



AgEcon SEARCH
RESEARCH IN AGRICULTURAL & APPLIED ECONOMICS

The World's Largest Open Access Agricultural & Applied Economics Digital Library

This document is discoverable and free to researchers across the globe due to the work of AgEcon Search.

Help ensure our sustainability.

Give to AgEcon Search

AgEcon Search
<http://ageconsearch.umn.edu>
aesearch@umn.edu

*Papers downloaded from **AgEcon Search** may be used for non-commercial purposes and personal study only. No other use, including posting to another Internet site, is permitted without permission from the copyright owner (not AgEcon Search), or as allowed under the provisions of Fair Use, U.S. Copyright Act, Title 17 U.S.C.*

The Impossibility of Causality Testing

By Roger K. Conway, P. A. V. B. Swamy, John F. Yanagida,
and Peter von zur Muehlen*

Abstract

Causality tests developed by Sims and Granger are fatally flawed for several reasons. First, when two variables, X and Y , are uncorrelated, X has no *linear* predictive value for Y , but X and Y may be nonlinearly related unless they are statistically independent, in which case X and Y are not related at all. The right-hand side variables in a regression equation are exogenous if they are mean independent of the disturbance term. Mean independence is stronger than uncorrelatedness. The proofs for deriving causality-exogeneity tests imply weaker results than statistical or mean independence. Second, transformations such as the Box-Cox transformation and Box-Jenkins stationarity-inducing transformations are not causality preserving. Third, counterexamples constructed by Price have invalidated the Pierce-Haugh theorem on instantaneous causality. Fourth, omission of other variables influencing those tested renders any test results spurious. Finally, causality tests are inconsistent because they are based on underidentified models. We provide a logically valid method of building models which does not use causality tests.

Keywords

Causality tests, statistical independence, mean independence, uncorrelatedness, orthogonality, covariance stationarity, stationarity-inducing transformations, economic laws

"Neglect by theorists evokes malpractice by empiricists"

Arthur S. Goldberger (30)¹

Introduction

Numerous recent studies in the agricultural literature use or proselytize tests of causality originally

developed by Sims (58).² The theoretical basis of this test is reproduced in Sargent (54, pp. 285-87) (For further discussion, see (52)). In an earlier study, Sargent (53) describes a causality test procedure, attributable to Granger (26) which is different from Sims' procedure. Both of these tests employ the following Granger (26) concept of causality. A time series (x_t) Granger causes another time series (y_t) if one can predict present y better by using past values of x than by not doing so. For example, in a given bivariate covariance stationary stochastic process (y_t, x_t) possessing a vector autoregressive representation, y fails to Granger cause x if and only if the coefficient matrices of the process are upper triangular. (We use the term, "Granger cause," to refer to causality in Granger's sense.) This result holds because the upper triangularity of coefficient matrices implies that y_t

*Conway is an economist with ERS, Swamy and von zur Muehlen are senior economists at the Federal Reserve Board, Washington, D.C., and Yanagida is an associate professor of agricultural economics at the University of Nevada at Reno. Views in this article are the authors' and do not reflect those of the Federal Reserve Board or the U.S. Department of Agriculture. The authors received valuable comments and help from Lorna Aldrich, James Barth, Michael Bradley, Richard Haidacher, Charles Hallahan, Arthur Haverner, Anil Kashyap, Nadine Loftin, Thomas Lutton, Lloyd Teigen, Michael Weiss, and especially J. Michael Price. The authors are also grateful to David A. Pierce whose remarks are incorporated into this article.

¹ Italicized numbers in parentheses refer to items in the References at the end of this article.

² For example, see (4, 5, 6, 8, 34, 39, 60, 67).

can be expressed as a distributed lag of current and past x 's (with no future x 's) with a disturbance process denoted by u_t and that past y 's do not help predict x_t , given past x 's. However, the disturbance u_t is uncorrelated with past, present, and future x 's for only one value of ρ in the regression $a_{yt} = \rho a_{xt} + \xi_t^\rho$ where (a_{yt}, a_{xt}) is the vector of innovations of the process (y_t, x_t) . If the coefficient matrices are not triangular, then u_t is not uncorrelated with past, present, and future x 's for any value of ρ . Because the value of ρ is usually unknown, for the disturbance u_t in the regression of y_t on current and past x 's to be uncorrelated with past, present, and future x 's, it is necessary, but not sufficient, that y fails to Granger cause x or that the coefficient matrices of the process (y_t, x_t) are upper triangular. The null hypothesis for Granger's causality test is that the coefficient matrices of the process (y_t, x_t) are upper triangular. This hypothesis can be equivalent to Sims' hypothesis that all the coefficients of future x 's in the regression of y on past, present, and future x 's are zero. Thus, Sims and Granger try to test a necessary condition for Granger noncausality. These tests were formerly associated predominantly with research in macroeconomics, which tests monetarist *versus* Keynesian assumptions about the causal ordering between money and income. They have recently been used in conjunction with rational expectations hypothesis testing.³ Various studies using the same testing procedures have produced contradictory evidence on the relationship between money and income (see (59)). The conflict between the conclusions of such studies were indeed heightened when different forms of causality testing procedures were employed (see (21)). Subsequent Monte Carlo tests offered suggestive results indicating differences in the power of various causality tests and showing that one could easily produce conflicting conclusions by employing a battery of causality tests on the same data sets (see (25, 38)). However, these empirical and Monte Carlo results are only symptomatic. It is now clear that there are profound problems, both theoretical and empirical, with causality tests. This viewpoint is most emphatically stated by statisticians who object to the apparent carelessness with which some

economists equate correlation with causality (see (37)). The purpose of our article is, therefore, to alert the agricultural profession to these problems and to allow agricultural researchers to better weigh the benefits and costs of utilizing these tests.

With that purpose in mind, we establish the following points:

- 1 The zero correlation between u_t and past, present, and future x 's is necessary, but not sufficient, for x to be strictly econometrically exogenous with respect to y . The proofs of causality and exogeneity advanced by proponents are based on weaker concepts than statistical or mean independence.
- 2 There is no good discriminant between stationary and nonstationary processes. Sims and Granger are testing a necessary condition for Granger noncausality only within the framework of covariance stationary processes.
- 3 The observed time series is necessarily finite, and the covariance stationary stochastic processes are infinite in length. Distinguishing between different stationary processes on the basis of observed time series poses fundamental difficulty. Therefore, the power of Sims' or Granger's test does not go to 1 as the sample size goes to infinity.
- 4 Even if we know the transformations which induce stationarity, these transformations are not causality preserving. Therefore, the causality relationships (or the lack thereof) among the transformed variables tell us nothing about the causality relationships (or the lack thereof) among the original variables.
- 5 Zellner (70) proposed a general definition of causality attributed to Feigl, according to whom the concept of causation is defined in terms of predictability according to a law. Therefore, we address a fundamental question in economics: Are there laws in economics? After answering this question, we suggest a logically valid method of building econometric models which does not use causality tests.

³ A key requirement of rational expectations observable reduced-form equations is that all right-hand side variables be at least orthogonal to the error term (see (17, 18)).

In subsequent sections, we define the various notions of Granger causality and contrast them with what statisticians call statistical or mean independence. We discuss problems of forming conditional operations based on linear models. We describe and critique the characterizations of Granger causality noted by Pierce and Haugh (41). We consider the causality tests as Sims proposed. We offer some general remarks on causality testing. Because we refer to laws in a philosophical definition of causation, we briefly discuss the meaning of the term "law" in economic contexts.

Correct Interpretations of Granger's Definitions of Causality

Before the causality literature can be carefully critiqued, we need to understand exactly what is meant by "causality" as posited by its proponents. Therefore, we review the various forms of Granger causality defined by Granger (26) and extended by Pierce and Haugh (41). A_t is assumed to represent a stationary stochastic vector process where

\bar{A}_t = the set of past values of A_t ,

$\bar{\bar{A}}_t$ = the set of past and present values of A_t ,

$\bar{A}_t(k)$ = the set $(A_{t-j}, j \geq k)$,

$E_t(A|B)$ = the optimal predictor of A_t , given some set of values of B_t ,⁴

$e_t(A|B)$ = the prediction error = $A_t - E_t(A|B)$,

$\text{Var}(e_t)$ = $\sigma^2(A|B)$;

U_t = the set of all information in the universe accumulated since time $t-1$, and

$U_t - Y_t$ = all information in the universe apart from Y_t .

