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Intra-Industry Trade, Imperfect Competition, Trade Integration and Invasive Species Risk

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Abstract: We analyze the linkage between protectionism and invasive species hazard in the context of imperfect competition, two-way trade, and multilateral trade liberalization, three major actual features of agricultural trade and policies in the real world. We revisit the reciprocal-dumping model with differentiated products, adding trade and agricultural policies into the framework in the presence of invasive-species risk associated with agriculture. We look at joint reduction of agricultural tariffs. This type of trade integration is much more likely to increase the damage from invasive species than predicted by unilateral trade liberalization under the classical HOS framework. We document the non-monotonic relationship between policy (trade barriers and farm subsidies) and the expected damages from invasive species. We illustrate our analytical results with a stylized model of the world wheat market.

# Intra-Industry Trade, Imperfect Competition, Trade Integration and Invasive Species Risk 1. Introduction

The links between international trade and the environment, are multiple, complex and have been a topic of continuing heated debate (Copeland and Taylor; Beghin, Roland-Holst, and van der Mensbrugghe). International trade can be an important driver of environmental change. In the 1990s a related literature has emerged on the interface between trade and sanitary and phyto sanitary (SPS) issues (see Beghin and Bureau for a review). A more recent literature is emerging at the triple interface of trade, the environment and SPS issues, namely on trade and invasive species (IS), with a focus on accidental introductions of exotic species like pests, weeds, and viruses, by way of trade (Perrings, Williamson and Dalmazzone; Mumford). The trade-SPS-environment interface is almost inherent to the economics of IS since trade is a major vector of propagation of these species, although it is not the only one. Many papers in this new literature are focused on the "right" criteria to use or the optimal environmental policy response to the hazard of IS (Sumner; Binder) and around quarantine as a legitimate policy response to phytosanitary risk (Cook and Frazer; Anderson et al.). Our paper contributes to this new literature on trade and IS risk in the specific context of agricultural markets and trade.

Agricultural imports have always been an important conduit for biological invasions (CABI). Despite of the Uruguay Round Agreement of the WTO, protection remains high in agriculture and its reduction in future trade agreements will influence agricultural trade patterns and associated IS damages. Elucidating the impact of the structure of agricultural protection on IS hazards and damages is an important question. In a standard one-way trade Hechsher-Ohlin-Samuelson (HOS) model, Costello and McAusland show that lowering agricultural tariffs could lower the damage from exotic species, even though the volume of trade rises and the rate of IS

<sup>&</sup>lt;sup>1</sup> "Natural" invasions occur because of natural vectors (weather related ones, animal migration).

introduction rises, because an increase in imports results in a reduced domestic agricultural output. Thus the crop volume susceptible and available for damage and the land area potentially affected by the pest are reduced, hence damages can be reduced as well leading to an ambiguous effect of trade on IS damages.

Our paper builds upon the enquiry of Costello and McAusland. We make major departures by analyzing the linkage between protectionism and damages from IS in the context of imperfect competition, two-way trade and multilateral trade liberalization. Intra-industry trade and imperfect competition characterize agricultural trade patterns in the real world. For example, wheat trade is oligopolistic and wheat is a differentiated commodity with most countries importing and exporting wheat (See Table 1). Two-way trade patterns hold even more for more broadly defined commodities such as coarse grains as shown in table 2. The HOS framework has limited empirical relevance in this context.

We also depart with the previous analysis by considering multilateral trade liberalization. Trade integration occurs mostly through multilateral or regional agreements (e.g., The Uruguay Round of the WTO, NAFTA). Seldom do countries engage in unilateral trade liberalization but rather commit to jointly reduce their protection through regional or multilateral agreements.<sup>2</sup> Another argument to consider joint reforms is that transaction costs have been falling for both exports and imports through cheaper transportation, cheaper refrigeration and insurance, etc. Joint tariff reduction mimics the joint lowering of transaction costs on both sides of any border.

We revisit the reciprocal dumping model considering differentiated products and adding trade into the framework. We consider joint tariff reductions and their effect on expected IS damage. We find that this type of trade integration is much more likely to increase expected

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<sup>&</sup>lt;sup>2</sup> There are exceptions such as New Zealand's unilateral trade liberalization in the 1980s but by and large joint reforms are much more common (Bhagwati).

damage from exotic species in our two-way trade model, as compared to unilateral liberalization and on-way trade. Hence the unexpected ambiguity of Costello and McAusland is much reduced in with our more realistic setup.

Domestic farm subsidies are another consideration. Agriculture in OECD countries is characterized by heavy subsidies which have to some extent, substituted for the lower border protection (OECD). Since 1996 these subsidies have been slowly reduced as part of the Uruguay Round Agreement on Agriculture (URAA). The current Doha round is also considering sharper reductions in production subsidies in agriculture. We incorporate this second-best dimension of domestic subsidies in our analysis of trade integration and their role on IS risk introduction and damages. We document the non-monotonic relationship between protection structure (border and domestic policies) and damages from exotic species introduction. We focus on the key role of domestic subsidies and their reform to either increase or decrease IS introduction and damage.

The remainder of the paper is organized as follows. The trade model is presented next. Section 3 models the IS introduction. Then the linkage between trade reform and IS introduction is then established. We illustrate and examine the robustness of the results in section 5 by calibrating the analytical model to recent data on wheat trade and the associated damages from exotic species. Summary remarks then conclude the paper.

#### 2. A segmented-market model with differentiated product

Assume that there are two countries, Home and Foreign, and that each country has one firm producing commodity Z. Assume that each firm regards each country as a separate market and therefore chooses the profit-maximizing quantity for each country separately by making price discrimination of the third degree. The Home firm produces output x for domestic consumption

and output x\* for Foreign consumption. Similarly, the Foreign firm produces output y for export to Home, and output y\* for its own market. The idea was first proposed by Brander (1981) and elaborated by Brander and Krugman (1983).

