating the resilience value of wetlands for nutrient reduction; however, her  
242 analysis did not incorporate spatial correlations, while Kampas and White (2003) have shown  
243 that ignoring correlations introduces larger bias in probabilistic constraints than incorrect  
244 distribution specification. Rabotyagov (2010) considered two agricultural conservation actions as  
245 well as spatial correlation for soil carbon sequestration. However, the introduction of multiple  
246 dimensions as well as distributional assumptions needed to make probability statements further  
247 complicate the issue. For instance, Kampas and Adamidis (2005) pointed out that under log-  
248 normality assumption of pollution reduction from a single action, the sum of reductions does not  
249 follow the log-normal distribution as Gren, Destouni, and Tempone (2002) assumed.

250 When, in addition, the natural science knowledge suggests that important dimensions of  
251  $S(\mathbf{x}; \boldsymbol{\varepsilon})$  are nonlinear and nonseparable (e.g., examples provided in Carpenter et al. 2015),  
252 obtaining analytical expressions for the overall resilience value becomes much more difficult.

253 However, as in simulation-aided econometric estimation, simulation approximation to the  
254 probability or other expected functions of interest such as the mean or the variance remains  
255 available. One issue that arises in this context is computational cost associated with evaluating  
256  $S(\mathbf{x}; \boldsymbol{\varepsilon})$  many times. For example, we could build the objective of resilience directly into the  
257 multiobjective tradeoff analysis (see Rabotyagov, Jha, and Campbell 2010) but instead we  
258 choose to opt to formulate the objectives in terms of means and standard deviations. Resilience  
259 is a property associated with a particular choice of actions to affect the provision of a vector of  
260 desirable outputs. Basic theory and empirical work to date suggest that resilience is costly.  
261 Resilience of the type we study is closely related to the variance in the desired output. To explore  
262 the potential tradeoffs among cost and proxies for aquatic ecosystem services, as well as evaluate  
263 potential synergies or tradeoffs associated with resilience, we choose to simultaneously optimize  
264 for the cost of economic inputs, and the mean and the variance of non-market ecosystem outputs.  
265 Further, we use bootstrap methods for a computationally fast way to provide resilience  
266 assessment of the optimized solutions.

## 267 **Tradeoff Development**

268 An efficient tradeoff frontier in the production of ecosystem services emerges when all  
269 Pareto-improvements have been exhausted: no single objective can be improved upon without  
270 sacrifice in terms of other objective(s). Some of the objectives may be formulated as resilience  
271 objectives. The classic example is tracing out the efficient mean-variance frontier of a stock  
272 portfolio. For multiple objectives when the economic-ecological production function can be  
273 explicitly written exact multiobjective optimization can generate tradeoffs across different  
274 ecosystem services (see Polasky et al. (2008) and Toth and McDill (2009)). In the case that

275  $S(\mathbf{x}; \boldsymbol{\varepsilon})$  function is cannot be written in a compact mathematical form but is represented by a  
276 computer simulation program, simulation-optimization methods can be used.

277 Multiobjective evolutionary algorithms are capable of dealing with potential non-convexities  
278 in optimization and can use simulation model output to (approximately) develop multiple-  
279 objective Pareto-efficient sets in a single optimization run. Deb (2001) is the classic introduction  
280 to evolutionary algorithms. Nicklow et al. (2010) and Maier et al. (2015) discuss some recent  
281 applications focused on water resources, and Kennedy et al (2008) and Porto et al (2014) provide  
282 terrestrial ecosystem management examples. Herman et al. (2014) explore tradeoff generation  
283 under deep uncertainty. Recent examples for tradeoff development using multiobjective  
284 evolutionary algorithms in agriculturally dominated ecosystems include Gramig et al. (2013),  
285 Bostian et al. (2015), Ahmadi et al. (2013), Rabotyagov et al. (2014) and Chichakly et al. (2013)  
286 who incorporate measures of resilience to anticipated climate change.

287 We consider a model of joint economic-ecological production process, where the human  
288 actions considered are “working land” agricultural conservation practices largely consistent with  
289 the prevailing crop system and “land retirement” of establishing perennial grass cover on  
290 cropland. These actions represent economic inputs into the production of (proxies for) freshwater  
291 and coastal aquatic ecosystem services associated with reducing nutrient fluxes, namely ambient  
292 Nitrogen (N) and Phosphorus (P) loads.

293 Scientific consensus exists on the fact that human activity has altered both the nitrogen  
294 and phosphorus cycles (Millenium Ecosystem Assessment, 2005, Ch. 12), with some beneficial  
295 (increased crop production), and some deleterious (eutrophication) effects on ecosystem services.  
296 The exact targets for nutrient loads and concentrations are an active area of research and  
297 policymaking (Evans-White et al., (2013), Heiskary and Bouchard (2015), US EPA, 2015  
298 <http://cfpub.epa.gov/wqsits/nnc-development/> ) but it is well understood that excess nutrient

299 loads negatively impact many ecosystem services from freshwater systems. We take as a starting  
300 point that it is desirable to reduce N and P and elucidate the tradeoffs involved in controlling the  
301 mean and standard deviation of nutrient pollution.

## 302 **Conceptual Model**

303 Our notation is similar to the notation used by Rabotyagov, Valcu, and Kling (2014).  
304 There are  $K$  decision-making units (“fields”) in the watershed, each field being characterized by  
305 a unique combination of physical characteristics (soil, slope) and location in the watershed. The  
306 ambient water quality is monitored both in stream and at the outlet of the watershed. Let  $r_i =$   
307  $r_i(\mathbf{x}_i, \xi) \forall i = 1, \dots, K$  be the  $i^{th}$  field emissions given the actions taken at field level, where  $\mathbf{x}_i$   
308 represents the  $J \times 1$  vector of actions implemented at each field, and  $\xi$  represents the stochastic  
309 weather factor. The set of actions consists of baseline activity and a set of working land  
310 conservation practices and land retirement.

311 To connect farm-level conservation actions to outcomes of interest, we need a specific  
312 version of the ecological production function. In our application, this function is represented by a  
313 water quality production function,  $W(\mathbf{r}(\mathbf{x}, \xi))$  that is the result of the complex spatial interactions  
314 between the edge-of-field emissions leaving the fields, and which is represented by an  
315 ecohydrologic simulation model.<sup>8</sup> Given the stochastic nature of the weather factor, we are  
316 interested in finding the least-cost spatial combinations  $\mathbf{x}$  that reduce expected values of nutrient  
317 pollution as well as its standard deviation. Using optimization results, we construct a measure of

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<sup>8</sup> As Lichtenberg (2002) explains: “... there is not a simple monotonic relationship between emissions at the level of an individual field and impacts on environmental quality at the ambient scale with which policy is actually concerned. Fate and transport are typically non-linear and depend on space and time in complex ways, making extrapolation of field-level emissions to ambient pollutant concentrations quite complex”. We refer the reader to Lichtenberg (2013), Shortle and Horan (2013) for reviews of these and other issues associated with nonpoint source pollution from agriculture, as well as to Rabotyagov et al (2014) for an attempt to simplify the ‘ecological production’ process. Uncertainty in the model structure itself is not considered in this article, although we recognize this as likely important for both better science and policy-relevance (see Herman et al. 2014).

318 resilience defined as the probability of achieving a particular target, and analyze the tradeoff  
 319 between costs and different levels of resilience. We start by considering the case of a single  
 320 nutrient pollutant (a proxy for diminished aquatic ecosystem services upstream and downstream)  
 321 and then move to the case of two pollutants.

322 *A single pollutant case*

323 We begin by solving the multi-objective problem that simultaneously minimizes

$$324 \text{Min}_{\mathbf{x}} [ C(\mathbf{x}), E_T[N(\mathbf{x})], \text{Var}[N(\mathbf{x})]^{0.5} ] \quad (1)$$

325 where  $\mathbf{x}$  represents a  $KJ \times 1$  vector representing a particular placement of conservation practices,  
 326  $W(\mathbf{r}(\mathbf{x}, \xi)) \equiv N(\mathbf{x})$  represents the simulated, over simulation period of length  $T$ , vector of  
 327 annual nitrogen loads,  $E_T[N(\mathbf{x})]$  is the mean nitrogen loads over the historical simulation  
 328 period,  $\text{Var}[N(\mathbf{x})]^{0.5}$  is the standard deviation, and  $C(\mathbf{x})$  is the (deterministic) estimated cost of  
 329 that particular combinations of conservation investments (economic inputs into aquatic  
 330 ecosystem service production) in the watershed.

331 The solution vector  $\mathbf{x}^*$  defines the Pareto-efficient set ( $P_f$ ), where each element is  
 332 represented by a unique combination of cost, expected nutrient load and the standard deviation of  
 333 loads:

$$334 P_f(\mathbf{x}^*) = \{ C(\mathbf{x}^*), E_T[N(\mathbf{x}^*)], \text{Var}[N(\mathbf{x}^*)]^{0.5} \mid \nexists \mathbf{x} \neq \mathbf{x}^*, P_f(\mathbf{x}) \succ P_f(\mathbf{x}^*) \} \quad (2)$$

335 That is, a pattern of conservation investments defines the Pareto-efficient frontier if there is no  
 336 other conservation action pattern which is a Pareto-improvement ( $\succ$ ) in the cost-mean-standard  
 337 deviation space. The Pareto-efficient frontier defines the set of optimal tradeoffs; for example,  
 338 the lower envelope of the set with respect to mean N and conservation action costs gives the  
 339 equivalent of the total abatement cost curve for expected nutrient pollution. It also offers



340 valuable information on the possible mean-variance tradeoffs, where, for a given cost, a tradeoff  
 341 between expected ecosystem service performance and its standard deviation could be seen.  
 342 However, we cannot directly infer how much would it cost to achieve a particular level of  
 343 nitrogen loads under different levels of resilience, where by resilience, we understand the  
 344 probability of achieving that target in any given year. However, for the single stochastic  
 345 objective, it is straightforward to “collapse” the three-dimensional Pareto-frontier into a set of  
 346 “resilient tradeoffs” between cost and resilient provision of an ecosystem service. Doing so  
 347 involves appropriately constructing the deterministic equivalent to the resilience objective using  
 348 the mean, standard deviation, and the critical value of the controlled distribution of the stochastic  
 349 objective.

350 Finding resilient solutions involves solving a chance- constrained optimization problem:

$$351 \text{Min}_{\mathbf{x}} C(\mathbf{x}) \text{ s. t. } \Pr\{N_t(\mathbf{x}) \leq \bar{N}\} \geq \alpha \quad \forall t = 1, \dots, T \quad (3)$$

352 where  $\bar{N}$  is the target level of N loads, and  $\alpha$  the desired level of resilience measured as the  
 353 probability of achieving the target.

354 We use the Pareto-frontier  $P_f(\mathbf{x}^*)$  and employ two approaches to approximate solutions  
 355 to the above problem, approaches that we identify as “normal” and “non-parametric”. Under  
 356 both approaches, we transform equation (3) using its deterministic counterpart as:

$$357 \text{Min}_{\mathbf{x}} C(\mathbf{x}) \text{ s. t. } E_T \{N(\mathbf{x})\} + \phi^\alpha \text{Var}(N(\mathbf{x}))_T^{0.5} \leq \bar{N} \quad (4)$$

358 where  $\phi^\alpha$  is the critical value of the standardized distribution of  $N(\mathbf{x})$ .