With this information, we can define the various forms of causality as follows

1 Causality If $\sigma^2(X|\bar{U}) < \sigma^2(X|\bar{U} - \bar{Y})$, then we say Y is Granger causing X , denoted by $Y_t \Rightarrow X_t$

2 Feedback There is feedback between X and Y , denoted by $X_t \Leftrightarrow Y_t$, if $Y_t \Rightarrow X_t$ and if $X_t \Rightarrow Y_t$

3 Instantaneous causality Instantaneous causality occurs when $\sigma^2(X|\bar{U}, \bar{Y}) < \sigma^2(X|\bar{U})$

4 Causality lag If $Y_t \Rightarrow X_t$, we then define the causality lag m as the lowest integer value of k so that the $\sigma^2(X|U - Y(k)) < \sigma^2(X|U - Y(k+1))$

We now show that these definitions cannot be used to discover causality relationships without their posing some serious problems. Specifically, Granger's definitions require unequal and finite mean square errors in the series being compared. These conditions may not be satisfied in practice as may be clarified if one considers two simple polar cases. Deterministic variables or components can be predicted perfectly by their own past history with zero mean square error (see (2, p. 420)), hence, the mean square errors of the predictions of deterministic components do not satisfy the strict inequalities stated in Granger's definitions. This limitation, however, does not mean that there are no causality relationships among deterministic components. At the other extreme, when the mean square errors of the predictions of stochastic variables are infinite (a frequent occurrence in practice), Granger's definitions stated in terms of the strict inequalities between finite mean square errors of predictions do not apply. The fundamental problems associated with Granger's definitions will be clearer once we discuss the statistician's definitions and interpretations of statistical independence, mean independence, uncorrelatedness, and orthogonality.⁵

The variable Y is said to be statistically independent of the variable X if the conditional distribution of

⁴ By use of a mean square error or quadratic loss criterion

⁵ Related to this discussion are three recent papers by Chamberlain (15), Florens and Mouchart (22), and Engle, Hendry, and Richard (19) also expressing certain limitations of Granger's and Sims' definitions of causality. We extend their work by explicitly contrasting various notions of Granger causality with the statistician's concept of statistical independence or mean independence.

Y, given $X = x$, is the same as the marginal distribution of Y, that is, $F(y|x) = F(y)$, in which case

$$F(y,x) = F(y) F(x) \quad (1)$$

where $F(y,x)$ is the joint distribution of Y and X, and $F(x)$ and $F(y)$ are the marginal distributions of X and Y, respectively. Then the conditional distribution of X, given $Y = y$, denoted by $F(x|y)$, is equal to $F(x)$, that is, X is independent of Y. These two variables, Y and X, are said to be independent if equation (1) holds, including the case where $F(y)$ or $F(x)$ is zero. It is difficult to establish the existence of $F(y|x)$ or $F(x|y)$ in the general case. The conditional probability of a set $A \in \mathcal{B}$ (a Borel field of sets), given $X = x$, can be exhibited as a conditional expectation if one chooses the random variable Y as the indicator function of the set A. Thus, $P(A|x) = E(Y|x)$, as may be verified from the definition of conditional probability as given by Rao (48, p 90), for example. One should note that the Radon-Nikodym theorem establishes the existence of $P(A|x)$ almost everywhere with respect to $[dF(x)]$ as a function of x for fixed A only where the exceptional x-set may depend on A. As a result, it may not be possible to define $P(A|x)$ for all A over an x-set of probability 1, unless the union of exceptional sets is of probability zero. Thus, a conditional probability distribution of Y, given $X = x$, may not always exist (see (48, p 98))⁶. The same is true of the conditional probability distribution of X, given $Y = y$. Because the existence of $F(y|x)$ does not imply the existence of $F(x|y)$, if $F(y|x) = F(y)$, it need not be true that $F(x|y) = F(x)$. Nonetheless, when equation (1) is true, X and Y are said to be independent regardless of whether $F(y|x)$ or $F(x|y)$ exists.

The intuitive idea of the phrase "Y is independent of X" is roughly that a knowledge of X does not help one to infer the value of Y. If Y and X are statistically independent, then there is no causal

relationship between Y and X. When $F(\cdot)$ and $F(\cdot, \cdot)$ are absolutely continuous, the probability density functions exist and equation (1) can be expressed as

$$f(y,x) = f(y)f(x) \quad (2)$$

where $f(\cdot)$ is a density function.

As Whittle (68, p 101) points out, we must live with the idea that we may know $E(Y)$ (or $E(X)$) only for certain Y (or X), or that, for a given random variable Y (or X), we may know $EK(Y)$ (or $EH(X)$) only for certain K (or H). Similarly, for a given pair of random variables, Y and X, we may be able to assert the validity of the independence condition

$$EH(X)K(Y) = EH(X)EK(Y) \quad (3)$$

where the functions H and K are such that $EH(X) < \infty$ and $EK(Y) < \infty$. In this case, Y and X have only partial degrees of independence because equation (1) implies equation (3), but the converse is not true. An extreme example of this is one where we can assert the validity of the independence condition (equation (3)) only when H and K are linear functions. This essentially means we know only that

$$EXY = EXEY \quad (4)$$

where $EX < \infty$ and $EY < \infty$. Two random variables, X and Y, are said to be uncorrelated if and only if both have finite second moments and equation (4) is true (see (16, p 102)). Consequently, equation (4) is equivalent to

$$\text{Cov}(X,Y) = 0 \quad (5)$$

provided $EX^2 < \infty$ and $EY^2 < \infty$. Random variables that satisfy equation (5) are said to be uncorrelated. In the special case when either $EX = 0$ or $EY = 0$, so that equation (4) becomes $EXY = 0$, the random variables are said to be mutually orthogonal. According to Whittle (68, p 102), "the concept of lack of correlation or orthogonality is important, because it is the nearest one can come to the concept of independence if one is restricted to a knowledge of second moments [as in the case of covariance stationary processes]".

⁶ If the sample space has only a countable number of points, then the conditional probability measure is always defined, provided $P(X = x) \neq 0$. Alternatively, if the sample space is the n dimensional real Euclidean space, then the conditional probability measure exists because in this case the union of exceptional sets is of zero probability measure (48, pp 98-99). Our subsequent discussion further clarifies this point.

Just as independence means that X has no predictive value for Y , lack of correlation means that X has no predictive value for Y in the linear least squares sense (see (68, p 102)) That is, suppose we consider a predictor of Y which is linear in X , $Y = \alpha + \beta X + U$, and we choose α and β so as to minimize EU^2 . One can then determine the optimal value of β by $\text{Cov}(Y, X) / \text{Var}(X)$. Thus, if case (5) is true, the variable X will receive a zero coefficient in the prediction formula for Y . When case (5) is true, X has no linear predictive value for Y , but X may be nonlinearly related unless equation (1) is true, in which case X and Y are not related at all

A case intermediate between lack of correlation and independence is that in which equation (3) holds only for linear K , so that $EH(X)Y = EYEH(X)$ for any H assuming $EH(X) < \infty$. The relation $EH(X)Y = EYEH(X)$ is equivalent to $E(Y|X) = EY$ because $EH(X)Y = E(E[H(X)Y|X]) = E[H(X)E(Y|X)]$ for all H so that $EH(X)Y < \infty$ (see (68, p 102)).⁷ Here $E(Y|X)$ is a function of x , say $G(x)$, which minimizes $E[Y - G(x)]^2$, at least in the case where $EY^2 < \infty$ (see (2, pp 417-24)). Following Goldberger (31), we may say that Y is mean independent of X if

$$E(Y|X) = EY \quad (6)$$

Now equation (6) holds if and only if $E(Ye^{tX}) = EYEe^{tX}$ for all real t (see (36, p 10))

It is instructive to observe that without further conditions there is no connection among the concepts (1), (5), and (6). If EY exists, it follows from the Radon-Nikodym theorem that $E(Y|X)$ exists (see Rao (48, pp 96-97)). In this case, equation (1) implies equation (6), but the converse is not true. Similarly, if EX exists, then equation (1) implies the condition, $E(X|Y) = EX$, but the converse is not true. Because the existence of $EH(X)$ and $EK(Y)$ is already assumed in condition (3), partial independence condition (3) implies the mean independence condition, $E(Y|X) = EY$ or $E(X|Y) = EX$, but the converse is not true. It is obvious that any pair of random variables, X and Y , which are fully independent in the sense of equation (1) and which have finite variances are

also uncorrelated, although the converse is not true. When X and Y have finite variances, mean independence (6) implies uncorrelatedness (5), but the converse is not true. (In the normal case, conditions (1-6) are equivalent.)