Assume that Home good and Foreign good are imperfect substitutes in each market such that the Home demands for domestic good and imports are

(1) 
$$x(p_x, p_y) = a_x - b_x p_x + k p_y$$
, and

(2) 
$$y(p_x, p_y) = a_y - b_y p_y + k p_x$$
,

where  $(p_x, p_y)$  are price of Home and Foreign goods in the Home market. All parameters are assumed to be positive and so is expression  $b_x b_y - k^2$  by integrability of a demand system derived by maximizing a quasi-linear utility under budget constraint (see appendix 1).

Similarly, Foreign demands for its own domestic good and the imports are

(3) 
$$y*(p_x^*, p_y^*) = a_y^* - b_{y*}p_y^* + kp_x^*$$
, and

(4) 
$$x*(p_x^*, p_y^*) = a_x^* - b_{x*}p_x^* + kp_y^*.$$

Again, all parameters are assumed to be positive and so is expression  $b_{x*}b_{y*}-k^2$ .

Assume that Home and Foreign governments impose tariffs on imports  $(\tau, \tau^*)$  and subsidize their production  $(s, s^*)$  with subsidies being proportional to their unit cost, c. Tariffs and subsidies are expressed in ad valorem rate. Home and Foreign firm' problems are

(5) 
$$\underset{w.r.t.\{p_x,p_x^*\}}{\text{Max}} \pi(\vec{p},\vec{\tau},s) = [p_x - c(1-s)]x(p_x,p_y(1+\tau)) + [p_x^* - c(1-s)]x*(p_x^*(1+\tau^*),p_y^*) - FC$$
, and

$$(6) \underset{w.r.t.\{p_{y},p_{y}^{*}\}}{\textit{Max}} \pi^{*}(\vec{p},\vec{\tau},s^{*}) = \left[p_{y} - c(1-s^{*})\right] y\left(p_{x},p_{y}(1+\tau)\right) + \left[p_{y}^{*} - c(1-s^{*})\right] y^{*}\left(p_{x}^{*}(1+\tau^{*}),p_{y}^{*}\right) - FC^{*},$$

respectively, where  $\vec{p} = (p_x, p_x^*, p_y, p_y^*)$ ,  $\vec{\tau} = (\tau, \tau^*)$ , and FC and FC\* are fixed costs of the Home and Foreign firm. This setting is similar to the "reciprocal dumping" model of Brander and

Krugman (1983), except that these authors worked with homogenous goods and did not introduce trade and agricultural policies into the analysis. The Home firm's best responses are

(7) 
$$BR_x^H(p_y) = \{ [a_x + b_x c(1-s)] + k(1+\tau) p_y \} / 2b_x$$
, and

(8) 
$$BR_{x^*}^H(p_y^*) = \left\{ \left[ a_x^* + b_{x^*}c(1-s)(1+\tau^*) \right] + kp_y^* \right\} / 2b_x^*(1+\tau^*).$$

The Foreign firm's best responses are

(9) 
$$BR_v^F(p_x) = \{ [a_v + b_v c(1-s^*)(1+\tau)] + kp_x \} / 2b_v (1+\tau), \text{ and } \}$$

(10) 
$$BR_{y^*}^F(p_x^*) = \left\{ \left[ a_y^* + b_{y^*}c(1-s^*) \right] + k(1+\tau^*)p_x^* \right\} / 2b_y^*.$$

Equilibrium in the two countries' markets can be solved independently. That is, equations (7) and (9) simultaneously define the equilibrium prices in the Home markets  $(P_x, P_y)$ , and equations (8) and (10) simultaneously define the equilibrium prices in the Foreign markets  $(P_x^*, P_y^*)$ . Appendix 2 establishes the existence and uniqueness of the Bertrand equilibrium in our model; two-way trade exists given arbitrary trade and agricultural policies.

Home and Foreign equilibrium quantities consumed for both goods are

(11) 
$$X(\vec{s},\tau) = \frac{b_x}{D} \left\{ 2a_x b_y + ka_y + c(1-s)(k^2 - 2b_x b_y) + kb_y (1-s^*)(1+\tau) \right\},$$

(12) 
$$Y(\vec{s},\tau) = \frac{b_y}{D} \left\{ 2a_y b_x + ka_x + ckb_x (1-s) + c(k^2 - 2b_x b_y)(1-s^*)(1+\tau) \right\},$$

(13) 
$$X * (\vec{s}, \tau^*) = \frac{b_x^*}{D^*} \left\{ 2a_x^* b_y^* + ka_y^* + c(1 - s^*)(k^2 - 2b_x^* b_y^*) + kb_y^* (1 - s)(1 + \tau^*) \right\}, \text{ and}$$

(14) 
$$Y * (\vec{s}, \tau^*) = \frac{b_y^*}{D^*} \left\{ 2a_y^* b_x^* + ka_x^* + ckb_x^* (1 - s^*) + c(k^2 - 2b_x^* b_y^*) (1 - s) (1 + \tau^*) \right\},$$

with  $\vec{s} = (s, s^*)$ ,  $D = 4b_x b_y - k^2$  and  $D^* = 4b_x^* b_y^* - k^2$ . Home equilibrium production is

$$Q(\vec{s}, \vec{\tau}) = X(\vec{s}, \tau) + X * (\vec{s}, \tau^*).$$

We use the following intermediate results, which are derived in appendix 3.

**Corollary 1:** Given the demand structure as specified in equations (1)-(4), the following relations hold in equilibrium: (i)  $\partial X */\partial \tau = 0$ ,  $\partial X */\partial s > 0$ ,  $\partial X */\partial \tau *< 0$ ,  $\partial X */\partial s *< 0$ ;

(ii) 
$$\partial X/\partial \tau > 0$$
,  $\partial X/\partial s > 0$ ,  $\partial X/\partial \tau^* = 0$ ,  $\partial X/\partial s^* < 0$ ; (iii)  $\partial Q/\partial \tau > 0$ ,  $\partial Q/\partial s > 0$ ,  $\partial Q/\partial \tau^* < 0$ ,  $\partial Q/\partial s^* < 0$ ; and (iv)  $\partial Y/\partial \tau < 0$ ,  $\partial Y/\partial s < 0$ ,  $\partial Y/\partial \tau^* = 0$ ,  $\partial Y/\partial s^* > 0$ .

