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Matrix Generator and Optionals (MGAO):

Users Guide

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MGAO - Operation Outline

H. McDowell

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Preface

Matrix Generator and Optionals (MGAO) is a computer software package developed by Paul Chang and Terry L. Roe. The program is designed to generate input data for a linear programming problem approximating a non-linear programming problem, submit the generated problem to an optimization package, from which the user receives standard computer output.

This paper results directly from efforts by the author to utilize the program and is the first comprehensive documentation written on the program. It is hoped that this paper will make available a useful computer program to those interested. Criticism and suggestions are welcome.

Terry L. Roe provided a significant contribution in the theoretical section and in the general organization of the paper. Reviews by Jeff Apland, Vernon Eidman, and Boyd Buxton are appreciated.

I. INTRODUCTION

Matrix Generator and Optionals (MGAO) is a fortran computer program developed to generate input matrices for mathematical programming algorithm.[1] Of primary importance is its capacity to generate a linear programming problem approximating a nonlinear programming problem.

Specifically, the program is capable of generating matrices for solving linear approximations of nonlinear programming problems incorporating linear or nonlinear supply and demand functions, linear and nonlinear production functions having multiple inputs, and substitutability in demand.

The program operates in conjunction with Multi Purpose Optimization System, MPOS, a system of mathematical programming algorithms developed for solving optimization problems on CDC 6000/CYBER computers. The system includes various linear programming (LP), integer programming (IP), and quadratic programming (QP) algorithms, and an interface with CDC's APEX, a system designed for solving large scale linear programming problems.[2]

For purposes of exposition each mathematical program may be viewed as being composed of two parts, a nonaugmented and an augmented section. The nonaugmented portion is perhaps best illustrated or characterized by most traditional linear programming problems. Following Intrilligator, this portion of the problem may be stated as "choosing nonnegative values of certain variables so as to maximize or minimize a given linear function subject to a given set of linear inequality constraints....

...
$$\max_{\underline{X}} F(\underline{X}) = \underline{CX}$$
Subject to
$$\underline{AX} \leq \underline{b}, X \geq 0$$
(where A is $\max_{\underline{X}}$, $\max_{\underline{X}}$, $\max_{\underline{X}}$, $\max_{\underline{X}}$, $\max_{\underline{X}}$), $\max_{\underline{X}}$)

"or, written out in full:

$$\max_{x_1, x_2, \dots x_n} F(x_1, x_2, \dots x_n) = c_1 x_1 + c_2 x_2 + \dots + c_n x_n$$

subject to:

Clearly, a problem of this nature requires nothing more than defining the activities (x's) the coefficients (c's and a's) and the right-hand-side (RHS) parameters (b's). Therefore in this respect, MGAO is simply a means of entering the data for a linear programming problem, or the linear portion of a nonlinear programming problem. This specification is referred to as the nonaugmented problem, i.e. it has not been augmented to include a nonlinear function.

The augmented portion of the matrix is that portion generated by the program from input data in linear functional form. The principle involved is that a nonlinear function may be approximated by a number of linear steps each of which is a separate linear programming activity. Hence, this technique is also known as separable programming. As the number of steps increases the loss in accuracy decreases. The nonlinear programming problem is stated by Intrilligator below.

"The nonlinear programming problem is that of choosing nonnegative values of certain variables so as to maximize (minimize) a given quasi-concave (convex) function subject to a set of inequality constraints....

... max
$$F(\underline{X})$$
 subject to $\underline{g}(\underline{X}) \le \underline{b}$ $\underline{X} \ge \underline{0}$

or written out in full:

$$\max_{\mathbf{x}_{1}...\mathbf{x}_{n}} \mathbf{F}(\mathbf{x}_{1}...\mathbf{x}_{n}) \text{ subject to}$$

$$\mathbf{g}_{1}(\mathbf{x}_{1}...\mathbf{x}_{n}) \leq \mathbf{b}_{1}$$

$$\mathbf{g}_{m}(\mathbf{x}_{1}...\mathbf{x}_{n}) \leq \mathbf{b}_{m}$$

$$\mathbf{x}_{1} \geq 0,..., \mathbf{x}_{n} \geq 0."[4]$$

This portion of the problem requires entering the objective function $F(\underline{X})$, and the constraints $\underline{g}(\underline{X})$, in nonlinear form. MGAO then defines discrete linear programming activities with the appropriate objective and constraint activities according to the instructions provided by the user.

The augmented portion of the matrix is also referred to as the extended portion of the matrix.

In specification of problems with both nonaugmented and augmented matrices, the user is advised to design the matrices such that the nonaugmented portion of the matrix, i.e. that part not containing linear approximations of nonlinear equations, is in the upper left hand portion of the matrix and that all transfer or summary columns from the generated rows of the matrix containing the linear approximations of nonlinear functions be on the left hand side. This will prevent respecification to fit the program input format. This will become apparent with examination of the same problems.

II. THEORETICAL REVIEW

Although the program can be used in solving many different types of problems it was designed to facilitate the solution of sectoral models. The user is referred to Duloy and Norton, and Klein and Roe.[5]

The concept is that given "well-behaved" supply and demand functions, a market equilibrium price and quantity may be found by maximizing the area bounded on the right by the supply and demand curves.

Referring to Figure 1. Equilibrium Solution, the equilibrium price and quantity, p*, q*, may be found by discovering the quantity that maximizes (area A and area B).

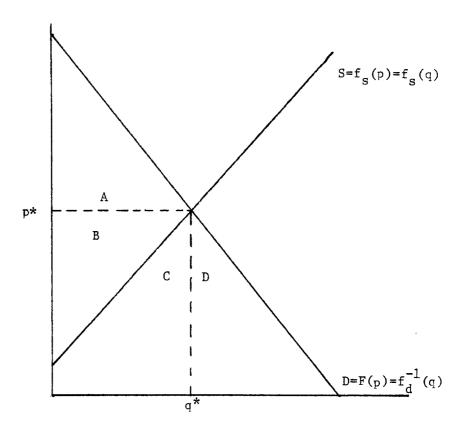


Figure 1. Equilibrium Solution.

Area A is the portion of the integral under the demand curve above p*, area B is the portion of the rectangle p*q* above the integral under the supply function. Under certain conditions these areas are commonly referred to as consumer and producer surplus, respectively. The total area, A + B = Z may be stated as follows:

(1)
$$Z = \int_0^{q^*} f_d^{-1}(q) dq - p^*q^* + p^*q^* - \int_0^{q^*} f_s(q) dq$$

where:

 $MC = f_s(q)$ marginal cost is a function of the quantity supplied.

Rearranging the equation for Z,

(2)
$$Z = \int_0^{q^*} f_d^{-1}(q) dq - \int_0^{q^*} f_s$$
 (q) dq.

Provided that Z is a quasi-concave function, is twice continuously differentiable, and in the domain of real numbers, q* may be found by maximizing Z with respect to q.

Applying the Kuhn-Tucker theorem, the necessary conditions for a maximum to exist are stated as follows:

(3)
$$\frac{\partial Z}{\partial q} = f_d^{-1}(q) - f_s$$
 (q) ≤ 0 and $\frac{\partial Z}{\partial q}q = 0$

Rearranging, $f_d^{-1}(q) = f_s(q)$

Substituting p for $f_d^{-1}(q)$ and MC for $f_s(q)$ results in the competitive solution of price and marginal cost being equal.

One may easily complicate this problem by moving to an interregional trade problem. Similarly, the total cost function, $\int_0^q f_s(q) dq$ could be replaced with input supply functions and a production function.

Following Klein and Roe, the following simple nonlinear programming problem is specified, and then converted to a linear programming problem. Both equation and tableau specifications are provided for the linear problem. For a simple case, deriviation of the economic information embodied in the dual variables of the LP problem is provided. [6]

Let the demand function for the j^{th} commodity, j = 1,..., J, be specified in inverse form as:

(4)
$$p_{j} = a_{j} - b_{j}q_{j}$$

where q_j is the quantity demanded, a_j is the intercept, and b_j is the change in the quantity of q_i demanded given a change in its own price, p_i .

Let the supply side be specified by the following total cost and conversion equations.

(5) Let
$$q_j = m_i x_i$$
, $j = 1,..., J$

where m > 0 is the conversion factor for x into q.

Let c_i be the unit cost of x_i , j = 1,...J.