Our discussion is important as, when Granger's definitions of causality are used, some researchers have confused these statistical concepts. For example, Sargent (52, pp 404-05) says that X in the following equation

$$Y_t = \sum_{j=0}^{\infty} h_j X_{t-j} + U_t \quad (7)$$

with $\sum_{j=0}^{\infty} |h_j| < \infty$, $EU_t = 0$, $EU_t^2 = \sigma_u^2$ for all t , and $EU_t U_s = 0$ for $t \neq s$, is econometrically exogenous with respect to Y_t if and only if $EU_t X_s = 0$ for all integers s and t . This definition runs counter to some textbook notions of exogeneity. For example, Theil (65, pp 110-11) and Goldberger (29, pp 380-81) have stated that X in equation (7) is econometrically exogenous with respect to Y if $E(U_t | X_s) = EU_t = 0$ for all integers s and t . This condition is stronger than Sargent's condition, as shown by the direction of the implication between equations (5) and (6).⁸ Furthermore, in his statement about a stricter form of the natural rate hypothesis, Sargent (53, p 215) incorrectly equates condition (1) with condition (6) by saying that the unemployment rate Un_t obeys the natural rate hypothesis if, in its univariate Wold representation (without a purely deterministic component)

$$Un_t = \sum_{j=0}^{\infty} a_j U_{t-j}, \quad \sum_{j=0}^{\infty} |a_j| < \infty \quad (8)$$

where the U 's are serially uncorrelated with mean zero and finite variance, σ_u^2 , the innovation U_t satisfies the condition

$$E(U_t | \theta_{t-1}) = 0 \quad (9)$$

where θ_t is a vector of the set of all variables observed at time t thought potentially to contribute to predicting unemployment, so that the innovation in the unemployment rate is statistically independent of each component of θ_{t-1} . Here some elements of θ_t represent policy instruments. Another difficulty is that Sargent's time series methods

⁷ One should note that when further expectation is taken, $E(Y|X) = E(Y|X = x)$ is replaced by $E(Y|X)$ (see (48, p 97)).

⁸ The direction of this implication has been recognized only recently by Hayashi and Sims (33).

based on non-Gaussian assumptions are only capable of examining the validity of the uncorrelatedness assumption between U_t and an element of θ_{t-1} but not the validity of the mean independence assumption (9) between these two variables

Conditional Expectations and Econometric Modeling

Note that the existence of $E(Y|x)$ does not imply the existence of $E(X|y)$.⁹ Necessary and sufficient conditions for the existence of the linear population regression function, $E(Y|x) = \alpha + \beta x$, and the constant conditional variance, $\text{Var}(Y|x) = \sigma_0^2$, have been established by Rao (see (36, p. 11, lemma 1.1.3)). Generalized conditions covering the cases of several independent variables are given by Kagan, Linnik, and Rao (36), hereafter referred to as KLR. Because these conditions have far-reaching implications for causality tests, we state them here

KLR's lemma (36). Let $\phi(t_0, t_2, \dots, t_K)$ be the characteristic function of the vector variable $(Y_t^*, X_{2t}^*, \dots, X_{Kt}^*) = (Y_t, X_{2t}, \dots, X_{Kt})$. Then, for the relations $E(Y_t | x_{1t}, \dots, x_{Kt}) = \sum_{k=2}^K \pi_k x_{kt}$ with $x_{1t} = 1$ and $\text{Var}(Y_t | x_{1t}, \dots, x_{Kt}) = \sigma_0^2 = \text{a positive constant}$ ($t = 1, 2, \dots, T$) to hold, it is necessary and sufficient that for $t = 1, 2, \dots, T$

$$\begin{aligned} D_0 \phi(t_0, t_2, \dots, t_K) |_{t_0=0} &= \sum_{k=2}^K \pi_k D_k \phi(0, t_2, \dots, t_K), \\ D_0^2 \phi(t_0, t_2, \dots, t_K) |_{t_0=0} &= -\sigma_0^2 \phi(0, t_2, \dots, t_K) \\ &+ \sum_{k=2}^K \sum_{k=2}^K \pi_k \pi_k D_k D_k \phi(0, t_2, \dots, t_K) \end{aligned} \quad (10)$$

where the time subscript t should be distinguished from the real arguments of $\phi(\cdot)$, $D_k \phi(\cdot) = \partial \phi(\cdot) / \partial t_k$, $D_k^2 \phi(\cdot) = \partial^2 \phi(\cdot) / \partial t_k^2$ and $D_k D_k \phi(\cdot) = \partial^2 \phi(\cdot) / \partial t_k \partial t_k$

If $(Y_t, X_{2t}, \dots, X_{Kt})$ is a multivariate normal, it is well-known that the conditional expectation and

conditional variance of any of these variables, given the remaining variables, are respectively linear in and independent of the conditioning vector (see (48, p. 523)). Although sufficient for the existence of these conditional expectations and variances, multivariate normality is by no means necessary, as KLR's lemma shows

KLR's lemma provides conditions for the existence of a linear reduced-form equation (or a linear population regression function) between an endogenous variable, Y , and a set of exogenous variables, X_1, \dots, X_K . In light of KLR's lemma, Granger's definitions of causality and Sargent's definition of exogeneity are clearly inadequate. The inequalities between predictive variances stated in Granger's definitions and the lack of correlation between the innovation (of a covariance-stationary, purely indeterministic and invertible process) and another variable (which follows a covariance-stationary, purely indeterministic and invertible process) stated in Sargent's definition are not sufficient for the existence of conditional expectations or linear population regression functions among the economic variables

The foregoing discussion provides the background for criticizing an econometric practice. Goldberger (29, pp. 380-88) reviews the reduced-form, recursive-form, and structural-form approaches to specify the population regression equations of endogenous variables on exogenous or predetermined variables. As he indicated in 1964 (29, pp. 386-87), each structural equation is intended to represent some aspect of the behavior of an economic unit, such as an individual, a firm, a sector, or a market. That the structural-form approach is a natural one in economics is demonstrated repeatedly in the large body of empirical literature in which models are built up equation by equation and unit by unit (see (65, pp. 468-83)). If the structural model is linear, under certain conditions we can derive an explicit reduced-form model (see (29, pp. 297-98)). Otherwise, we can only assume—incorrectly perhaps—the existence of an appropriate reduced-form model (as in (24)). Without sufficient *a priori* restrictions, the structural-form parameters will not be identified in either linear or nonlinear cases

It is vital to realize that, in the linear case, KLR's lemma points to a possible danger inherent in using

⁹ Conditions for the existence of these conditional expectations are given in (48, pp. 96-97)

a priori restrictions on the structural parameters because they may contradict the conditions of KLR's lemma and thereby prevent the existence of (1) the population regression function between each endogenous variable and a set of exogenous variables and (2) the constant conditional variance of each endogenous variable, given the exogenous variables. Thus, because the π_k 's are functions of the structural parameters (29, p. 298), the identifying restrictions on the structural parameters may imply that some of the π_k 's are restricted so that the conditions of KLR's lemma are not true. To better understand this difficulty, let us consider a simultaneous equation model which, if linear, may be expressed in the general form

$$Y\Gamma + XB = U \quad (11)$$

where Y is a $T \times L$ matrix of observations on L endogenous variables, Γ is a $L \times L$ matrix of coefficients, X is a $T \times K$ matrix of observations on K exogenous variables, B is a $K \times L$ matrix of coefficients, and U is a $T \times L$ matrix of disturbances. The elements of Γ and B are the structural coefficients (see (65, p. 440)).

Assuming that Γ is nonsingular, we can derive the reduced form as

$$Y = X\Pi + V \quad (12)$$

where $\Pi = -B\Gamma^{-1}$ is the matrix of reduced-form coefficients and $V = U\Gamma^{-1}$ is the matrix of reduced-form disturbances. Equation (12) exists if the joint characteristic functions of each endogenous variable and all the exogenous variables satisfy the conditions of KLR's lemma. In this case, we can interpret $X\Pi$ as the conditional mean of Y , given X and the covariance matrix of V as the conditional covariance matrix of Y given X . Furthermore, the covariance matrix of V will be independent of X . The reduced-form matrix of coefficients, Π , will be identified if and only if X has full-column rank. The connection between structural and reduced-form coefficients can be written as

$$\Pi\Gamma + B = 0$$

or

$$WC = 0 \quad (13)$$

where $W = (\Pi, I_K)$ is the $K \times (K+L)$ matrix of rank K and $C = (\Gamma', B')$ is the $(K+L) \times L$ matrix of structural coefficients. The i th equation of (13) may be written as

$$Wc_i = 0 \quad (14)$$

where c_i is the i th column of C . Because this is a consistent system of equations, a general solution is

$$c_i = (I - W^-W)z_i \quad (15)$$

where W^- is a generalized inverse of W and where z_i is arbitrary (see (48, p. 25)).