#### The comparative-statics of policy reform

We now consider the effects of trade integration and domestic reforms on Home import and Home production in equilibrium. Recall that under the URAA, WTO member countries had to achieve two major policy changes. First, "tariffication" and market access had to occur. Countries had to convert quantitative restrictions on imports into bound tariffs, and then reduce these tariffs over an implementation period, and open their markets to imports under the minimum access provision. Second, a reduction of distorting domestic support was implemented to limit and reduce the most trade-distorting forms of domestic subsidies. We parameterize these reforms in our model as a joint reduction of tariffs and production subsidies as follows.

Assume that trade negotiations yields the joint trade policy reform outcome  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$ , i.e., a proportional decrease of tariffs, where  $\kappa$  is any arbitrary positive fraction. We also look at the case in which domestic policy is also reduced. To simplify the comparative-statics we assume that the reduction in domestic subsidies is a fraction  $\alpha$  of the tariff reduction or  $ds = \alpha d\tau$  and  $ds^* = \alpha d\tau^*$ .

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<sup>&</sup>lt;sup>3</sup> Alternatively one could consider that domestic support actually endogenously increases by political economic forces to offset the loss of border protection.

Totally differentiate Home equilibrium production  $Q(\vec{s}, \vec{\tau})$  to get <sup>4</sup>

$$dQ = \frac{\partial Q}{\partial \tau} d\tau + \frac{\partial Q}{\partial \tau^*} d\tau^* + \frac{\partial Q}{\partial s} ds + \frac{\partial Q}{\partial s^*} ds^*$$

$$(15) \qquad = \tau \frac{\partial Q}{\partial \tau} \frac{d\tau}{\tau} + \tau^* \frac{\partial Q}{\partial \tau^*} \frac{d\tau^*}{\tau^*} + \alpha \tau \frac{\partial Q}{\partial s} \frac{d\tau}{\tau} + \alpha \tau^* \frac{\partial Q}{\partial s^*} \frac{d\tau^*}{\tau^*}$$

$$= -\kappa \left( \tau \frac{\partial Q}{\partial \tau} + \tau^* \frac{\partial Q}{\partial \tau^*} + \alpha \tau \frac{\partial Q}{\partial s} + \alpha \tau^* \frac{\partial Q}{\partial s^*} \right).$$

Similarly, we obtain the following by taking total differentiation of  $Y(\vec{s},\tau)$ :

(16) 
$$dY = -\kappa \left( \tau \frac{\partial Y}{\partial \tau} + \alpha \tau \frac{\partial Y}{\partial s} + \alpha \tau * \frac{\partial Y}{\partial s *} \right).$$

We will use equations (15) and (16) in different trade "integration" and domestic reform scenarios to examine the relation between trade and domestic policy reforms and the damages from exotic species. We consider the following scenarios:

- 1. Only trade policies are active and reformed, i.e.  $s = s^* = 0$ , and  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$ .
- 2. Both trade and agricultural policies are active, but only tariffs are lowered,  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa \text{ and } ds = ds^* = 0, \text{ although s and s* are different from zero.}$
- 3. Both trade and agricultural policies are active, but only Home government subsidizes their production, i.e.  $s^* = 0$ . Trade and agricultural policy reforms take place such that  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa \text{ and } ds = \alpha d\tau.$
- 4. Both trade and agricultural policies are active. Trade and agricultural policy reforms take place such that  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$ ,  $ds = \alpha d\tau$  and  $ds^* = \alpha d\tau^*$ .

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<sup>&</sup>lt;sup>4</sup> Since  $ds = \alpha d\tau$  and  $ds^* = \alpha d\tau^*$ .

#### 3. Modeling IS hazard and policy interface

We elaborate on the framework followed by Costello and McAusland accounting for our setup with an oligopolistic industry, two-way trade and multilateral trade reforms. We assume that the arrival time of exotic species is stochastic and that the inter-arrival time between two successive introductions is an exponentially distributed random variable with mean  $1/\gamma$ . Assume that  $\gamma$  is increasing in the volume of imports Y. Adopting Costello and McAusland's formulation, we write the expected value of type-k damage through time T as

(17) 
$$E[D^{k}(T)] = \rho \gamma(Y) E_{\delta} \int_{0}^{T} F_{t}^{k}(\delta, Q) dt,$$

where  $\rho$  is the probability that an introduced species established a viable population in Home, and  $F_t^k(\delta,Q)$  is the cumulative density function for the present value of type k damage through time T caused by the  $i^{th}$  successful introduction  $D_i^k(T)$ , conditional on  $t_i$ , that is the probability that a successful arrival at time  $t_i$  has a present value of type-k damage by time T of less than  $\delta$ , given the total production Q.

To understand the effect of trade liberalization on the damage from exotic species, we seek the sign of the total derivative

(18) 
$$dED = \rho \gamma F_{Q} \left[ Q_{\tau} d\tau + Q_{s} ds + Q_{\tau*} d\tau^{*} + Q_{s*} ds^{*} \right] + \rho \gamma_{Y} F \left[ Y_{\tau} d\tau + Y_{s} ds + Y_{\tau*} d\tau^{*} + Y_{s*} ds^{*} \right],$$

where  $F \equiv E_{\delta} \int_{0}^{T} F_{t}^{k}(\delta, Q) dt$  and  $Z_{\theta} \equiv \partial Z / \partial \theta$  where Z is F, Q or Y, and  $\theta$  is Q,  $\tau, \tau^{*}$ , s or  $s^{*}$ .