The nonlinear programming specification of this problem is

(6)
$$\max_{\mathbf{q},\mathbf{x}} Z = \sum_{j=0}^{\infty} \mathbf{q}(\mathbf{a}_{j} - \mathbf{b}_{j}\mathbf{q}_{j}) d\mathbf{q}_{j} - \sum_{j=0}^{\infty} \mathbf{c}_{j}^{\mathbf{x}} + \sum_{j=0}^{\infty} \mathbf{m}_{j}^{\mathbf{x}} \mathbf{q}_{j} - \mathbf{q}_{j})$$

or in matrix form,

(7)
$$\max_{Q,X} Z = Q'(A - .5BQ) - C'X + \lambda((MX)' - Q')$$

where:

Q is Jxl of elements q_j

B is JxJ of elements b_{j}

C is Jxl of elements c_i

X is Jxl of elements x_{i}

 λ is Jxl of elements $\lambda_{\hat{\mathbf{j}}}$

M is JxJ of elements $m_{i,j}$, all $m_{i,j} = 0$ for $i \neq j$.

The procedure for linearizing the problem is to find the definite integral of each of the j demand equations,

$$p_j = a_j - b_j q_j$$
, and evaluate the integrals for q_j varying over i, or q_{ji} , $i = 1, ..., I$, over $j = 1, ..., J$, or $w_{ji} = a_j q_{ji} - 0.5 b_j q^2$

For each commodity, q_j , the area under its demand curve is found for i=1 to I steps. Each of these steps, w_{ji} , are to be activities in the linear programming format, and enter the solution at levels a_{ji} . Certain restrictions (to be explained) are placed on the a_{ji} in order to insure feasibility.

The linear programming problem may be stated as follows:

(8.1) max
$$Z^{\circ} = \sum_{i=1}^{\infty} i^{w} j i - \sum_{i=1}^{\infty} j^{x} j$$

Subject to the J commodity balance constraints

(8.2)
$$m_j x_j - \sum_{i} a_{ji} q_{ji} \ge 0 \quad j = 1,..., J,$$

and J convexity constraints,

(8.3)
$$\sum_{i \neq j} a_{ij} \leq 1 \quad j = 1, ..., J$$

or max
$$Z^{\circ} = \sum_{j \in J} a_{ji} w_{ji} - \sum_{j \in J} x_{j} + \sum_{j \in J} (m_{j} x_{j} - \sum_{j \in J} a_{ji} q_{ji}) + \sum_{j \in J} (1 - \sum_{j \in J} a_{ji})$$

This problem is shown in tableau form below in Table 1..

The convexity constraints are crucial to the problem. Duloy and Norton have shown that if the nonlinear problem is concave, a nontrivial solution will exist where the following will hold for each of the j activities. Either,

(a)
$$a_{ii} = 1$$
, all other $a_{is} = 0$ for a particular j,

(b)
$$a_{ii} < 1$$
, all other $a_{js} = 0$ for a particular j, or

(c)
$$a_{ji} + a_{j(i+1)} = 1$$
 and all other $a_{js} = 0$, $s \neq i$, $i+1$. [7]

Table 1. Specification of Commodity Market Demand in Linear Programming Format.

Constraint Constants	····	····	Supply Activities (x)	Demand Activities (λ)	Dual
Commodity Balance	0	<u><</u>	m	-q ₁ -q ₂ q _I	Market Price (π)
Convexity Constraint	1	<u>></u>		1 11	Consumer Surplus (
Objective Function	Z =	=	- c	^w 1 ^w 2 ··· ^w I	Consumer Plus Producer Surplus

Source: Klein, Harold E. and Terry L. Roe, "Agriculture Sector Analysis Model Design: The Influence of Administrative Infrustructure Characteristics," Table A.1, p. 299.

The implication is that depending on the difference between segments $q_{\text{ji}} \text{ and } q_{\text{j}(i+1)} \text{ the solution to the linear problem, Z}^{\circ}, \text{ can be shown to be an arbitrarily close approximation of the solution to the nonlinear problem Z.}$

Given this arbitrary closeness of the linear to the nonlinear problem, it can be shown that the duals of commodity balance rows are equal to the prices, and that the duals of convexity constraints are equal to consumer surpluses. Case (a) is used for simplicity, otherwise the problem is complicated by combination of a_{ij} , or fractional values of a_{ij} .

For a positive a;;, the Kuhn-Tucker conditions require that,

$$\frac{\partial Z^{\circ}}{\partial a_{ji}} = w_{ji} - \lambda_{j} q_{ji} - \lambda_{j}^{*} = 0.$$

For a basis variable, it follows from the nonlinear problem that

$$\frac{\partial Z}{\partial q_{ji}} = \frac{\partial (w_{ji})}{\partial q_{ji}} - \lambda_{j} = 0$$
$$= p_{ji} - \lambda_{j} = 0.$$

Therefore λ_j , the shadow price or dual for the commodity balance row is equal to the equilibrium commodity price.

Since a $_{\mbox{ji}}$ is assumed to be one, and Z° is an approximation of Z, $p_{\mbox{ji}}$ may be substituted for $\lambda_{\mbox{i}}$ and

$$\frac{\partial Z^{\circ}}{\partial a_{ij}} = w_{ji} - p_{ji}q_{ji} - \lambda_{j}^{*} = 0.$$

That is, λ_j^* , the shadow price on the convexity constraint is shown to be the consumer surplus for q_{ii} at p_{ii} .

These results can be extended to the production side in the case of total cost expressed as an integral of marginal cost instead of average cost times quantity. In the case of production functions, it is asserted that the shadow prices on the convexity constraints are producer surpluses accrued to the holder of the processes.

It should be pointed out that fixed factors having a positive opportunity cost are also included in calculations of other relevant shadow prices. The same is true for any other form of price or quantity restriction. In order to determine exactly what is involved in the determination of a dual value, Kuhn-Tucker conditions should be stated for each problem, from which expressions for all dual values may be derived.

In summary:

- The shadow prices on commodity balance constraints for demand functions are equilibrium market prices for the commodities.
- 2. The shadow prices on convexity constraints for demand functions are consumer surpluses associated with the commodities.
- The shadow prices on factor balance constraints for supply functions are equilibrium market prices for the factors.
- 4. The shadow prices on convexity constraints for supply functions are producer surpluses associated with the factors.
- 5. The shadow prices on convexity constraints for production functions are producer surpluses associated with production of the commodities.

III. DATA ENTRY

In proceeding to the section explaining the data entry it should be useful for the user to have a broad view of how the program operates.

The first block of information includes the dimensions of the nonaugmented portion of the matrix, the algorithm and/or system desired (one of several MPOS algorithms or APEX). The objective function, constraints, and if an integer program, the integer variables are read in.

The second possible block of information is in conjunction with an option to read in a second data set to be inserted some place within the data set previously read in for the initial

models. This option could be useful in the case of expanding the number of columns or rows somewhere in the middle of the nonaugmented portion of the matrix, without having to repunch a new data deck.

The third possible block of data includes the information necessary to generate linear activities approximating a nonlinear function. This block is further divided into two groups of functions and associated procedures.

The simpler of the two entails taking linear steps of a single variable function, and calculating the coefficients for the objective function and the row constraints. Examples of this type of function include supply and demand curves where quantity is a function of price. The program calculates the area under the curve at each quantity increment. These values are then placed into the objective and appropriate constraint specification by the algorithm.

The more complex of the two nonlinear functions involves the generation of an input substitution surface. An isoquant defining the relationship of an output, Q, two inputs X_1 , and X_2 , in Cobb-Douglas functional form is provided for. It is also conceivable that if Q were viewed as a composite consumption good, the surface could represent how X_1 and X_2 substitute in the consumption of Q. For example Q could be fruit, X_1 oranges, and X_2 apples, the program will calculate as many activities as necessary to satisfy the steps in Q desired.

Card Format

In moving through the data input cards, the user may wish to refer to the listing of variable names and options, the flow chart, and the program listing found in Appendices A, B, and C, respectively.

Input cards are listed in read statement form, each with its fortran format given. A short explanation is given where program branches occur, or where an explanation may otherwise be helpful.