A priori restrictions may be exclusion restrictions stating that certain elements of c_i are zero because the variables to which they relate do not appear in the i th equation of the structural form (11), or they may be linear homogenous restrictions involving two or more of the elements of c_i . In any case, *a priori* restrictions on the elements of Γ and B do not violate the conditions of KLR's lemma if they are consistent with the class of solutions in equation (15). The vector, c_i , satisfying *a priori* identifying restrictions, should belong to the null space of W . Otherwise, *a priori* restrictions used to identify a structure may invalidate an interpretation of the right-hand side of each corresponding reduced-form equation (with the disturbance suppressed) as the conditional expectation of an endogenous variable, given the exogenous variables. Nonlinear structural models, incidentally, share this problem unless the identifying restrictions imposed on them are consistent with the following alternative sets of conditions which guarantee the existence of the nonlinear population regression functions of the form $E(Y_t | x_{1t}, \dots, x_{Kt}) = g(x_{1t}, \dots, x_{Kt}) = g(x_t)$ (48, pp. 96-99).

- 1 If $F(y, x)$ is the joint distribution function of $(Y, X_1, \dots, X_K) = (Y, X)$, then the set function $\int_{R_1 \times S} y dF(y, x)$, where $R_1 \times S$ is the cylinder set in the (Y, X) -plane with base S in the X -plane and $S \in \mathcal{B}_K$ (a Borel field of sets), is absolutely continuous with respect to $\int_S dF(x)$. Furthermore, $EY_t < \infty$.

or

- 2 The sample space for the variable (Y, X_1, \dots, X_K) is the $(K+1)$ -dimensional Euclidean space.

To elaborate on these conditions, we hold that if $EY_t = \infty$, then the (sufficient) conditions of the Radon-Nikodym theorem for the existence of $g(x_t)$ are not true. However, in many economic applications, the sample space is the n -dimensional Euclidean space, in which case the conditional expectation of Y (the indicator function of a set $A \in \mathcal{B}$, a Borel field of sets), given $X_t = x_t$, denoted by $P(A|x_t) = E(Y_t|x_t)$, is defined for all A over a x_t -set of probability 1 because the union of exceptional x_t -sets over which $P(A|x_t)$ is not defined is of zero probability measure. This finding does not mean that there are no problems if $EY_t = \infty$ whenever the sample space is the n -dimensional Euclidean space because even if $g(x_t)$ exists, it may not be consistent with the marginal distribution of x_t . Roughly speaking, $F(y_t|x_t)$ and $F(x_t)$ are consistent if they are the conditional and marginal distributions corresponding to some joint distribution of (Y_t, X_t) . This hypothesis follows from Kolmogorov's consistency theorem which is stated in (48, p. 108). If this consistency condition is not met, then the probability laws fail. By not specifying $F(x_t)$, econometricians typically ignore this consistency problem.

Goldberger (29, p. 380) points out that, by formulating a model, econometricians attempt to characterize a joint conditional probability distribution of the endogenous variables conditional on the values of the exogenous variables using available *a priori* information. In view of the preceding discussion, this task may not be feasible because econometricians' *a priori* information may prevent interpretation of each reduced-form equation as a regression equation if the information violates the conditions under which such an interpretation is valid. Thus, econometricians cannot succeed if their *a priori* information on the structural parameters is incoherent in the sense that it is inconsistent with conditions permitting the existence of the expectation of each endogenous variable, conditional on the values of the exogenous variables. This point confirms the importance of de Finetti's and Savage's coherency condition that must always be imposed on *a priori* distributions. Furthermore, a structural model is logically invalid and the attractiveness of the structural-form approach mentioned by Goldberger (29, pp. 386-87) is illusory if *a priori* restrictions on structural parameters do not permit the

interpretation of the corresponding reduced-form equations as the population regression equations. In light of a landmark paper by Boland (10, p. 506), who argues that a logically valid model is necessary before one can produce "true" empirical results, one must view this conclusion as a fundamental objection to current econometric practice.

Pierce-Haugh Characterizations of Causality

Coming full circle, we return to Granger's definitions of causality, which appeared in our initial investigation of the definitions of causality. Now that we have fully discussed the direction of the implications of full independence, partial independence, mean independence, uncorrelatedness, and orthogonality, as well as KLR's conditions for the existence of a linear regression and a constant conditional variance, we rigorously appraise works by Pierce and Haugh (41), Sims (58), and Sargent (54) based on Granger's definitions of causality.

In their survey article, Pierce and Haugh (41) developed characterizations of Granger causality, using the time series approach and certain assumptions. One of these assumptions is that there exist transformations $X_t = T_x X_t^*$ and $Y_t = T_y Y_t^*$ of the observable variables X_t^* and Y_t^* so that (X_t, Y_t) is a bivariate, nonsingular, linear covariance stationary, purely indeterministic time series and so that X_t and Y_t are causally related in the same way that X_t^* and Y_t^* are.

Very often, Pierce and Haugh argue, T_x and T_y will consist of first-difference or seasonal-difference operators because this type of transformation is frequently (presumed to be) necessary and sufficient to render the observed series stationary. Because such transformations are linear and because the optimal predictions in terms of which causality was defined by Granger are now also linear, each causality event is true of (X^*, Y^*) if and only if it is true of (X, Y) . Moreover, Pierce and Haugh argue that certain nonlinear transformations of individual variables, such as logarithms or those of Box and Cox (12), are also causality-preserving in the above sense.

Such statements, offered as assertions, have no logical proofs verifying their truth. If they are false, a study of the relationship between the transformed variables will tell us nothing about the relationship between the untransformed variables in which we are interested. Indeed, counterexamples may be constructed to show that the transformations T_x and T_y are not causality-preserving. For example, if Y_t^* is a nonstationary process with infinite mean (as would occur if Y_t^* followed a random walk), it is possible that the first difference of this series, $Y_t = Y_t^* - Y_{t-1}^*$, is stationary with a finite mean and displays causality with X_t . Yet, because Y_t^* has no finite mean, the variance of the prediction of Y_t^* may be infinite, in which case Granger's definitions of causality cannot apply. One should also remember that the Pierce-Haugh criterion assumes covariance stationarity. However, this is a condition on only the first two moments. Statistical independence, as described earlier, is concerned with the *whole* distribution. The direction of the implications between equations (5) and (6) indicates that differencing and Box-Cox transformations are not causality-preserving.

Furthermore, certain recent papers point to serious problems with the Box-Cox transformation. In their book Box and Jenkins (13) argue that, given $Y_t = Y_t^*$, the transformation $Y_t^{(\lambda)} = [(Y_t^* - 1)/\lambda]$ gives a covariance stationary process for some λ and, under normality conditions, one may consider the model

$$\phi(B) \Delta^{d_1} \Delta_s^{d_2} \left(\frac{Y_t^{(\lambda)} - 1}{\lambda} \right) = \theta(B) a_t, \quad (16)$$

$$a_t \sim N(0, \sigma_a^2)$$

where B is the backward shift operator, $\Delta = I - B$, $\Delta_s = I - B^s$, $d_1 > 0$, $d_2 > 0$, $\phi(B) = 1 - \phi_1 B - \phi_2 B^2 - \dots - \phi_p B^p$, $\theta(B) = 1 - \theta_1 B - \theta_2 B^2 - \dots - \theta_q B^q$, and the roots of $\phi(z) = 0$ and $\theta(z) = 0$ lie outside the unit circle where z is a complex variable.

A paper by Poirier (44) elaborates on the Box-Cox transformation. First, equation (16) requires the condition that $Y_t > 0$. Thus, if $(Y_t + \mu) > 0$ for some $\mu > 0$, the Box-Cox transformation can always be made on $(Y_t + \mu)$. However, if μ is unknown, the maximum likelihood estimates of the parameters of equation (16) for $Y_t + \mu$ may

not exist, and the effects of μ on estimating λ and orders p , q , d_1 , and d_2 become unknown. The question then arises how to assess the causality relationship among the original variables in equation (16) when μ is unknown.

On a related matter, Poirier and Melino (45) have shown that $E(Y_t^{(\lambda)}) = \infty$ if $-1 \leq \lambda < 0$ and $\text{Var}(Y_t^{(\lambda)}) = \infty$ if $-2 \leq \lambda < 0$ for the normal Y_t . Their conclusion is important because the concept of Granger causality is not appropriate if $E(Y_t^{(\lambda)}) = \infty$.