Using 
$$\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$$
,  $ds = \alpha d\tau$  and  $ds^* = \alpha d\tau^*$ , after some manipulations, we get

(19) 
$$dED = -\kappa \rho \gamma F \begin{bmatrix} \frac{F_Q}{F} Q_\tau \tau + \frac{\gamma_Y}{\gamma} Y_\tau \tau + \frac{F_Q}{F} Q_{\tau^*} \tau^* + \frac{\gamma_Y}{\gamma} Y_{\tau^*} \tau^* \\ + \frac{F_Q}{F} Q_s \alpha \tau + \frac{\gamma_Y}{\gamma} Y_s \alpha \tau + \frac{F_Q}{F} Q_{s^*} \alpha \tau^* + \frac{\gamma_Y}{\gamma} Y_{s^*} \alpha \tau^* \end{bmatrix}$$
 or

$$=-\kappa\rho\gamma F\begin{bmatrix} \varepsilon^{F_{Q}}\varepsilon^{Q_{r}}+\varepsilon^{\gamma_{r}}\varepsilon^{Y_{r}}+\varepsilon^{F_{Q}}\varepsilon^{Q_{r^{*}}}+\varepsilon^{\gamma_{r}}\varepsilon^{Y_{r^{*}}}\\ +(\varepsilon^{F_{Q}}\varepsilon^{Q_{s}}+\varepsilon^{\gamma_{r}}\varepsilon^{Y_{s}})\alpha\tau/s+(\varepsilon^{F_{Q}}\varepsilon^{Q_{s^{*}}}+\varepsilon^{\gamma_{r}}\varepsilon^{Y_{s^{*}}})\alpha\tau^{*}/s^{*} \end{bmatrix},$$

where  $\varepsilon^{F_Q}$  is the elasticity of expected k damage to the level of agricultural activity,  $\varepsilon^{\gamma_{\ell}}$  is the elasticity of the arrival rate with respect to the volume of imports, and  $\varepsilon^{Q_{\varphi}}$  and  $\varepsilon^{Y_{\varphi}}$  are elasticities of Home production and imports with respect to a policy  $\varphi = (\tau, \tau^*, s, s^*)$ . Variable F is positive as long as expected type-k damage is positive, which we assume to be the case.  $\varepsilon^{\gamma_{\ell}} > 0$  by assumption that high volume of imports increases the arrival rate of success of exotic species introductions. Damages are called augmented (neutral, or diminished) if they increase (remain unchanged, or decrease) as the level of agricultural activity increases (Costello and McAusland). Using this classification, the sign of  $\varepsilon^{F_Q}$  can be determined as the following:

$$\varepsilon^{F_Q} \begin{pmatrix} > 0 \\ = 0 \\ < 0 \end{pmatrix}$$
 if the damages are  $\begin{pmatrix} \text{augmented} \\ \text{neutral} \\ \text{diminished} \end{pmatrix}$ . The first two cases  $(\varepsilon^{F_Q} \ge 0)$  are the most relevant

cases. The signs of the policy effect on imports and productions are left to be determined, and they vary with different policy scenarios.

#### 4. Policy reforms impact on damages from IS introduction

We start with scenarios 1 and 2, that is, policy reform only concerns trade and leads to lower tariffs or  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$ . Under these policy scenarios, equation (16) becomes

$$^{5} \text{ We use } dED = -\kappa \rho \gamma F \begin{bmatrix} \frac{F_{o}Q}{F} \frac{Q_{\tau}\tau}{Q} + \frac{\gamma_{\gamma}Y}{\gamma} \frac{Y_{\tau}\tau}{Y} + \frac{F_{o}Q}{F} \frac{Q_{\tau^{*}}\tau^{*}}{Q} + \frac{\gamma_{\gamma}Y}{\gamma} \frac{Y_{\tau^{*}}\tau^{*}}{Y} \\ + \frac{F_{o}Q}{F} \frac{Q_{s}s}{Q} \frac{\alpha\tau}{s} + \frac{\gamma_{\gamma}Y}{\gamma} \frac{Y_{s}s}{Y} \frac{\alpha\tau}{s} + \frac{F_{o}Q}{F} \frac{Q_{s^{*}}s^{*}}{Q} \frac{\alpha\tau^{*}}{s^{*}} + \frac{\gamma_{\gamma}Y}{\gamma} \frac{Y_{s^{*}}s^{*}}{Y} \frac{\alpha\tau^{*}}{s^{*}} \end{bmatrix}.$$

$$dY = -\kappa \left( \tau \frac{\partial Y}{\partial \tau} + \tau * \frac{\partial Y}{\partial \tau^*} \right).$$

**Proposition 1**: Given the demand structure (1)-(4), a joint tariff reduction without domestic policy reform increases the rate of successful IS introduction to Home.

**Proof**: See Appendix 4.

The proposition points out the straightforward relation between trade integration and the rate of successful introductions of IS. Trade integration via multilateral trade liberalization increases imports, hence the platform for IS introduction. One should however, remember that not all successful introductions cause damages, and that the extent of damages is endogenous. The correlation between trade liberalization and damages caused by exotic species is represented by equation (19) under scenario 1, or  $dED = -\kappa \rho \gamma F \left[ \varepsilon^{F_Q} \varepsilon^{Q_T} + \varepsilon^{\gamma_{\gamma}} \varepsilon^{Y_T} + \varepsilon^{F_Q} \varepsilon^{Q_{T^*}} + \varepsilon^{\gamma_{\gamma}} \varepsilon^{Y_{T^*}} \right]$ .

Hence, the expected change in damages has four components corresponding to the two policy types (tariffs, production subsidies), and the two vectors (production, imports).

**Proposition 2:** Given the demand structure (1)-(4), a joint tariff reduction without domestic policy reform  $\begin{pmatrix} increases \\ does not affect \\ decreases \end{pmatrix}$  the expected damages if and only if

$$(20) \quad \frac{\varepsilon^{F_{Q}}}{\varepsilon^{\gamma_{\gamma}}} (\varepsilon^{Q_{r}} + \varepsilon^{Q_{r^{*}}}) \stackrel{<}{>} - \varepsilon^{\gamma_{r}}.$$

**Proof:** The proposition follows directly from applying elements of corollary 1 to equation (19). QED.

To provide intuition, we compare the IS damages induced by the trade reform in our imperfect-competition and two-way trade setup to the outcome in the one-way trade *cum* unilateral reform case. The "one-way trade" context can be interpreted in our framework as when the Home firm's

export  $X^*$  does not exist.<sup>6</sup> Therefore, the demand system is characterized only by equations (1), (2) and (4). A Bertrand equilibrium exists and is unique in this "one-way trade" version of the model (See appendix 5). As a result, the relation between trade reform and the damages from the exotic species in the one-way trade model is characterized by equation (20) but with  $\varepsilon^{Q_{T^*}} = 0$ . Corollary 2 follows this argument.