1. READ (5,500) IDM, M1, COL, ROW

500 FORMAT [11, 12,215]

IDM =0 for maximum

= 1 for minimum

Ml, algorithm within MPOS

- = 01, REGULAR -, 2-phase simplex (LP)
- = 02, REVISED -, revised simplex (LP)
- = 03, DUAL -, dual simplex (LP)
- = 04, MINIT -, primal-dual (LP)
- = 05, BBMIP -, branch and bound mixed integer program (IP)
- = 06, DSZ1IP -, direct search 0-1 integer program (IP)
- = 07, GOMORY -, Gomory's cutting plane (IP)
- = 08, WOLFE -, Wolfe's quadratic simplex (QP)
- = 09, BEALE -, Beale's algorithm (QP)
- = 10, LEMKE -, Lemke's complementary pivot algorithm (QP)
- = 11, APEX 1 -, MPOS-APEX data file interface (GENERAL)
- = 12, APEX 2 -, MPOS-APEX data file interface (GENERAL)

COL, number of columns in nonaugmented matrix

ROW, number of rows in nonaugmented matrix.

2. READ (5,501) TITLE

501 FORMAT (8A10)

3. If the problem is an integer programming problem, the following cards are punched indicating the number of integer variables and variable names. If the problem is not IP, then the card block is left out.

READ (5,503) N2, (ACT(I1), I1 = 2,N2)

503 FORMAT (I3, 11A7/(3X, 11A7))

N2, the member of integer variables

ACT (I2), the activity names

4. Read in the nonaugmented or traditional LP activities
READ (5,505) (ACT(IA), IA = 1, COL)

505 FORMAT (3X, 11A7)

ACT(IA), activity names

COL, number of columns in nonaugmented matrix

5. Read in the nonzero coefficients of the objective function of the nonaugmented matrix. Activities such as transfer columns having no objective value need not be entered.

READ (5,506) (ICOL(IB), SIGN(IB), COEF(IB), IB = J1, J1+4)
506 FORMAT (5(I4, A1, F11.2))

ICOL(IB), the integer number of the activity, ACT(IA) for which an objective value is entered. Numbers begin with the left hand side of the matrix with 1, and run consecutively up through COL.

SIGN(IB), the sign, \div or -, of the objective value COEF(IB), the real value of the objective function.

Note that up to five such entries may be entered on each card.

FLAG - Once all objective values are read in, or if there are no nonzero values associated with the nonaugmented matrix, then ICOL = -999. So at least one card, with entry -999 in the first four columns is necessary if any nonaugmented activities are entered.

6. Read in the constraints for the nonaugmented matrix.

READ (5,506) (ICOL(IF), SIGN(IF), COEF(IF), IF = J2, J2 +4)

506 FORMAT (5(I4, A1, F11.2))

Exactly as in the case of the objective function, only the nonzero coefficients need be entered. In order to signify the completion of input for each constraint, three possible values may be assigned to ICOL. These values coincide with the nature of the constraints.

ICOL = -100, $---- \le RHS$ constraint

ICOL = -200, —— = RHS constraint

ICOL = -300, $---- \ge RHS$ constraint

Just as in the case of the column coefficients, the right hand side parameter is entered with SIGN and COEF along with the appropriate ICOL value. No other indicator is necessary to signify the completion of constraint input.

If this block of cards complete the data input, it is followed by an end-of-file (EOF) card. This card is multiple punched, 7-8-9, in the first column, and completes the input.

7. Read in data for the insertion option.

READ (5,511) ISID

511 FORMAT (15)

If new activities are to be inserted, ISID is given the value of 99999, and a subroutine called INSERT is called. If the user does not desire to use the insert option, a blank card is necessary.

If the insert option is used, the cards following ISID, and used by the subroutine INSERT are listed below.

1. Location of insertion

READ (5,511) NINS

511 FORMAT (I5)

NINS is the column number of the existing nonaugmented matrix at which the new activities are to be inserted.

2. Number and name of inserted activities
 READ (5,503) NAA, (AACT(IA), IA = 1, NAA)
503 FORMAT (I3, 11A7/(3X, 11A7))

NAA, the number of new activites to be inserted.

AACT, names of the new activities.

3. Read in objective of inserted activites.

READ (5,506) (AICOL(IB), ASIGN(IB), ACOEF(IB), IB = 1,NAA)
506 FORMAT (5(I4, A1, F11.2))

This input is identical in format to the objective data entered above. However unlike the earlier case in which only nonzero coefficients were entered, an objective value for each inserted activity must be entered.

ASIGN, the sign on the coefficient.

ACOEF, the objective coefficient.

4. Read in number of nonzero coefficients to be inserted.

READ (5,511) NBB

511 FORMAT (I5)

NBB, the number of nonzero constraint coefficients to be inserted.

5. Read in the coefficients

READ (5,512) (AEWROW(IX), AEWCOL(IX), AEWSIGN(IX), AEWCOEF(IX),

IX = 1, NBB)

512 FORMAT (4(2I3, A1, F13.2))

AEWROW, row number of the coefficient.

AEWCOL, column number of the coefficient.

AEWSIGN, sign of the coefficient.

AEWCOEF, the coefficient.

Note, this option has not been tested and it is unclear whether or not the numbers for AEWROW and AEWCOL are row and column numbers of the new matrix. However, this appears to be the most logical first choice. As above, if this block of data is final, then an EOF card follows the insertion and the input is completed.

 Read in information for extended functions from which the augmented portion of the matrix is composed.

This section is characterized by having two options. The first is to generate linear activites from a single nonlinear function, such as a supply or demand function, the second is to generate a substitution relationship between 2 variables according to an exponential function, such as a production function with 2 input variables. Data entry is given for both of these cases.

READ (5,510) EID, RM, IDPV(JA)

510 FORMAT (I5, F10.2, I5)

IDPV, flag for two variable function,

- = 0, single variable function,
- ≠ 0, three variable function.

EID, for IDPV = 0, denotes the number of nonzero coefficients for activities in the nonaugmented matrix in the same row as the generated activities; for IDPV \neq 0, EID = 3, denoting the number of rows necessary for the exponential function, one row each for X_1 , X_2 , and Y.

RM, the right-hand-side value for the extended row. This program is designed for the RHS value of an extended row to be either 1.0 or 0.0. For each set of activities generated, a convexity constraint is generated automatically having a RHS value of 1.0. If a RHS value of zero is desired then RM is given a value of zero. Although no example is readily available for which it may be useful, it is possible to enter a negative RHS value but not possible to enter a positive RHS value. In general, RM will be given a value of 0.0.

Case a. Single Variable Function

This type of function will require the use of a single quantity constraint row. In the case of a supply or demand function, the generated activities in the augmented portion of the matrix will require at least one transfer activity in the same row in the nonaugmented portion of the matrix. It is possible, however, to generate augmented activities with no other coefficients in the same row.

In this case, IDPV = 0, EID = K, where K is the number of nonzero coefficients for the row in the nonaugmented portion of the matrix, and RM = 0.0, unless a negative RHS is desired. Note that in the case where all three values equal zero, a blank card is still necessary for the program to proceed.

The following cards are punched in the case of IDPV = 0.

 If EID ≠ 0, read in coefficients, otherwise, skip this card and proceed to 2.

READ (5,506) (ICOL(II), SIGN(II), COEF(II), II = 1,EID)
506 FORMAT (5(I4, A1, F11.2))

ICO6, the number of columns in which the coefficient is to be entered. SIGN, the sign of the coefficient, + or -.

COEF, the coefficient to be entered.

2. Read in mathematical function to be extended.

The program is designed for input of exponential functions of the following form:

$$W = c_1 x^{\alpha_1} + c_2 x^{\alpha_2} + \dots + c_n x^{\alpha_n}.$$

Note that in the case of X being a commodity for which a supply or demand function is defined, the equation entered is the integral of the supply or demand function. In the case of supply, the equation above would represent the total cost function associated with a marginal cost or supply function of the form:

$$\frac{\partial W}{\partial X} = MC = \alpha_1 C_1 X^{\alpha_1 - 1} + \alpha_2 C_2 X^{\alpha_2 - 2} + \dots + \alpha_n C_n X^{\alpha_n - 1}.$$

If the first term were an intercept, α_1 would have the value of 1, so that the value would simply be C_1 .

READ (5,508) IJ, (CC(IK), IEXP(IK), IK = 1,IJ)

508 FORMAT (15,5(F10.4, F5.0))

IJ, the number of terms in the function.

CC, the coefficients C, for the function.

IEXP, the exponents $\boldsymbol{\alpha}_{\boldsymbol{i}}$ for the function.

 Read in the initial value, the magnitude, and number of steps to be taken in the linearization procedure.

