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Estimation of ordered response models with sample selection

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Abstract. We introduce two new Stata commands for the estimation of an ordered response model with sample selection. The `opsel` command uses a standard maximum-likelihood approach to fit a parametric specification of the model where errors are assumed to follow a bivariate Gaussian distribution. The `snpopsel` command uses the semi-nonparametric approach of [Gallant and Nychka](#) (1987, *Econometrica* 55: 363–390) to fit a semiparametric specification of the model where the bivariate density function of the errors is approximated by a Hermite polynomial expansion. The `snpopsel` command extends the set of Stata routines for semi-nonparametric estimation of discrete response models. Compared to the other semi-nonparametric estimators, our routine is relatively faster because it is programmed in Mata. In addition, we provide new postestimation routines to compute linear predictions, predicted probabilities, and marginal effects. These improvements are also extended to the set of semi-nonparametric Stata commands originally written by [Stewart](#) (2004, *Stata Journal* 4: 27–39) and [De Luca](#) (2008, *Stata Journal* 8: 190–220). An illustration of the new `opsel` and `snpopsel` commands is provided through an empirical application on self-reported health with selectivity due to sample attrition.

Keywords: st0226, opsel, opsel postestimation, sneop, sneop postestimation, snp2, snp2 postestimation, snp2s, snp2s postestimation, snpopsel, snpopsel postestimation, snp, snp postestimation, ordered response models, sample selection, parametric maximum-likelihood estimation, semi-nonparametric estimation

1 Introduction

This article is concerned with the estimation of ordered response models with sample selection. Such models can be applied to a variety of empirical applications in which the outcome of interest is discrete, its values are naturally ordered (for example, performances in a training program, educational achievements, measures of well-being, job satisfaction, health, and cognitive abilities), and data observability is restricted by a binary selection mechanism (for example, participation in a training program, self-selection in the labor market, issues of nonresponse, and sample attrition). An extended

review of the model and other interesting empirical applications can be found in the recent survey on ordered response models by [Greene and Hensher \(2009\)](#).

After describing the structure of the basic model, we focus on consistent estimation of two alternative specifications. The parametric specification extends the classical ordered probit model by assuming that errors in the latent regression equations for the selection mechanism and the outcome variable, respectively, follow a bivariate Gaussian distribution. Under this distributional assumption, the model parameters are estimated by a maximum likelihood (ML) estimator, which accounts for sample selection. This is the same estimator implemented by the `ssm` command of [Miranda and Rabe-Hesketh \(2006\)](#), a wrapper program that calls `gllamm` (see [Rabe-Hesketh, Skrondal, and Pickles \[2004\]](#)). The `opse1` command provided in this article is, however, much faster because it is directly programmed in the Stata ML environment. This estimator generalizes the ML estimator of an ordered probit model provided by the official Stata command `oprobit`, which is known to be inconsistent if the unobservable factors affecting the outcome of interest are correlated with the unobservable factors affecting the selection mechanism.

Because parametric estimators of discrete choice models are known to be sensitive to departure from distributional assumptions, we also consider a semiparametric specification that avoids imposing assumptions on the distribution of the error terms. To our knowledge, the literature on semiparametric estimation of ordered response models is quite recent, and it has been mainly concerned with the estimation of standard models where the ordered outcome is not subject to sample selection. Semiparametric estimators of a standard ordered response model have been analyzed by [Lewbel \(2000\)](#), [Klein and Sherman \(2002\)](#), [Chen and Khan \(2003\)](#), [Stewart \(2004, 2005\)](#), and [Copejans \(2007\)](#).

The estimator considered in this article relies on the semi-nonparametric (SNP) approach of [Gallant and Nychka \(1987\)](#) by generalizing the estimator of [Stewart \(2004\)](#). Two features of this approach are worth noticing: First, it is less computationally demanding than other semiparametric approaches based on kernel density estimation. Second, the Monte Carlo simulations by [Stewart \(2005\)](#) and [De Luca \(2008\)](#) suggest that SNP estimators of discrete choice models have good finite sample performances relative to both parametric estimators and other semiparametric estimators. The basic idea of the SNP approach is to approximate the unknown densities of the error terms by Hermite polynomial expansions and to use the resulting approximations to derive a pseudo-ML estimator for the vector of model parameters. For the model considered in this article, SNP approximations to the unknown density and distribution functions correspond to the ones derived by [De Luca \(2008\)](#). The underlying Stata routines have only been improved by using Mata to speed up the estimation process. In addition, we provide new postestimation routines to compute linear predictions, predicted probabilities, and marginal effects. These improvements are extended to the set of SNP Stata commands written by [Stewart \(2004\)](#) and [De Luca \(2008\)](#).

The remainder of the article is organized as follows: Section 2 introduces the statistical model. The parametric ML estimator and the SNP estimator are discussed in sections 3 and 4, respectively. Section 5 presents the syntax of the new and updated

commands. Examples of the use of the new `opsel` and `snpopsel` commands are provided in section 6. Finally, in section 7, we use data from the first two waves of the Survey of Health, Ageing, and Retirement in Europe (SHARE) to present results of an empirical application on self-reported health with selectivity due to sample attrition.

2 The statistical model

An ordered response model with sample selection can be represented through the following bivariate threshold-crossing model

$$Y_j^* = \beta_j^\top \mathbf{X}_j + U_j \quad j = 1, 2 \quad (1)$$

$$Y_1 = I(Y_1^* \geq 0) \quad (2)$$

$$Y_2 = \sum_{h=0}^H h I(\alpha_h < Y_2^* \leq \alpha_{h+1}) \quad \text{if } Y_1 = 1 \quad (3)$$

where Y_1^* and Y_2^* represent continuous latent variables for the selection process and the outcome of interest, respectively; the β_j are k_j vectors of unknown parameters; the \mathbf{X}_j are k_j vectors of exogenous variables; and the U_j are random errors. The latent variable Y_1^* is related to the binary indicator Y_1 through the observational rule (2), where $I(A)$ denotes the indicator function of the event A . The latent variable Y_2^* is related to the outcome Y_2 through the observational rule (3), where $\alpha = (\alpha_1, \dots, \alpha_H)$ —with $\alpha_h < \alpha_{h+1}$, $\alpha_0 = -\infty$, and $\alpha_{H+1} = +\infty$ —is a vector of H strictly increasing thresholds that partition Y_2^* into $H + 1$ exhaustive and mutually exclusive intervals.¹ As in a classical sample selection model, observability of Y_2 is confined to the subsample of observations for which $Y_1 = 1$ (the selected sample). Selectivity effects are allowed to operate through the correlation between the latent regression errors U_1 and U_2 .

Identifiability of the model parameters requires three restrictions. First, the intercept coefficient in β_2 is normalized to zero because it is not separately identified from the threshold coefficients in α . This is a standard identifiability restriction that is also imposed in the ordered logit and ordered probit models. Second, we assume that X_1 contains at least one variable that is not contained in X_2 . The role of this exclusion restriction has been discussed at length in the literature on sample selection models and multinomial choice models. In principle, a parametric specification of the model could be identified through nonlinearity of the underlying distribution functions. However, as argued in similar models by [Meng and Schmidt \(1985\)](#) and by [Keane \(1992\)](#), relying on identification via functional form restrictions is not very appealing because it may lead to problems of weak identification.² Furthermore, as pointed out by [Lee \(1995\)](#), this exclusion restriction is needed to identify the semiparametric specification of the model

-
1. If $H = 1$, (3) corresponds to a binary response model where the threshold α_1 is equal to the opposite of the intercept coefficient. In the text, the values of Y_2 are ordered from 0 to H to simplify notation. In practice, however, Y_2 can assume any ordered sequence of integer numbers.
 2. As argued by [Keane \(1992\)](#), common symptoms of this problem are close-to-singular Hessian, large standard errors, and inability of the optimization algorithms to find steps that improve the likelihood or to achieve convergence.

where the distribution of U_1 and U_2 is not assumed to be known. Third, as argued by [Manski \(1988\)](#), identification of the semiparametric specification requires that X_1 and X_2 each contain at least one continuous variable. This is another standard assumption that guarantees that X_1 and X_2 have sufficiently rich supports.