**Corollary 2**: If it were the one-way trade context, trade liberalization  $\begin{pmatrix} increases \\ does not affect \\ decreases \end{pmatrix}$  the expected damages if and only if  $\frac{\mathcal{E}^{F_Q}}{\mathcal{E}^{\gamma_T}} \mathcal{E}^{Q_T} \stackrel{<}{\sim} -\mathcal{E}^{\gamma_T}$ .

The counter-intuitive part of proposition 2 and corollary 2 is that the trade integration could leads to a decrease of the expected damages from exotic species in a two-way (or one-way) trade context if  $\frac{\mathcal{E}^{F_Q}}{\mathcal{E}^{\gamma_{\tau}}}(\mathcal{E}^{\mathcal{Q}_{\tau}}+\mathcal{E}^{\mathcal{Q}_{\tau^*}})>-\mathcal{E}^{\gamma_{\tau}}$  (or  $\frac{\mathcal{E}^{F_Q}}{\mathcal{E}^{\gamma_{\tau}}}\mathcal{E}^{\mathcal{Q}_{\tau}}>-\mathcal{E}^{\gamma_{\tau}}$ ). Assuming damages are augmented, i.e.

 $\varepsilon^{F_{\varrho}} > 0$ , the underlying outcome is much less likely to occur in a two-way-trade cum multilateral-reform situation than in a one-way-trade cum unilateral reform case, since by corollary 1,  $\varepsilon^{\mathcal{Q}_{\tau^*}} < 0$ . The oligopolistic nature of our model here is not crucial to obtain this decrease in ambiguity. One should notice that it is reasonable to compare the two conditions for two-way and one-way trade since, though the two-way trade occurs which leads to  $\mathcal{Q}_{\tau} = X_{\tau} + X_{\tau}^*$ , by element (i) of corollary 1,  $X_{\tau}^* = 0$ . Therefore, corollary 2 still holds.

The possibility that trade liberalization reduces the damages caused by exotic species exists because total production of Home may decrease. The reply of Home production to trade

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<sup>&</sup>lt;sup>6</sup> This situation can be justified as i) if Home products do not generate any utility to the foreign consumers. Hence the foreign utility is of the form  $u*(y*) = A_{y*}y*-0.5B_{y*}y*^2$ ; or ii) if foreign purchasers do want to consume Home products, but their demand is not high enough to be realized (i.e.  $a_x^*$  is so small that  $x^* \le 0$ ).

reform in these scenarios is represented by

(21') 
$$dQ = -\kappa \left( \tau \frac{\partial Q}{\partial \tau} + \tau^* \frac{\partial Q}{\partial \tau^*} \right).$$

By (21') and elements of corollary 1, the following holds

(22) 
$$dQ \stackrel{>}{\sim} 0 \Leftrightarrow \frac{\tau}{\tau^*} \stackrel{<}{\sim} -\frac{\partial Q/\partial \tau^*}{\partial Q/\partial \tau} = \frac{b_{x^*} (4b_x b_y - k^2)(2b_{x^*} b_{y^*} - k^2)}{kb_x b_y (4b_{x^*} b_{y^*} - k^2)}.$$

We have dQ > 0 if

(23) 
$$\frac{\tau}{\tau^*} < \frac{b_{x^*} (4b_x b_y - k^2)(2b_{x^*} b_{y^*} - k^2)}{k b_x b_y (4b_{x^*} b_{y^*} - k^2)}.$$

This condition tells us that to have dY>0 and dQ>0, Home pre-reform tariff must not be "too high" relative to the Foreign pre-reform tariff. Further and for sake of intuition, let's assume some symmetric price responses such that  $b_x=b_{y^*}=b$  and  $b_{x^*}=b_y=b^*$ , i.e. the own-price and cross-price effects are the same in the two markets, but the size of the market (the intercepts of the demands) is different. Then (23) becomes  $\frac{\tau}{\tau^*}<\frac{2bb^*-k^2}{kb}\equiv\omega(k,b,b^*)$ . It is worth to notice that  $\omega>1$ . This leads to a corollary.

Corollary 3: Given the demand structure (1)-(4), and assuming  $b_x = b_{y*} = b$  and  $b_{x*} = b_y = b^*$ , multilateral trade reform involving joint tariff reduction always increases expected damages, if i) Home pre-reform tariff is lower than foreign pre-reform tariff, or if ii) Home pre-reform tariff is higher than Foreign pre-reform tariff but not substantially so that  $1 < \frac{\tau}{\tau^*} < \omega$ .

The first condition holds because  $\tau < \tau^* \Rightarrow \frac{\tau}{\tau^*} < 1 < \omega$ . Note also in case ii, since  $\frac{\partial \omega}{\partial k} < 0$ ,

 $\frac{\partial \omega}{\partial b} > 0$  and  $\frac{\partial \omega}{\partial b^*} > 0$ , the condition is more likely to hold for large b and b\* and for small k, i.e.,

for large own-price effects and/or for small degree of substitution between foreign and home goods. This corollary suggests that a relatively open country liberalizing its trade with a more protectionist partner will face increase expected damages, other things being equal.

Next we consider scenarios 3 and 4. Both trade and agricultural distortions are in place. **Proposition 3**: Given the demand structure (1)-(4), and assuming both trade and agricultural policies active, then trade and domestic reforms  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$ ,  $ds = \alpha d\tau$  and  $ds^* = \alpha d\tau^*$ , increase the rate of successful IS introduction to Home.

**Proof:** See appendix 6. Since subsidies and tariffs provide parallel protection in both countries, their reduction have parallel influences on IS introduction.