359 Note that a solution to the chance-constrained problem (3) must be a member of the  
 360 Pareto frontier in the cost-mean-standard deviation space:  $\hat{\mathbf{x}} \subset \mathbf{x}^*$ . The converse is not true: that  
 361 is, a particular solution from a multiobjective optimization program need not be optimal for a

362 chance-constraint program. Appendix 1 in supplemental materials provides the demonstration of  
363 this point.

364 Under the normal approach, we assume the standardized distribution of pollution load  
365 follows a normal distribution and use  $\phi^\alpha = \Phi^{-1}(\alpha)$ , the standard normal critical value that  
366 depends on  $\alpha$  (1.64 for  $\alpha = 0.95$ ). Under the normality assumption, we consider  $\alpha -$   
367 *resilient* pollution loads to be  $E_T \{N(\hat{\mathbf{x}})\} + \Phi^{-1}(\alpha)Var(N(\hat{\mathbf{x}}))_T^{0.5}$  and can focus on the results  
368 in terms of tradeoffs between cost and resilient nitrogen loads.

### 369 *Non-parametric approach*

370 An alternative approach is to employ non-parametric bootstrap methods (Efron (1979)),  
371 and define the resilience pollution loads in terms of the bootstrapped quantiles. Since our data  
372 (nitrogen loads simulated over a period of time) is serially dependent, we employ the block  
373 stationary bootstrap method (Politis and Romano (1992), (1994)). Under this approach,  
374 observations are re-sampled in blocks of random length, with the length of the block being  
375 determined by a geometric distribution. The block re-sampling (observations are drawn  
376 consecutively) preserves the lag dependence in the original data. The bootstrapped data is  
377 stationary if the block length is determined using a geometric distribution. Additionally, the  
378 block bootstrap works well under very weak conditions on the dependency structure of the  
379 original data.

380 For any efficient combination of conservation practices ( $\mathbf{x}^*$ ) that is part of the Pareto  
381 frontier  $P_f(\mathbf{x}^*)$ , we take the model-simulated  $T \times 1$  vector of nitrogen values  $N(\mathbf{x}^*)$  to construct  
382 a non-parametric distribution using a stationary bootstrapping approach using blocks of unequal  
383 length. To obtain tradeoffs involving  $\alpha -$  *resilient* nitrogen loads, we compute, for each  
384 bootstrap replicate series, the sample  $\alpha$ -quantile and average the results over many bootstrap

385 replications. The interpretation of the new  $\alpha$  – *resilient* Pareto frontier is similar to the  
 386 previous one, each solution representing a non-dominated combination of cost and  $\alpha$  – *resilient*  
 387 nitrogen loads that correspond to a given level of resilience,  $\alpha$ . The magnitude of the differences  
 388 between the normal and non-parametric approaches is an empirical question.

389 *Multiple pollutants: A case of nitrogen and phosphorus*

390 We also consider developing tradeoffs which involve the means and the variances of  
 391 multiple ecological objectives. In this case, we modify the multiobjective minimization problem  
 392 to include the means and standard deviations of two nutrient pollutants, nitrogen and  
 393 phosphorus:<sup>9</sup>

$$394 \quad \text{Min}_{\mathbf{x}} [ C(\mathbf{x}), E_T[N(\mathbf{x})], \text{Var}[N(\mathbf{x})]^{0.5}, E_T[P(\mathbf{x})], \text{Var}[P(\mathbf{x})]^{0.5} ] \quad (5)$$

395 where  $\mathbf{x}$  represents a particular placement of conservation practices,  $N(\mathbf{x}), P(\mathbf{x})$ , the vectors of  
 396 nitrogen and phosphorus loads of length  $T$ ,  $E[.]$  is the expected water quality outcome measured  
 397 as (historical) sample mean of nitrogen and phosphorus,  $\text{Var}[N(\mathbf{x})]^{0.5}$  and  $\text{Var}[P(\mathbf{x})]^{0.5}$  are  
 398 respective standard deviations, and  $C(\mathbf{x})$  is the estimated annual cost of the particular  
 399 combination of conservation investments in the watershed.

400 Similarly to the univariate case, the solution is represented by a Pareto set,  $P_f^{NP}$ , where  
 401 each element represent a non-dominant combination of cost, mean and standard deviation values  
 402 for nitrogen and phosphorus emissions associated with a spatial combination of conservation  
 403 practices. As discussed above, it is more intuitive to consider actual tradeoffs between mean and

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<sup>9</sup> If the objective were to be specified as minimizing the variance, for example, the sum, or a linear index of two nutrients, the covariance term would enter into problem specification. Alternatively, the resilience objective specified as a joint probability could be simulated within the optimization loop (as in Poojari and Varghese (2008)). We leave those extensions to future work.

404 variance control or to characterize a particular solution in terms of a probability (resilience value)  
405 of meeting a specified target.

406 In order to characterize joint resilience implied by the solutions in the Pareto-frontier, we  
407 rely on the nonparametric bootstrap, now using two dimensions. Resilience is defined as the joint  
408 simulated probability of achieving both N and P targets. Similarly to the univariate stationary  
409 bootstrapping, we use the vectors of simulated nitrogen and phosphorus loads to generate  
410 bootstrap replicates using blocks of unequal length. The stationary bootstrapping procedure  
411 involves using both vectors simultaneously, thus preserving the correlation between controlled  
412 loads of N and P. That is, given a particular joint target  $(\bar{N}, \bar{P})$ , we can construct characterize the  
413 tradeoff frontier in terms of cost, mean nitrogen, mean phosphorus and simulated joint resilience  
414 of achieving the specified target. The resilience level is estimated as the simulated probability,  
415  $p(\mathbf{x}_i)$ :

$$416 \quad p(\mathbf{x}_i) = \frac{\sum_{r=1}^M \{\sum_{t=1}^T I(N(\mathbf{x})_{rt} \leq \bar{N}, P(\mathbf{x})_{rt} \leq \bar{P})/T\}}{M} \quad (6)$$

417 where  $T$  is the length of the model simulation,  $\mathbf{x}_i$  is the particular pattern of conservation  
418 investments evaluated and  $M$  is the number of bootstrap repetitions.

419 To approximate the solution sets for the multiobjective problems (1) and (5), we use a  
420 simulation-optimization framework using Soil and Water Assessment Tool (SWAT) as the  
421 simulation model and a modification of the Strength Pareto Evolutionary Algorithm 2 (SPEA2)  
422 (Zitzler, Laumans, and Thiele, 2002) as the multiobjective optimization heuristic, as described by  
423 Rabotyagov et al. (2010). The simulation-optimization framework simultaneously minimizes the  
424 cost, the 20-year means ( $T = 20$ ) and standard deviations of annual N for the single pollutant

425 case and N and P loads for the two pollutant case.<sup>10</sup> The solutions are sets of Pareto-  
426 nondominated watershed configurations  $P_f$  and  $P_f^{NP}$ . To assess convergence, we use a  
427 consolidation ratio proposed by Goel and Stander (2010) and used by Rabotyagov et al. (2014).

428 SWAT is designed to run watershed simulations based on a wide range of inputs: weather  
429 data, soil characteristic, plant growth and crop rotations, nutrient management, nutrient transport  
430 and transformation, land use and management practices. The model can be used to estimate the  
431 changes in nutrient emission in response to the land changes associated with alternative  
432 conservation practice, crop choices, and rotation alternatives. The model was developed by the  
433 U.S Department of Agriculture and has been used in a wide range of applications (Arnold et al.  
434 (1998); Arnold and Fohrer (2005); and Gassman et al. (2008)).

435

### 436 **Empirical Application: The Boone River Watershed**

437 Our empirical results focus on The Boone River Watershed (BRW). The BRW is a  
438 typical agricultural watershed in central Iowa with more than 90% of its area dedicated to corn  
439 and soybean production. The watershed's tributaries offer habitat to the Topeka shiner, a  
440 federally listed endangered species, and to other fish and mussel species. Additionally, the  
441 watershed tributaries feed the Des Moines River, a major water source for the biggest  
442 metropolitan area in Iowa. The lower part of the watershed is used for recreation activities.

443 Given the extent of the agricultural activities, high levels of agriculture-contributed  
444 nitrogen, phosphorus and sediment loads contribute to the water quality impairments. A

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<sup>10</sup> The resulting relatively small sample size used to construct the model-simulated mean and the standard deviation is one of the limitations of the study, and can introduce imprecision in resilience estimates. To the extent that mean and standard deviation estimates are not biased, we try to improve precision by bootstrapping optimized series.

445 successful calibration for the current Boone River Watershed SWAT baseline was obtained by  
446 using monthly streamflow nutrient data and incorporating earlier calibration efforts (Gassman,  
447 (2008)).<sup>11</sup> The set of conservation practices selected for achieving the nutrient reduction  
448 includes working land practices: cover crop, no-till, the combination of cover crops and no-till,  
449 and land retirement. Typically, cover crops are grown during late fall and early spring. In the  
450 Midwest, where there are no markets for cover crops, cover crops are promoted for their direct  
451 environmental benefits (recycle nutrient and prevent nutrients leaching) and indirect economic  
452 benefits (improve soil health by preventing soil erosion). Cover crops are effective in reducing  
453 both nitrogen and phosphorus losses. No-till is a type of tillage where no more than 30% of the  
454 crop residue is removed. No-till is effective in reducing erosion and phosphorus runoff. Land  
455 retirement involves taking land out of production and the establishment of perennial grasses.

456 The costs estimates for conservation practices used in this study are drawn from several  
457 sources: no-till at \$6 per acre (Iowa State Extension budgets), cover crops at \$35 per acre (Iowa  
458 Nutrient Reduction Strategy), \$41 per acre for the combination of no-till and cover crops, and  
459 \$254 per acre, the average cash rental rate for the BRW (Iowa State Extension cash rental rates  
460 estimates) as the cost of land retirement. The cost of conservation practices is additional to the  
461 cost of baseline activities, considered to be zero in this application.

## 462 **Results and discussion**

463 The simulation framework allows us to evaluate counterfactual watershed-based  
464 scenarios in terms of estimated costs of conservation practices and their implications for mean

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<sup>11</sup> The present SWAT simulations are being performed with an updated SWAT version 2012 code (SWAT2012, Release 6150 that contains corrected algorithms that more correctly simulate movement of nitrate through subsurface tile lines as well as numerous other enhancements that were not present in the SWAT2005 code.

465 and variance of corresponding nutrient loads over a 20-year period (1993-2013). We estimate the  
466 Pareto- efficient frontiers for a single pollutant (N) and multiple pollutants (N and P). We offer a  
467 short analysis of the mean-variance tradeoffs and how these tradeoffs relate to the choice of the  
468 conservation actions. Next, we analyze the trade-offs between achieving a pollution target with a  
469 given resilience level and the estimated cost of conservation actions. The set of resilience values  
470 ( $\alpha$ ) ranges from 50 percent to 95 percent in increments of 5 percent, as well as 99 percent.  
471 Nutrient pollution targets are chosen to be equivalent to a range of percent reductions from the  
472 historical baseline emissions.