The primary aim of our analysis is to obtain consistent estimates of the vector of parameters $\theta_2 = (\beta_2, \alpha)$ by using observations from the selected sample. Unlike a classical sample selection model, estimators based on Heckman's estimator cannot be applied because of nonlinearity of the conditional mean in the second estimation step.³ In this type of model, a ML estimator remains the most attractive choice because it only requires computing the contributions to the likelihood function for the $H + 2$ possible realizations of the two discrete indicators Y_1 and Y_2 , namely $(Y_1 = 0), (Y_1 = 1, Y_2 = 0), \dots, (Y_1 = 1, Y_2 = H)$. Parametric and SNP versions of this estimator are presented in sections 3 and 4, respectively.

3 The parametric ML estimator

Our parametric specification of the model assumes that the errors U_1 and U_2 follow a bivariate Gaussian distribution with zero means, unit variances, and correlation coefficient ρ . This is the same distributional assumption imposed by the `ssm` command of [Miranda and Rabe-Hesketh \(2006\)](#) when specifying a binomial family with an ordered probit link.⁴ Under this parametric assumption on the distribution of the latent regression errors, the log-likelihood function for a random sample of n observations $\{(Y_{1i}, Y_{2i}, \mathbf{X}_{1i}, \mathbf{X}_{2i}) : i = 1, \dots, n\}$ is

$$L(\theta) = \sum_{i=1}^n \left\{ (1 - Y_{1i}) \ln \pi_{0i}(\theta) + \sum_{h=0}^H Y_{1i} I(Y_{2i} = h) \ln \pi_{1hi}(\theta) \right\} \quad (4)$$

where $\theta = (\beta_1, \beta_2, \alpha, \rho)$ is the vector of all model parameters and $(\pi_0, \pi_{10}, \dots, \pi_{1H})$ are the conditional probabilities associated with the $H + 2$ possible realizations of Y_1 and Y_2 ,⁵

$$\begin{aligned} \pi_0(\theta) &= \Pr(Y_1 = 0) = 1 - \Phi(\beta_1^\top \mathbf{X}_1) \\ \pi_{1h}(\theta) &= \Pr(Y_1 = 1, Y_2 = h) \\ &= \Phi_2(\beta_1^\top \mathbf{X}_1, \alpha_{h+1} - \beta_2^\top \mathbf{X}_2; -\rho) - \Phi_2(\beta_1^\top \mathbf{X}_1, \alpha_h - \beta_2^\top \mathbf{X}_2; -\rho) \end{aligned} \quad (5)$$

with Φ denoting the standardized Gaussian distribution and Φ_2 denoting the bivariate Gaussian distribution with zero means, unit variances, and correlation coefficient ρ . A parametric ML estimator of θ maximizes the log-likelihood function (4) over the parameter space $\Theta = \Re^{k_1+k_2+H} \times (-1, 1)$. If model (1)–(3) is correctly specified and

3. An exception is the special regressor-based approach analyzed by [Dong and Lewbel \(2010\)](#) in the context of binary choice models.

4. The parameterization of the model considered by [Miranda and Rabe-Hesketh \(2006\)](#) is slightly different because the correlation between U_1 and U_2 is driven by a common random error.

5. We keep the individual subscript and the conditioning on covariates implicit to simplify notation.

the assumption on the distribution of U_1 and U_2 holds, then this estimator is consistent and asymptotically efficient under standard regularity conditions.

4 The SNP estimator

The SNP estimator for an ordered response model with sample selection is a straightforward generalization of the SNP estimators developed by [Stewart \(2004\)](#) and [De Luca \(2008\)](#). After relaxing assumptions on the distribution of U_1 and U_2 , a semiparametric specification of model (1)–(3) gives the following set of conditional probabilities

$$\begin{aligned}\pi_0(\beta_1, \beta_2, \alpha) &= F_1(-\beta_1^\top \mathbf{X}_1) \\ \pi_{1h}(\beta_1, \beta_2, \alpha) &= \{F_2(\alpha_{h+1} - \beta_2^\top \mathbf{X}_2) - F(-\beta_1^\top \mathbf{X}_1, \alpha_{h+1} - \beta_2^\top \mathbf{X}_2)\} \\ &\quad - \{F_2(\alpha_h - \beta_2^\top \mathbf{X}_2) - F(-\beta_1^\top \mathbf{X}_1, \alpha_h - \beta_2^\top \mathbf{X}_2)\}\end{aligned}\tag{6}$$

where F_1 , F_2 , and F denote, respectively, the unknown marginal distribution functions of U_1 and U_2 , and their joint distribution function.⁶

Following [Gallant and Nychka \(1987\)](#), we first approximate the unknown joint density f of the error terms by a Hermite polynomial expansion of the form

$$f^*(u_1, u_2; \gamma) = \frac{1}{\psi_R(\gamma)} \tau_R(u_1, u_2; \gamma)^2 \phi(u_1) \phi(u_2)\tag{7}$$

where $\tau_R(u_1, u_2; \gamma)$ is a polynomial of order $R = (R_1, R_2)$ in u_1 and u_2 , γ is a vector of $R_1 \times R_2$ unknown parameters, ϕ is the standardized Gaussian density, and $\psi_R(\gamma)$ is a normalization factor ensuring that f^* is a proper density. [De Luca \(2008\)](#) shows that integrating the joint density (7) gives the following approximations to the joint distribution function of U_1 and U_2 ,

$$\begin{aligned}F^*(u_1, u_2; \gamma) &= \Phi(u_1)\Phi(u_2) + \frac{1}{\psi_R(\gamma)} A_{12}^*(u_1, u_2; \gamma)\phi(u_1)\phi(u_2) \\ &\quad - \frac{1}{\psi_R(\gamma)} A_1^*(u_1; \gamma)\Phi(u_2)\phi(u_1) - \frac{1}{\psi_R(\gamma)} A_2^*(u_2; \gamma)\Phi(u_1)\phi(u_2)\end{aligned}$$

and to the marginal distribution functions of U_1 and U_2 ,

$$\begin{aligned}F_1^*(u_1; \gamma) &= \Phi(u_1) - \frac{1}{\psi_R(\gamma)} A_1^*(u_1; \gamma)\phi(u_1) \\ F_2^*(u_2; \gamma) &= \Phi(u_2) - \frac{1}{\psi_R(\gamma)} A_2^*(u_2; \gamma)\phi(u_2)\end{aligned}$$

where $A_{12}^*(u_1, u_2; \gamma)$, $A_1^*(u_1; \gamma)$ and $A_2^*(u_2; \gamma)$ are polynomials in u_1 and u_2 . The SNP estimator of the vector of parameters $\delta = (\beta_1, \beta_2, \alpha, \gamma)$ is obtained by maximizing the pseudo-log-likelihood function (4) with the probabilities specified as in (6) and the

6. The parametric conditional probabilities in (5) can be easily obtained from (6) using the properties of the Gaussian distribution.

unknown distribution functions F , F_1 , and F_2 replaced by their approximations F^* , F_1^* , and F_2^* . This estimator is \sqrt{n} -consistent, provided that R_1 and R_2 both increase with sample size. Because results on the asymptotic distribution of the SNP estimator are not available, inference is typically conducted using a parametric ML approach by treating the order R as known. Thus, the SNP model is better viewed as a flexible parametric specification for a fixed value of R , with the choice of R as part of the model selection procedure. For a given sample size, the value of R may be selected either through a sequence of likelihood-ratio tests or by model selection criteria such as Akaike's information criterion and Bayesian information criterion (BIC), or by the cross-validation strategies in [Coppejans and Gallant \(2002\)](#).