READ (5,509) A(1), DELTA Q, STEP

509 FORMAT (2F10.4, I5)

Q(1), initial value of the function.

DELTAQ, the increment value, $(Q_i - Q_{i-1}) \forall_i = 1$, n.

STEP, the number of steps, n, taken.

From the function and linearization information, the program adds
the number of columns consistent with the number of steps, and calculates
the area under the function at each step for the objective function.
Two constraints are generated, a quantity allocation constraint
containing the quantity steps specified, and a convexity constraint.

All quantity steps are generated having negative signs. The direction of the constraint is determined by the program to be, \leq , in the case of a supply function, \geq , in the case of a demand function.

Case b. Multiple Variable Function

As stated above, the most obvious use of this option is to incorporate a production function where two inputs, \mathbf{X}_1 and \mathbf{X}_2 , are combined in the production of various quantities of some Y, specified by a Cobb-Douglas type function.

The concept used is to define several input ratios, or expansion paths at various levels of Y. From the ratio and Y values, values for \mathbf{X}_1 and \mathbf{X}_2 are determined. The calculation of the ratios follow:

$$Y = AX_1^{\alpha_1}X_2^{\alpha_2}$$

$$RATIO = (X_1/X_2), rearranging$$

$$X_1 = X_2R, where R = RATIO.$$

$$Substituting for X_1, and solving for X_2.$$

$$Y = A(X_2R)^{\alpha_1}X_2^{\alpha_2}$$

$$Y = AX_2^{\alpha_1}R^{\alpha_1}X_2^{\alpha_2}$$

$$Y = AX_2^{\alpha_1+\alpha_2} = YA^{-1}R^{-\alpha_1}$$

$$X_2 = (YA^{-1}R^{-\alpha_1})^{\frac{1}{\alpha_1+\alpha_2}}$$

For each ratio r_i , $i=1,\ldots,n$, and for varying levels of Y,a unique value of X_2 is calculated which in turn determines the appropriate value of X_1 . This grid linearization is illustrated in Figure 2. The Linearized Specification of Y = $f(X_1,X_2)$.

The number of activities generated in the number of steps in Y times the number of ratios. Three quantity constraint rows, one each for \mathbf{X}_1 , \mathbf{X}_2 , and Y, and a convexity constraint row are generated by the program. Zeroes are placed in the objective function.

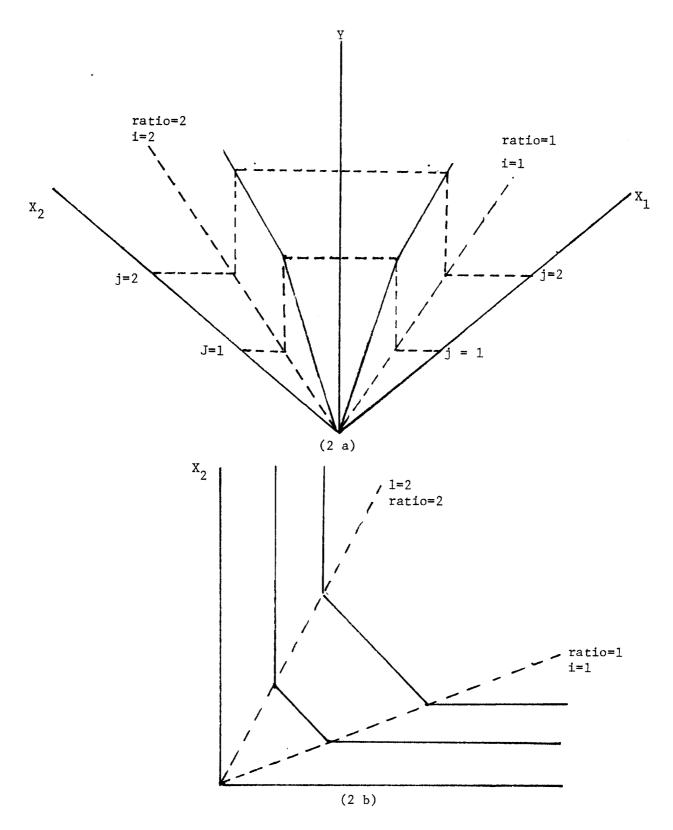


Figure 2. The Linearized Specification of $Y=f(X_1,X_2)$.

Source: Roe, Terry. "Modeling of Nonlinear Functions into A Linear Programming Format". Staff Paper P75-9 [8]

Values for the first card of this group are as follows:

IDPV \neq 0, the value 99999 is given in some sample decks

EID = 3, the number of quantity rows to be generated

RM = 0.0, right hand side values.

For each of the three rows, the following sequence of cards is necessary.

 Read in the number of coefficients in the row in the nonaugmented portion of the matrix.

READ (5,507) IEID

507 FORMAT (15).

IEID, the number of coefficients.

2. Read in the column, sign, and value of the coefficients

READ (5,506) (ICOL(II), SIGN(II), COEF(II), II=1, IEID(I3)+1)

506 FORMAT (5(I4, A1, F11.2))

ICOL, the column number in which the coefficient is to be entered.

SIGN, the sign of the coefficient.

COEF, the value of the coefficient.

Important! Note that the right hand side value and the constraint type must be entered by the user. Therefore the final entry will

have one of the following values for ICOL:

ICOL = $-100 - \le RHS$ constraint,

ICOL = -200 ---- = RHS constraint,

ICOL = -300 - 2 RHS constraint.

 Read in information pertaining to the ratios to be used in generating activities.

READ (5,584) NOR, (RATIO(12), 12=1, NOR)

584 FORMAT (I3, 11F7.2/(3X, 11F7.2))

NOR, the number of ratios.

RATIO, the ratio, (x_1/x_2) .

4. Read in the Cobb-Douglas function parameters

$$Q = AAX_1^{\alpha_1} X_2^{\alpha_2}$$

READ (5,585) AA, ALPH1, ALPH2

585 FORMAT (3F10.2)

AA, the multiplicative coefficient

ALPH1, the exponent on \mathbf{X}_1 .

ALPH2, the exponent on \mathbf{X}_2 .

5. Read in the initial value, the magnitude, and the number of steps to be taken.

READ (5,509) Q(1), DELTAQ, STEP

509 FORMAT (2F10.4, I5)

Q(1), initial value of the function.

DELTAQ, the increment value.

STEP, the number of steps taken.

This concludes the data input section. It should be pointed out that once the input is complete, end of file (EOF) card is required. This card is punched 7-8-9 in the first column.

IV. SAMPLE PROBLEMS

For illustrative purposes, two sample problems developed by Roe are provided. The first problem is stated in nonlinear form and then restated in linear form. Results concerning the values of shadow prices on commodity balance and convexity constraints are provided.

Provided for both problems are verbal and mathematical specification, tableau representation, data input deck, MPOS specification, and finally MPOS summary of results.

Problem One

The first problem is one of maximizing the sum of producers' and consumers' surplus, with a variety of perfectly inelastic and elastic, and sloping supply and demand functions, and a production function.

Three commodities which are perfectly inelastically supplied may be combined. One of these inputs and an input supplied with an upward sloping function, may be combined to produce another commodity. The produced commodity faces a downward sloping demand.

The nonlinear programming specification of the problem follows: $MAX Z = .5LACT1 + .9LACT2 + .7LACT3 - 1.5X_1$

$$- \int_{0}^{X_{2}} (X_{2}) dX_{2} + \int_{0}^{Y} (90-1.2Y) dY$$

$$+ \lambda_{1} (90 - .4LACT1 - .3LACT2)$$

$$+ \lambda_{2} (80 - .3LACT1 - .2LACT3)$$

$$+ \lambda_{3} (200 - .4LACT2 - .9LACT3 - X_{1})$$

$$+ \lambda_{4} (4X_{1}^{*3} X_{2}^{*5} - Y)$$

where:

 \mathbf{X}_2 = supply or marginal cost of \mathbf{X}_2 , and

90 - 1.2Y = Inverse demand function for Y.

The nonlinear programming problem is now converted to a linear programming problem. Notice that each of the constraints stated in Lagrangian form corresponds exactly to a row constraint in the tableau specification of the problem found below.