#### 473 *Single pollutant case: Nitrogen, Mean-Variance Tradeoffs*

474 The results of the multi-objective optimization defined by equation (1) can be visually depicted  
475 by a three dimensional scatterplot ( $P_f$ ), where each point on the frontier represents the least cost  
476 watershed configuration that achieves a given expected value of N loads and has the lowest  
477 standard deviation (see Figure A2 in the supplementary material). Figure 1 depicts the extent of  
478 the mean-variance tradeoffs from the frontier. Specifically 1(a) shows a fairly linear positive  
479 relationship between the mean and the standard deviation of N loads, as standard deviations  
480 increase with the means. Additionally, the analysis of mean-coefficient of variation (ratio of  
481 standard deviation to the mean) plot (Figure 1(b)) shows three patterns: a steep increasing trend  
482 for the low range nitrogen emissions (below three thousand tons) where the standard deviation  
483 increases at a faster rate than the mean, followed by a smoother declining pattern where the  
484 standard deviation increases at a slower rate than the mean. For larger loads (above 4.5 thousand  
485 tons), the ratio of standard deviation to mean settles around 0.5. These patterns can be explained  
486 by the distribution of the conservation practices selected by the algorithm (see supplementary  
487 material Figure A3).

488           Next, we quantify the cost to achieve a particular level of nitrogen loads under different  
489 levels of resilience. More explicitly, for any level of resilience  $\alpha$ , we construct resilient Pareto  
490 frontiers, where each Pareto frontier can be viewed as the total cost curve where the  
491 corresponding nitrogen emissions are achieved with probability  $\alpha$ . As previously described, we  
492 use two approaches (normal and non-parametric) to construct the resilient Pareto frontiers that  
493 corresponds to different resilience levels. The “normal” approach assumes that the standard  
494 normal critical values are used to weigh the standard deviations, while the non-parametric  
495 approach uses stationary bootstrap to simulate the quantiles. Simulated nutrient load series pass  
496 stationarity tests, and we use 10,000 bootstrap replications with mean block length of 5. The new  
497 Pareto frontiers transform the mean nitrogen values of the original Pareto frontier into  $\alpha$  resilient  
498 levels while keeping the costs and the watershed configurations unchanged.

499           Figures 2 depicts the  $\alpha$  resilient Pareto frontiers for four levels of resilience: median (50),  
500 75, 90, and 99 given the two approaches, as well as the mean-cost tradeoff. The horizontal axis  
501 depicts the resilient loads, and the vertical axis shows annual costs. Notice that under the normal  
502 approach (left panel), the corresponding levels of resilience for mean and median are identical,  
503 while under the non-parametric approach the two tradeoff frontiers are different, the  
504 bootstrapped mean curve being entirely above the median (right panel). Under the both  
505 approaches, the Pareto frontiers move further away from the left corner as the resilience levels  
506 increase. For any cost level (consider a horizontal line), the resilient level of N loads increases as  
507 we move from one frontier to another. This shows us how much resilience can be achieved under  
508 a given budget. Likewise, for any level of resilient N loads, the cost increases as we move from  
509 one frontier to another. The distance between two consecutive frontiers represents how much it  
510 would cost to make the same level of N load more resilient. (Pairwise comparisons between the  
511 two distributions are provided in the supplementary material).



512 Each cost-resilient curve corresponds to a resilient N target expressed as a percentage  
513 reduction from the baseline. As expected, more stringent targets (higher percentage reductions,  
514 lower loads) cost more and the costs of achieving a given target increases with the resilience  
515 level. For less stringent targets, the costs-resilience curves are convex, with a non-convexity  
516 patterns for more stringent targets. For example, when the target is set to 70 percent reductions,  
517 the cost is flat once a high level of resilience (80) is achieved.

### 518 *Resilience-Marginal Cost Curves*

519 Another way to analyze the resilience-cost trade-off is to answer the question how much would it  
520 cost to achieve an additional level of resilience. We focus our analysis on three levels of  
521 reductions: low (20 percent), average (the Iowa Nutrient Reduction Strategy 45 percent), and  
522 high (70 percent reductions). For each of the three targets, Figure 3 summarizes the cost curves  
523 for securing the targets at an additional resilience level. These curves can be interpreted as the  
524 marginal cost of resilience. Although the marginal cost curves have a similar shape, their  
525 magnitudes differ across the two approaches. The marginal cost curve when the target is low (20  
526 percent reductions) is almost flat for resilience levels lower than 80. However, for higher  
527 resilience, the marginal costs display a sharp increase, with the increase being sharper under  
528 normal approach. The marginal cost curve for the intermediate target displays more than one  
529 pattern. Under the normal approach, marginal costs are increasing for lower resilience, linear for  
530 moderate resilience, and again increasing for higher resilience levels. However, the patterns are  
531 different under the non-parametric approach: linear for lower levels, increasing for moderate  
532 levels, decreasing and linear for higher levels of resilience. The marginal costs for the most  
533 stringent target are increasing for lower levels, decreasing for moderate levels, and linear for  
534 higher resilience level. The diversity of patterns across targets and resilience levels can be

535 explained by the distribution of the conservation practices (these are provided in Table A1 of  
536 supplementary materials). The costs of achieving resilient loads corresponding to 45 percent  
537 reductions (3.39 thousand tons) range from 13 to 87 million over the considered resilience levels.  
538 Similarly to McSweeney and Shortle (1990), we find that to control a single-year N load with 99  
539 percent resilience is almost 7 times costlier than controlling N with median resilience

#### 540 *Resilient N loads for different cost (budget) levels*

541 The  $\alpha$  resilient Pareto frontiers can also provide insight into the different load levels that can be  
542 secured under different levels of resilience when we impose a limit on total costs (iso-cost  
543 curves). Figure 4 can be used to see how much resilience can be obtained under a given budget.  
544 Next, we present the results for four cost (budget) levels: 10, 20, 50, and 100 million. For each  
545 budget level, we construct iso-cost curves showing the tradeoffs between resilience and different  
546 levels of attainable loads.

547 Figure 4 shows that the iso-costs are convex shaped, showing that when considering cost  
548 constant, higher levels of resilience translate in higher levels of emissions, or alternatively lower  
549 emission level have lower resilience levels. The empirical findings also show that the size of  
550 these tradeoffs decrease as the total costs increase, as the iso-cost curves corresponding to lower  
551 total cost have steeper slopes. For any of the chosen cost and any resilience levels, fewer  
552 emissions (more reductions) can be claimed under the non-parametric approach (Figure 4 right  
553 vs. left panel). Also, the slopes of the non-parametric iso-cost curves are smoother.

#### 554 *Multiple targets: nitrogen and phosphorus*

555 Next, we present the simulation results for the case when two pollutants (N and P) are jointly  
556 targeted. We approximate the Pareto-frontier for 5 objectives: cost and means and standard

557 deviations of N and P. Pareto-frontier we obtain is valuable in that can show the nature of  
558 tradeoffs along different values of N and P as well as corresponding variability and cost.

559 Visualizing tradeoffs across more than two dimensions is challenging, and pairwise  
560 projections of the Pareto-frontier could be most helpful to see a particular scope of synergies or  
561 tradeoffs. Visualizing across 5 dimensions is possible; however, interpretation can be  
562 challenging. To aid this process, we present a radar (spider) plot in all 5 dimensions. Specific  
563 solutions of interest (a few at a time) can be analyzed as well. Consider the left panel of Figure  
564 5, and the mean N (mean P) and Cost axes. The non-convex shape of the plot between those axes  
565 says that there are no solutions in the Pareto-frontier which simultaneously have high cost and  
566 high mean N (and P) loads (and compensating for those with smaller values on other axes). This  
567 suggests a strong tradeoff existing between mean nutrient loads and cost. A convex shape with  
568 respect to other axes *does not* mean that tradeoffs do not exist among the remaining pairs of  
569 objectives, but that there *exist* efficient solutions which exhibit synergies (co-movement) along  
570 those dimensions. For example, as we see subsequently (Figure 6), tradeoffs between N and P  
571 control exist, but synergies are also present (pairwise comparison of mean N and P on the right  
572 panel of figure 5). A presence of at least some synergies is also apparent by considering pairwise  
573 tradeoffs between means and standard deviations (consistent with a limited nature of mean-  
574 variance tradeoff for N explored above). Whereas, as can be seen from the nature of the tradeoffs  
575 between costs and standard deviations (shown on the right panel of Figure 5 for the case of  
576 standard deviation of P—N results are similar), there are no synergies between cost and risk, and  
577 we see strong tradeoffs consistent with the notion that resilience is always costly. However, we  
578 do not see strong tradeoffs between means or standard deviations of nutrient reduction  
579 objectives. Of course, this finding may not generalize to other contexts.

580 Next, we make the connection to resilience. Note that, unlike in a single stochastic  
581 objective case, we can no longer claim that a solution to a chance-constrained formulation has to  
582 be a member of the Pareto-frontier. For the case of separate resilience objectives, where each  
583 pollutant has to be controlled in a resilient fashion that is still the case (using the same logic as  
584 above). That is, single pollutant resilient levels can be obtained in exactly the same way we  
585 proceeded above with N. Because of that reason, we do not present single-pollutant resilience  
586 tradeoffs.

587 However, if one is interested in the joint constraint of the type:  $\Pr\{N_t(\mathbf{x}) \leq \bar{N}, P_t(\mathbf{x}) \leq$   
588  $\bar{P}\} \geq \alpha \quad \forall t = 1, \dots, T$ , we cannot be assured of joint resilience optimality of solutions obtained  
589 by the multiobjective program, as the algorithm does not directly simulate joint probability  
590 which is a function of variances and the covariance between N and P. To assess cost-joint  
591 resilience efficiency for specific  $\bar{N}$  and  $\bar{P}$  targets, one could formulate a two-objective  
592 evolutionary optimization program involving cost and simulated probability of joint goal  
593 attainment (akin to Poojari and Varghese (2008) or Rabotyagov, Jha, and Campbell (2010)).  
594 Despite the possibility that the solutions in the Pareto frontier may not be optimally resilient for  
595 joint nutrient targets, we can still provide ex-post assessment of the solutions in terms of joint  
596 resilience. To do so, we again rely on (now joint) non-parametric bootstrap approach, using  
597 10,000 replicates and computing the simulated resilience using (6).

598 A three dimension illustration of these tradeoffs when the targets are set equal to 45  
599 percent reductions for both N and P (equation 9) is presented in the supplemental material  
600 (Figure A6). Each element on this frontier (a 3-dimensional projection of the 5-dimensional  
601 Pareto-frontier  $P_f^{NP}$ ) is assessed for a resilience (probability) level of achieving this joint target.  
602 As for the single pollutant case: securing higher level of resilience demands higher costs. We

603 present the lower envelopes of the plot in Figure 6. Figure 7 depicts the marginal costs of  
604 achieving additional levels of resilience for the three specified targets, while Table A2 (contained  
605 in supplementary details) describes in detail the total and marginal costs as well as the  
606 distribution of conservation practices. For example, the least cost way to achieve 45 percent  
607 reductions with 70 percent resilience is higher than the least cost to achieve the same level of  
608 reductions with 75 percent resilience (Figure 6). The negative marginal costs are unexpected but  
609 we interpret them as the inefficiencies embedded in the spikes, and, should one focus on a  
610 specific set of N and P reductions with a resilience objective, we expect those to disappear. With  
611 those caveats in mind, we provide a broad assessment of joint resilience implied by the 5-  
612 dimensional Pareto-frontier.

