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# A Generalized Model for Birth and Death Mathematical Procedures in the Visitor Management: Evidence from a Protected Area 

Ioannis E. Kyritsis and Nikolaos M. Tabakis*


#### Abstract

This paper proposes a generalized model to explain the formation of the annual number of domestic and foreign visitors to Mount Olympus National Park extending the usual birth and death mathematical models. By considering that the time variable takes values from a continuum, we study the dynamics of the population via the calculation of the corresponding marginal changes. The results suggest that these changes could be expressed as the sum of two terms: The first term expresses the change that corresponds to the size of population (phenomenon of "birth" or "death" in the population), while the second term is exclusively a function of time (phenomenon of "out-migration" from or "in-migration" to the population). The proposed method could be used to study similar population structures aiming at the more efficient management of natural areas.


Key Words: stochastic processes, birth-death models, dynamics of a population

## Introduction

The birth and death stochastic processes constitute a direct generalization of Poisson process and are mainly used by the biological sciences to describe the development of populations (Edelstein-Keshet, 1988; Coquillard and Hill, 1997). In these models it is possible to have a transition from a situation of the system not only to the next (birth) but also to the previous one (death). The realizations of these transitions are not of a constant rate, as in the case of a Poisson process, but they depend on the situation in which the system is found each time, which expresses the size of population.

Moreover, birth-death stochastic processes have been used in queueing systems, since in such a system, the number of customers does not remain constant but is altered depending on arrivals and departures (Kleinrock, 1976; Newell, 1982). In addition, stochastic models that represent real populations or systems subject to various types of catastrophes (e.g. mild environmental changes or extreme natural phenomena, violent human influences) have also been studied extensively (see for example Renshaw, 1991; Matis and Kiffe, 2000; Kyriakidis, 2001). Recently, Economou and Fakinos (2003) presented real applications in population models and queueing systems (stochastic models with catastrophes, general immigration-birth-death models, $M / M / 1$ and $M / M / \infty$ queues). In particular, Kyriakidis (2003) proposed a variation of such a system where the optimal

[^0]policy initiates the controlling action if and only if the state of the process (e.g. number of customers in a queue degree of deterioration of a machine, size of biological population) exceeds a critical number. Such a policy is known as "control-limit policy".

In this paper, the application of a generalized birth-death model in the visitor management of a protected natural area is attempted. It should be noted that, based on the existing sample information, the total number of visitors is divided into subgroups, and for each one of them a different modelling is initially applied.

More specifically, in a recent publication (Parastavrou \& Kyritsis, 2001), the structure of the population of visitors to Mount Olympus National Park (Greece) was calculated in relation to the states "new visitor-"0"" and "returning visitor-" 1 "" for the past two decades. The total number of visitors to the mountain was divided into two strata of non-overlapping populations: $\mathbf{D}$ (domestic) and $\mathbf{F}$ (foreigners). The results of the above study are considered in this paper aiming at the appropriate specification, for each one of the strata $\mathbf{D}$ and $\mathbf{F}$, of a model ${ }^{2}$ which will be able to describe the formation of the total number of visitors at period $t$. Considering that the time variable $t$ takes values from a continuum, we will further study the dynamics of the population via the corresponding marginal changes.

The contribution of the paper is twofold. First, it extends the usual birth and death mathematical models by incorporating a term that is related to the phenomenon of "migration" either from or towards the population under study. Second, the model is applied in a field, which nowadays attracts a growing interest since protected natural areas and the management of the visitors in these areas is considered part of the plan for an integrated sustainable environment.

The remaining parts of the paper are organized as follows: Section 2, presents the data, discusses some methodological issues and reports the empirical results. In section 3 , the dynamics of the population via the corresponding marginal changes are studied. Concluding remarks are given in section 4 . The relevant tables of the study are presented in the Appendix.