Three remarks on the SNP estimator are worth making: First, two location restrictions are needed because the polynomial expansion in (7) does not guarantee that U_1 and U_2 have zero means. As a consequence, we normalize the intercept in β_1 and the first threshold in α to their parametric ML estimates. Second, the estimated coefficients from the parametric and the SNP models are not directly comparable because in the former, the variances of U_1 and U_2 are normalized to one, while in the latter they are unconstrained functions of the Hermite polynomial parameters γ . As suggested by [Stewart \(2004\)](#) and [De Luca \(2008\)](#), these scale differences can be taken into account by comparing ratios of estimated coefficients. Alternatively, one can compare predicted probabilities and marginal effects, which are not affected by scale differences. Third, we notice that the SNP estimator analyzed in this article is more computationally demanding than the SNP estimator for a bivariate binary response model because the approximations to F and F_2 must be evaluated at H different points, rather than at a single point. To speed up the estimation process, we use a Mata version of the SNP routines written by [De Luca \(2008\)](#). For this model, the Mata routine is between four and six times faster than the standard Stata routine.⁷

5 Stata commands

The new Stata commands `opsel` and `snpopsel` provide, respectively, the parametric ML estimator and the SNP estimator of an ordered response model with sample selection. The general syntax of these commands is as follows:

```
opsel equation1 [if] [in] [weight], select(equation2, [noconstant
    offset(varname)]) [offset(varname) robust from(matname) level(#)
    maximize_options]
```

```
snpopsel equation1 [if] [in] [weight], select(equation2, [noconstant
    offset(varname)]) [offset(varname) order1(#) order2(#)]
    dplot(filename) from(matname) level(#) robust maximize_options]
```

7. Estimation time usually increases with the number of observations, the number of categories of the ordered outcome Y_2 , and the order $R = (R_1, R_2)$ of the Hermite polynomial expansion.

where *equation1* is specified as⁸

depvar varlist

and *equation2* is specified as

depvar_s = varlist_s

Both commands are written using `ml model lf` and share the same features of all Stata estimation commands, including access to the estimation results and options for the maximization process (see [R] **maximize**). `version 10.1` is the earliest version of Stata that can be used to run the routines. However, due to the new optimization engine used by the `ml` command under `version 11` (see [R] **ml**), the routines use version control to allow for use of both `version 10.1` and `version 11.0`.⁹ This version control is established on the basis of `c(version)` so it can be easily changed by users (see [P] **version**). `fweight`, `iweight`, and `pweight` are allowed (see [U] **11.1.6 weight**). Most options are similar to those of other Stata estimation commands. A description of command-specific options and the available postestimation commands is provided below. See the `opsl` and `snopsl` help file for descriptions of other options.

5.1 Option of the `opsl` command

`from(matname)` specifies the name of the matrix containing the starting values. By default, starting values are the `probit` estimates for the coefficients in the binary selection equation, the `oprobit` estimates for the coefficients in the outcome equation, and zero for the correlation coefficient.

5.2 Options of the `snopsl` command

`order1(#)` specifies the order R_1 to be used in the bivariate Hermite polynomial expansion. The default is `order1(3)`.

`order2(#)` specifies the order R_2 to be used in the bivariate Hermite polynomial expansion. The default is `order2(3)`.

`dplot(filename)` plots the estimated marginal densities of the two error terms together with Gaussian densities with the same estimated means and variances. This option generates three new graphs: The first is a plot of the estimated marginal density of U_1 and is stored as *filename_1*. The second is a plot of the estimated marginal density of U_2 and is stored as *filename_2*. The third combines *filename_1* and *filename_2* in a single graph and is stored as *filename*.

8. In *equation1*, the `noconstant` option is specified by default.

9. Our tests suggest that the `ml` command under `version 11` has slightly better numerical stability than the `ml` command under `version 10`.

`from(matname)` specifies the name of the matrix containing starting values. By default, starting values are the parametric ML estimates from the `opsel` command, plus a vector of zeros for the Hermite polynomial parameters γ . If the `opsel` command does not converge, then starting values are the `probit` estimates for the coefficients in the selection equation, the `oprobit` estimates for the coefficients in the outcome equation, plus a vector of zeros for the Hermite polynomial parameters γ .

5.3 Postestimation commands after `opsel` and `snpopsel`

After parametric and SNP estimation with `opsel` or `snpopsel`, the `predict` command can be used to compute linear predictions and predicted probabilities. The syntax of this command is

```
predict newvarlist [if] [in] [, pmargin pjoint pcond psel xb xbsel
      outcome(#)]
```

where

`pmargin` calculates the predicted marginal probabilities $\Pr(Y_2 = h)$. If the `outcome()` option is not specified, `newvarlist` must contain $H + 1$ new variables, where H is the number of categories of the dependent variable. If the `outcome()` option is specified, `newvarlist` must contain only one new variable. `pmargin` is the default.

`pjoint` calculates the predicted joint probabilities $\Pr(Y_1 = 1, Y_2 = h)$. If the `outcome()` option is not specified, `newvarlist` must contain $H + 1$ new variables. If the `outcome()` option is specified, `newvarlist` must contain only one new variable.

`pcond` calculates the predicted conditional probabilities $\Pr(Y_2 = h \mid Y_1 = 1)$. If the `outcome()` option is not specified, `newvarlist` must contain $H + 1$ new variables, where H is the number of categories of the dependent variable. If the `outcome()` option is specified, `newvarlist` must contain only one new variable.

`pselect` calculates the predicted selection probability $\Pr(Y_1 = 1)$. In this case, `newvarlist` must contain only one new variable.

`xb` calculates the linear prediction $\hat{\beta}_2^\top \mathbf{X}_2$ of the outcome equation. In this case, `newvarlist` must contain only one new variable.

`xbsel` calculates the linear prediction $\hat{\beta}_1^\top \mathbf{X}_1$ for the selection equation, including the contribution of the constrained intercept. In this case, `newvarlist` must contain only one new variable.

`outcome(#)` specifies the category of the dependent variable Y_2 for which the marginal, joint, or conditional probability must be calculated.

In addition, the `margins` command allows the user to make an inference on any of the statistics that can be computed from predictions of a previously fit model at fixed values of the covariates (see [R] `margins`). The lists of covariates in *equation1* and

equation2 cannot contain factor-variable operators. Thus it is the user's responsibility to ensure that all functionally related covariates in the model are set to the appropriate fixed values when one of them is set to a fixed value. Some examples are provided in sections 6 and 7.

5.4 Updated routines of other SNP commands

Updated versions of the SNP Stata commands (*sneop*, *snp*, *snp2*, and *snp2s*) written by Stewart (2004) and De Luca (2008) are also provided. As discussed at length in this article, these commands fit, respectively, a univariate ordered response model, a univariate binary response model, a bivariate binary response model, and a bivariate binary response model with sample selection. The updated routines account for two important improvements. First, they are faster and more precise because they are written in Mata. Second, after SNP estimation, one can use the *predict* and the *margins* commands to compute linear predictions, predicted probabilities, and marginal effects.¹⁰ In the following sections, we refer to the models considered by Stewart (2004) and De Luca (2008) to briefly describe the syntax of the *predict* commands associated with these SNP estimators.

The syntax of *predict* after *sneop* is

```
predict newvarlist [if] [in] [, pr xb outcome(#)]
```

where *pr*, the default, calculates the predicted probabilities $\Pr(Y_2 = h)$ and *xb* calculates the linear prediction, ignoring the contribution of the cutpoints.

The syntax of *predict* after *snp* is

```
predict newvar [if] [in] [, pr xb]
```

where *pr*, the default, calculates the predicted probability of success $\Pr(Y_1 = 1)$ and *xb* calculates the linear prediction, including the contribution of the constrained intercept.