Max
$$Z^{\circ}$$
 = .5LACT1 + .9LACT2 + .7LACT3 - 1.5 X_1 - Σ $A_m Y_m + \Sigma$ $A_n W_n$ L, X_1 , $A_n W_n$

+
$$\lambda_1$$
 (90 - .4LACT1 - .3LACT2)

+
$$\lambda_2$$
 (80 - .3LACT1 - .2LACT3)

+
$$\lambda_3$$
 (200 - .4LACT2 - .9LACT3 - X_1)

+
$$\lambda_4$$
 (X2 - $\sum_{m=1}^{M} a_m X_{2m}$)

+
$$\lambda_5$$
 (1 - $\sum_{m=1}^{M} a_m$)

+
$$\lambda_6 \left(\sum_{p=1}^{p} a_p X_{1p} - X_1 \right)$$

+
$$\lambda_7 \begin{pmatrix} p \\ \Sigma \\ p=1 \end{pmatrix} = a_p X_{2p} - X_2$$

+
$$\lambda_8$$
 $(\sum_{p=1}^{p} a_p Y_p - Y)$

$$+ \lambda_{9} (1 - \sum_{p=1}^{P} a_{p}) + \lambda_{10} (Y - \sum_{n=1}^{N} a_{n}Y_{n}) + \lambda_{11} (1 - \sum_{n=1}^{N} a_{n})$$

Where:

 $\gamma_{\rm m} = \int_0^{\rm X2m} (\rm X2).d\rm X_2 = [0.5\rm X2^2]_0^{\rm X2m}$, the area under marginal cost curve, or total cost, of X2, at the mth quantity of X2.

 $W_n = \int_0^{Y_n} (90 - 1.2Y) dY = 90Y - 0.6Y^2, \text{ the area under the demand function}$ (marginal revenue under competitive assumptions), or total revenue for Y, at the nth quantity of Y.

 a_{m} , the level at which the m^{th} quantity steps of X_{2} is supplied in the solution

 a_n , the level at which the n^{th} quantity step of Y is demanded in the solution.

 a_p , the level at which the p^{th} step in the production of Y, from inputs X_1 and X_2 , enters the solution. Note that the index P embodies both ratios and quantities. Referring to Figure 2 may be of some help. Given a particular input ratio i, as quantities j of Y are changed, quantities of X_1 and X_2 change accordingly. Therefore the index p runs over both ratio numbers, and the quantity steps in Y, or P = (ratios)(M).

Linearization Parameters, Problem 1.

Supply of X_2 :

Total cost: $W = -0.5X2^2$ area under supply

Initial
$$X_2 = 0$$

$$\Delta X_2 = 10$$
STEPS = 12

Production of Y

$$y = 4x_1^{3} x_2^{5}$$

Initial Y = 10

$$\Delta Y = 10$$

RATIOS

$$R1 = .4$$
 $R2 - .8$ $R3 = 1.4$ $R4 = 1.8$

Demand for Y

Initial Y = 0

$$\Delta Y = 7.5$$

STEPS = 12

The matrix, data input, computer specification and results follows:

Table 2. Problem 1 Tableau Specification

				,								1
				No. 1	TEST	TRAD.	No. 1 TEST TRAD. LP, INPUT, SUPPLY, PRODUCTION FUNCTION AND DEMAND	PRODUCTION FUNCTION	AND DEMAND	•		
	τ	7	ε									
	TOAL	TDAI	TOAL	TTX	TCX	IX	SUPPLY OF X2	PRODUCTION	DEMAND, Y			
OBJECTIVE	- 5	.6.	.7.	-1.5		10 -	$\gamma_1 - \gamma_2 \dots - \gamma_2$	0 0	W ₁ W _n			i
CONSTRAINT	. 					-	Nonaugmented submatrix					
1.	1.4	£.								V 1	06	
2.	د.	,	.2			-				۷ ۱	80	
3.		4.	6.			-		Augment submatr		٧I	200	۷,
4.		! }	; }	 	l	i I	$-\mathring{\mathbf{X}}_2$ $-\mathring{\mathbf{X}}_2$ $-\mathring{\mathbf{X}}_2$		i i i i	٧I	0	
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.9				7				x_1 ₁ x_1 _p		V I	0	
7.					1	. <u></u>		x_2 x_p		٧١	0	
8						-T		$\hat{Y}_1 \dots \hat{Y}_p$		^ I	0	
.6								1 1		٧١	H	
10.							, ,		$^{-Y}_1$ $^{-Y}_n$	A 1	0	
11.							1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1		v	-	

Problem One Input

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-100+80.0
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3+0.2 -100+80.0

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    7.
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21. 4.0 0.3 0.5
22. 10.0 10.0 5
23.
24.
                      6+1.0
                     25.
26. 0.0 7.5 . 12
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An explanation for each card follows

Problem One, Input Explanation

- maximum problem, MPOS regular algorithm, 6 columns and 3 rows in the nonaugmented matrix
- 2. title
- 3. variable names
- 4. objective, nonaugmented
- 5. row 1, coefficients by column, constraint type, RHS value
- 6. row 2, coefficients by column, constraint type, RHS value
- 7. row 3, coefficients by column, constraint type, RHS value
- 8. blank card for no data insertion
 9-12 generate supply of X2
- 9. 1 nonzero coefficient in nonaugmented portion of row 4
- 10. entry of row A, column 5, equal to 1.0.
- 11. integrated supply function, 1 term, coefficient = -0.5, exponent = 2.0
- 12. initial step = 0.0, increment = 10, 12 steps $13\text{--}22 \text{ generate production surface Y = AX} \quad \text{al X} \quad \text{$\alpha2
- 13. 3 rows generated, 99999 = DEPV subroutine
- 14. 1 nonzero coefficient in row 6, (X1)
- 15. row 6, coefficient by column, constraint type, RHS value
- 16. 1 coefficient row 7, (X2)
- 17. row 7
- 18. 1 coefficient row 8, (Y)
- 19. row 8
- 20. 4 ratios, $\gamma 1 = 0.4$, $\gamma 2 = 0.8$, $\gamma 3 = 1.4$, $\gamma 4 = 1.8$
- 21. production function Y = $4X_1^{0.3} X_2^{0.5}$
- 22. initial Y = 10, increment = 10, 5 steps
 23-26 generate demand for Y
- 23. 1 coefficient row 10

- 24. row 10 coefficient
- 25. integrated demand function, 2 terms, coefficient 1 = 90, exponent 1 = 1.0, coefficient 2 = -0.6, exponent 2 = 2.0
- 26. initial Y = 0.0, increment = 7.5, 12 steps