When $\lambda \neq 0$, the density for Y_t corresponding to the normal density for $Y_t^{(\lambda)}$ will usually be that of a truncated normal and Box and Cox's likelihood function will be incorrect. Recognizing this problem, Amemiya and Powell (1) assumed that the untransformed variable followed a two-parameter gamma distribution and then studied the limiting behavior of the Box-Cox (incorrect) maximum likelihood estimator both for the identically and independently distributed (i.i.d.) case and the regression case. Although they acknowledge that their results were based on the assumption of the gamma distribution and thus might not be universally true, "they do point to the possible danger of using the Box-Cox method." Altogether, the weight of these various studies analyzing the properties of the Box-Cox transformation cast considerable doubt on its ability to transform two time series without distorting a causal relationship between them.¹⁰

In another section of their paper, Pierce and Haugh (41) developed a test for instantaneous causality. They argued that one can determine instantaneous causality by individually prewhitening the two series of interest, using linear one-sided filters and then by analyzing the contemporaneous cross-correlation of the two created innovation series. However, Price (46) has constructed two counterexamples to show that the existence of instantaneous causality is neither necessary nor sufficient for a nonzero contemporaneous cross-correlation. As Price (46, p. 256) states, "[t]his implies that a number of the [proofs] presented by Pierce and Haugh concerning the relationship between

¹⁰ See (7) for a further discussion and other limitations.

the causal patterns of two time series and the restrictions on the cross-correlations of the corresponding 'whitened' series are either invalid or in need of further justification " Replying, Pierce and Haugh (42) conceded their earlier mistake, but maintained that the contemporaneous cross-correlation coefficient is a useful indicator of instantaneous causality when feedback from X to Y is not present Their argument is unclear to us as no proof is given Furthermore, in a recent paper, Evans and Wells (20) amend the set of equivalent and sufficient conditions under which Y does not cause X, provided by Pierce and Haugh (41)

In answer to Pierce and Haugh's statement that a nonlinear transformation such as autoregressive integrated moving average (ARIMA) modeling preserves causality relationships, an important paper by Schwert (55) uses three counterexamples to demonstrate that causal relationships among the innovations can be quite different in pattern and magnitude from the relationships among the original variables, depending upon the ARIMA models chosen to represent the variables By implication, the Box-Jenkins methods are also not causality-preserving

As Schwert (55, p 81) points out, the use of estimates of the residuals from ARIMA models, necessitated by lack of observations on the true innovations, is analogous to an errors-in-variables approach which leads to another problem

If the original variables, Y_t and X_t , are measured with error, the measurement errors will generally have a different influence on the estimators of the relationship between the innovations than on the estimators of the relationship between the original variables Thus, if the original variables are measured with random errors, causality tests based on the estimated innovations series could fail to detect relationships that would be detected using the untransformed data

There is certainly no pat procedure for choosing the proper specification of an ARIMA model Box and Jenkins' method is, as honest practitioners readily acknowledge, "an art form " Pindyck and

Rubinfeld (43, p 473) state that "it is important to realize that the specification of an ARIMA model is an art, rather than a science," while Granger and Newbold (28, p 107) affirm that "it remains the case that there does not exist a clearly defined procedure leading in any given situation to a unique identification " The basic problem is that the ARIMA models are not logically valid unless specific assumptions are true (see (61, p 139)) As in the case of many assumptions, the truth of assumptions underlying ARIMA models cannot be determined *a priori*

A related problem with Box and Jenkins' methods is that the sample autocorrelation function will not accurately reflect the properties of the population autocorrelation function (see (47, p 331)) As a result, a researcher could easily misidentify some model as an ARIMA process

One should stress that, however elaborate one's assumptions (or wishes), it is impossible to ascertain whether the time series sample (or some transform thereof) is from a covariance-stationary process because samples are finite and covariance-stationary processes are infinite in length Thus, one may choose a sample that appears to be covariance-stationary, whereas a larger sample would show this not to be the case In this regard, Tukey (66, p 50) has proved that any "finite-extent function can arise, to an arbitrarily close approximation, as a sample from a process with any spectrum " One cannot distinguish among infinite-duration processes on the basis of a finite-length time series without making strong assumptions whose truth we do not know

Finally, there is a logical problem with Box and Jenkins' method of determining the order q of the moving-average part of an ARIMA model The moving-average process of finite order q has an autocorrelation function which is zero beyond the order q It is incorrect to conclude from this that, given the j th autocorrelation coefficient, $\rho_j \neq 0$ for $j = 1, 2, \dots, q$ and $\rho_j = 0$ for $j > q$, the process has a moving-average representation The condition that a real valued series (Y_t) has a non-zero autocorrelation of order q and no nonzero autocorrelation of order greater than q is necessary, but *not* sufficient, for Y_t to have a moving average representation (see (51, lemma 1)) If

one looks at a sample autocorrelation function, which happens to have a cutoff after lag q and concludes that a moving average model of order q is appropriate for the series, then one would be erroneously treating a necessary condition as if it were a sufficient condition

Sims-Granger Causality Testing

Sims (58) proved two theorems (also described in Sargent's book (54)) that provide the basis for his causality test. Theorem 1 states: Let (X_t, Y_t) be a jointly-covariance-stationary-strictly-indeterministic-process with mean zero. Then (Y_t) fails to Granger cause (X_t) if and only if there exists a vector-moving-average-representation of the form

$$\begin{bmatrix} X_t \\ Y_t \end{bmatrix} = \begin{bmatrix} C_{11}(B) & 0 \\ C_{21}(B) & C_{22}(B) \end{bmatrix} \begin{bmatrix} \epsilon_t \\ U_t \end{bmatrix} \quad (17)$$

where ϵ_t and U_t are serially uncorrelated processes with means zero and $E\epsilon_t U_s = 0$ for all t and s . In addition, the one-step ahead prediction errors

$$X_t - E(X_t | X_{t-1}, \dots, Y_{t-1}, \dots)$$

and

$$Y_t - E(Y_t | Y_{t-1}, \dots, X_{t-1}, \dots) \quad (18)$$

are each linear combinations of ϵ_t and U_t

Theorem 2 of Sims states Y_t can be expressed as a distributed lag of current and past X 's (with no future X 's) with a disturbance process that is orthogonal to past, present, and future X 's if and only if Y does not Granger cause X . That is

$$Y_t = \sum_{j=0}^{\infty} b_j X_{t-j} + A_t \quad (19)$$

where $E(A_t X_s) = 0 \forall (t, s)$ if and only if Y does not Granger cause X .¹¹ Sims uses these theorems to develop a test of Granger causality. His method is to regress Y_t on all X 's

¹¹ Recall that the condition $E(A_t X_s) = 0 \forall (t, s)$ does not imply that $E(A_t | X_s) = EA_t = 0$ which is required to show that X_t is econometrically exogenous with respect to Y_t (see the discussion after equation (7))

$$Y_t = (X_{t+1}, X_t, X_{t-1}, \dots) + V_t \quad (20)$$

A researcher then tests the joint hypothesis that coefficients of all future X 's are zero.

Our first comment on this test is that equation (17) is an infinite order process. In practice, one can only estimate a model of the form (20) with a finite number of independent variables. Unfortunately, truncation of lag and lead lengths of model (20) destroys the logical validity of the model in the sense described by Boland (10). Indeed, in view of Boland's (11, p. 85) demonstration that there is no valid *approximate modus ponens*, the conclusions given by a truncated model of the form (20) cannot be approximately true, even when the truncated model is approximately true.

Second, the procedure proposed by Sims is a test of only a necessary, but not a sufficient, condition for Granger noncausality. The reason is that the lower triangularity restriction on the coefficient matrix of equation (17) only implies the condition that the coefficients of the future values of X in equation (19) are zero. The restriction does not imply the condition that $E\epsilon_t U_s = 0$ for all t and s or $E(A_t X_s) = 0 \forall (t, s)$ (see (52)). Even if we reject a necessary condition for Granger noncausality on the basis of Sims' test, the probability that Granger noncausality is false is less than 1 because conclusions of statistical tests do not hold with probability 1. A statement claiming that Granger's causality holds with probability less than 1 is thus neither absolutely true nor absolutely false.¹

In large samples, the situation is even worse because the power of Sims' test does not go to 1 as the sample size goes to infinity (see (52, p. 407)). Behind Sargent's conclusion that Sims' test may fail to reject the hypothesis in infinite samples, even when it is false, is an identification problem corresponding to an infinite duration process (see (61, pp. 140-41)). Gabrielsen (23) presented an important proof that the existence of a consistent estimator $\hat{\theta}$ for a parameter θ is a sufficient condition for its identifiability. An equivalent statement is that identifiability is a necessary condition for consistency. If a parameter is not identifiable in a model, then it has no consistent estimator, and consistent tests of hypotheses about

the parameter do not exist. Therefore, without additional restrictions on the coefficients and the covariance between ϵ_t and U_t , the model (20) is not identified. Tukey (66, p. 50) adds that

the existence of such a difficult connection between observables and infinite-duration processes is, for me, a good reason to doubt the adequacy of a logical structure focused on infinite-duration processes to guide the analysis of data. We cannot know precisely what the spectrum is if we know only the finite-length process, even exactly. Our fate in the real world is worse, of course, since we cannot know even the finite-length process exactly.¹²

For further discussion on spectral estimation, see (3).