## Estimation Results

## The Data

The data used in the empirical analysis are obtained from the archives of the Hellenic Federation of Mountaineering and Climbing and are presented in Table 1 (Appendix). More specifically, the table reports the observed total number of visitors to the mountain (Actual Total), followed by the observed number of domestic (Actual Domestic) and the observed number of foreign (Actual Foreigners) visitors. It also reports, in two columns for each one of the strata $\mathbf{D}$ (Domestics) and $\mathbf{F}$ (Foreigners), the annual composition of the population of visitors, with respect to each one of the states "new visitor" 0 "" and "returning visitor-" 1 "" (respectively $D_{0}$ and $F_{0}, D_{1}$ and $F_{1}$ ).

In order to smooth out the seasonal variability and to determine the long-term trend of the data series, a moving average transformation has been applied: thus, instead of the variable $X_{t}$ we use $\hat{X}_{t}=\left(X_{t-1}+X_{t}+X_{t+1}\right) / 3$ : this transformed variable is henceforth used as the visitor variable. The next columns in Table 1, report the estimated values $\operatorname{Smooth} D_{0}$ and $D_{1}, \operatorname{Smooth} F_{0}$ and $F_{l}$ as derived from the smoothing operation. Using
these figures, we estimate models for the annual number of domestic visitors and the annual number of foreign visitors.

## A Model for the Number of Domestic Visitors

Given that the annual number of domestic visitors equals the sum of "new" and "returning" visitors, we proceed with separate estimates for each one of its constituent parts as follows:
a. Following Kyritsis et al. (1996), the number of "new" visitors $\left(D_{0}\right)$ at period $t$ does not depend directly on the number of visitors in previous periods, but it depends on other factors, such as advertising, information, general conditions, etc. Thus, the model specified for the dependent variable $D_{0}$, including time $t$ as the predictor variable, is $D_{0}=b_{1} t+b_{0}+u_{t}$, where $u_{t}$ is the disturbance term. We made use of the Microfit 4.1 econometrics package and the initial estimation results were:

$$
\begin{equation*}
\hat{D}_{0}=12.326 t+882.870 \tag{1}
\end{equation*}
$$

The relevant diagnostic tests appear in Table 2 and reveal the existence of serious autocorrelation. Therefore, we proceeded with the necessary correction (Griffiths et al., 1993). The tests for the order of autocorrelation appear at the end of the table, and the model corrected for autocorrelation is:

$$
\begin{equation*}
\hat{D}_{0}=13.393 t+861.770 \tag{2}
\end{equation*}
$$

with $R^{2}=0.972$ and $\overline{\mathrm{R}}^{2}=0.968$ (the adjusted coefficient of determination), and $\mathrm{F}=223.254$ [0.000]. The numbers in parentheses in (2) are the estimated standard errors for the corresponding coefficients.
b. The number $D_{1}$ of "returning" visitors for a period $t$, by contrast, is supposed to depend on the number of visitors in previous periods. We therefore employ a first-order autoregressive model. The initial estimates were:

$$
\begin{equation*}
\hat{D}_{1}=0.942 D_{1}(-1)+152.424 . \tag{3}
\end{equation*}
$$

On the basis of the relevant diagnostic tests, reported in detail in Table 3, we corrected for autocorrelation and obtained the following estimate of the model:

$$
\begin{equation*}
\hat{D}_{1}=\underset{(0.047)}{0.912} D_{1}(-1)+\underset{(79.563)}{199.736}, \tag{4}
\end{equation*}
$$

with $\mathrm{R}^{2}=0.994, \overline{\mathrm{R}}^{2}=0.993$ and $\mathrm{F}=1665.1$ [0.000].
This autoregressive model can be solved as a difference equation. The solution ${ }^{3}$ of the general form of the equation

$$
\begin{equation*}
X_{t+1}=\alpha X_{t}+b \tag{5}
\end{equation*}
$$

This gives

$$
\begin{equation*}
\hat{D}_{1}=C \cdot 0.912^{t}+2269.727 \tag{7}
\end{equation*}
$$