Following is the computer output generated for problem one.

```
MP05 VERSION 4.0
                                                                                                                                                          NORTHWESTERM UNIVERSITY
                                                                                                                       VERSION 4.0
                                             * MULTI-PURPOSE OPTIMIZATION SYSTEM *
**** PROBLEM NUMBER 1 ****
                               LACT3
YA5
Y31
Y39
Y317
YCo
                                                                                                                                                                                                                               X27
Y03
Y011
Y011
Y07
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4013
4014
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                                                  Y97
Y915
                                YC3
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USING REGULAR

** NO. 1 # TEST TRAD. LP.INPUT. SUPPLY. PRODUCTION FUNC AND DEMAND SPECIFICATION *

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MPOS VERSION 6.0

LORTHWESTERM UNIVERSITY

考察的证券企业发展的基本。大学文化发展的 本《PROPLEM 1001136R 1 参 专家农民工艺术来解写的基本工作本意和企业

USING REGULAR
** NO. I M TEST TRAD. LP.INDUT.SUPPLY.PRODUCTION FUNC AND DEMAND SPECIFICATION**

SUMMARY OF RESULTS

No		VAR.	VAR		RO.	STATUS		ACTIVITY	OPPORTUNITY	LOWED	(ibb=B
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29		20	Y58	-	eo en				- 495• 9026667		
29		芸ん	Yain		40 gr.	눈일			280+1414444 60:7706667		
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154 Y316 L8		31	Y 3 1 3			LB			#58.8733355		
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39 YS1		35			ea 64	LB			699.4073637		
39 YS1		35	3318		~~	٣ã			561 • 9 % 68 333		
39 YS1		36	4839			L S	,		44/*3432//3		
40 YG2 LB 0.0000000 1912.5000000 0.0000 195 41 YG3 LB 0.0000000 675.0000000 0.0000 195 42 YG4 LB 0.0000000 465.0000000 0.0000 195 43 YG5 LB 0.0000000 202.5000000 0.0000 195 44 YG6 LB 0.0000000 67.5000000 0.0000		39	YCi		20 mg	LB.			1417.5000000		
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- 43 YS5 - →- LB - 0.0000000 - 202.5000000 - 0.0000 - 1M# - 44 YS6 - →- LB - 0.0000000 - 67.5000000 - 0.0000 - 1M#			Y 63		44 pp	L3			575 . 0000000		
- 4¼ Υθβ ΕΒ - ἄ•ὐἀθὰρα		42			9 - g -				#855,40000000 \$50,5066000		
45 YC7 - B .3333333 0.0000000 0.0000 1NF			Y06		***	โร					
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MPOS VERSION 4.0

NORTHWESTERY UNIVERSITY

******************* * PROBLEM NUMBER 1 *

USING REGULAR
** NO. 1 # TEST TRAD. LP.INPUT.SUPPLY.PRODUCTION FUNC AND DEMAND SPECIFICATION**

SUMMARY OF RESULTS

					SUMMARY OF RESULTS			
•	VAR NO	NXAE	RO#	STATUS		OPPORTUNITY COST	10453	Habea
	45	YC3 YC9		LB	•6665667 0•000000c	0.0000000 67.500000	0.0000 0.0000	INE INE
	48 49	YC10 YC11		្ ទ	û•000000 0•000000	202.5040690 465.0040090	0.0000 0.0000	INE INE
	50 51	SLACK	p-	1 L8	0 • 00 00 00 0 0 • 00 0 00 0	675.0000000 1.9629530	0.0000 0.0000	THE
	52 53	SLACK-	0- 0-	1234 1234	69•767000 3•000000	0.0000000 .777773	0 • 0000 0 • 0000	I 41=
	54 55	SLACK	ე -	5 LB	0.000000 0.000000	15.0000000 100.000000	0•040v 0•040v	IMF
	56 57	SLACK-	<u>9</u> -	6 LB	0.000000 0.00000	2.2777778 15.0000000	0 • 0 0 0 n 0 • 0 0 0 n	J Mg J Mg
	58 69	SLACK	<u>ي</u> -	8 LB 9 LB	0.000000	31.5000000 =31.500000	0•0101 0•0101	I VE
	59 50	SLACK	1	0 L3	0 • 0 0 0 0 0 0 0 • 0 0 0 0 0 0	1214.8857773 31.5000000	0 • 0 0 0 0 0 • 0 0 0 0	INE
	61	ARTIF SLACK		O EB	0 • 0 0 0 0 0 0 0 • 0 0 0 0 0 0	-31.5000000 1417.5000000	0 • 0 0 0 0 · · · · ·	THE

WAXIMUM VALUE OF THE OBJECTIVE FUNCTION = 3064.609000

CALCULATION TIME WAS .0930 SECONDS FOR 19 ITERATIONS.

Output Interpretation - Problem One

A brief description of the output follows. Those needing further explanation should refer to the MPOS manual.[2]

REGULAR - The particular MPOS algorithm requested by the user.

TITLE - Followed by user provided title

VARIABLES - The names of variables in the nonaugmented position of the matrix are given first, followed by the augmented or generated variables. Variables associated with the supply of X2 YA1 through YA12; production, YB1 to YB20; demand for Y, YC1 to YC12.

MAXIMIZE - The type of optimization requested for the objective function that follows. Note that the sign and objective value for each variable is provided.

CONSTRAINT - Followed by each row constraint in the problem.

Variables having zero coefficients are not listed. Note that constraint (4) is the commodity balance row for X2. The values at each step are the quantities associated with the total cost values in the objective function. Constraint (5) is the convexity constraint for X2.

Summary of Results

For each variable the following information is provided.

STATUS - Whether the variable is in the optimal basis at a zero or positive value. LB indicates zero; B positive value.

ACTIVITY LEVEL - The level or value a variable takes on in the optimal solution.

OPPORTUNITY COST - The cost in terms of a change in the objective function given a marginal increase in the particular variable.

This item is used synonymously with shadow price or dual.

LOWER, UPPER BOUNDS - The lower and upper limits of a variable

within which the opportunity cost is unchanged.

Interpretation of the slack variables of the row constraints is the equivalent of finding the values of the dual problem.

The first three slack variables are associated with row constraints of the nonaugmented portions of the matrix. They are the commodity balance rows of fixed resources.

STATUS - Whether the slack variable is in the optimal basis at a zero or positive level. LB indicates zero; B a positive value.

That is, SLACK takes on a positive value only when the resource is not totally exhausted.

OPPORTUNITY COST - The change in the objective function given an additional unit of the commodity constrained, or the value of an additional unit of the commodity.

The resource in row 2 has a positive value (69.76), indicating that it is not used up or is not a constraining resource. Since it is not constraining, its worth or value is zero as indicated in the opportunity cost column.

Additional units of the resources in rows 1 and 3 would be worth \$1.96 and \$0.78 respectively.

The interpretation of the Lagrangians or dual values of the rows of the augmented portion of the matrix was discussed in the theory review above. Again this value is given as the opportunity cost here. These values, taken from the computer output are listed below.

$$\lambda 4$$
 - dual row 4 - price of X_2 - 15.00

 $\lambda 5$ - dual row 5 - producer surplus X_2 - 100.00

 $\lambda 9$ - dual row 9 - producer surplus Y - 1214.89

 $\lambda 10$ - dual row 10 - price of Y - 31.50

 λ 11 - dual row 11 - consumer surplus Y - 1417.50

The value of the objective function is 3064.61.

Problem Two

In problem two, surplus is maximized from two limited resources, which may be combined by two different production functions into a commodity facing a downward sloping demand.

The nonlinear programming specification follows:

Max
$$Z = 2.0X_{11} - 2.0X_{12} - 1.8X_{21} - 1.8X_{22} + \int_{0}^{Y} (90 - 1.2Y) dY$$

 $+\lambda_1 (25 - X_{21} - X_{22})$
 $+\lambda_2 (75 - X_{11} - X_{12})$
 $+\lambda_3 (Y - 4X_{11}^{\cdot 3}X_{21}^{\cdot 5} - 3X_{12}^{\cdot 6}X_{22}^{\cdot 15})$

Linearization Parameters

Production Y_1

$$Y_1 = 4X_{11}^{\cdot 3} X_{21}^{\cdot 5}$$
Initial $Y_1 = 10$

$$\Delta Y_1 = 10$$
STEPS = 5

RATIOS

Production Y2

$$Y_2 = 3X_{12}^{.6} X_{22}^{.15}$$
Initial $Y_2 = 10$

$$\Delta Y_2 = 10$$

STEPS = 5

Demand for Y

$$W = 90Y - .6Y^2$$
 area under demand

Initial Y = 0

$$\Delta Y = 5$$

STEPS = 12

The matrix, data input, computer specification and results follow:

Table 3. Problem 2 Tableau Specification

					NO.	2 TEST T	WO PROD. FNTS.	TEST TWO PROD. FNTS. AND ONE DEMAND		-	
	TIY	TY2	IIXT	TXI	IXXI	TX22	PROD 1	PROD 2	DEMAND		
OBJECTIVE	0	0	-2.0	-2.0	-1.8	-1.8	00	00	$^{W}_{1}\cdots ^{W}_{n}$		
CONSTRAINT											
						1				V I	25
2.			П	H						V I	75
3.			ij				$x_{11}x_{1n}$			V I	0
. 4					-1		$x_{21}x_{2n}$			V I	0
5.	ī						$^{Y}_{11}$ $^{Y}_{1n}$			۸ I	0
.9							11			٧١	
7.				Ţ				$^{\mathrm{X}}_{11}^{\mathrm{X}}_{\mathrm{1n}}$		V I	0
8						1		$x_{21}x_{2n}$		٧١	0
.6		-						$^{\mathrm{Y}}_{21}^{\mathrm{Y}}_{2\mathrm{n}}$		V 1	0
10.								11		٧١	Н
11.		Н							$ _1$ $_n$ $_n$	^ I	0
12.										٧I	Н

Input Deck - Problem 2