**Proposition 4:** Given the demand structure (1)-(4),

i) if both trade and agricultural policies exist, then the reform  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$ ,  $ds = \alpha d\tau$  and  $ds^* = \alpha d\tau^*$   $\begin{pmatrix} increases \\ does not affect \\ decreases \end{pmatrix}$  the expected damages if and only if

$$(24) \quad \frac{\varepsilon^{F_{Q}}}{\varepsilon^{\gamma_{r}}} \Big( \varepsilon^{Q_{r}} + \varepsilon^{Q_{r^{*}}} + \varepsilon^{Q_{s}} \alpha \tau / s + \varepsilon^{Q_{s^{*}}} \alpha \tau^{*} / s^{*} \Big) \frac{<}{>} - \Big( \varepsilon^{Y_{s}} \alpha \tau / s + \varepsilon^{Y_{s^{*}}} \alpha \tau^{*} / s^{*} + \varepsilon^{Y_{r}} \Big);$$

ii) if both trade and agricultural policies exist but only Home government subsidizes its production, then the policy reform  $\frac{d\tau}{\tau} = \frac{d\tau^*}{\tau^*} = -\kappa$  and  $ds = \alpha d\tau$   $\begin{pmatrix} increases \\ does not affect \\ decreases \end{pmatrix}$  the expected damages if and only if  $\frac{\mathcal{E}^{F_Q}}{\mathcal{E}^{\gamma_{\tau}}} \left( \mathcal{E}^{Q_{\tau}} + \mathcal{E}^{Q_{\tau^*}} + \mathcal{E}^{Q_{s}} \alpha \tau / s \right) \lesssim - \left( \mathcal{E}^{\gamma_{s}} \alpha \tau / s + \mathcal{E}^{\gamma_{\tau}} \right)$ .

**Proof:** i) The result follows directly from applying elements of the corollary 1 to equation (24).

ii) If the Foreign Government does not subsidizes their production, the s\* is irrelevant in equation (24). Q.E.D.

In the presence of both trade policy and production subsidy, not only the Home

production's reply to trade reform is non-monotonic, but also is the Home's imports. The non-monotonicity of production in this case can be seen by expressing (15) in terms of elasticity, which leads to

(25) 
$$dQ \stackrel{>}{<} 0 \Leftrightarrow \varepsilon^{Q_{\tau}} + \varepsilon^{Q_{\tau^*}} \stackrel{<}{>} - \alpha \left( \frac{\tau}{s} \varepsilon^{Q_s} + \frac{\tau^*}{s^*} \varepsilon^{Q_{s^*}} \right).$$

There are large and increasing differences in the levels of support and market protection among OECD countries, reflecting different historical uses of policy instruments, and the varying pace and degree of progress in agricultural policy reform. For the 2000-02 period, the average PSE was below 5% in Australia and New Zealand, below 25% for the United States, 35% in the European Union and around 60% for Japan, Korea among others (figure 2). Support to Australian agriculture, for example, is extremely low and domestic producer prices, which were on average 5% higher than world price in the mid-1980s, have been broadly aligned with world prices since 2001 (OECD, 2003, page 120). Proposition 4(i) can refer to the trade activities between the US and EU or Japan, while US-Australia or US-New Zealand exchange could be the case in proposition 4(ii).

#### 5. Calibration of the wheat model in the presence of IS

Wheat provides an excellent opportunity to illustrate our analytical results. Wheat trade can be a major vector of IS (CABI), and as mentioned before wheat is differentiated and its trade is oligopolistic. Table 1 summarizes the bilateral trade on wheat between the US, the European Union 15 (EU), Canada and the "rest of the world" in the marketing year of July 2001-June 2002. There is a large two-way trade between the US and Canada: 98% of US wheat imports come from Canada, while 25% of Canada wheat imports are from the US. In total, EU's total wheat imports are almost as large as its total wheat exports. Therefore, to illustrate the theoretical

findings in the previous sections, we calibrate the model using data on wheat production and trade and on invasive species associated with wheat for the four-country case (the US, the EU, Canada, and the rest of the world (ROW)).

Table 3 indicates the summary policy distortions at the border and farm subsidies for major players in the wheat market for 2001 using OECD and WITS data. As noted by Mitchell and Mielke, despite these significant achievements in improved rules for trade with the URAA, the amount of trade liberalization achieved in wheat was modest because of the way these reforms were done. Many countries applied the Uruguay Round provisions so that they could protect producers in key sectors from foreign competition. Applied tariffs were often set high and bound tariffs were often set even higher which leaves open the possibility of future increases in applied tariffs. Wheat export subsides have been largely eliminated, but the possibility they could be resumed remains. Implementation of minimum access and tariff reduction has also met with problems as countries have introduced new measures to offset agreed reforms.

While trade barrier has the tendency to reduce, the domestic policies still support and protect the agriculture activities. In 2002, for the OECD countries, the level of support to producers stabilized, but with a slight increase in protection and a slight reduction in market orientation. Support to producers for the OECD as a whole, as measure by the %PSE, remained unchanged at 31% in 2002 compared to 2001 (Figure 1, OECD 2003). For the three-year period 2000-2002, the %PSE averaged 31% compared with the 1986-88 average of 38%. In output-linked support, the nominal rate of protection, as measure by the producer nominal assistance coefficients increased slightly with average producer prices 31% above the world price in 2002 compared to 30% in 2001.

Output-linked support reduces the transmission of world price changes to producers and

thus dampens the influence of world market price changes on domestic production decisions.

Over the long-term market protection has decreased as prices in domestic markets were, on

average, 57% higher in 1986-88. The nominal assistance coefficient for the whole OECD, as

measured by the producer NAC, also slightly increased in 2002 compared to 2001 indicating a

slight reduction in market orientation. Total farm receipt in 2000-02 were on average 46% higher

than they would have be if entirely generated in markets without any support, while they were

61% higher in 1986-88. This is an indicator of an improvement in market orientation in terms of

greater share of farm receipts generated in markets than created by government intervention.

**Structure of the wheat model:** 

Equations (1) to (4) specified in the previous section are calibrated to 2001/2 data. To account

for damages we decompose output into a land component and a yield component. Damages are

expressed as production losses via decreased yield. This is the way plant pathologists model the

impact of pest on crops (CABI). We calibrate the four-country model, which are the US, the EU,

Canada and the rest of the world (ROW), with a vector of exports and imports for each country

since there are several partners for each country. Wheat is assumed to be differentiated, hence we

have 4 kinds of wheat: US wheat, EU wheat, Canada wheat, and wheat produced by the rest of

the world.