613 Overall, the costs of achieving the joint target are higher than in the case of a single  
614 pollutant and range from 22.3 to 107.4 million. This is to be expected as a joint probability is  
615 going to be smaller than a marginal one. The distribution of the conservation practice is different,  
616 with more land retirement being used more extensively at any resilience level. The spatial  
617 placement of the conservation practices associated with these solutions is provided in the  
618 supplemental materials.

## 619 **Conclusions and caveats**

620 Many ecosystem services are rival and important tradeoffs exist in their production  
621 process. Understanding the nature of these tradeoffs requires: (a) defining a quantifiable measure  
622 of the underlying ecosystem production process and of the economic inputs that go into this  
623 productions functions, and (b) exploring alternative resource allocation decisions to identify, if  
624 only approximately, Pareto-efficient ways of producing different ecosystem services.  
625 Uncertainty in the provision of a particular ecosystem service adds another dimension to the

626 nature of these tradeoffs, where different ecosystem services differ both in terms of the expected  
627 outcomes and in terms of risks. Closely related to uncertainty is the notion of resilience, and the  
628 cost of providing the ecosystem service under different levels of desired resilience.

629         We focus on understanding and quantifying the tradeoffs for the case of proxies for  
630 aquatic ecosystem services in the landscapes dominated by agricultural activity. Particularly, we  
631 focus on controlling the flux of agricultural nutrients (N and P) as means to improve the  
632 upstream and downstream water quality. Economic inputs into water quality production are a set  
633 of conservation practices that can be implemented on agricultural landscapes for controlling the  
634 flux of nutrients, while the (intermediate) ecological production function is an ecohydrologic  
635 simulation model relating human actions to changes in nutrient loads. By integrating a heuristic  
636 global optimization with a ecohydrologic model we meet the conditions of having science-based  
637 representation of the water quality production function ( $W_t(\mathbf{r}(\mathbf{x}, \boldsymbol{\xi}_t))$ ) and its dependence on the  
638 exogenous stochastic weather factors and of having the ability to produce an approximate Pareto-  
639 frontier that accounts for multiple tradeoff dimensions.

640         We quantify the tradeoffs involved in achieving different levels of nutrient loads with  
641 different levels of resilience where resilience is defined as the probability of attaining the desired  
642 level of nutrient load. We spatially optimize the selection of least-cost patterns of agricultural  
643 conservation practices or both the expected performance of the conservation actions and its  
644 variance. We analyze the tradeoffs for a single nutrient (ecosystem service), and then expand our  
645 analysis to include multiple nutrients (multiple ecosystem services).

646         We apply our modeling framework to the Boone River Watershed in Iowa. The empirical  
647 results confirm expectations and are consistent with previous studies: securing nutrient loads  
648 with higher level of resilience is costly. However, the marginal cost is not necessarily increasing:

649 that is, focusing on larger nutrient reductions allows one to obtain resilience at a smaller  
650 additional cost than if one is seeking only modest nutrient reductions. In our application, this is  
651 due to the ability of perennial grassland to buffer against exogenous shocks and to drastically  
652 reduce variability in nutrient loads (as shown before, e.g., in Rabotyagov, Jha, and Campbell  
653 2010). Furthermore, the main tradeoff dimension is between cost of conservation investments  
654 and ecosystem service objectives, as opposed to pronounced mean-variance tradeoffs or strong  
655 tradeoffs between the two nutrient objectives. While some meaningful tradeoffs exist between  
656 nutrient objectives, our findings highlight the presence of relative synergies in agricultural  
657 conservation investments aimed at nutrient reductions. However, while *relative* synergies exist,  
658 controlling risk of nutrient loads has high opportunity costs, and resilience comes at a significant  
659 premium.<sup>12</sup>

660         Among many caveats, we point out that our optimization algorithm was not exactly  
661 tailored to the optimal joint resilience question, but instead focused on providing an overall  
662 picture of feasible tradeoffs. Additional limitations associated with uncertainty in model  
663 structure, the simplicity of economic cost representation, and the level of spatial resolution of the  
664 ecohydrologic model present ample opportunities for future research. However, we hope to show  
665 the utility and the promise of the general approach which integrates scientific understanding of  
666 complex systems with the practical need to see how production of non-market ecosystem  
667 services can be accomplished at the lowest possible sacrifice of economic inputs.

668

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<sup>12</sup> We note recent research by Carpenter et al. (2015) who provide examples where, in nonlinear systems, reducing high-frequency variance can lead to an increase in low-frequency variance, thereby undermining the resilience objective. We constructed spectrum plots of controlled variance of nutrients and we see a decrease in variance at all spectra with an increase in conservation investment cost.

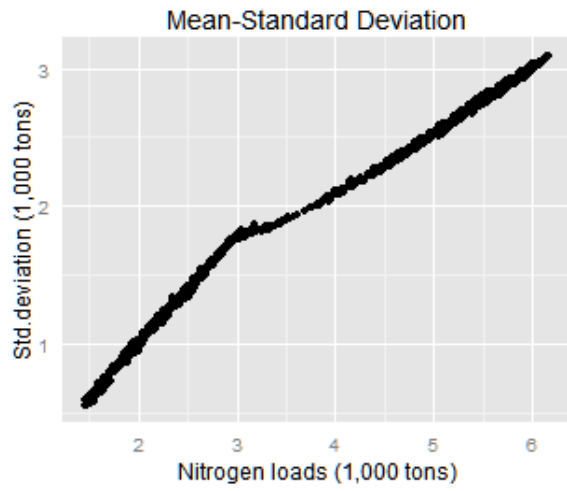
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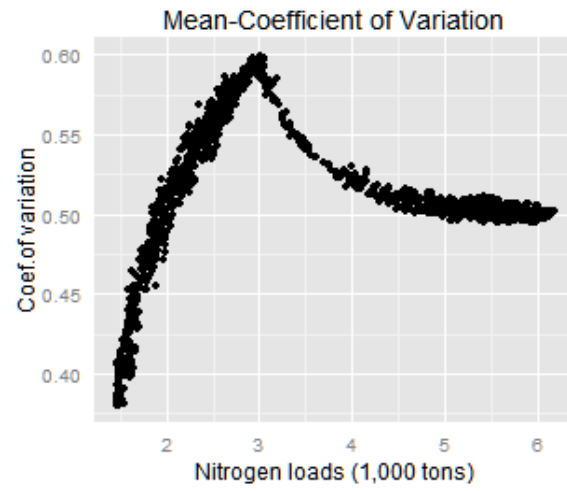
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672 Figure 1 (a) Mean-Variance Trade-Offs



(b) Mean-Coefficient of Variation

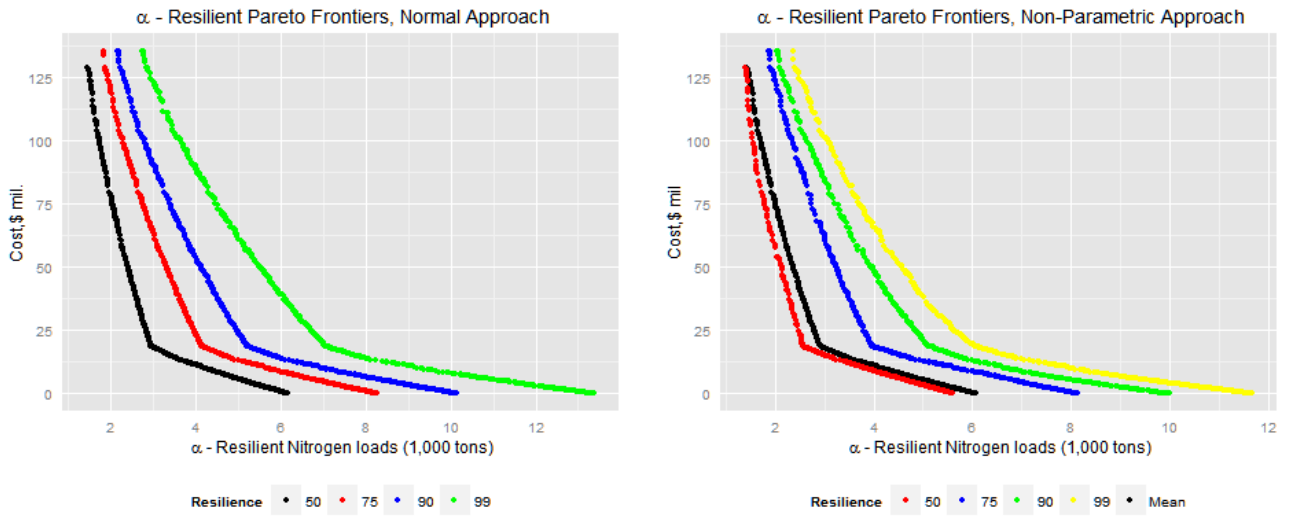


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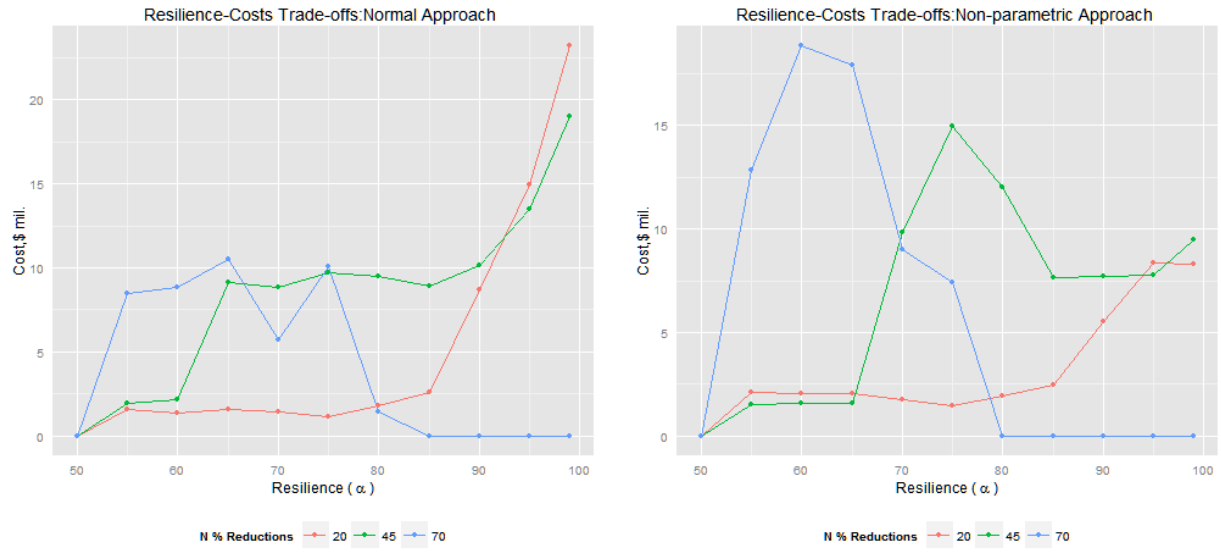
676 Figure 2:  $\alpha$  Resilient Pareto Frontiers (Normal Approach (left), Non-parametric Approach  
677 (right))