where the parameter $C$ is determined by the initial conditions. An application of the initial condition $D_{1(t=1)}=862$ to (7) yields $C=-1543.560$, so the solution of (4) becomes

$$
\begin{equation*}
\hat{D}_{1}=2269.727-1543.560 \cdot 0.912^{t} \tag{8}
\end{equation*}
$$

and if we take into account that $0.912^{t}=e^{-0.092 t}$, (8) takes finally the form

$$
\begin{equation*}
\hat{D}_{1}=2269.727-1543.560 \cdot e^{-0.092 t} \tag{9}
\end{equation*}
$$

Therefore, in order to predict the total number of domestic visitors, we substitute (2) and (9) in the equation $\hat{D}_{t}=\hat{D}_{0}+\hat{D}_{1}$, which gives the below final estimate:

$$
\begin{equation*}
\hat{D}_{t}=3131.497+13.393 t-1543.560 \cdot e^{-0.092 t} \tag{10}
\end{equation*}
$$

## A Model for the Number of Foreign Visitors

We repeat the same process, using the data for stratum $\mathbf{F}$ (foreign visitors). However, we found out that a better fit was obtained with a non-linear second-order model, instead of a linear one between the independent variable $t$ and the dependent variable $\mathrm{F}_{0}$. Thus, after appropriate corrections similar to the ones applied to stratum $\mathbf{D}$ (which are not reproduced here in order to save space), we obtained the following estimate:

$$
\begin{equation*}
\hat{F}_{t}=\left(-6.938 t^{2}+177.445 t+3359.555\right)-233.056 \cdot e^{-0.428 t} \tag{11}
\end{equation*}
$$

The fitted values (dotted line) and the observed-smoothed values (solid line) of the total number of domestic and foreign visitors to the region are graphically presented below:


Domestic Visitors

Foreign Visitors

## The Dynamics of the Population

Next, if we consider that the time variable $t$ takes values from a continuum instead of taking discrete values $t=0,1,2 \ldots$, that have been used so far for the construction of the equations, we are able to study the dynamics of the population via the corresponding marginal changes.

In stratum $\mathbf{D}$, for the measure of the total number of visitors, we use a function of the form

$$
\begin{equation*}
D_{t}=a t+b+c e^{k t} \tag{12}
\end{equation*}
$$

If we take the derivative of (12), we obtain

$$
\begin{equation*}
\dot{D}_{t}=a+c k e^{k t} \tag{13}
\end{equation*}
$$

which presents the rate of change of the visitor population. Finally, if we eliminate the term $e^{k t}$ between the function and its derivative, we obtain the differential equation

$$
\begin{equation*}
\dot{D}_{t}=k \cdot D_{t}+(a-b k-a k t), \tag{14}
\end{equation*}
$$

and by substituting the numerical values, we obtain:

$$
\begin{equation*}
\dot{D}_{t}=-0.092 \cdot D_{t}+(301.491+1.232 t) \tag{15}
\end{equation*}
$$

Similarly, for stratum F, we find that

$$
\begin{equation*}
\dot{F}_{t}=-0.428 \cdot F_{t}+\left(-2.969 t^{2}+62.070 t+1615.335\right) \tag{16}
\end{equation*}
$$