General Remarks on Causality Testing

A common problem with any of the causality tests described is that the simple bivariate models can obscure more subtle (and not so subtle) relationships involving other variables. When two events are the effects of a third event which is the cause of them, logicians describe the causal relationship between the two events as the "fallacy of the common cause." This is a problem acknowledged by proponents such as Granger (26), Pierce (40), and Sims (56, 57) and is analyzed by Jacobs, Leamer, and Ward (35) who show that "any specification error renders the causality tests uninterpretable." Not only can causality tests reject exogeneity when the variable is exogenous because of the identification problems mentioned above, it can also accept exogeneity when the variable is, in fact, endogenous.

The stationarity assumption used by Sims (58) and Sargent (53) is inappropriate for aggregate time series. This problem can be seen from Swamy, Barth, and Tinsley (61, pp. 133-36) who prove that aggregation over disparate micro relations

can yield models with time-varying coefficients, a result that is not always appreciated in either time series or conventional econometric literature. As shown by Swamy and Tinsley (63), a time-varying parameter model can accommodate a great variety of nonstationary processes. Also related to this argument is the Lucas critique, namely, when structural parameters are not invariant under alternative policy regimes, the stationarity assumptions used by Sims and Sargent are not reasonable.

Some Thoughts on Causality and Related Topics

In a wide-ranging, yet cogent, essay on the nature of causation, Zellner (70) argues articulately about the inadequacy of Granger's definition of causality and the superiority of the philosophical definition of causality provided by Feigl for econometric work. According to Feigl, the concept of causation is defined in terms of *predictability according to a law* (or more properly, according to a set of laws) (see (70, p. 12)). The reason Zellner (70, p. 51) prefers Feigl's definition of causation to all the other definitions he considers is that departures from Feigl's definition have produced problems, while offering little in the way of dependable and convincing results. Zellner (70, p. 51) further points out that in establishing and using economic laws in econometrics one can have little doubt that economic theory, data, and other subject matter considerations, as well as econometric techniques including modern time series analysis, must all play a role.

Although we agree with Zellner's views, Blaug's statement (9, pp. 160-62) concerning economic laws also deserves some attention. In Blaug's view, the term "law" has gradually acquired an old-fashioned ring and economists now prefer to present their most cherished general statements as "theorems" rather than as "laws." He further says

At any rate, if by laws we mean well-corroborated, universal relations between events or classes of events deduced from independently tested initial conditions, few modern economists would claim that economics has so far produced more than one or two laws.

¹² Other papers by Jacobs, Leamer, and Ward (35), Engle, Hendry and Richard (19), and Buiter (14) have discussed this subject and suggested that there is a problem of testing for exogeneity. However, none has discussed the identification problem with any degree of comprehensiveness.

The statement is accompanied by the following illuminating footnote

Samuelson remarks that years of experience have taught him how treacherous are economic "laws" in economic life e.g. Bowley's Law of constant relative wage share, Long's Law of constant population participation in the labor force, Pareto's Law of unchangeable inequality of incomes, Denison's Law of constant private saving ratio, Colin Clark's Law of a 25 percent ceiling on government expenditure and taxation, Modigliani's Law of constant wealth-income ratio, Marx's Law of the falling rate of real wage and/or the falling rate of profit, Everybody's Law of a constant capital-output ratio. If these be Laws Mother Nature is a criminal by nature

As indicated earlier, some econometric assumptions have become so dear that they have assumed a power nearly as compelling as law. Thus, if stationarity for the transformation of the variable Y_t in equation (16) (given some d_1 , d_2 and λ), is taken to be a law, then Mother Nature must surely be a scofflaw

In view of these statements, a more modest, but more realistic, approach might be to define causation in terms of "predictability according to a sufficient and logically consistent explanation or theory"¹³ The qualification "sufficient and logically consistent" is added to indicate that, at the very minimum, real economic theories must be logically valid if they are to provide "true" explanations of real economic phenomena. This requirement holds even though the logical validity of any explanation does not imply its truth. Nevertheless, consistency of knowledge plays a major role in how one explains the world, the *truth* of knowledge is much more difficult to ascertain (see (10)). A modest research program then becomes if all the predictions of a logically valid theory pass a conventional test (of observation), then we may say without contradiction that the theory is so far confirmed

¹³ Perhaps by "law" Zellner (70) meant a "sufficient and logically consistent explanation or theory"

Swamy, Barth, and Tinsley (61, pp. 131-36) make serious efforts to exploit economic theories in empirical research by using a minimal set of auxiliary assumptions and coherent prior information. In their expectations model, offered as an alternative to rational expectations, subjective probabilities are not carelessly equated to "objective probabilities" and all regression coefficients are allowed to vary over time as a concession to Samuelson's ironic list of so-called laws. We sometimes prefer the above model because (1) it avoids Box and Jenkins', Pierce and Haugh's, and Sims and Sargent's stationarity assumptions or stationarity-inducing transformations and (2) it is not forced to rely on econometric assumptions about *a priori* structural parameter information that may contradict necessary and sufficient conditions for the existence of the conditional expectations of endogenous variables, given the exogenous variables. Furthermore, deviating from usual practice, the model does not confine all uncertainty to the intercept term, but allocates it over all coefficients in each equation. Because the model is less restrictive, this procedure of first distributing uncertainty to all coefficients and then of letting data determine the major channels of uncertainty is less objectionable than the conventional procedure which first arbitrarily allocates all uncertainty to the intercept term and then forces the data to satisfy this restriction (see (49) for a survey of initial efforts in this research program and also (50, 63, 64) for some of the latest theoretical and empirical results)

In the above model, the conditions for logical validity are weaker than those which derive ARIMA and conventional econometric models. Because the problem of induction is unsolved, logical validity requires that the truth of one's premises or assumptions must be assumed.¹⁴ Under these circumstances, it is prudent to work with a minimal set of assumptions. How compelling the above advice is depends, of course, on the purpose of a model. If forecasting future events is the single object of a modeling endeavor, then predictive success is a sufficient argument in favor of the model. This view of the *role* of

¹⁴ For a demonstration that causality proponents have fallen into the trap of attempting to solve the well known "problem of induction," see (62)

models is called "instrumentalism" (see 10, p 508)) In this case, *a priori* truth of the assumptions is not required if it is already known that the predictions are true or acceptable by some conventional criterion (see (10, p 509)) In contrast, those economists who see the object of science as finding the *one* true theory of the economy will find their task difficult, if not impossible On the surface, instrumentalism offers a valid guide for scientific investigation It is unfortunate that no single model predicts all variables better than all other models for all time periods This predictive criterion must eventually exhaust itself Because it is impossible to foretell the time of failure, we cannot even pick a model based on instrumentalism However, we can reject models on the grounds of logical invalidity, as we did in the preceding sections

Given the difficulty of choosing among logically valid models, the principle of parsimony has sometimes been invoked as a tempting guide The imposition of certain restrictions on the time-varying parameter models can lead to conventional regression models with heteroscedastic or serially correlated error terms (or the ARIMA models) (see (63, pp 107-08)) Although these restrictions produce substantial economies in parameterizing a model, such economies are not without cost Despite its tempting name, the principle of parsimony—preferring restricted specifications to more complex modeling whenever the performance of the former in prediction is *almost as good* as that of the latter—has little justification unless the conventional or ARIMA models perform *at least as well* as some more general model, for example, the alternative expectations model proposed by Swamy, Barth, and Tinsley (61)

The conventional models, including ARIMA models, exhibit episodic breakdowns and perform poorly in prediction The usual practice is to repair such models by extensive respecification or, more often in the shorter run, with judgmental "add factors," dummy variables, and "ratchet" arguments Following Lakatos (see (9, p 36)), we may call this research practice "degenerating" because it involves endlessly adding *ad hoc* adjustments that merely accommodate whatever new facts become available A positive contribution is possible only if the scientific research program is *theoretically pro-*

gressive—that is, if a successive formulation of the program contains "excess empirical content" over its predecessor, that is, the program predicts "some novel, hitherto unexpected fact" or if the program is *empirically progressive*—that is, if "this excess empirical content is corroborated" The limited evidence presented by Havenner and Swamy (32), Resler, Barth, Swamy, and Davis (50), and Swamy, Tinsley, and Moore (64) appears to favor the claim that the time-varying coefficient models facilitate progressive scientific research programs Just as the philosophy of instrumentalism does not permit us to call one of the existing models the best predictor of all variables for all time periods, so the principle of parsimony does not permit us to call one model the best