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680 Figure 3 Marginal Costs of Additional Resilience for Different Resilient N Targets



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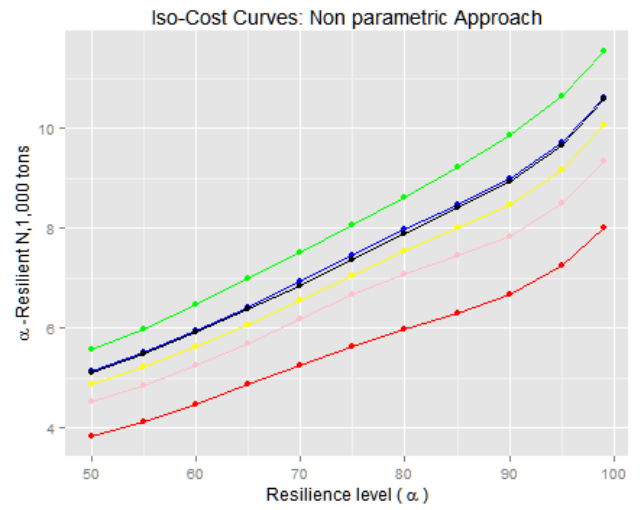
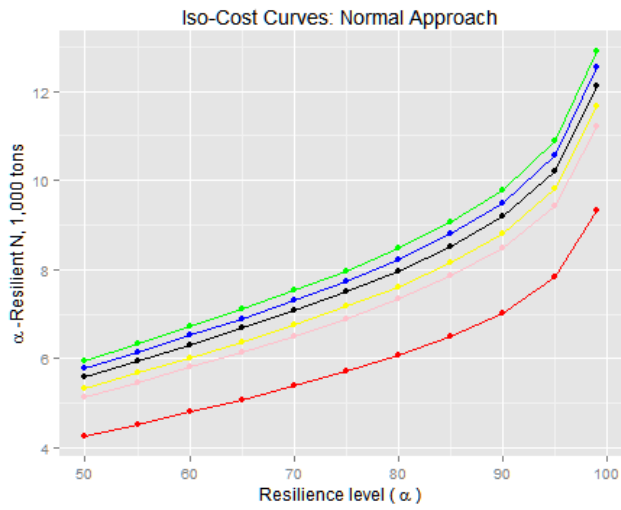
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693 Figure 4 Resilience: Iso-Cost Curves(Normal Approach: left, Non parametric approach right)



— B.10mil — B.20mil — B.30mil — B.40mil — B.50mil — B.100mil

— B.10mil — B.20mil — B.30mil — B.40mil — B.50mil — B.100mil

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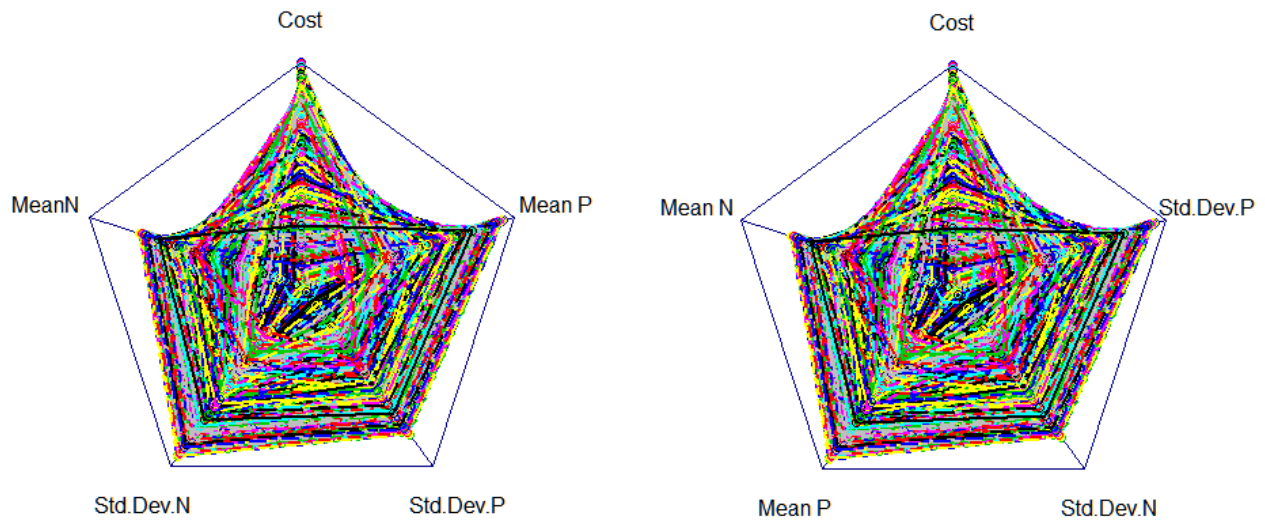
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Figure 5. Pareto Optimal Frontier: Cost, Means (N, P), Standard deviation (N ,P)

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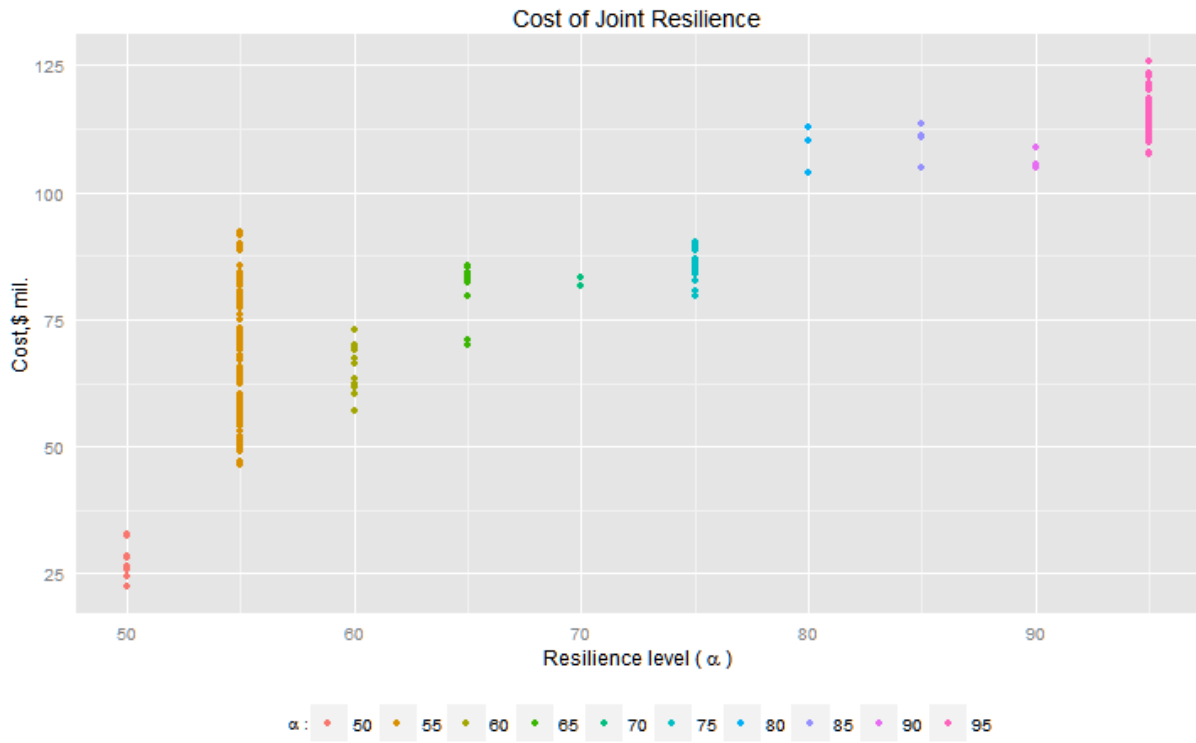
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718 Figure 6 Cost of Achieving Resilience When Target is Equal to 45 percent Reductions for Both  
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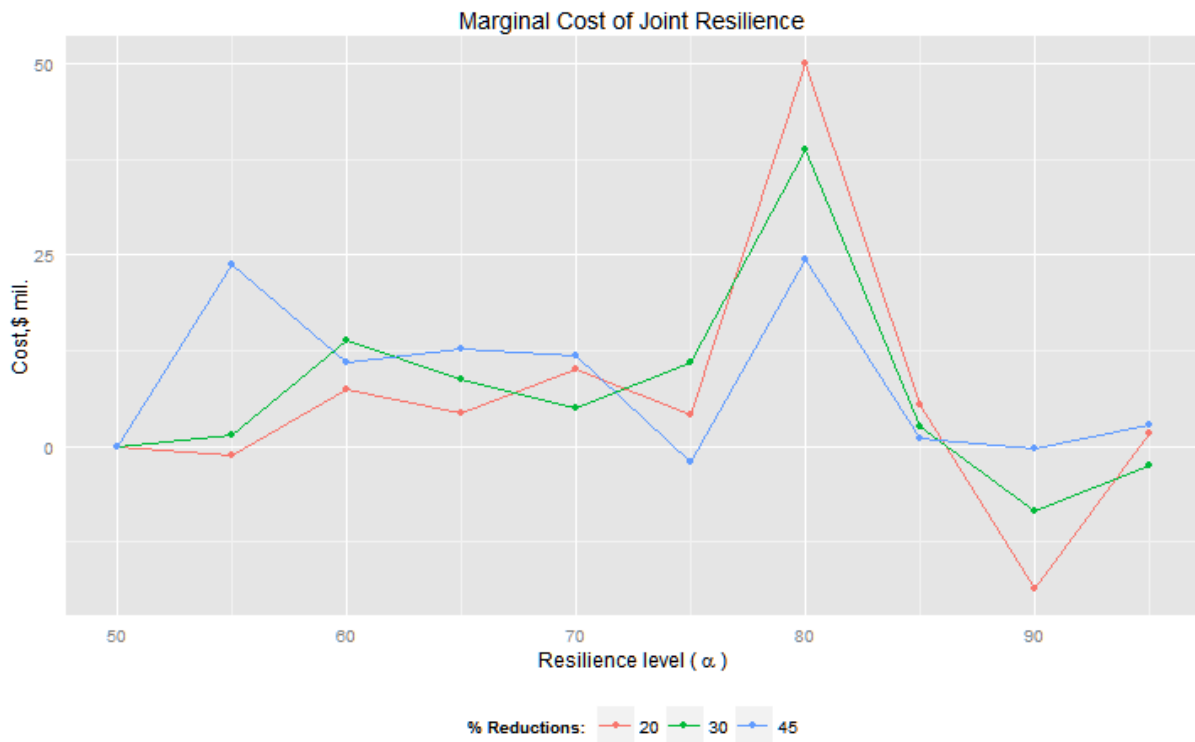
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729 Figure 7 Marginal Costs of Joint Resilience



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920 Appendix 1

921 As noted in the text, a solution to the chance-constrained problem (3) must be a member of the Pareto  
922 frontier in the cost-mean-standard deviation space:  $\hat{\mathbf{x}} \subset \mathbf{x}^*$ . The converse is not true: that is, a particular  
923 solution from a multiobjective optimization program need not be optimal for a chance-constraint program.  
924 Obtaining a Pareto-frontier (and a mean-variance frontier) is, in principle, more general, and the specific  
925 weight placed on the standard deviation determines the point of “tangency” between the efficient frontier  
926 and the “ $\alpha$ -isoresilient” pollution load line of form  $E_T \{N(\hat{\mathbf{x}})\} + \phi^\alpha Var(N(\hat{\mathbf{x}}))_T^{0.5} \equiv N(\alpha)$ . Figure 1  
927 graphically depicts this point. For a particular weight  $\phi^\alpha$  placed on the standard deviation, point  $A$  in the  
928 Pareto-frontier would be optimal, while point  $B$  would appear to be suboptimal given  $\phi^\alpha$ . However, for a  
929 different reliability requirement associated with a lower probability of reaching pollution reduction goal,  
930 point  $B$  would be optimal. These considerations require us to “post-process” the simulated Pareto-frontier  
931 when they are collapsed to “resilient” pollution quantities to eliminate original members of the mean-  
932 variance efficient frontiers which appear dominated given a specific distributional assumption or the  
933 desired level of resilience. By construction, any nitrogen load level equal to  $N(\alpha)$  is achieved with  
934 probability  $\alpha$ .