Equations (15) and (16), which express the marginal changes in the populations of strata $\mathbf{D}$ and $\mathbf{F}$ respectively, show that these changes equal the sum of two terms. The first term, $-0.092 \cdot D_{t}$ and $-0.428 \cdot F_{t}$ respectively, (generally $k \cdot X_{t}$ ), depends on the value of $X_{t}$ of the population and expresses the change that corresponds to its size. This is described as a phenomenon of "birth" or "death", according to whether $k>0$ or $k<0$ respectively. More specifically, for the populations under study, we observe that the factor $k$ is negative in both strata, thus expressing the coefficient of death in the population.
The second term, $(301.491+1.232 t)$ in stratum $\mathbf{D}$ and $\left(-2.969 t^{2}+62.070 t+1615.335\right)$ in stratum $\mathbf{F}$, depends exclusively on time $t$ and not on the size of the population. This is described as a phenomenon of "migration" from or towards the population, depending, respectively, on whether this second term is negative or positive. More specifically, when the term is negative we refer to "out-migration", while when the term is positive we refer to "in-migration" . For the populations under study, we observe that the term is positive in stratum $\mathbf{D}$ (assuming no negative values of $t$ ), while in stratum $\mathbf{F}$ the term is positive, when $t$ belongs to the interval [ $0,36.01$ ].

## Conclusions

In this paper we present a generalized model for the annual number of domestic and foreign visitors to Mount Olympus National Park. The number of "new" visitors at any period $t$ is considered to be independent of the number of visitors in previous periods, while the number of "returning" visitors is considered to be a function of the number of visitors in previous periods. Next, by considering that the time variable $t$ takes values from a continuum, we studied the dynamics of the population via the corresponding marginal changes. The results suggest that these changes are the sum of two terms: The first term $k \cdot X_{t}$ depends on the value $X_{t}$ of the population and expresses the change that corresponds to its size (phenomenon of "birth" or "death" in the population). The second term depends exclusively on time $t$ (phenomenon of "out-migration" from or "in-migration" to the population).

The numerical values found for the two strata $\mathbf{D}$ and $\mathbf{F}$ can readily be interpreted on the basis of the particular characteristics of the two populations. A very small proportion of the population of domestic visitors who have already visited the Park is lost $(k \approx 9 \%)$, while the remaining ones visit the area repeatedly. This phenomenon could be explained by the fact that the coefficient of satisfaction of expectations is high, as it was revealed by a relevant survey (Kyritsis et al., 1996). By contrast, foreign visitors usually visit just once, but, despite the "deaths" ( $k \approx 43 \%$ ), their population is swelled by an inmigration of new individuals, in the same way as it happens with the population of domestic visitors. A further analysis of the different patterns that these models propose with regard to the phenomenon of migration would furnish useful results, while the proposed method could provide more clear inferences and be used to study similar population structures leading to more efficient management of natural areas.

## Notes

${ }^{1}$ The term "new visitor" is applied to those visiting the area for the first time, and the term "returning visitor" to those who have visited the area at least once in the past.
2 The model can be specified/estimated by applying a number of alterative appropriate techniques, e.g. Box-Jenkins time series analysis, VAR, co-integration. Here, we simply use a heuristic method, which is easy to apply and requires no expertise, making it user-friendly to a broader range of analysts (Makridakis \& Wheelwright, 1982) and suitable for the study of changes in the dynamics of a population.
${ }^{3}$ For difference equations see e.g. Goldberg, (1961).
4 These are terms that are commonly used in sociology texts.