The syntax of *predict* after *snp2* is

```
predict newvar [if] [in] [, p11 p10 p01 p00 pmarg1 pmarg2 pcond1 pcond2  
    xb1 xb2]
```

where *p11*, the default, calculates the joint probability $\Pr(Y_1 = 1, Y_2 = 1)$; *p10* calculates the joint probability $\Pr(Y_1 = 1, Y_2 = 0)$; *p01* calculates the joint probability $\Pr(Y_1 = 0, Y_2 = 1)$; *p00* calculates the joint probability $\Pr(Y_1 = 0, Y_2 = 0)$; *pmarg1* calculates the marginal probability $\Pr(Y_1 = 1)$; *pmarg2* calculates the marginal probability $\Pr(Y_2 = 1)$; *pcond1* calculates the conditional probability $\Pr(Y_1 = 1 \mid Y_2 = 1)$; *pcond2* calculates the conditional probability $\Pr(Y_2 = 1 \mid Y_1 = 1)$; *xb1* calculates the linear prediction of the first equation, including the contribution of the constrained intercept; and

10. The new routines also take into account other minor drawbacks of the old routines.

xb2 calculates the linear prediction of the second equation, including the contribution of the constrained intercept.

The syntax of **predict** after **snps2s** is

```
predict newvar [if] [in] [, pmargin p11 p10 p01 p00 pcond psel xb xbsel]
```

where **pmargin**, the default, calculates the marginal probability of success $\Pr(Y_2 = 1)$ in the outcome equation; **p11** calculates the joint probability $\Pr(Y_1 = 1, Y_2 = 1)$; **p10** calculates the joint probability $\Pr(Y_1 = 1, Y_2 = 0)$; **p01** calculates the joint probability $\Pr(Y_1 = 0, Y_2 = 1)$; **p00** calculates the joint probability $\Pr(Y_1 = 0, Y_2 = 0)$; **pcond** calculates the conditional probability of success $\Pr(Y_2 = 1 \mid Y_1 = 1)$; **psel** calculates the selection probability of success $\Pr(Y_1 = 1)$ for the selection equation; **xb** calculates the linear prediction of the outcome equation, including the contribution of the constrained intercept; and **xbsel** calculates the linear prediction of the selection equation, including the contribution of the constrained intercept.

As before, the **margins** command allows the user to make an inference on any of the statistics computed from prediction of a previously fit model.

6 Examples

In this section, we use simulated data to provide some examples of the new **opsel** and **snppsel** commands. The Stata codes for our data-generating process are:

```
. version 11.1
. set seed 1234
. matrix define sig=(1,.3 \ .3,1)
. quietly drawnorm u1 u2, n(5000) cov(sig) double
. generate double x1=(runiform()*2-1)*sqrt(3)
. generate double x2=rnormal()
. generate double x3=(rchi2(1)-1)/sqrt(2)
. generate double y1s=-.1+x1-x2+2*x3+u1
. generate double y2s=.5*x2-.5*x3+u2
. generate y1=(y1s>0)
. quietly generate y2=1 if y1==1 & y2s<=-2
. quietly replace y2=2 if y1==1 & y2s>-2 & y2s<=-1
. quietly replace y2=3 if y1==1 & y2s>-1 & y2s<=0
. quietly replace y2=4 if y1==1 & y2s>0 & y2s<=1
. quietly replace y2=5 if y1==1 & y2s>1 & y2s<=2
. quietly replace y2=6 if y1==1 & y2s>2
```

This generated model includes two equations—one for the binary indicator of sample selection **y1** and one for the ordered outcome **y2**. The indicator **y1** is equal to one for positive values of the latent variable **y1s**, and it is equal to zero otherwise. The outcome **y2** can assume six values, depending on the interval in which the latent variable **y2s** falls. The sample size is set to 5,000 observations, but observability of **y2** is restricted

to the subsample of 2,142 observations for which `y1` is equal to one. The set of covariates includes three independent variables: `x1` is drawn from a uniform distribution on $(-\sqrt{3}, \sqrt{3})$, `x2` is drawn from a standardized Gaussian distribution, and `x3` is drawn from a chi-squared distribution with one degree of freedom and then transformed by subtracting 1 and dividing the results by $\sqrt{2}$. The model is identified by excluding `x1` from the predictors of `y2s`. The errors `u1` and `u2` are drawn from a bivariate Gaussian distribution with zero means, unit variances, and a correlation coefficient equal to 0.3. The ordered probit estimates of the equation for `y2` are

```
. oprobit y2 x2 x3, nolog
Ordered probit regression
```

Number of obs	=	2142
LR chi2(2)	=	966.95
Prob > chi2	=	0.0000
Pseudo R2	=	0.1405

```
Log likelihood = -2956.4436
```

y2	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x2	.5474133	.0272248	20.11	0.000	.4940536	.6007731
x3	-.6348228	.0232483	-27.31	0.000	-.6803886	-.589257
/cut1	-2.291752	.0570215			-2.403513	-2.179992
/cut2	-1.213969	.0391274			-1.290657	-1.13728
/cut3	-.1844953	.0331939			-.2495542	-.1194364
/cut4	.7816241	.0373806			.7083594	.8548888
/cut5	1.750415	.0597042			1.633397	1.867433

```
. estimates store oprobit
```

This ML estimator is inconsistent because it does not account for the selectivity effects operating through the unobservables in the model. Because errors are drawn from a Gaussian distribution, a consistent ML estimator can be obtained with the `opsel` command¹¹

11. The same estimator can be obtained with the `ssm` command of [Miranda and Rabe-Hesketh \(2006\)](#) by specifying a binomial family with an ordered probit link. In this example, the `opsel` command is about nine times faster than the `ssm` command.

```
. opsel y2 x2 x3, select(y1=x1 x2 x3) nolog
oprobit with sample selection
Log likelihood = -4495.5214
```

Number of obs = 5000
Wald chi2(2) = 427.96
Prob > chi2 = 0.0000

		Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
y2							
	x2	.4923275	.0299206	16.45	0.000	.4336843	.5509708
	x3	-.5588938	.0287723	-19.42	0.000	-.6152864	-.5025011
y1							
	x1	.9744772	.0327524	29.75	0.000	.9102837	1.038671
	x2	-.9883017	.0343198	-28.80	0.000	-1.055567	-.9210361
	x3	1.986383	.0623045	31.88	0.000	1.864269	2.108498
	_cons	-.0954922	.027679	-3.45	0.001	-.149742	-.0412423
Thresholds:							
	/cut1	-2.106863	.071516	-29.46	0.000	-2.247032	-1.966694
	/cut2	-1.043992	.0552638	-18.89	0.000	-1.152307	-.9356765
	/cut3	-.0210024	.0484422	-0.43	0.665	-.1159473	.0739426
	/cut4	.9429836	.0489877	19.25	0.000	.8469695	1.038998
	/cut5	1.911481	.065758	29.07	0.000	1.782598	2.040365
	/athrho	.2750448	.0607469	4.53	0.000	.1559831	.3941065
	rho	.2683128	.0563736			.1547303	.374895
LR test of indep. eqns. (rho = 0): chi2(1) = 20.25 Prob > chi2 = 0.0000							

```
. estimates store opsel
```

This command detects a positive and statistically significant correlation coefficient. The resulting ML estimator performs much better than the ML estimator of the `oprobit` command. Next we use the `snpopssel` command with $R = (3, 3)$

```
. snpposel y2 x2 x3, select(y1=x1 x2 x3) order1(3) order2(3) nolog
Order of SNP polynomial - (R1,R2)=(3,3)
```

```
SNP oprobit with sample selection      Number of obs   =      5000
                                         Wald chi2(2)      =      734.71
Log likelihood = -4495.0926             Prob > chi2       =      0.0000
```

		Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
y2							
	x2	.4929962	.0260326	18.94	0.000	.4419733	.5440192
	x3	-.561258	.0229991	-24.40	0.000	-.6063354	-.5161805
y1							
	x1	.9938567	.0422441	23.53	0.000	.9110598	1.076654
	x2	-1.007823	.0444209	-22.69	0.000	-1.094886	-.9207598
	x3	2.030603	.0822262	24.70	0.000	1.869443	2.191764
Intercept:							
	_cons1	-.0954922	Fixed				
Thresholds:							
	/cut1	-2.106863	Fixed				
	/cut2	-1.057836	.0455188	-23.24	0.000	-1.147051	-.9686208
	/cut3	-.035201	.0570138	-0.62	0.537	-.146946	.076544
	/cut4	.9346139	.0764289	12.23	0.000	.7848159	1.084412
	/cut5	1.917374	.1269033	15.11	0.000	1.668648	2.1661
SNP coeffs:							
	g_1_1	.0745515	.0956116	0.78	0.436	-.1128437	.2619467
	g_1_2	-.0049985	.0258943	-0.19	0.847	-.0557504	.0457534
	g_1_3	.0084641	.0242935	0.35	0.728	-.0391504	.0560785
	g_2_1	-.0080358	.0604061	-0.13	0.894	-.1264295	.1103579
	g_2_2	-.0113104	.0198303	-0.57	0.568	-.050177	.0275562
	g_2_3	.0000508	.0161207	0.00	0.997	-.0315453	.0316468
	g_3_1	.0192734	.0325395	0.59	0.554	-.0445029	.0830497
	g_3_2	.0042744	.0100659	0.42	0.671	-.0154544	.0240033
	g_3_3	-.0012314	.0091104	-0.14	0.892	-.0190874	.0166246

Estimated moments of errors distribution

Main equation	Selection equation
Standard Deviation = 1.007877	Standard Deviation = 1.021227
Variance = 1.015816	Variance = 1.042905
Skewness = .0223663	Skewness = .0105038
Kurtosis = 3.046291	Kurtosis = 3.168797

Estimated correlation coefficient

rho = .2461318

```
. estimates store snpposel
```

Because of the large sample size, the estimated correlation coefficient and moments (standard deviation, skewness, and kurtosis) of the distributions of the error terms are quite close to the true values. The intercept coefficient in the selection equation and the first threshold coefficient are set equal to their parametric estimates because they can be absorbed in the unknown distribution functions and are not separately identified. Moreover, because of the different scale normalizations, SNP estimates of the remaining coefficients are not directly comparable with the parametric probit estimates. Below we compare ratios of the estimated coefficients using the `nlcom` command:

```
. quietly estimates restore opsel
. nlcom (b12_b11: [y1]_b[x2]/[y1]_b[x1]) (b13_b11: [y1]_b[x3]/[y1]_b[x1])
> (b23_b22: [y2]_b[x3]/[y2]_b[x2]) (cut2_b22: [cut2]_b[_cons]/[y2]_b[x2])
> (cut3_b22: [cut3]_b[_cons]/[y2]_b[x2]) (cut4_b22: [cut4]_b[_cons]/[y2]_b[x2])
> (cut5_b22: [cut5]_b[_cons]/[y2]_b[x2]), nohead
```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
b12_b11	-1.014187	.0363359	-27.91	0.000	-1.085404	-.9429695
b13_b11	2.038409	.065566	31.09	0.000	1.909902	2.166916
b23_b22	-1.135207	.0619191	-18.33	0.000	-1.256566	-1.013848
cut2_b22	-2.120522	.1083519	-19.57	0.000	-2.332888	-1.908157
cut3_b22	-.0426593	.0969984	-0.44	0.660	-.2327727	.1474541
cut4_b22	1.915358	.18147	10.55	0.000	1.559684	2.271033
cut5_b22	3.88254	.2947022	13.17	0.000	3.304934	4.460145

```
. quietly estimates restore snpopsel
. nlcom (b12_b11: [y1]_b[x2]/[y1]_b[x1]) (b13_b11: [y1]_b[x3]/[y1]_b[x1])
> (b23_b22: [y2]_b[x3]/[y2]_b[x2]) (cut2_b22: [cut2]_b[_cons]/[y2]_b[x2])
> (cut3_b22: [cut3]_b[_cons]/[y2]_b[x2]) (cut4_b22: [cut4]_b[_cons]/[y2]_b[x2])
> (cut5_b22: [cut5]_b[_cons]/[y2]_b[x2]), nohead
```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
b12_b11	-1.014053	.0362937	-27.94	0.000	-1.085187	-.9429183
b13_b11	2.043155	.065341	31.27	0.000	1.915089	2.171221
b23_b22	-1.138463	.0633154	-17.98	0.000	-1.262559	-1.014367
cut2_b22	-2.145728	.1320379	-16.25	0.000	-2.404518	-1.886939
cut3_b22	-.0714022	.1151801	-0.62	0.535	-.2971509	.1543466
cut4_b22	1.895783	.1858832	10.20	0.000	1.531459	2.260107
cut5_b22	3.889227	.3119916	12.47	0.000	3.277735	4.50072

Once differences in the scale of the error terms are taken into account, the SNP estimates of the coefficients and their standard errors are very close to those obtained with the parametric ML estimator. Of course, in this Gaussian design, the SNP estimates are somewhat less efficient than the parametric ML estimates. An alternative way of comparing the estimation results is that of using the `margins` command to compute marginal effects. Below we compare the true and the estimated marginal effects for the probability $\Pr(Y_2 = 1)$ at the sample means of the continuous covariates `x2` and `x3`:

```

. quietly summarize x2
. local m_x2=r(mean)
. quietly summarize x3
. local m_x3=r(mean)
. noisily display "The true marginal effect of x2 is "
> normalden(-2-.5*`m_x2`+.5*`m_x3`)*(-.5)
The true marginal effect of x2 is -.02710986
. noisily display "The true marginal effect of x3 is "
> normalden(-2-.5*`m_x2`+.5*`m_x3`)*(.)5)
The true marginal effect of x3 is .02710986
. quietly estimates restore oprobit
. margins, dydx(_all) predict(outcome(1)) atmeans noesample noatlegend
Conditional marginal effects                Number of obs   =       5000
Model VCE      : OIM
Expression     : Pr(y2==1), predict(outcome(1))
dy/dx w.r.t.   : x2 x3

```

	Delta-method		z	P> z	[95% Conf. Interval]	
	dy/dx	Std. Err.				
x2	-.0159133	.0018665	-8.53	0.000	-.0195717	-.012255
x3	.0184543	.0021164	8.72	0.000	.0143063	.0226023

```

. quietly estimates restore opsel
. margins, dydx(x2 x3) predict(pm outcome(1)) atmeans noesample noatlegend
Conditional marginal effects                Number of obs   =       5000
Model VCE      : OIM
Expression     : predict(pm outcome(1))
dy/dx w.r.t.   : x2 x3

```

	Delta-method		z	P> z	[95% Conf. Interval]	
	dy/dx	Std. Err.				
x2	-.0214554	.0026902	-7.98	0.000	-.0267282	-.0161826
x3	.0243563	.0029028	8.39	0.000	.018667	.0300457

```

. quietly estimates restore snpopsel
. margins, dydx(x2 x3) predict(pm outcome(1)) atmeans noesample noatlegend
Conditional marginal effects                Number of obs   =       5000
Model VCE      : OIM
Expression     : predict(pm outcome(1))
dy/dx w.r.t.   : x2 x3

```

	Delta-method		z	P> z	[95% Conf. Interval]	
	dy/dx	Std. Err.				
x2	-.0218608	.0041623	-5.25	0.000	-.0300187	-.0137029
x3	.0248877	.0046567	5.34	0.000	.0157608	.0340147

The marginal effects of the `oprobit` command are clearly underestimated, and the 95% confidence intervals do not include the true values. On the other hand, the marginal effects of the `opsl` and `snpopsl` commands are not statistically different from the true values.