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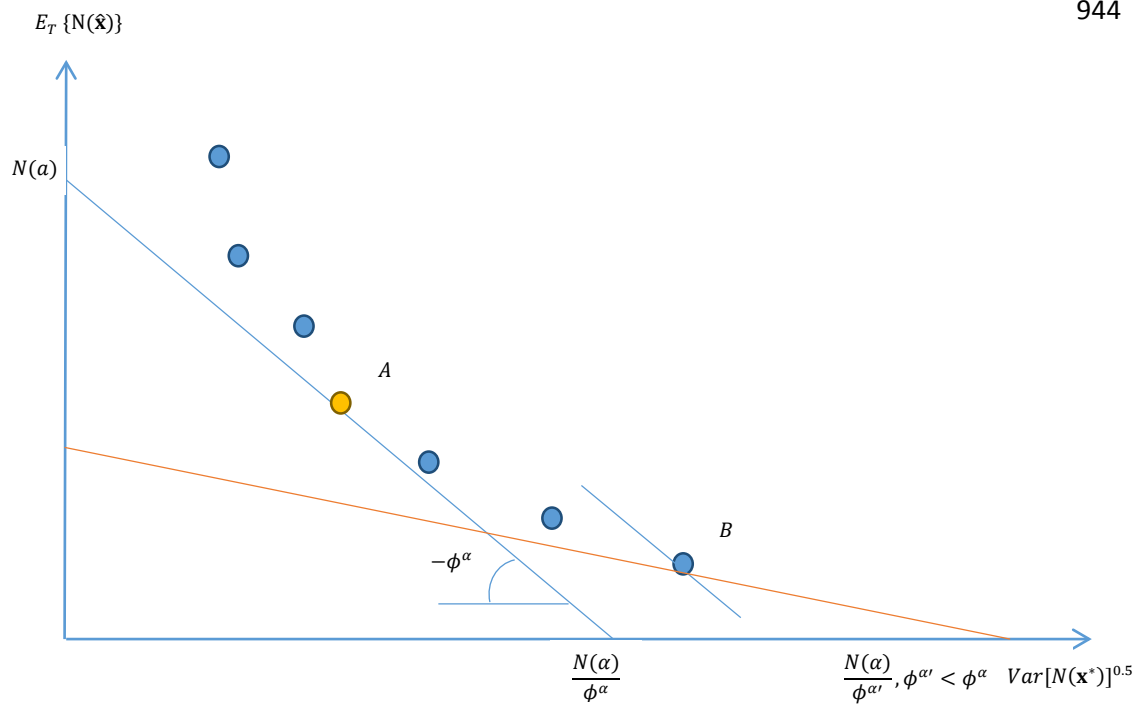
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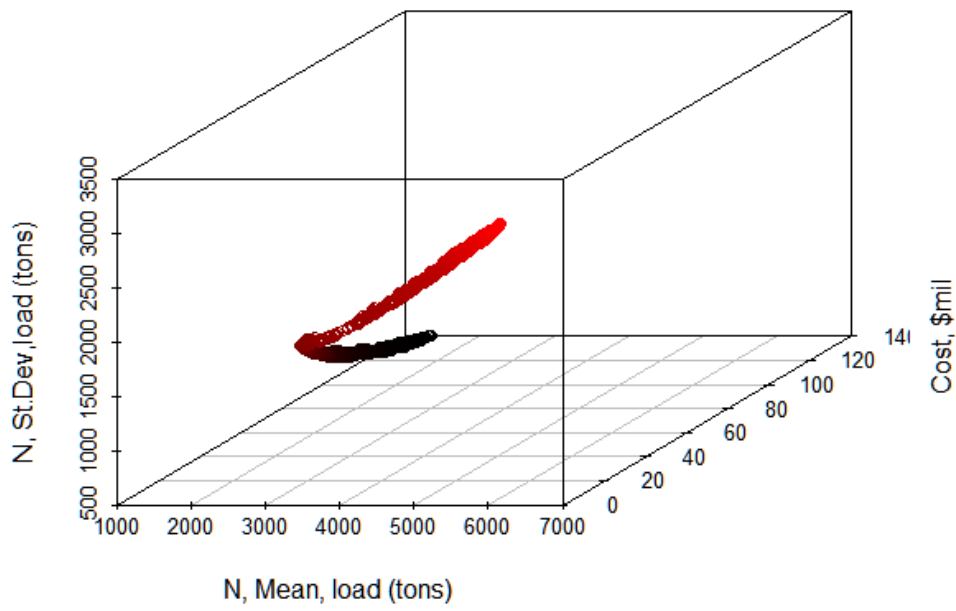




945 Figure A2 The Pareto frontier: Cost-Mean-Standard deviation

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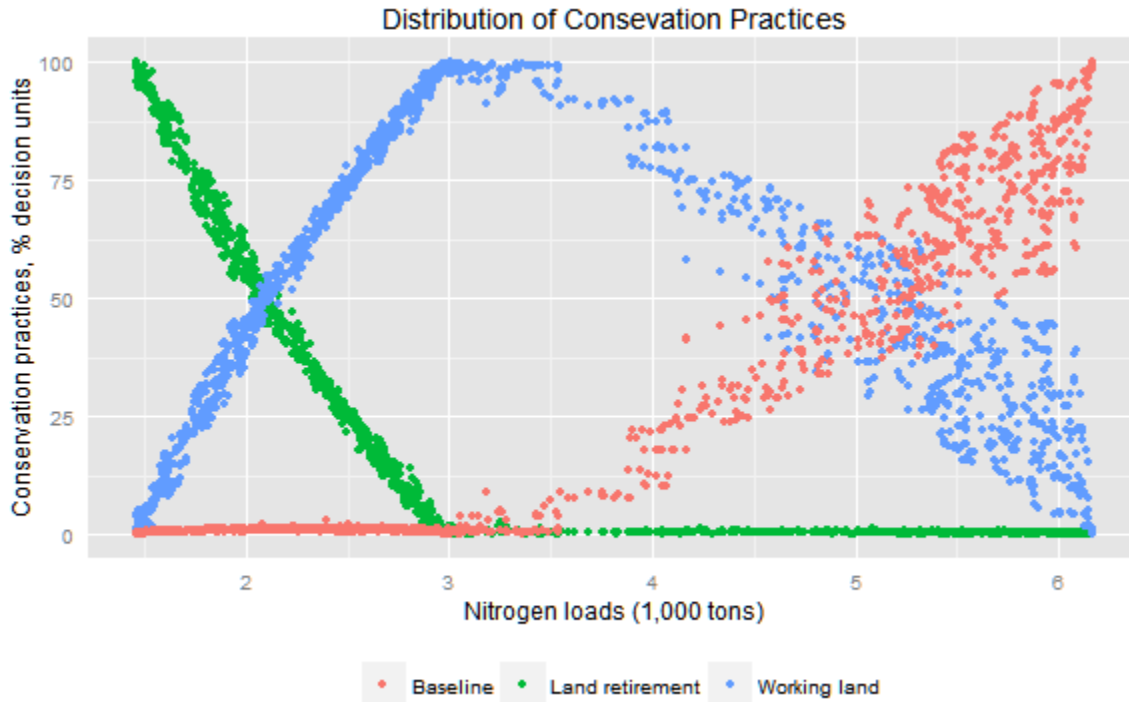


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951 Figure A3: Distribution of Conservation Practices



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953 Figure A3 shows the distribution of conservation practices across the entire set of Pareto-  
954 efficient solutions expressed as the percentage of the number of decision-making units (“fields”)  
955 selected to a type of conservation practice.<sup>13</sup>

956 We group cover crops, no-till and their combination into a single category labeled as  
957 “Working Land”. “Baseline” represents the case where no action is taken, and “Land  
958 Retirement” considers taking land out of agricultural production. As expected, lower levels of  
959 nutrient loads can be achieved by placing land in land retirement, and larger loads correspond to  
960 using “Working Land” conservation actions.

<sup>13</sup> The decision-making unit in the analysis is an HRU, or a Hydrologic Response Unit (see Gassman, 2008).