The general framework for each country sub-model consists of the following:

Planted area: 
$$AH^i = f(WP^i, AP^i)$$
,

Yield: 
$$Y^i = g(WP^i) * (1 - E \lceil YL^i \rceil)$$
,

Wheat production:  $PROD^i = AH^i * Y^i$ ,

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where  $i = \{US, EU, CAN, ROW\}$ , AH is the acreage, WP denotes the real wheat price, AP represents the real price of alternative crops (corn, barley, oats and rye, etc), Y stands for yield, YL is the yield loss due to the non-indigenous species and PROD is the wheat production. The inventory demands are assumed to be constant across the period.

Data for area, yield, production and consumption were gathered from the World Grain Statistics of the International Grains Council. Price data were obtained from the USDA, Attaché Reports, AgCanada and the International Grains Councils. The protection data were collected from the OECD and WITS. Finally, CABI's *Crop Protection Compendium* provides most of the data for the underlying pests. Price responses come from the FAPRI elasticity database. Damages D of the pest p are expressed in the value of crop losses:  $E[D_p^i] = h(E[YL^i])$ . Simulated results will be presented at the conference.

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Figure 1: Evolution of Producer Support Estimate (%PSE), Producer Nominal Protection Coefficient (NPCp) and Producer Nominal Assistance Coefficient (NACp)

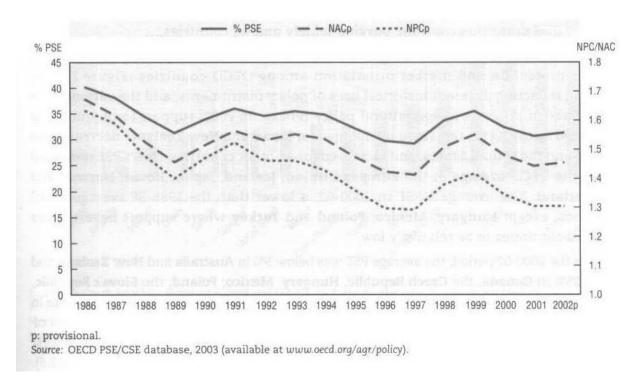
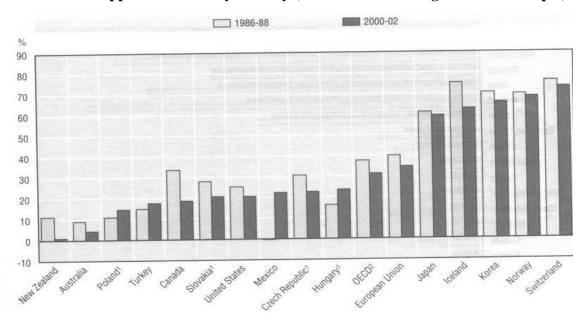


Figure 2:Producer Support Estimate by country (Percent of value of gross farm receipts)



<sup>1.</sup> For the Czech Republic, Hungary, Poland and the Slovak Republic, the reference years are 1991-93.

For 1986-88, the Czech Republic, Hungary, Poland and the Slovak Republic are excluded. Notes: Countries are ranked according to 2000-2002 levels. For more detail, see Table III.3.
 Source: OECD PSE/CSE database, 2003 (available at www.oecd.org/agr/policy).

Table 1: Trade in all wheat (including durum wheat), wheat flour and semolina Metric tons (wheat equivalent)

Importing		Exporting Country			
Country	Canada	EU	USA	ROW	Total
Canada		1,041	25,486	76,915	103,442
$oldsymbol{EU}$	1,232,910		2,234,378	6,849,852	10,317,140
USA	1,910,964	1,695		46,337	1,958,996
ROW	12,949,148	10,760,918	24,529,819		96,265,975
<b>Total</b>	16,093,022	10,763,654	26,789,683	54,999,194	108,645,553

Source: Wheat and Coarse Grains Shipments 2001/2002, International Grains Council.

Table 2: Trade in Coarse Grains (corn, barley, sorghum, oats, rye, millet and trinicale)

Metric tons

Wette tons						
<b>Importing</b>	Exporting Country					
Country	Canada	EU	USA	ROW	Total	
Canada		160	3,651,002	34,930	3,686,092	
$oldsymbol{EU}$	10,388		138,903	4,104,721	4,254,012	
<b>USA</b>	1,795,701	540,169		16,552	2,352,422	
ROW	729,945	4,427,342	52,738,304		95,316,517	
Total	2,536,034	4,967,671	56,528,209	41,577,129	105,609,043	

Source: Wheat and Coarse Grains Shipments 2001/2002, International Grains Council.

Table 3: Tariff and Producer Support Estimate (PSE) on wheat in 2001

	Tariff	Percentage PSE		
	(i)	(ii)		
Canada	53.72	17		
$oldsymbol{EU}$	12.80	46		
USA	1.87	42		

Sources: (i): World Integrated Trade Solution (WITS) of the World Bank and the United Nations Conference on Trade and Development (UNCTAD). (ii): OECD 2003.

#### **Appendix**

#### **Appendix 1:**

The inverse demands corresponding to equations (1)-(2) are  $p_x(x,y) = A_x - B_x x - Ky$ , and  $p_y(x,y) = A_y - B_y y - Kx$ . All parameters are positive and so is expression  $B_x B_y - K^2$ . This demand system can be derived by maximizing quasi-linear utility, subject to the budget constraint  $I = z + p_x x + p_y y$ , where I is Home income. The aggregate utility function is of the form U = z + u(x,y), where z is the aggregate consumption of a competitive numeraire good and u is a quadratic function defined by  $u(x,y) = A_x x + A_y y - 0.5(B_x x^2 + B_y y^2 + 2Kxy)$ .

## Appendix 2: Existence and uniqueness of a Bertrand Equilibrium in the model.

Given the demand structure as specified in equations (1)-(4), we show that the Bertrand equilibrium of the game exists and is unique for any ad-valorem tariffs  $(\tau, \tau^*)$  and any production ad-valorem subsidies  $\{s, s^*\} \in [0,1)$  proportioning on the production cost.