Finally, we use the `predict` command to compute the predicted marginal probabilities of each of the six possible categories of `y2`:

```
. quietly estimates restore oprobit
. predict p1_op p2_op p3_op p4_op p5_op p6_op
(option pr assumed; predicted probabilities)
. summarize p*_op
```

Variable	Obs	Mean	Std. Dev.	Min	Max
p1_op	5000	.0439708	.1120831	2.24e-06	.9999826
p2_op	5000	.122631	.1096923	.0000173	.4100385
p3_op	5000	.2611747	.1031767	9.06e-08	.393263
p4_op	5000	.2967529	.0902117	2.09e-10	.3709466
p5_op	5000	.1946248	.1122201	2.74e-13	.3718935
p6_op	5000	.0808459	.0917647	1.40e-16	.7071775

```
. quietly estimates restore opsl
. predict p1_ops p2_ops p3_ops p4_ops p5_ops p6_ops
Predicted marginal probabilities
. summarize p*_ops
```

Variable	Obs	Mean	Std. Dev.	Min	Max
p1_ops	5000	.0487627	.1067814	.0000157	.9998292
p2_ops	5000	.1435943	.1068764	.0001691	.4048828
p3_ops	5000	.2893592	.0895097	1.70e-06	.3909952
p4_ops	5000	.295368	.0898223	7.23e-09	.370189
p5_ops	5000	.1672553	.1021479	1.66e-11	.3717906
p6_ops	5000	.0556606	.0640666	1.48e-14	.5576032

```
. quietly estimates restore snpopsl
. predict p1_snp p2_snp p3_snp p4_snp p5_snp p6_snp
Predicted marginal probabilities
. summarize p*_snp
```

Variable	Obs	Mean	Std. Dev.	Min	Max
p1_snp	5000	.0497109	.1077748	.0000231	.9997523
p2_snp	5000	.1417356	.1056396	.0002434	.399078
p3_snp	5000	.2880323	.0895862	4.23e-06	.389899
p4_snp	5000	.2961262	.0899017	3.25e-08	.3713396
p5_snp	5000	.1683228	.1023657	1.29e-10	.3759109
p6_snp	5000	.0560722	.0632733	1.83e-13	.5533184

As for the estimated coefficients and marginal effects, the predicted marginal probabilities of the SNP model are quite close to those of the parametric model. Because of the positive correlation between `u1` and `u2`, ignoring sample selection leads instead to underestimating the marginal probabilities of low outcomes and overestimating the marginal probability of high outcomes.

7 Empirical application

In this section, we present an empirical application on self-reported health (SRH) status of the elderly European population. Our data are from the first two waves of SHARE, a multidisciplinary and cross-national household panel survey coordinated by the Mannheim Research Institute for the Economics of Aging. In each wave, the target population of SHARE consists of people aged 50 and older, plus their (possibly younger) partners. The first wave, conducted in 2004, covers about 28,500 individuals in 11 European countries (Austria, Belgium, Denmark, France, Germany, Greece, Italy, the Netherlands, Spain, Sweden, and Switzerland). The second wave, conducted in 2006, covers about 33,300 individuals in a larger set of countries. In this analysis, we only focus on the countries that have participated in both waves of the panel, and we exclude refreshment samples that have been drawn in the second wave to compensate for sample attrition between the first and the second waves. After selecting respondents aged 50 and older in the first wave, our sample consists of 25,278 individuals, of whom 8,376 were interviewed in the first wave only and of whom 16,902 were interviewed in both waves. Further information on survey design and response rates can be found in Börsch-Supan et al. (2005).

In SHARE, SRH is measured on a five-point ordered scale (poor, fair, good, very good, excellent). We are interested in estimating a model for the transition probabilities $\Pr(\text{SRH}_2 = s \mid \text{SRH}_1 = j, X_2)$, $s, j = 1, \dots, 5$, where SRH_t is the SRH status in wave t and X_2 is an additional set of conditioning variables from the first wave. For simplicity, we fit an ordered response model for SRH_2 by using as predictors four binary indicators for SRH_1 and the conditioning variables in X_2 .¹² However, a more general approach could be estimating separate ordered response models for each status of SRH_1 to account for both differential effects of the conditioning variables in X_2 and for differential attrition effects.¹³ The conditioning variables in X_2 include a set of socio-demographic characteristics, a set of cognitive ability measures, a set of mental and physical health indicators. In particular, we use a second-order polynomial in age, household size, the logarithm of household income, the scores obtained in the cognitive ability tests (mathematical, orientation in time, recall, and fluency), the Euro-D depression scale, a set of binary indicators for being female, educational attainments, living without a partner, living in a small city, having children, and having health diseases (heart attack, stroke, arthritis, cancer, or Parkinson's disease) diagnosed by a doctor. Due to the high level of comparability of the SHARE data, we also pool data from the various countries and include a set of country dummies to control for unobserved heterogeneity at the country level.

Because of sample attrition that occurred between the first and the second waves, SRH_2 cannot be observed for about one-third of the original sample. Moreover, there are reasons to believe that the selection mechanism underlying sample attrition is not random. Deaths, serious illness, cognitive impairments, and moving into institutional

12. Good SRH is our reference category.

13. We thank Franco Peracchi for this comment. Here we use a more parsimonious model specification because of the large number of covariates included in X_2 .

care are health-related reasons for sample attrition that may induce a positive survivorship bias in SRH (that is, those remaining in the panel are likely to be healthier than those dropping out). To allow for selection on unobservables due to sample attrition, we need some variable that helps predict the attrition probability but does not help predict SRH₂. As suggested by [Fitzgerald, Gottschalk, and Moffitt \(1998\)](#), [Nicoletti and Peracchi \(2005\)](#), and [De Luca and Peracchi \(2010\)](#), interviewers' characteristics and features of the interview process may provide the required set of exclusion restrictions. Because these variables are external to the individuals under investigation and are not under their control, one may expect them to be irrelevant for SRH. On the other hand, results from several validation studies suggest that these variables are important predictors of the attrition probability. Thus, in addition to variables used to predict SRH₂, predictors of the attrition probability include age, gender, and educational attainments of the interviewers, an indicator for good willingness to answer (as perceived by the interviewer during the interview of the first wave), and an indicator for completing the self-administered paper-and-pencil questionnaire that is handed to respondents after the computer assisted personal interview (CAPI).¹⁴ Definitions and summary statistics of all the relevant variables are presented in table 1.

14. The unique interview mode adopted by SHARE is CAPI supplemented by a self-administered paper and pencil questionnaire (the drop-off questionnaire). The CAPI interview represents the largest part of the interview, while the drop-off questionnaire is used to ask more sensitive questions. As a fieldwork rule, the drop-off questionnaire is handed to respondents only after completing the CAPI interview. Thus completing the drop-off questionnaire can be interpreted as an indicator of the respondent's motivation toward the survey request.