```
*** NO. 2 = TEST TWO PROD. FNTS. AND ONE DEMAND ***
       TY2 TY1 TX11 TX12 TX21 TX22
3-2.0 - 4-2.0 5-1.8
                    - 4-2.0
   4.
                                                   6-1.8
   5.
        541.0
                      6+1.0
                                  -100+25.0
                                  -100+75.0
   ٤.
        3+1.0
                      441.0
   7.
                   99999
   8.
         Ś
   9.
         1
  - 10.
        3-1.0
                    -100+0.0
   11.
         1
                    -100+0.0
  12.
        5-1.0
        1 ....
13.
        2-1.0
  14.
                    -300+0.0
                   1.4 1.8
       40.4 0.8
  15.
  16. 4.0
              0.3
  17. 10.0
              10.0
        3
                   99999
  18.
         1 .....
                    19.
        4-1.0
                    -100+0.0
  20.
        1
  21.
        5-1.0
                    -100+0.0
  22.
        1
  23.
                   -300+0.0
        1-1.0
  24.
             +0.8
       4+0.4
  25.
             0.6
  26. 3.0
              10.0 5
  27. 10.0
              10.0
      2
  28.
        1+1.0 2+1.0
  ,29.
        2+90.0 1.0 ~0.6 2.0
0 -- 5.0 -- 12 -- --
  30.
  31. 0.0
```

Problem Two Input Explanation

- maximum, MPOS regular algouthm, 6 columns and 2 rows in the nonaugmented matrix.
- 2. title
- 3. variable names
- 4. objective, nonaugmented
- 5. row 1, coefficients by column, constraint type, RHS value
- 6. row 2, coefficients by column, constraint type, RHS value
- 7. blank card for no data insertion 8-17 generate production surface $Y_1 = 4x_{11}^{3} x_{21}^{5}$
- 8. 3 rows generated, 99999 = DEPV subroutine
- 9. 1 nonzero coefficient in row 3, (XII)
- 10. row 3, coefficient by column, constraint type, RHS value
- 11. 1 nonzero coefficient in row 4, (X_{21})
- 12. row 4, coefficient by column, constraint type, RHS value
- 13. 1 nonzero coefficient in row 5, (Y_1)
- 14. row 5, coefficient by column, constraint type, RHS value
- 15. 4 ratios,
- 16. production function $Y_1 = 3X_{11}^{0.3} X_{21}^{0.5}$
- 17. initial Y=10, increment =10, 5 steps $18-27 \text{ generate production surface Y}_2 = 3X_{12}^{0.6} X_{22}^{0.15} \text{ similar to } 8-17$ 28-31 generate demand for Y
- 28. 2 nonzero coefficients in row 11 (Y_1 and Y_2)
- 29. row 11, coefficients by column
- 30. integrated demand function, 2 terms, coefficient 1 = 90, exponent 1 = 1.0, coefficient 2 = -0.6, exponent 2 = 2.0
- 31. initial Y = 0.0, increment = 5.0, 18 steps

```
MPOS VERSION 4.0
                              NORTHWESIERN UNIVERSITY
         数点表 家d 1. 4. 数数表表表数数 1. 次数数数深度 表面激励发出 表现发出参加表现更重要
                          MPOS
                        VERSION 4.0
         * MULTI-PURPOSE OPTIMIZATION SYSTEM
***** PROBLEM NUMBER 1 ****
       KEGULAR
       HILLE
       *** NO. 2 # TEST TWO PROD. FATS. AND ONE DEMAND ***
       VARIABLES
                                                                             YA1
                                                                                        YA2
          112
                     111
                                TX11
                                            TX12
                                                       TX21
                                                                  Tx22
                                                       YA7
                                                                             YA9
                     YA4
                                YA5
                                            YAb
                                                                  YAB
                                                                                        YA10
          YAS
          YALL
                                YA13
                                            YA14
                                                       YA15
                                                                  YA16
                                                                             YA17
                                                                                        YA18
                     YA12
          YALS
                     YA2U
                                YEL
                                            Y132
                                                       YH3
                                                                  Y84
                                                                             YB5
                                                                                        Y36
                                                       YU11
                                                                             1313
                                                                                        Y614
                                Y09
                                                                  Y812
          YEst
                     YBB
                                           YB10
                     1810
                                Y517
                                                       Y619
                                                                  Y320
                                                                             YC1
                                                                                        YC2
                                            YB18
          ARTA
                                            YCo
                                                       YC7
                                                                             YC9
                                                                                        YC10
          YC$
                     YC4
                                YC5
                                                                  YC8
          YU11
                                 YC13
                                                                  YC16
                                                                                        YC18
                     YC12
                                            YC14
       MAXIMIZE
                                                                        1.80000TX21
                  2.000001X11
                                             2.00000TX12
                  1.8000007.222
                         UYAI
                                                   SAYO
                                                                              OYA3
                                                                              0YA6
                                                    OYAS
                         UYA4
                         OYA7
                                                    OYAB
                                                                              OYA9
                                                    OYALL
                                                                              OYA12
                         UYALU
                                                                              0YA15
                                                    OYA14
                                                    OYA17
                                                                              0YA18
                         UYAlo
                                                    UYA2U
                                                                              0Y81
                         UYA19
                                                                              CYB4
                         UYB2
                                                    0Y83
                         UYB5
                                                    0YB6
                                                                              0YB7
                         86Y0
                                                    0189
                                                                              01810
                                                                              0 Y B 1 3
                         OYBII
                                                    01812
                                                    0Y815
                                                                              0YB16
                         UYBL4
                                                                              0Y819-
                                                    01818
                                                    OYCI
                                                                     435.00000YC2
                         07850
                                          1215.00000YC4
                840.00000TC3
                                                                     1560.00000YC5
                                          2160.00000YC7
                                                                    2415.00000YC8 -
               1575 • 000 0 0 0 YC6
                                                                     3000.00000YC11
                                          2835.00000YC10
               2040.00000109
                                          3240,00000YC13
                                                                     3315.000000YC14
               3135.00000VC12
               3360.000000YC15
                                          3375.00000YC16
                                                                     3360.000000YC17
               3315.000007C18
       CONSTRAINT
                                             1.000001 x22
                  1.000001X21
                            25.00000
                                             1.00000TX12
   ۷.
                  1.000001X11
                            75.00000
                  1.00000TX11
                                             4.21700YA2
                                                                        7.00000YA3
                  1.77300741
                                                                        2.73400YA6
                 10.03000YA4
                                            13.25600YA5
                                                                       15.46800YA9
                                            10.79600YA8
                  6.50300YA7
                                             3.87900YA11
                                                                        9.22700YA12
                 2U.444HUTA1U
```

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MPUS SCHSICH 4.0
                             NORTHWESTERN UNIVERSITY
***********
* PROOLEM NUMBER I *
*********************
JOING REGULAR
*** NO. 2 , TEST TWO PROD. FNTS. AND ONE DEMAND ***
                                          21.945U0YA14
                 15.31600YA13
                                                                    29.00500YA15
                 4.5390UTALD
                                          10.79600YA1/
                                                                    17.92100YA18
                25.677001A19
                                          33.93800YA20
                                   0
                 1.00000TX21
                 4.4330UYA1
                                          10.54200YA2
                                                                    17.50100YA3
                25.07400YA4
                                          33.14100YA5
                                                                     3.418JOYA6
                 8.1290UYA7
                                          13,49500YA8
                                                                    19.33500179
                25.5550UYA1U
                                           2.771UCYA11
                                                                     6.59000YA12
                10.94000YA13
                                          15.67500YA14
                                                                    20.71800YA15
                 2.52200YA16
                                           5.99800YA17
                                                                     9.95600YA18
                14.26500YA19
                                          18.85400YA20
                 1.000GUTY1
                10.00000YAI
                                          20.00000YA2
                                                                    30.00000YA3
                40.00000YA4
                                          50.00000YA5
                                                                    10.00000YA6
                20.00000YA7
                                t
                                          30.000U0YA3
                                                                    40.00000YA9
                50.0000007710
                                          10.000U0YA11
                                                                    20.00000YA12
                                                                    50.00000YA15
                59.00000YA13
                                          40.000U0YA14
                ALAYUUGUU.UI.
                                          20.00000YA17
                                                                    30.00000YA18
                40.00000YA19
                                          50.000U0YA2U
                 1.00000YA1
  ó.
                                           1.000U0YA2
                                                                     1.00000YA3
                 1.00000VA4
                                           1.000U0YA5
                                                                     1.00000446
                 1.00000YA7
                                           1.00000YA6
                                                                     1.00000YA9
                 T.OUUUUYAIU
                                           1.00000YA11
                                                                     1,00000YA12
                 1. UUUUUUYALS
                                           1.00000TA14
                                                                     1.00000YA15
                 1.00000UYALO
                                           1,00000YA17
                                                                     1.00000YA13
                 1.0000UYA19
                                           1.000007/20
                            1.00000
 -7.
                 1+000001X12
                 4.14500YB1
                                          10.446u0YB2
                                                                    17.93700Y83
                26.32300784
                                          35.44400YB5
                                                                    4.76200YBS
                11.999667
                                          20.60400188
                                                                    30,23700Y69
                                           5.32600YB11
                40.71500YB10
                                                                    13.42100YB12
                23.044007313
                                          33.81800YB14
                                                                    45,53600YB15
                 5.50000YB15
                                          14.112001B17
                                                                    24.23200YB18
                35.561007619
                                          47.88400YB20
                 1.000001X22
                10.3640UYB1
                                          26.11500YB2
                                                                    44.84200YB3
                65.80700YB4
                                          88,61000YUS
                                                                    5.95300Y86
                14.99900187
                                          25.75500YBB
                                                                    37.79600YB9
                50.893007810
                                           3,80400YB11
                                                                    9.58600YB12
                10.400007813
                                          24.15500Y814
                                                                    32,52600YB15
                 3.111007010
                                           7.84000751/
                                                                    13.46200Y818
                19.756007819
                                          26.602v0YB20
                                  0
  9.
                 1.000001Y2
                TOPROPORTEY
                                          20.00000702
                                                                    30.00000Y63
                40.00000164
                                          50,00000765
                                                                    10.00000YB6
```

```
MPOS VERSION 4.0
                             MORTHWESTERN UNIVERSITY
*********
* PRUBLEM NUMBER 1 &
USING REGULAR
*** NO. 2 4 TEST TWO PROD. FNTS. AND ONE DEMAND ***
                20.00000YB7
                                         30.00000YB8
                                                                  40.00000YB9
                50.000007810
                                         10.00000Y611
                                                                  20.00000YB12
                                                                  50,00000YB15
                30.000001333
                                         40.00000Yd14
                10.000007610
                                         20.000007817
                                                                  30.00000YB1a
                40.000007819
                                         50,000007820
                                  n
                                          1.00000YB2
                                                                   1.00000183
  10.
                 1.600000481
                 1.0000017:54
                                          1.00000735
                                                                   1.00000156
                 1.00000187
                                          1.000000183
                                                                   1.00000Y89
                 1.00000YB10
                                          1.00000YB11
                                                                   1.00000Y612
                                                                   1.000007815
                 1.0000001813
                                          1.00000YB14
                 1.0000097816
                                          1.000000Y817
                                                                   1.00000YB18
                 1.000007519
                                          1.000007820
                            1.00000
                                          1.00000111
                 1.0000nUTY2
                                +
                       0 rC1
                                          5.00000YC2
                                                                -10.00000YC3
                15.00000704
                                         20,00000705
                                                                  25.00000YC6
                30.00000VC7
                                         35.00000YC3
                                                                  40.00000YC9
                45.00000YC10
                                         50,00000YC11
                                                                  55.00000YC12
                                         65,00000YC14
                60.00000YC13
                                                                  70.00000YC15
                75.900g0YC16
                                         80.00000YC17
                                                                  85.00000YC18
                                                                   1.00000YC3
                 1.00000YC1
                                          1.00000YC2
                 1.000000704
                                          1.00000YC5
                                                                   1.00000YC6
                 1.000uuYC7
                                          80Y00000.1
                                                                   1.00000YC9
                 1.00000YC10
                                          1.00500YC11
                                                                   1.00000YC12
                 1.00000YC13
                                          1.00000YC14
                                                                   1.00000YC15
                -1.00000UYC16
                                          1.00000YC17
                                                                   1.00000YC18
                            1.00000
```