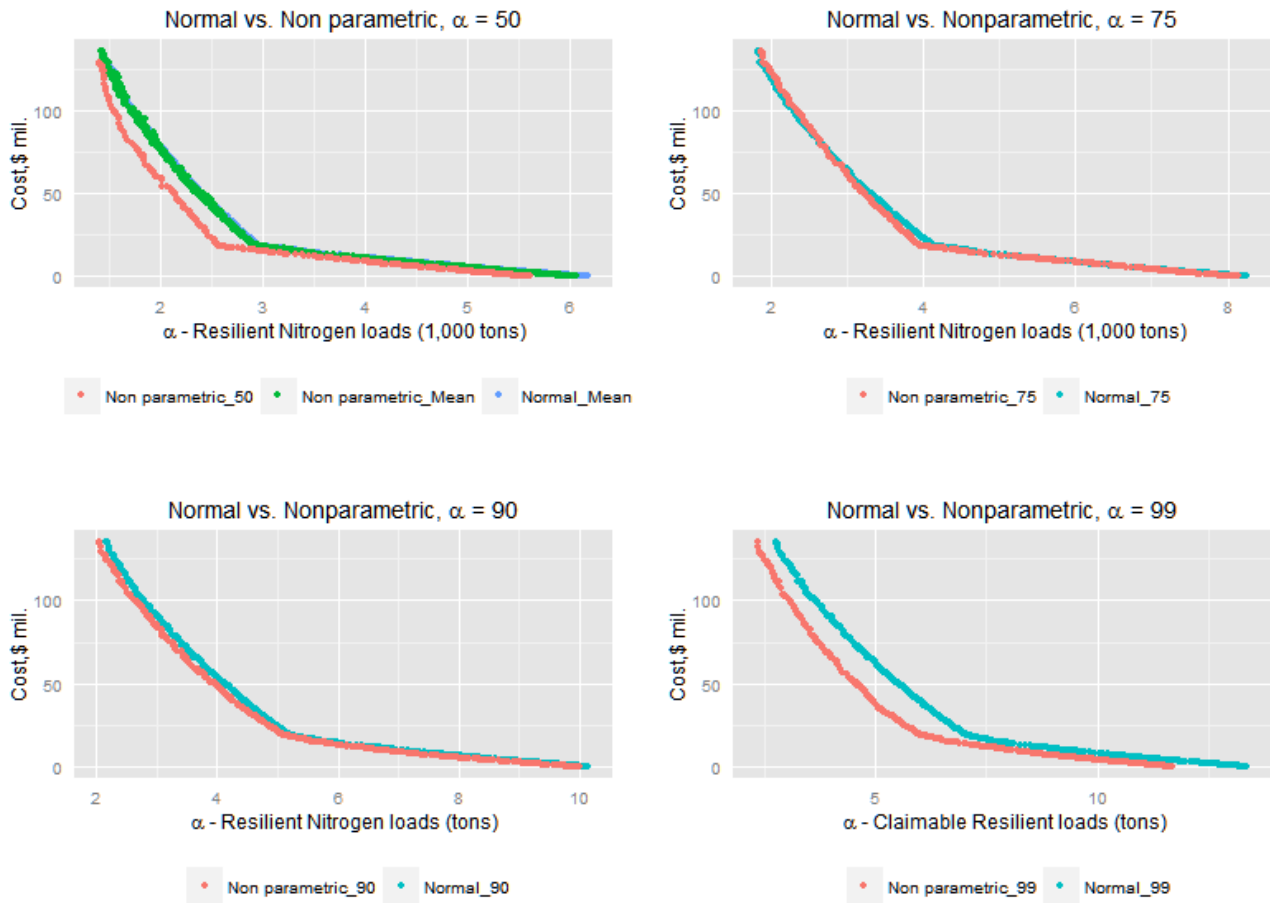
961           The three groups each display an inflection point that corresponds approximatively to the  
962 same level of emissions. Hence, the steeper part in Figure 1(b) can be explained by the decline in  
963 the use of “Land Retirement”; the smoother decreasing part is explained by the decline in  
964 ”Working Land”, while the relatively flat area is explained by the increase in the baseline. These  
965 trends suggest that land retirement leads to lower variation in N pollution and targets with higher  
966 resilience will require using it extensively (following Gren 2010, one can say that land retirement  
967 possesses “resilience value” with respect to nutrient reductions). Similar variation-reducing  
968 properties of simulating land retirement were reported in Rabotyagov, Jha, and Campbell (2010).  
969 The inflection point can be also explained by the limited effectiveness of the “working land”  
970 practices considered in reducing N and by the fact that “Land Retirement” is the most effective  
971 conservation practice. The inflection point corresponds to a low level of emissions (high level of  
972 targets), where steep increases in land retirement are needed to attain those expected reductions  
973 in N.

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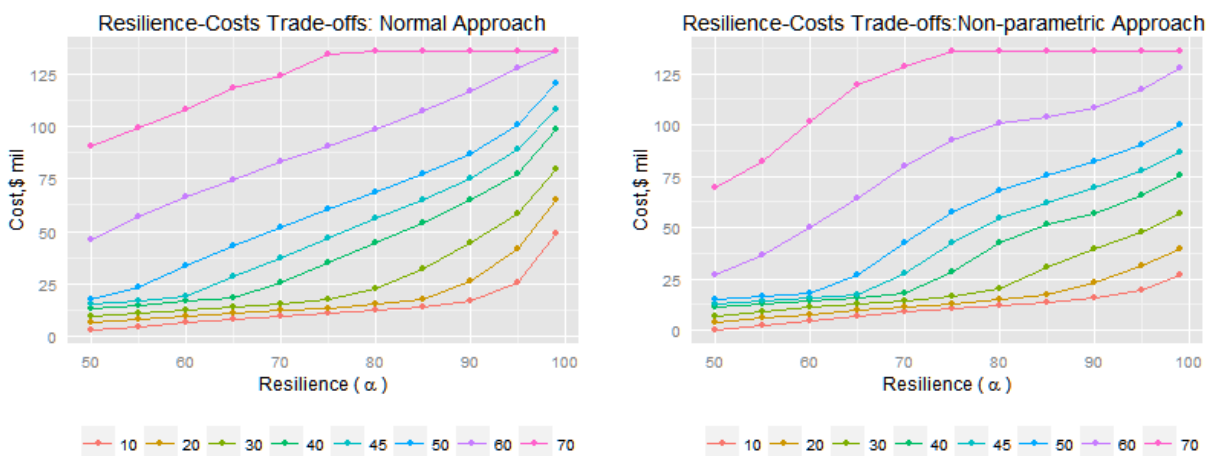
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Figure A4 Comparison  $\alpha$ -resilient Pareto Frontiers



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978 Figure A5 Cost-Resilience Trade-offs



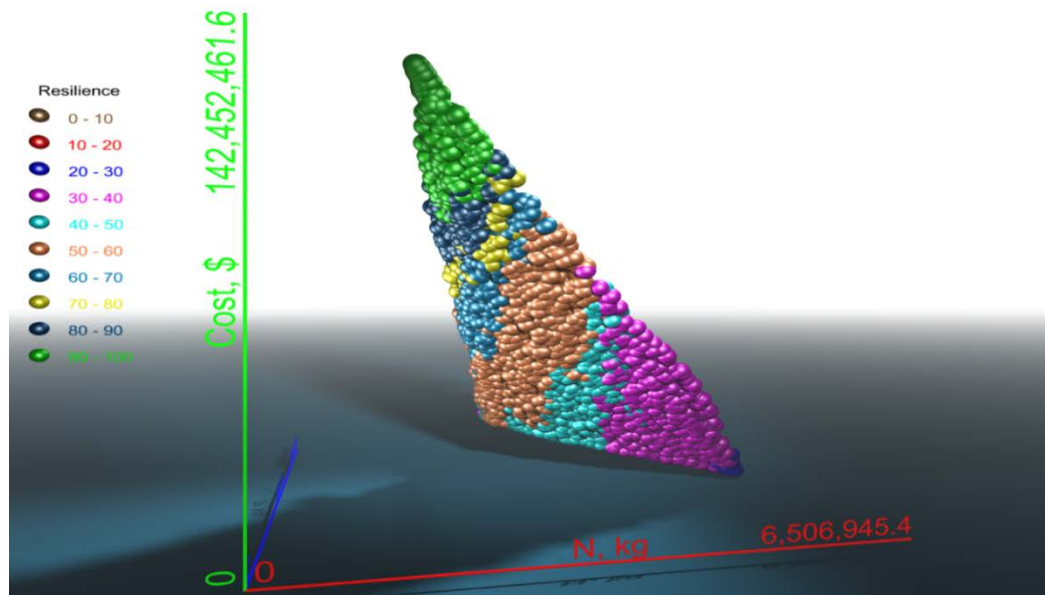
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980           Figure A4 compares pairwise the resilient Pareto frontiers under the two approaches. The  
981 comparisons suggest that the non-parametric distribution has lighter tails than the normal  
982 distribution. This difference suggests that for a very large resilience (99), the critical value for  
983 standard normal is too conservative relative to the corresponding bootstrapped quantile. Figure  
984 A5 summarizes the resilience - cost trade-offs for achieving the same level of resilient N loads.  
985 We define a set of eight nitrogen load targets ( $\bar{N}_i$ ) each corresponding to reductions in the  
986 historical loads ranging from 10 percent to 70 percent.

987

988 Figure A6 Resilience-Nitrogen-Phosphorus Trade-offs

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990

991 A three dimension illustration of this tradeoffs when the targets are set equal to 45  
992 percent reductions for both N and P (equation 9) is presented in the supplemental material  
993 (Figure A6). Each element on this frontier (a 3-dimensional projection of the 5-dimensional  
994 Pareto-frontier  $P_f^{NP}$ ) is assessed for a resilience (probability) level of achieving this joint target.  
995 As for the single pollutant case: securing higher level of resilience demands higher costs.  
996 Furthermore, the elements in the upper part of the curve (green colored) have the highest level of  
997 resilience (higher than 90 percent) but at the same time they have the highest total costs. From  
998 Figure 10, one can see that for a particular interval of joint resilience, there is more than one  
999 solution on the frontier. Thus, it is likely, that for a particular level of simulated joint resilience,  
1000 multiple solutions would be present (for example, both a solution which over-reduces N but just  
1001 reduces P to satisfy the desired P-resilience and a solution that just satisfies the criterion of joint  
1002 resilience would be present). Figure A7 summarizes the results of this kind of phenomenon for

1003 ten levels of joint resilience. Note the similarity to considerations discussed in connection with  
1004 figure 1.

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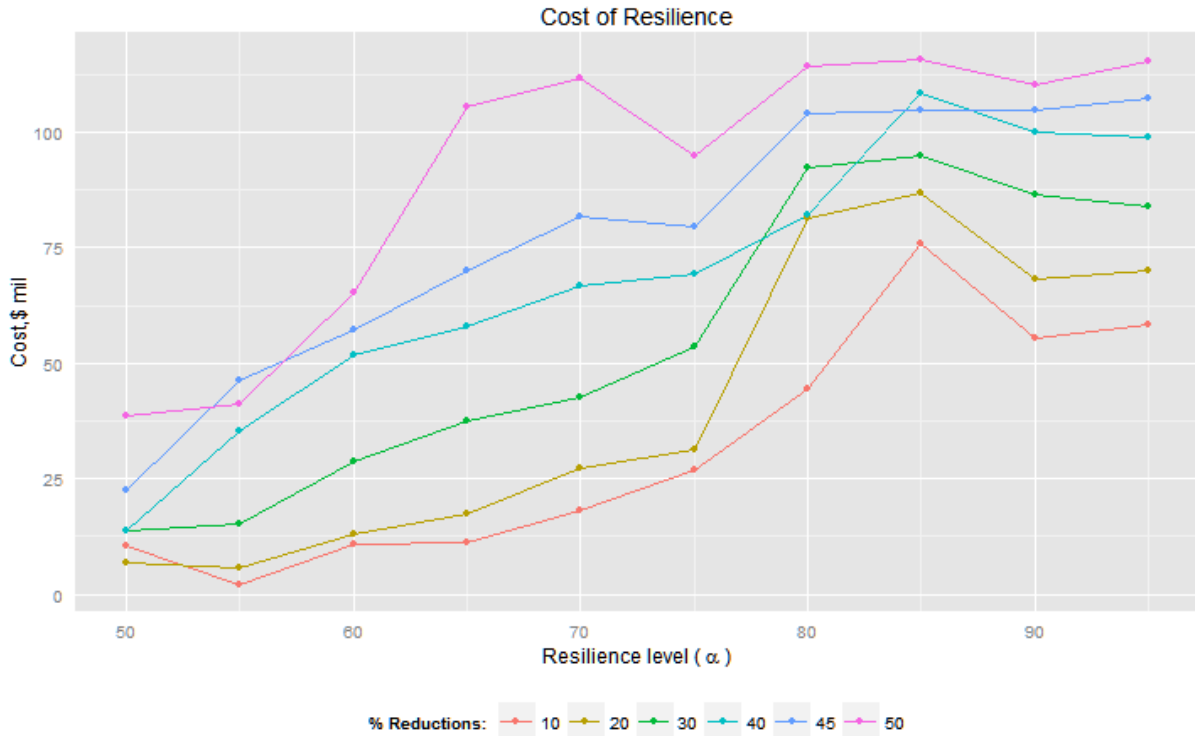
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1010 **Figure A7 Cost of Resilience under Joint Target**



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1012 Figure A7 depicts the cost curves associated with the set of joint resilient targets. As in the single

1013 pollutant case, these curves are mostly increasing, although some of the cost curves for less

1014 stringent targets cross the cost curves for more restrictive targets, although the overlaps take

1015 place in the range of higher resilient levels. This behavior is a manifestation of inefficiencies

1016 present in the overall tradeoff frontier when evaluated from a point of view of specific nutrient

1017 reductions and their joint resilience. We conjecture that developing tailored algorithms

1018 associated with each of the lines presented would a) restore the ranking of the curves and

1019 eliminate the overlap and b) would eliminate the spikes in individual curves and therefore

1020 negative marginal costs of additional resilience.