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## APPENDIX

Table 1. Visitors to Olympus National Park during the last twenty five years

| YEAR | $t$ | Actual <br> Total | Actual <br> Domestic | Actual <br> Foreigners | $D_{0}$ | $D_{1}$ | Smooth <br> $D_{0}$ | Smooth <br> $D_{1}$ | $F_{0}$ | $F_{1}$ | Smooth <br> $F_{0}$ | Smooth <br> $F_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1980 | 0 | 4749 | 1673 | 3076 | 903 | 770 |  |  | 2778 | 298 |  |  |
| 1981 | 1 | 5266 | 1746 | 3520 | 899 | 847 | 914 | 862 | 2944 | 576 | 2736 | 446 |
| 1982 | 2 | 4859 | 1909 | 2950 | 941 | 968 | 957 | 987 | 2485 | 465 | 2778 | 521 |
| 1983 | 3 | 5602 | 2177 | 3425 | 1031 | 1146 | 974 | 1082 | 2904 | 521 | 2893 | 519 |
| 1984 | 4 | 5945 | 2084 | 3861 | 951 | 1133 | 963 | 1143 | 3289 | 572 | 3324 | 578 |
| 1985 | 5 | 6475 | 2055 | 4420 | 906 | 1149 | 918 | 1161 | 3779 | 641 | 3675 | 624 |
| 1986 | 6 | 6717 | 2100 | 4617 | 898 | 1202 | 896 | 1197 | 3957 | 660 | 3953 | 659 |
| 1987 | 7 | 6925 | 2124 | 4801 | 883 | 1241 | 892 | 1253 | 4124 | 677 | 3913 | 644 |
| 1988 | 8 | 6467 | 2213 | 4254 | 897 | 1316 | 920 | 1351 | 3659 | 595 | 3783 | 616 |
| 1989 | 9 | 6615 | 2474 | 4141 | 979 | 1495 | 930 | 1418 | 3566 | 575 | 4100 | 660 |
| 1990 | 10 | 8241 | 2356 | 5885 | 913 | 1443 | 927 | 1462 | 5073 | 812 | 4144 | 663 |
| 1991 | 11 | 6735 | 2339 | 4396 | 889 | 1450 | 959 | 1564 | 3792 | 604 | 4281 | 682 |
| 1992 | 12 | 7481 | 2872 | 4609 | 1074 | 1798 | 1007 | 1687 | 3978 | 631 | 3756 | 596 |
| 1993 | 13 | 6921 | 2870 | 4051 | 1057 | 1813 | 1085 | 1862 | 3498 | 553 | 3681 | 582 |
| 1994 | 14 | 7230 | 3100 | 4130 | 1126 | 1974 | 1129 | 1981 | 3567 | 563 | 3660 | 577 |
| 1995 | 15 | 7889 | 3359 | 4530 | 1205 | 2154 | 1165 | 2083 | 3914 | 616 | 3664 | 577 |
| 1996 | 16 | 7350 | 3286 | 4064 | 1165 | 2121 | 1194 | 2171 | 3512 | 552 | 3556 | 559 |
| 1997 | 17 | 7201 | 3450 | 3751 | 1212 | 2238 | 1189 | 2196 | 3242 | 509 | 3389 | 532 |
| 1998 | 18 | 7369 | 3419 | 3950 | 1190 | 2229 | 1158 | 2166 | 3414 | 536 | 3287 | 516 |
| 1999 | 19 | 6813 | 3104 | 3709 | 1072 | 2032 | 1147 | 2173 | 3206 | 503 | 3309 | 519 |
| 2000 | 20 | 7261 | 3437 | 3824 | 1179 | 2258 | 1117 | 2140 | 3306 | 518 | 3582 | 562 |
| 2001 | 21 | 8129 | 3230 | 4899 | 1101 | 2129 | 1105 | 2136 | 4235 | 664 | 3849 | 604 |
| 2002 | 22 | 7691 | 3055 | 4636 | 1035 | 2020 | 1086 | 2121 | 4006 | 630 | 3984 | 626 |
| 2003 | 23 | 7633 | 3336 | 4297 | 1123 | 2213 | 1076 | 2118 | 3712 | 585 | 3481 | 548 |
| 2004 | 24 | 6343 | 3190 | 3153 | 1069 | 2121 |  |  | 2724 | 429 |  |  |

The data of the first five columns derive from the archives of the Hellenic Federation of Mountaineering and Climbing. As visitors were considered all those who, within each year, reached an altitude of 2100 m (where the refuge of the Federation is located) and stayed at least for one night. The rest of the columns are based on the Papastavrou \& Kyritsis paper (2001).