Time-varying coefficient models such as those Swamy and Tinsley (63) propose may be too complex to be useful Indeed, Popper has argued that theoretical simplicity may be equated to the degree to which a theory can be falsified, in the sense that the simpler the theory, the stricter its observable implications and, hence, the greater its testability It is because simpler theories have these properties that we aim for simplicity in science But this principle is not universally agreed upon Thus, Blaug (9, p 25) casts his doubts about Popper's notion of simplicity as follows

It is doubtful that this is a convincing argument, since the very notion of simplicity of a theory is itself highly conditioned by the historical perspective of scientists More than one historian of science has noted that the elegant simplicity of Newton's theory of gravitation, which so impressed nineteenth-century thinkers, did not particularly strike seventeenth-century contemporaries, and if modern quantum mechanics and relativity theory are true, it must be conceded that they are not very simple theories Attempts to define precisely what is meant by a simpler theory have so far failed, and Oscar Wilde may have been right when he quipped that the truth is rarely pure and never simple

One of these statements is accompanied by the following footnote

As Polanyi has observed, "great theories are rarely simple in the ordinary sense of the term. Both quantum mechanics and relativity theory are very difficult to understand, it takes only a few minutes to memorize the facts accounted for by relativity, but years of study may not suffice to master the theory and to see these facts in its context."

Conclusions

The term, "causality," as used by Granger and his followers, has been erroneously identified with feedback or dependence and loosely with correlation (see (71, p. 313)). We have contrasted this new usage with traditional approaches proposed by scientific philosophers and surveyed by Zellner (70). By every acceptable norm, the latter approach may still offer sharper views on the definition of causation. There is evidence (see (71, p. 313)) that Granger himself has altered his views since his initial article. Granger now argues "Provided I define what I personally mean by causation, I can use the term" (27, pp. 333 and 337). What Granger means by causality is that knowledge of Y_t increases one's ability to forecast X_{t+1} in a least squares sense. Truth, like beauty, may be in the eyes of the beholder, but it is still fair to insist that the purpose of language is to communicate and clarify. Perhaps much of the confusion surrounding the interpretation of causality tests would not have arisen if such tests had instead been labeled "tests of relative predictive efficiencies" or some other neutral terms suggested by Schwert (55, p. 82).

More important, the difficulty with using Granger's causality definitions, even as a measure of relative forecasting efficiency, is that the same relationship may not continue into the forecast period. There is indeed every reason to believe that such a relationship will change. One may support this belief by contemplating the numerous structural upheavals of the seventies as well as the implication of Lucas' critique suggesting that individual behavior (and hence structural coefficients) will change when policy rules change.

Zellner (70) recommends using Feigl's definition of causation, which we respectfully modify to read, "predictability according to a sufficient and

logically consistent theory." This modification is necessary because contemporary economists prefer to present their most cherished general statements as theorems rather than as laws.

Causality tests were created with the best of intentions, but one must be careful never to ask more of the data than they can deliver. It is unfortunate that these tests seem to ask for more. However, if one can find a way to avoid the contradictions between the *a priori* restrictions on the structural parameters and the conditions of KLR's lemma and if these restrictions are overidentifying, then one can invoke Wu's procedures (69) to examine the significance of the covariances between independent variables and the disturbances (provided we have an identifiable maintained hypothesis).¹⁵ Unlike causality tests, Wu's procedures adhere to a law of large numbers, the powers of his tests, therefore, equal 1 in sufficiently large samples.

Where, then, is the econometrician left in devising a modeling strategy to determine causality? Zellner's fundamental argument is that the soundness of our conclusion about causality is ultimately based on the soundness of economic theory to determine causality. In our view, this advice is wise, and in the spirit of Zellner's theme, we end with a revealing conversation between Fisher and Cochran, which Zellner quotes (72, p. 13).

About 20 years ago, when asked in a meeting what can be done in observational studies to clarify the step from association to causation, Sir Ronald Fisher replied "Make your theories elaborate." The reply puzzled me at first, since by Occam's razor the advice usually given is to make theories as simple as is consistent with known data. What Sir Ronald meant, as the subsequent discussion showed, was that when constructing a causal hypothesis one should envisage as many *different* consequences of its truth as possible, and plan observational studies to discover whether each of these consequences is found to hold.

¹⁵ Our earlier discussion indicates that in the normal case uncorrelatedness is equivalent to mean independence.

References

- (1) Amemiya, T, and J L Powell "A Comparison of the Box-Cox Maximum Likelihood Estimator and the Non-Linear Two-Stage Least Squares Estimator," *Journal of Econometrics*, Vol 17, Dec 1981, pp 351-81
- (2) Anderson, T W *The Statistical Analysis of Time Series* New York John Wiley & Sons, 1971
- (3) Barth, J R, and J T Bennett "Cyclical Behavior Seasonality, and Trend in Economic Time Series," *Nebraska Journal of Economics and Business*, Vol 13, No 1, Winter 1974, pp 48-69
- (4) Belongia, M, and D A Dickey "Prefiltering and Causality Tests," *Agricultural Economics Research*, Vol 34, No 4, Oct 1982, pp 10-14
- (5) Bessler, D A, and J A Brandt "Causality Tests in Livestock Markets," *American Journal of Agricultural Economics*, Vol 64, No 1, Feb 1982, pp 140-44
- (6) Bessler, D A, and L F Schrader "Measuring Leads and Lags Among Prices Turkey Products," *Agricultural Economics Research*, Vol 32, No 1, Jan 1980, pp 1-7
- (7) Bickell, P J, and K A Doksum "An Analysis of Transformation Revisited," *Journal of the American Statistical Association*, Vol 374, No 3, June 1981, pp 296-311
- (8) Bishop, R V "The Construction and Use of Causality Tests," *Agricultural Economics Research*, Vol 31, No 4, Oct 1979, pp 1-6
- (9) Blaug, M *The Methodology of Economics* New York Cambridge Univ Press, 1980
- (10) Boland, L A "A Critique of Friedman's Critics," *Journal of Economic Literature*, Vol 17, No 2, June 1979, pp 503-22
- (11) Boland, L A "Satisficing in Methodology A Reply," *Journal of Economic Literature*, Vol 19, No 1, Mar 1981, pp 84-86
- (12) Box, G E P, and D R Cox "An Analysis of Transformations," *Journal of the Royal Statistical Society, Series B*, Vol 26, 1964, pp 211-52
- (13) Box, G E P, and G M Jenkins *Time-Series Analysis Forecasting and Control* 2nd ed San Francisco Holden-Day, 1976
- (14) Buiter, W "Granger-Causality and Stabilization Policy " NBER Technical Working Paper No 10 1981
- (15) Chamberlain, G "The General Equivalence of Granger and Sims Causality," *Econometrica*, Vol 50, No 3, May 1982, pp 569-82
- (16) Chung, K L *A Course in Probability Theory* 2nd ed New York Academic Press, 1974
- (17) Conway, R K, and J R Barth "New Developments in Macroeconomic Theory A Prospectus and Appraisal," *Agricultural Economics Research*, Vol 35, No 3, July 1982, pp 23-29
- (18) Conway, R K, and E G Fryar, Jr "Rational Expectations in Agricultural Economics Research and Policy Analysis Some Pitfalls " Univ of Arkansas Agricultural Economics Staff Report 1983
- (19) Engle, R F, D F Hendry, and J F Richard "Exogeneity," *Econometrica*, Vol 51, No 2, Mar 1983, pp 277-304
- (20) Evans, L, and G Wells "Pierce and Haugh on Characterizations of Causality A Re-examination," *Journal of Econometrics*, Vol 23, No 3, Dec 1983, pp 331-36
- (21) Feige, E, and D K Pearce "The Casual Causal Relationship Between Money and Income Some Caveats for Time Series Analysis," *Review of Economics and Statistics*, Vol 61, No 4, Nov 1979, pp 521-33