Table 1. Definitions and summary statistics

Variable	Description	Obs.	Mean	Std.
part	Dummy for participating to wave 2	27519	0.66	0.47
SRH2	SRH wave 2	18070	2.93	1.06
SRH1_1	Dummy for SRH wave 1 poor	27378	0.07	0.25
SRH1_2	Dummy for SRH wave 1 fair	27378	0.23	0.42
SRH1_4	Dummy for SRH wave 1 very good	27378	0.20	0.40
SRH1_5	Dummy for SRH wave 1 excellent	27378	0.10	0.30
female	Dummy for female respondent	27519	0.54	0.50
age	Age of respondent	27519	64.88	10.16
edu_l	Dummy for primary respondent's education	27234	0.52	0.50
edu_h	Dummy for tertiary respondent's education	27234	0.19	0.39
single	Dummy for respondent living as single	27477	0.27	0.44
hsize	Household size	27519	2.16	0.98
children	Dummy for having any children	27383	0.89	0.31
small_city	Dummy for respondent living in a small city	27519	0.49	0.50
working	Dummy for respondent working	27317	0.31	0.46
ln_income	Log household income	27322	10.20	1.10
heart_attack	Dummy for heart attack	27367	0.12	0.33
stroke	Dummy for stroke	27367	0.04	0.19
arthritis	Dummy for arthritis	27367	0.20	0.40
cancer	Dummy for cancer	27367	0.05	0.23
parkinson	Dummy for Parkinson's	27367	0.01	0.08
eurod	Euro-D depression scale (0–12)	26858	2.29	2.23
orient	Respondent score on orientation in time (1–5)	27335	3.75	0.71
recall	Respondent score on recall (0–10)	26949	4.78	1.87
math	Respondent score on math (1–5)	27246	3.29	1.16
fluency	Respondent score on fluency (0–90)	26793	18.71	7.41
iv_fem	Dummy for female interviewer	26810	0.65	0.48
iv_age	Age of interviewer	26754	47.46	13.33
iv_edu_l	Dummy for primary interviewer's education	26596	0.10	0.30
iv_edu_h	Dummy for tertiary interviewer's education	26596	0.46	0.50
will_ans	Willingness to answer	27117	0.88	0.32
drop_off	Dummy for completing the drop-off quest.	27519	0.82	0.38
AT	Dummy for Austria	27519	0.07	0.25
BE	Dummy for Belgium	27519	0.13	0.34
CH	Dummy for Switzerland	27519	0.03	0.18
DE	Dummy for Germany	27519	0.11	0.31
DK	Dummy for Denmark	27519	0.06	0.24
ES	Dummy for Spain	27519	0.09	0.28
FR	Dummy for France	27519	0.11	0.31
GR	Dummy for Greece	27519	0.10	0.30
IT	Dummy for Italy	27519	0.09	0.29
NL	Dummy for the Netherlands	27519	0.10	0.31

7.1 Sample attrition

In the first two columns of table 2, we compare the probit and SNP estimates of a univariate binary response model for the probability of participating in wave 2 given participation in wave 1. For the SNP estimator, we considered three alternative specifications obtained by varying the order of the Hermite polynomial expansion ($R = 3, 4, 5$). For brevity, we present only the estimates of the specification with $R = 3$, which is the one selected by BIC. As mentioned above, the estimated coefficients of the probit and SNP models are not directly comparable because of the different scale normalizations. Accordingly, we compare ratios of the estimated coefficients by dividing the coefficient of each variable by the coefficient of the dummy variable for completing the drop-off questionnaire. The standard errors of these ratios are computed through the delta method (see [R] `nlcom`).

Table 2. Estimates for the probability of participating in wave 2 given participation in wave 1. Results are based on the normalization $|\beta_{\text{drop-off}}| = 1$. SNP-estimated coefficients of the Hermite polynomial expansions are omitted to save space. * denotes a p -value between 1 and 5%, ** denotes a p -value below 1%. Sample size $n_1 = 25,278$.

Variable	probit	snp	opsel	snpopsel
SRH1_1	-0.411 **	-0.421 **	-0.411 **	-0.456 **
SRH1_2	-0.306 **	-0.302 **	-0.306 **	-0.318 **
SRH1_4	-0.036	-0.038	-0.037	-0.069
SRH1_5	0.119	0.108	0.119	0.041
female	0.040	0.039	0.040	0.050
age1	0.010 *	0.010 *	0.010 *	0.010 *
age2	-0.002 **	-0.002 **	-0.002 **	-0.002 **
edu_l	0.093	0.101	0.093	0.046
edu_h	0.143	0.139	0.143	0.157
single	0.266 **	0.260 **	0.268 **	0.241 **
hsize	0.072 *	0.070 *	0.073 *	0.069
children	0.426 **	0.413 **	0.427 **	0.430 **
small_city	0.352 **	0.338 **	0.353 **	0.353 **
working	0.030	0.031	0.030	0.043
ln_income	-0.051	-0.048	-0.051	-0.079 **
orient	0.114 *	0.120 *	0.114 *	0.078
recall	0.059 **	0.057 **	0.059 **	0.059 **
math	-0.001	0.005	-0.001	-0.007
fluency	0.033 **	0.032 **	0.033 **	0.035 **
eurod	0.046 **	0.044 **	0.046 **	0.046 **
heart_attack	0.141	0.146	0.142	0.106
stroke	0.247	0.245	0.247	0.263
arthritis	0.242 **	0.241 **	0.243 **	0.244 **
cancer	-0.365 **	-0.360 **	-0.363 **	-0.423 **
parkinson	-0.368	-0.376	-0.371	-0.361

iv_fem	0.037	0.037	0.031	0.042
iv_age1	−0.002	−0.002	−0.002	−0.000
iv_age2	−0.000 *	−0.000 *	−0.000 *	−0.000
iv_edu_l	−0.074	−0.070	−0.077	−0.076
iv_edu_h	0.170 **	0.167 **	0.172 **	0.173 **
will_ans	1.166 **	1.176 **	1.175 **	1.149 **
AT	−0.001	0.015	−0.007	0.001
BE	0.614 **	0.601 **	0.611 **	0.702 **
CH	0.497 **	0.504 **	0.496 **	0.554 **
DE	−0.969 **	−0.958 **	−0.977 **	−0.958 **
DK	0.858 **	0.829 **	0.860 **	0.865 **
ES	−0.291 *	−0.276 *	−0.297 *	−0.281 *
FR	0.013	0.021	0.010	0.073
GR	1.518 **	1.453 **	1.507 **	1.808 **
IT	0.552 **	0.542 **	0.550 **	0.590 **
NL	−0.309 **	−0.297 *	−0.308 *	−0.280 *
<hr/>				
Skewness		0.382		−0.190
Kurtosis		3.059		3.873
<hr/>				

Our estimation results suggest that the relationship between sample attrition and the health status of the first wave may differ across health dimensions. On the one hand, we find that the attrition probability is negatively associated with cognitive abilities, and it is significantly higher for respondents with a diagnosed cancer and for those with fair and poor SRH₁. On the other hand, the attrition probability is significantly lower for respondents suffering from arthritis and depression problems—probably because they can be easily traced and approached by the interviewers. Other things being equal, the relationship between the attrition probability and the age of the respondents is U-shaped, with a minimum at 67 years. Furthermore, we find that the attrition probability increases with household income; decreases with household size; and is significantly lower for people who are single, have children, and live in a small city. Coherently with the findings of the survey nonresponse literature, we also find that interviewer characteristics and features of the interview process are important predictors of the attrition probability. The assumption that the error term follows a Gaussian distribution cannot be rejected by a likelihood ratio test that compares the SNP model with the probit model. Once the different scale is taken into account, the differences between probit and SNP estimates are small.

7.2 SRH status

Table 3 presents the estimates of four alternative ordered response models for SRH₂, which are labeled with the names of the corresponding Stata commands. `oprobit` is a univariate ordered probit model that ignores attrition and assumes Gaussianity of the error term in the outcome equation. `sneop` is a univariate SNP ordered response model that ignores attrition but relaxes the Gaussian distributional assumption. `opse1` is

our parametric ordered response model with sample selection that corrects for attrition by assuming that errors in the outcome and the selection equations follow a bivariate Gaussian distribution. Finally, **snpopsel** is our SNP ordered response model with sample selection that corrects for attrition without imposing strong parametric assumptions on the distribution of the two error terms. For the SNP models, we again considered alternative specifications by varying the order of the univariate and the bivariate Hermite polynomial expansions.¹⁵ The preferred model specifications, selected through the BIC, have $R = 4$ in Model 2 and $R = (3, 3)$ in Model 4. In this case, we compare ratios of the estimated coefficients by dividing the coefficient of each variable by the coefficient of the dummy variable for respondents' tertiary education. The standard errors of these ratios are computed through the delta method.

Table 3. Estimates of ordered response models for SRH in wave 2. Results are based on the normalization $|\beta_{\text{edu.h}}| = 1$. SNP-estimated coefficients of the Hermite polynomial expansions are omitted to save space. Sample size $n_2 = 16,902$.