Table 2. Estimation Results and Summary Statistics (Dependent Variable: $D_{0}$ )

| Estimation Prior to Autocorrelation Correction |  |  |  |
| :---: | :---: | :---: | :---: |
| Regressors | Coefficients | Standard <br> Errors | T-Ratio <br> [Prob] |
| Constant | 882.870 | 28.561 | $30.912[0.000]$ |
| T | 12.326 | 2.083 | $5.918[0.000]$ |
| Test Statistic |  |  |  |
| Diagnostic Tests |  |  |  |
| A. Serial Correlation | $X^{2}(1)=18.101[0.000]$ | $\mathrm{F}(1,20)=73.903$ |  |
| B. Functional Form |  | $X^{2}(1)=0.292[0.589]$ | $\mathrm{F}(1,20)=0.257[0.617]$ |
| C. Normality | $X^{2}(2)=1.823[0.402]$ |  |  |
| D. Heteroscedasticity | $X^{2}(1)=1.878[0.171]$ | $\mathrm{F}(1,21)=1.867[0.186]$ |  |


| Estimation Corrected for Autocorrelation |  |  |  |
| :---: | :---: | :---: | :---: |
| Regressors | Coefficients | Standard <br> Errors | T-Ratio <br> [Prob] |
| Constant | 861.770 | 38.233 | $22.540[0.000]$ |
| T | 13.393 | 2.797 | $4.788[0.000]$ |

Parameters of the Autoregressive Error Specification
$\hat{u}=1.607 \hat{u}(-1)-0.824 \hat{u}(-2)$
(13.609) (-6.979)
(T-ratios based on asymptotic standard errors in parentheses)
Log-likelihood ratio test of AR(1) versus OLS: $X^{2}(1)=33.807$ [0.000]
Log-likelihood ratio test of $\operatorname{AR}(2)$ versus $\operatorname{AR}(1): X^{2}(1)=22.437$ [0.000]

Table 3. Estimation Results and Summary Statistics (Dependent Variable

| Estimation Prior to Autocorrelation Correction |  |  |  |
| :---: | :---: | :---: | :---: |
| Regressors | Coefficients | Standard Errors | T-Ratic [Prob] |
| Constant | 152.424 | 41.253 | 3.695 [0.0 |
| $\mathrm{D}_{1}(-1)$ | 0.942 | 0.024 | 38.989 [0.1 |
| Diagnostic Tests |  |  |  |
| Test Statistic | LM Version |  | F Version |
| A. Serial Correlation | $X^{2}(1)=12.319$ [0.000] |  | $\overline{\mathrm{F}}(1,19)=24.17$ |
|  |  |  | [0.001] |
| B. Functional Form | $X^{2}(1)=4.783$ [0.029] |  | $\mathrm{F}(1,19)=5.278[0$. |
| C. Normality | $X^{2}(2)=1.941[0.379]$ |  |  |
| D. Heteroscedasticity | $X^{2}(1)=0.308[0.579]$ |  | $\mathrm{F}(1,20)=0.284[0$. |
| Estimation Corrected for Autocorrelation |  |  |  |
| Regressors | Coefficients | Standard Errors | T-Ratic [Prob] |
| Constant | 199.736 | 79.563 | 2.510 [0.0 |
| $\mathrm{D}_{1}(-1)$ | 0.912 | 0.047 | 19.558 [0.1 |

Parameters of the Autoregressive Error Specification

$$
\hat{u}=0.743 \hat{u}(-1)
$$

$$
(5.208)
$$

(T-ratio based on asymptotic standard errors in parentheses)
Log-likelihood ratio test of $\operatorname{AR}(1)$ versus OLS: $X^{2}(1)=17.416$ [0.000]
B. Ramsey's RESET test using the square of the fitted values
C. Test based on skewness and kurtosis of residuals
D. Test based on the regression of squared residuals on squared fitted valu


[^0]:    * Correspondence address: Ioannis E. Kyritsis, Department of Economics, Aristotle University of Thessaloniki, P.O. Box 170, 54124 Thessaloniki, Greece Tel.: +30-2310-996440, Fax: +30-2310-996426, e-mail: ikyr@econ.auth.gr