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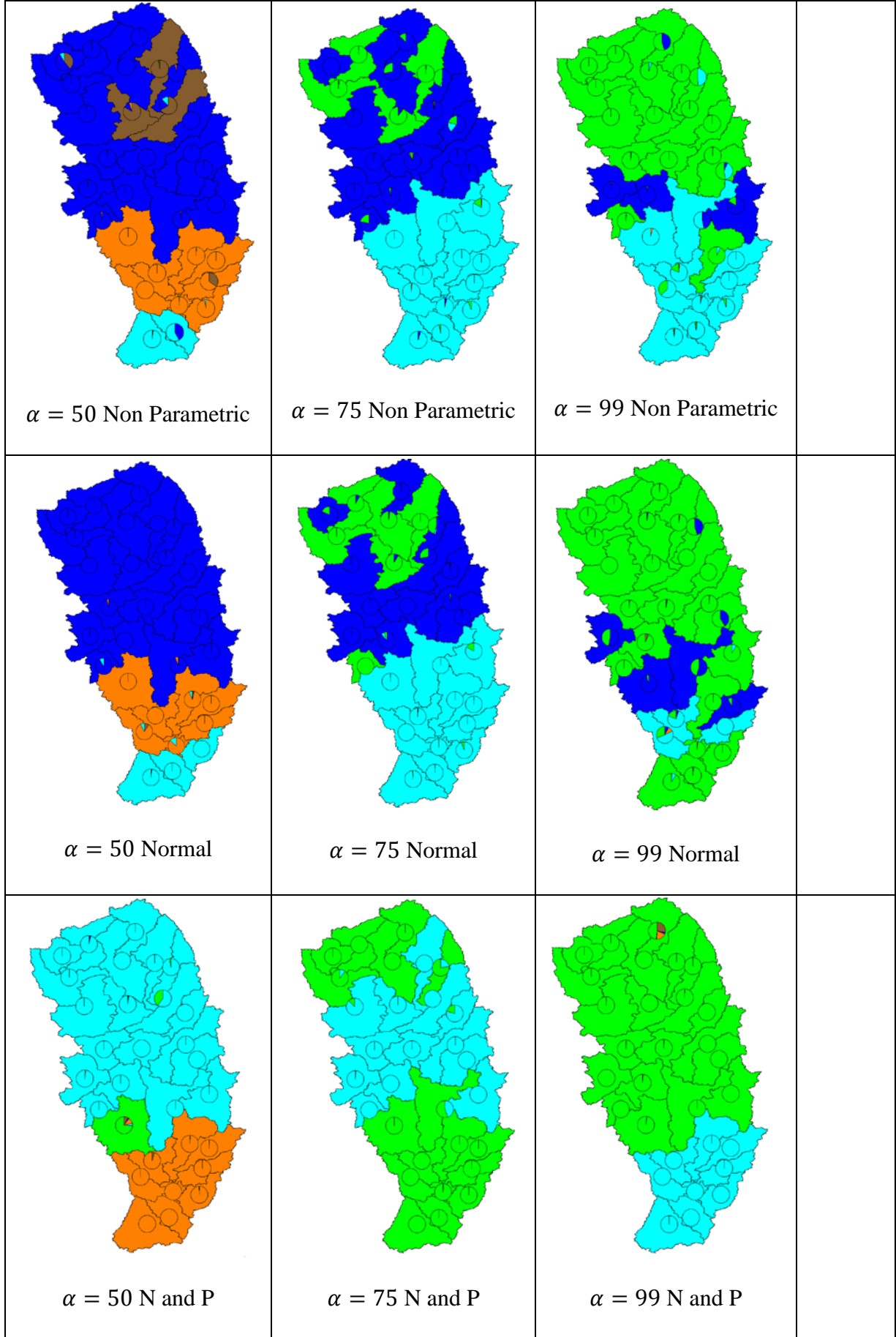
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1025 Figure A8 Spatial Distribution of Conservation Practices in the Watershed.

1026 As shown by our empirical findings, the distribution of conservation practices differs across  
1027 resilience level. This implies that the spatial distribution will be very different. The next figures  
1028 show the spatial placement of conservation practices when the target is set to 45 percent  
1029 reductions and for three resilience levels: 50, 75, and 99.

1030 Figure A8 depicts the spatial placement of the conservation practices in the watershed  
1031 when the target is set equal to 45 percent reductions for N only and for joint N and P for three  
1032 resilience levels: 50, 75, and 99. The watershed configurations reinforce the previous findings:  
1033 higher resilience levels require extensive use of land retirement, with more land retirement being  
1034 used when both N and P are targeted. The non-parametric and normal watershed configurations  
1035 are very similar when resilience levels are 50 or 75. However, the normal 99 resilience  
1036 configuration has higher use of land retirement. This confirms the fact that the 99<sup>th</sup> quantile value  
1037 for the standard normal is too conservative relative to the non-parametric quantile.

1038



1039 Brown: Baseline; Orange: No-till; Blue: Cover Crops, Light Blue: Cover Crop and No-till,  
1040 Green: Land Retirement. The main color represents the dominant color at sub-basin level. The  
1041 pie charts represent percentage use for the entire set of practices<sup>14</sup>.  
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<sup>14</sup> There are 2122 HRUs (*K* decision units). They are grouped in thirty sub-basins.

1043 Table A1 Cost-Resilient Solutions; N reductions = 45% (target N=3.39 thousand tons N)

Resilience( $\alpha$ , %)	Cost	Marginal	Working	Land	Baseline	Cost	Marginal	Working	Land	Baseline
	(mil. \$)	Cost (mil. \$)	Land (%)	Retirement (%)	(%)	(mil. \$)	Cost (mil. \$)	Land (%)	Retirement (%)	(%)
Non-parametric						Normal				
50	12.94	0.00	91.70	0.50	7.90	15.16	0.00	99.20	0.20	0.60
55	14.47	1.52	99.20	0.20	0.60	17.08	1.92	98.30	1.00	0.80
60	16.04	1.57	96.70	0.30	3.00	19.25	2.17	98.90	0.60	0.50
65	17.61	1.57	97.90	0.20	1.90	28.36	9.11	89.80	9.50	0.80
70	27.47	9.86	93.10	5.90	1.00	37.21	8.85	78.80	20.00	1.20
75	42.40	14.93	75.50	23.20	1.20	46.89	9.68	71.40	28.00	0.60
80	54.38	11.99	63.10	35.90	1.00	56.39	9.50	64.10	35.10	0.80
85	62.06	7.68	54.40	44.60	0.90	65.27	8.88	54.90	44.20	0.90
90	69.76	7.70	48.60	50.20	1.20	75.43	10.16	44.70	54.10	1.30
95	77.54	7.78	41.20	57.80	0.90	88.93	13.50	31.50	67.60	0.90
99	86.99	9.45	40.80	58.40	0.80	107.96	19.03	17.80	81.60	0.60

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1045 Table A1 describes in detail the cost-resilient solutions for achieving the three levels of  
 1046 claimable nitrogen reductions for increments of about five percent increase in the resilience level  
 1047 from 50 to 99 probability levels for the two approaches. Column 1 shows the resilience levels  $\alpha$ ;  
 1048 and subsequent columns show the annual costs for achieving the required resilient loads for each  
 1049 level of resilience (million \$), the marginal cost of achieving each additional level of resilience  
 1050 (million \$). The following columns describe the distribution of the conservations practices:  
 1051 working land, land retirement and baseline (percentages of total decision-making units). We  
 1052 focus our analysis for case where the target is set equal to 45 percent reductions. . Resilience

1053 levels lower than 70 percent are characterized by high use of working land conservation practices  
1054 (higher than 93 percent). In order to secure higher levels of resilience more land is allocated to  
1055 land retirement, but the increase takes place at a decreasing rate. For example, the use of land  
1056 retirement increases from 5.9 percent (resilience level 70) to 23.2 percent (resilience level 75) (  
1057 i.e. a total increase of 17 percent), but it takes only 6 additional percent to move for a resilience  
1058 level of 85 to 90.

1059           Next, we compare the costs and distribution of the conservation practices when the target  
1060 is set at 45 percent reductions using normal approach with the ones described above. The total  
1061 costs under the normal approach are slightly higher than under the non-parametric approach  
1062 ranging from 15.94 to 107.96 million per year across different level of resilience. Lower levels of  
1063 resilience are achieved by using working land conservation on a large number of fields (higher  
1064 than 98 percent). Similarly, securing higher level of resilience requires putting more land in land  
1065 retirement, but the use of land retirement increases at an increasing rather than decreasing rate.  
1066 The increasing factor also explains the increasing trends in the marginal costs. Additionally, the  
1067 optimal resilient loads ( $N(\alpha)$ ) are a bit higher (less reductions) under the normal approach.

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1070 Table A2 Cost of Joint Resilience, 45% Reduction Target in N and P (N=3.39 thousand tons,  
 1071 P=0.09 thousand tons)

Resilience ( $\alpha$ , %)	Cost (mil. \$)	Marginal Cost (mil. \$)	Working Land (%)	Land Retirement (%)	Baseline (%)
50	22.39	0.00	97.64	1.23	1.13
55	46.23	23.84	71.58	26.20	2.21
60	57.18	10.95	62.16	36.66	1.18
65	69.96	12.78	54.71	42.27	3.02
70	81.67	11.72	37.23	59.38	3.39
75	79.54	-2.13	44.16	55.75	0.09
80	103.92	24.37	22.48	76.34	1.18
85	104.99	1.07	21.54	77.43	1.04
90	104.72	-0.27	23.61	75.59	0.80
95	107.38	2.67	29.59	69.70	0.71

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