Variable	oprobit	sneop	opsel	snpopsel
SRH1.1	-15.135 **	-14.981 **	-15.409 **	-15.530 **
SRH1.2	-8.028 **	-7.956 **	-8.165 **	-8.210 **
SRH1.4	5.915 **	5.925 **	6.062 **	5.930 **
SRH1.5	12.937 **	12.734 **	13.221 **	12.790 **
female	0.164	0.183	0.157	0.204
age1	-0.075 **	-0.065 **	-0.078 **	-0.065 **
age2	-0.002	-0.002	-0.001	-0.002 *
edu_1	-0.601	-0.473	-0.630	-0.478
single	0.629 *	0.589 *	0.606	0.562
hsize	0.184	0.188	0.178	0.178
children	0.469	0.514	0.398	0.645
small.city	0.090	-0.023	0.036	0.045
working	1.063 **	0.996 **	1.088 **	0.974 **
ln_income	0.222	0.271 **	0.236 *	0.249 *
orient	0.560 *	0.585 *	0.540 *	0.573 *
recall	0.142	0.139	0.132	0.148 *
math	0.183	0.200	0.181	0.206
fluency	0.134 **	0.128 **	0.131 **	0.134 **
eurod	-0.584 **	-0.553 **	-0.603 **	-0.557 **
heart_attack	-3.331 **	-3.173 **	-3.435 **	-3.219 **
stroke	-2.110 **	-1.845 **	-2.194 **	-1.876 **
arthritis	-2.140 **	-2.078 **	-2.233 **	-2.107 **
cancer	-1.171 *	-1.197 *	-1.141 *	-1.322 *
parkinson	-6.939 **	-6.568 **	-7.037 **	-6.894 **
AT	0.197	0.084	0.186	0.038

15. For the univariate SNP model, we compared three specifications with $R = 3, 4$, and 5. For the bivariate SNP model, we compared nine specifications with $R_1, R_2 = 3, 4$, and 5.

BE	1.845 **	1.546 **	1.760 **	1.629 **
CH	3.137 **	2.931 **	3.142 **	2.957 **
DE	-1.566 *	-1.628 **	-1.425 *	-1.937 **
DK	2.704 **	2.599 **	2.628 **	2.642 **
ES	-0.746	-0.769	-0.730	-0.929
FR	0.065	-0.047	0.071	-0.131
GR	3.393 **	3.020 **	3.224 **	3.078 **
IT	0.156	-0.088	0.060	-0.021
NL	0.637	0.210	0.694	0.120
<hr/>				
cut1	-12.440 **		-13.664 **	
cut2	2.095	3.194 **	1.217	3.766 **
cut3	17.380 **	17.540 **	16.866 **	18.330 **
cut4	28.185 **	28.077 **	27.926 **	28.863 **
<hr/>				
ρ			-0.089	0.215
Skewness		-0.035		-0.218
Kurtosis		4.126		3.875
<hr/>				

Estimates of the selection equation for the `opsel` and `snpopsel` models are presented, respectively, in the third and fourth columns of table 3. Overall, our estimation results reveal that ignoring attrition or potential departures from Gaussianity hardly affects estimated coefficients of the selection equation.

In table 3, estimated coefficients of the dummies for SRH_1 suggest that SRH is highly persistent. This result is consistent with the findings of [Contoyannis, Jones, and Rice \(2004\)](#), who analyze the dynamics of SRH using eight waves of British Household Panel Survey. We also find that SRH_2 decreases with the age of the respondent; it increases with household income; and it is significantly lower for people not working, those with lower cognitive abilities, and those suffering from mental and physical health problems. According to our parametric sample selection model, the estimate of the correlation coefficient ρ is not statistically different from zero. The sign of this estimated coefficient is somewhat counterintuitive because it would imply a positive correlation between sample attrition and SRH_2 . A sizable and positive estimate of the correlation coefficient is found in the SNP specification of our sample selection model where the point estimate of $\rho = 0.215$. The differences between parametric and SNP estimates are likely to be due to a misspecification of the distributional assumption in the outcome equation. In this equation, Gaussianity is strongly rejected at the 1% level by a likelihood-ratio test that compares the `sneop` estimates with the `oprobit` estimates.

7.3 Transition probabilities for SRH status

Although ratios of the estimated coefficients provide an easy way of comparing alternative estimation methods, their interpretation is not always straightforward. This statement explains why in discrete choice models one is usually interested in predicted probabilities and marginal effects.

In this section, we analyze the implications of the alternative estimation methods for the transition probabilities $\Pr(\text{SRH}_2 = s \mid \text{SRH}_1 = j, X_2)$, $s, j = 1, \dots, 5$. These probabilities can be easily computed through the `margins` command by varying the values of both the outcome variable SRH_2 and the binary indicators for SRH_1 , while setting the variables in X_2 to their sample means \bar{X}_2 . Below we present an example of the Stata codes used to obtain transition probabilities after `snppopsel` estimation:

```
. forvalues s=1(1)5 {
2.     margins, predict(pr outcome(`s`)) noesample
> at((means) _all SRH1_1=1 SRH1_2=0 SRH1_4=0 SRH1_5=0)
> at((means) _all SRH1_1=0 SRH1_2=1 SRH1_4=0 SRH1_5=0)
> at((means) _all SRH1_1=0 SRH1_2=0 SRH1_4=0 SRH1_5=0)
> at((means) _all SRH1_1=0 SRH1_2=0 SRH1_4=1 SRH1_5=0)
> at((means) _all SRH1_1=0 SRH1_2=0 SRH1_4=0 SRH1_5=1)
> noatlegend
3.     matrix snppopsel_`s`=r(b)
4.     forvalues j=1(1)5 {
5.         local snppopsel_`j`_`s`=snppopsel_`s`[1,`j`]
6.     }
7. }
```

Table 4 presents the estimated transition probabilities in SRH for the four models considered in the previous sections. For each model, the elements on the main diagonal correspond to the probabilities of reporting the same health status; those above the diagonal correspond to the probabilities of reporting a better health status; while those below the diagonal correspond to the probabilities of reporting a worse health status. Our estimation results clearly reveal that sample attrition and departures from the parametric distributional assumptions may seriously bias estimates of the transition probabilities. For instance, let us focus on the transition probability from poor SRH_1 to good SRH_2 . The estimate from a simple ordered probit model is equal to 18.1%. The parametric correction for sample attrition leads to a slightly higher estimate of 19.4%. If sample attrition is associated with a positive survivorship bias, this result is somewhat counterintuitive because we would expect a downward correction of improving health. This is exactly the effect captured by our SNP sample selection model where the estimated transition probability is equal to 10.7%. Similar discrepancies can be observed for most of the other transition probabilities.

Table 4. Estimates of the transition probabilities for SRH between the first and the second waves.

Model	SRH ₁	SRH ₂				
		Poor	Fair	Good	V. good	Excell.
oprobit	Poor	0.320	0.488	0.181	0.011	0.001
	Fair	0.131	0.455	0.362	0.048	0.004
	Good	0.031	0.269	0.511	0.158	0.030
	V. good	0.008	0.135	0.490	0.276	0.091
	Excell.	0.001	0.042	0.336	0.375	0.246
sneop	Poor	0.308	0.534	0.140	0.016	0.003
	Fair	0.118	0.495	0.335	0.042	0.011
	Good	0.037	0.250	0.539	0.137	0.036
	V. good	0.016	0.112	0.504	0.281	0.087
	Excell.	0.005	0.042	0.300	0.417	0.235
opssel	Poor	0.301	0.491	0.194	0.013	0.001
	Fair	0.121	0.445	0.376	0.053	0.005
	Good	0.029	0.257	0.514	0.168	0.034
	V. good	0.007	0.126	0.482	0.286	0.099
	Excell.	0.001	0.039	0.324	0.377	0.260
snpopssel	Poor	0.317	0.560	0.107	0.014	0.001
	Fair	0.141	0.489	0.330	0.032	0.009
	Good	0.055	0.237	0.563	0.114	0.031
	V. good	0.022	0.129	0.497	0.285	0.067
	Excell.	0.004	0.066	0.284	0.435	0.210

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