- (22) Florens, J. P., and M. Mouchart "A Note on Noncausality," *Econometrica*, Vol 50, No 3, May 1982, pp 583-92
- (23) Gabrielsen, A "Consistency and Identifiability," *Journal of Econometrics*, Vol 8, No 2, Oct 1978, pp 261-64
- (24) Gallant, A. R., and A. Holly "Statistical Inference in An Implicit, Non-Linear, Simultaneous Equation Model in the Context of Maximum Likelihood Estimation," *Econometrica*, Vol 48, No 3, Apr 1980, pp 697-720
- (25) Geweke, J., R. Meese, and W. Dent "Comparing Alternative Tests of Causality in Temporal Systems: Analytic Results and Experimental Evidence," *Journal of Econometrics*, Vol 21, No 3, Feb 1983, pp 161-94
- (26) Granger, C. W. J. "Investigating Causal Relations by Econometric Models and Cross-Spectral Methods," *Econometrica*, Vol 37, No 3, July 1969, pp 424-38
- (27) ——— "Testing for Causality: A Personal Viewpoint," *Journal of Economic Dynamics and Control*, Vol 2, No 4, Nov 1980, pp 329-52
- (28) ———, and P. Newbold *Forecasting Economic Time Series* New York: Academic Press, 1977
- (29) Goldberger, A. S. *Econometric Theory* New York: John Wiley & Sons, 1964
- (30) ——— "Structural Equation Methods in the Social Sciences," *Econometrica*, Vol 40, No 6, Nov 1972, pp 979-1002
- (31) ——— *Topics in Regression Analysis* New York: The Macmillan Company, 1968
- (32) Havenner, A., and P. A. V. B. Swamy "A Random Coefficient Approach to Seasonal Adjustment of Economic Time Series," *Journal of Econometrics*, Vol 15, No 2, Feb 1981, pp 177-209
- (33) Hayashi, F., and C. A. Sims "Nearly Efficient Estimation of Time Series Models with Predetermined, But Not Exogenous, Instruments," *Econometrica*, Vol 51, No 3, May 1983, pp 783-98
- (34) Heien, D. M. "Markup Pricing in a Dynamic Model of the Food Industry," *American Journal of Agricultural Economics*, Vol 62, No 1, Feb 1980, pp 10-18
- (35) Jacobs, R. L., E. E. Leamer, and M. P. Ward "Difficulties with Testing for Causation," *Economic Inquiry*, Vol 17, July 1979, pp 401-13
- (36) Kagan, A. M., Y. V. Linnik, and C. R. Rao *Characterization Problems in Mathematical Statistics* New York: John Wiley & Sons, 1973
- (37) Ling, R. F. "Review of Correlation and Causation by David A. Kenny," *Journal of the American Statistical Association*, Vol 77, No 378, June 1982, pp 488-91
- (38) Nelson, C. R., and G. W. Schwert "Tests for Predictive Relationships Between Time Series Variables: A Monte Carlo Investigation," *Journal of the American Statistical Association*, Vol 377, No 1, Mar 1982, pp 11-18
- (39) Phipps, T. "Farmland Prices and the Return to Land: An Application of Causality Testing." Paper presented at American Agricultural Economics Association Meetings, Logan, Utah, 1982
- (40) Pierce, D. A. "Relationships—and the lack thereof—Between Economic Time Series, with Special Reference to Money and Interest Rates," *Journal of the American Statistical Association*, Vol 72, No 357, Mar 1972, pp 11-21
- (41) ———, and L. D. Haugh "Causality in Temporal Systems: Characterizations and a Survey," *Journal of Econometrics*, Vol 5, No 3, May 1977, pp 265-95

- (42) _____ "The Characterization of Instantaneous Causality A Comment," *Journal of Econometrics*, Vol 10, No 2, June 1979, pp 257-59
- (43) Pindyck, R S, and D L Rubinfeld *Econometric Models and Economic Forecasts* New York McGraw-Hill Book Company, 1976
- (44) Poirier, D J "Experience with Using the Box-Cox Transformation when Forecasting Economic Time Series—A Comment," *Journal of Econometrics*, Vol 14, No 2, Oct 1980, pp 277-80
- (45) _____, and A Melino "A Note on the Interpretation of Regression Coefficients Within a Class of Truncated Distributions," *Econometrica*, Vol 46, No 5, Sept 1978, pp 1207-09
- (46) Price, J M "The Characterization of Instantaneous Causality A Correction," *Journal of Econometrics*, Vol 10, No 2, June 1979, pp 253-6
- (47) Priestley, M B *Spectral Analysis and Time Series* New York Academic Press, 1983
- (48) Rao, C R *Linear Statistical Inference and Its Applications* 2nd ed New York John Wiley & Sons, 1973
- (49) Rausser, G C, Y Mundlak, and S R Johnson "Structural Change, Parameter Variation and Forecasting," *New Directions in Econometric Modeling and Forecasting in US Agriculture* (ed G C Rausser) New York American Elsevier Publishing Co, 1983
- (50) Resler, D H, J R Barth, P A V B Swamy, and W D Davis "Detecting and Estimating Changing Economic Relationships The Case of Discount Window Borrowings" Special Studies Paper 165 Washington, D C Federal Reserve Board, 1982
- (51) Rose, D E "Forecasting Aggregates of Independent ARIMA Processes," *Journal of Econometrics*, Vol 5, No 3, May 1977, pp 323-46
- (52) Sargent, T J "Causality, Exogeneity, and Natural Rate Models Reply to C R Nelson and B T McCallum," *Journal of Political Economy*, Vol 87, 1979, pp 403-09.
- (53) _____ "A Classical Macroeconometric Model for the United States," *Journal of Political Economy*, Vol 84, No 2, Apr 1976, pp 207-37
- (54) _____ *Macroeconomic Theory* New York Academic Press, 1979
- (55) Schwert, G W "Tests of Causality The Message in the Innovations," *Carnegie-Rochester Conference Series on Public Policy*, Vol 10 (ed Karl Brunner and Allan H Meltzer) Supplement to *Journal of Monetary Economics* Amsterdam North-Holland Publishing Company, 1979, pp 55-96
- (56) Sims, C A "Exogeneity and Causal Ordering in Macroeconomic Models," *New Methods in Business Cycle Research Proceedings from a Conference* (ed C A Sims) Minneapolis Federal Reserve Bank of Minneapolis, 1977, pp 23-43
- (57) _____ "Macroeconomics and Reality" *Econometrica*, Vol 48, No 1, Jan 1980, pp 1-49
- (58) _____ "Money, Income, and Causality" *American Economic Review*, Vol 62, No 4, Sept 1972, p 540-52
- (59) Slaugh, J R "Granger-Sims Causality A Brief Survey of Its Use and Misuse" Unpublished manuscript National Science Foundation, 1981
- (60) Spreen, T H, and J S Shonkwiler "Causal Relationships in the Fed Cattle Market," *Southern Journal of Agricultural Economics*, Vol 13, No 1, July 1981, pp 149-53
- (61) Swamy, P A V B, J R Barth, and P A Tinsley "The Rational Expectations Approach to Economic Modelling," *Journal of Economic Dynamics and Control*, Vol 4, No 2, May 1982, pp 125-47

- (62) Swamy, P A V B , R K Conway, and P von zur Muehlen "The Foundations of Econometrics—Are There Any?" Special Studies Paper 182. Washington, D C Federal Reserve Board, 1984
- (63) Swamy, P A V B , and P A Tinsley "Linear Prediction and Estimation Methods for Regression Models with Stationary Stochastic Coefficients," *Journal of Econometrics*, Vol 12, No 2, Feb 1980, pp 103-42
- (64) _____, and G Moore "An Autopsy of a Conventional Macroeconomic Relation The Case of Money Demand " Special Studies Paper 167 Washington, D C Federal Reserve Board, 1982
- (65) Theil, H *Principles of Econometrics* New York John Wiley & Sons, 1971
- (66) Tukey, J W "Comments on Seasonality Causation, Interpretation, and Implications by C W J Granger," *Seasonal Analysis of Economic Time Series* (ed A Zellner) U S Department of Commerce, Bureau of the Census, 1978, pp 50-53
- (67) Ward, R W "Asymmetry in Retail, Wholesale, and Shipping Point Pricing for Fresh Vegetables," *American Journal of Agricultural Economics*, Vol 64, No 2, May 1982, pp 205-12
- (68) Whittle, P *Probability* New York John Wiley & Sons, 1976
- (69) Wu, D M "Alternative Tests of Independence Between Stochastic Regressors and Disturbances," *Econometrica*, Vol 41, No 3, July 1973, pp 733-50
- (70) Zellner, A "Causality and Econometrics," *Carnegie-Rochester Conference Series on Public Policy* Vol 10 (ed Karl Brunner and Allan H Meltzer) Supplement to *Journal of Monetary Economics* Amsterdam North-Holland Publishing Company, 1979
- (71) _____ "Comment," *Journal of the American Statistical Association*, Vol 77, No 378, June 1982, pp 313-14
- (72) _____ *An Introduction to Bayesian Inference in Econometrics* New York John Wiley & Sons, 1971