**Proof**: Rewrite the Foreign firm's best response  $BR_v^F(p_x)$  under the form  $BR_x^F(p_y)$ , that is

(14') 
$$BR_x^F(p_y) = \left\{ -\left[ a_y + b_y c(1 - s^*) \right] + 2b_y p_y \right\} (1 + \tau)/k .$$

The two best responses  $BR_x^H(p_y)$  and  $BR_x^F(p_y)$  are two linear functions of  $p_y$ . One sees that

$$\partial BR_{x}^{H}/\partial p_{y}=k(1+\tau)/2b_{x}>2b_{y}(1+\tau)/k=\partial BR_{x}^{F}/\partial p_{y}.$$

On the other hand,

$$BR_x^H \Big|_{p_y=0} \equiv \left[ a_x + b_x c(1-s) \right] / 2b_x > 0 > -\left[ a_y + b_y c(1-s^*) \right] (1+\tau) / k \equiv BR_x^F \Big|_{p_y=0}.$$

Hence, the Bertrand equilibrium in the Home market which is represented by the intersection point of these two linear correspondences always exists and is unique.

Q.E.D.

Similar argument holds for the equilibrium in the Foreign market.

#### **Appendix 3: Proof of corollary 1.**

By equations (16a)-(16d), we have:

(i) 
$$\partial X * / \partial \tau = 0$$
,  $\partial X * / \partial s = b_x^* c (2b_x^* b_y^* - k^2) / D^* > 0$ ,

$$\partial X^*/\partial \tau^* = -b_x^* c (2b_x^* b_y^* - k^2)(1-s)/D^* < 0, \ \partial X^*/\partial s^* = -b_x^* b_y^* c k/D^* < 0;$$

(ii) 
$$\partial X / \partial \tau = c b_x b_y k (1 - s^*) / D > 0$$
,  $\partial X / \partial s = c b_x (2 b_x b_y - k^2) / D > 0$ ,  $\partial X / \partial \tau^* = 0$ ,

$$\partial X/\partial s^* = -cb_xb_xk(1+\tau)/D < 0$$
;

(iii) 
$$\partial Q/\partial \tau = cb_x b_y k(1-s^*)/D > 0$$
,  $\partial Q/\partial s = cb_x (2b_x b_y - k^2)/D + b_x^* (2b_x^* b_y^* - k^2)(1+\tau^*)/D^* > 0$ ,

$$\partial Q/\partial \tau^* = -cb^*(2b_x^*b_y^* - k^2)(1-s)/D^* < 0, \ \partial Q/\partial s^* = -ck \left[ b_x^*b_y^*/D^* + b_xb_y(1+\tau)/D \right] < 0;$$
 and

(iv) 
$$\partial Y/\partial \tau = -cb_y(2b_xb_y - k^2)(1-s^*)/D < 0$$
,  $\partial Y/\partial s = -cb_xb_yk/D < 0$ ,  $\partial Y/\partial \tau^* = 0$ ,

$$\partial Y / \partial s^* = c b_v (2b_x b_v - k^2)(1+\tau)/D > 0$$
. Q.E.D.

### Appendix 4: Existence and uniqueness of a Bertrand Equilibrium in one-way trade model

Home firm chooses the price level  $(p_x)$ , and foreign firm decides  $(p_y, p_y^*)$  to maximize its profits. Given the demand structure as specified in equations (1), (2) and (8), the Bertrand

equilibrium of the game exists and is unique for any ad-valorem tariffs  $(\tau, \tau^*)$  and any production ad-valorem subsidies  $\{s, s^*\} \in [0,1)$  proportioning on the production cost.

**Proof**: Expressing the Home and the Foreign firm's best response under the form  $p_x(p_y)$ , we have:  $BR_x^H(p_y) = \{ [a_x + b_x c(1-s)] + k(1+\tau)p_y \} / 2b_x$ , and

$$BR_x^F(p_y) = \left\{ -\left[a_y + b_y c(1-s^*)\right] + 2b_y p_y \right\} (1+\tau)/k$$
. The same argument holds as in appendix 1.

Hence, the Bertrand equilibrium in the Home market which is represented by the intersection point of these two linear correspondences always exists and is unique.

The equilibrium price in the Foreign market is determined solely by the Foreign firm. That is:  $P_y^* = \left[a_y^* + b_y^* c(1-s^*)\right]/2b_y^*$ , which obviously always exists and is unique. Q.E.D.

#### **Appendix 5: Proof of proposition 1.**

The rate of successful exotic species introduction to Home is  $\mu(Y) = \rho \gamma(Y)$ . Totally differentiate this to get  $d\mu = \rho \frac{\partial \gamma}{\partial Y} dY = -\kappa \rho \frac{\partial \gamma}{\partial Y} \left( \tau \frac{\partial Y}{\partial \tau} + \tau * \frac{\partial Y}{\partial \tau^*} \right)$  by (20').

Since  $\partial \gamma / \partial Y > 0$  by construction,  $\partial Y / \partial \tau < 0$  and  $\partial Y / \partial \tau^* = 0$  by elements (iv) of corollary 1, it must be true that  $d\mu > 0$ . Q.E.D.

#### Appendix 6: Proof of proposition 3.

Totally differentiate the rate of successful introductions to get

$$d\mu = \rho \frac{\partial \gamma}{\partial Y} dY = -\kappa \rho \frac{\partial \gamma}{\partial Y} \left( \tau \frac{\partial Y}{\partial \tau} + \alpha \tau \frac{\partial Y}{\partial s} + \alpha \tau * \frac{\partial Y}{\partial s *} \right)$$
 by (21).

Substituting the expressions for  $Y_{\tau}, Y_{s}$ , and  $Y_{s^{*}}$  from the appendix 2 into equation (21) and rearranging to get  $dY = b_{y}\kappa\tau c \left[ \left( 2b_{x}b_{y} - k^{2}\right) \left( 1 - s^{*} \right) + \alpha k b_{x} \right] / D > 0$ .

Since  $\partial \gamma / \partial Y > 0$ , it must be true that  $d\mu > 0$  for any  $s^* \ge 0$ . Q.E.D.