OPTIMIZE

one in the second of the secon

mPUS yERSIUM 4.0

NORTHWESTERN UNIVERSITY

办券未承示在公司采申录车基示业率出来了基本 中 FINCOLLIM NOONDER A 不 年单小小大大大大大大大大大大大大大大大大大

USING REGULAR *** NO. 2 # TEST THO PROD. FNTS. AND ONE DEMAND ***

			SUMI	MARY OF RESUL	TS		
VAK	VAR		STATUS	ACTIVITY	CPPORTUNITY	LOWER	UPPED
·· NO	THAME	140	** *	LEVEL	COST	BOUND	BOUND
į	112	***	В	16.4178473	0.0000000	0.0000	INF
2	111	. tree sales	ರ	50 . 0000000	0.000000	0.0000	INE
ر ۱۰۰	IVIT		В	33.9380000	C.00000000	0.0000	INF
4	17475	en ⁷ em	B .	11.0628710	0.000000	0.0000	INF
ິວ	1757	em 400	ರ	18.6540000	0.0000000	0.0000	INF
გ	INZC	/ · · · · · · · · · · · · · · · · · · ·	B · · ·	6.1460000	0.0000000	0.0000	INF
7	TAY	po TA	Lö	0.0000000	73.1310074	0.0000	INF
Ó	Y 1/2	***	LB	0 .00 00000	62+2906048	0.0000	INF
ः ः ध	YAZ		- LB	0.00000000	105.2450556	0.0000	INF
¥ψ	YA4	-	LB	0.0000000	158.1685041	0.0000	INF
1. 1	YA5	er to	L O	0.0000000	179.10/1592	0.0000	INF
···· 1 2··			- La.	0 • 40000100	- 59+3899412 -	0.0000	INF
ز ا	YAY	top the	LU	0.0000000	49.6261726	0.0000	INF
1 4	BAY		Li3	0.0000000	51. 0130968	0.0000	INF
· 15	1A9		Lb	0.0000000	60,4825959	0.0000	- INF
∔ن	TALU	A14 640	LB	0.0000000	76.4191000	0.0000	INF
17	THIL	es es	Ļij	0.0000000	51.6957010	0.0000	INF
-10	TALE		LB	0.000000g	31.3249520	- 0.0000	- INF
19	1A15	M/1 100	LU	0.0000000	20.6303785	0.0000	INF
20	1414		Ld	0.00000000	16.9559681	0.0000	INF
- <1	TA15	-	LB	0.0000000	18.6984881	0.0000	-INF
42	TALO	*** 40*	LB	0.0000000	49.1732345	0.0000	INF
رک	1417		LB	0.0000000	25.3274494	0.0000	INF
- 64	Talo	** ***	·· FB ··· ·	0.0000000	10.6556917	0.0000	INF
25	TALY		Ld	0.0000000	2.6524229	0.0000	INF
خ′ ن	TAZU	Apr. 200	В	1.0000000	0.0000000	0.0000	INF
27	X to X			0.0000000	109.01/3390	0.0000	INF
40	Yu2		Lb	0.0000000	274.6803493	0.0000	INF
والح	103	** ***	LB	0.60 00000	488.6497784	0.0000	INF
၁ပ	Y == 4		- LB	- 0 .00 00000	730.9451110	0.0000	-INF
31	Y U 5	en cur	LtJ	0.0000000	1019.0737103	0.0000	INF
ےد	YUÓ	441 40	LB	0.0000000	42.1805853	0.0000	INF
ా ఎ	167		Lb	0.0000000	- 1u6,248769 3	-0.0000	- INF
34	Yus	643 PM	LB	0.0000000	199.4409701	0.0000	INF
ఎస	169	010 E2	LB	0.0000000	314.5107790	0.0000	INF
పం	1910		LB	0.0000000	- 447.5823434	0.0000	INF
27	YULL	***	LU	0.0000000	10.1460935	0.0000	INF
၁၀	1612		LB	0.0000000	25.5615602	0.0000	INF
-	YELS		LB	0.00000000	60.8843257	0.0000	INF
# U	Y114		Lu	0.00000000	111.1784284	0.0000	INF
41	TULD	00 TH	しい	0.0000000	1/3.7922876	0.0000	INF
	1010	***	Ħ	•3582153	0.0000000	0.0000	INF
_	Tall		티	•6417047	0.000000	0.0000	INF
	1515	6# 00	L B	0•0000000	16.9904119	0.0000	INF
45	1019	M4 179	Lti	0.0000000	46.78085 3 9	0.0000	INF

MPOS VERSION 4.0

NORTHWESTERN ULIVERSITY

USING REGULAR

*** NO. 2 " TEST TWO PROD. FNTS. AND ONE DEMAND ***

SUMMARY OF RESULTS

VAR	VAK	. 14	(UW	STATUS	ACTIVITY		OPPORTUNITY	LOWER	UPPER
NU	HAME		NO		LEVEL		COST	BOUND	BOUND
40	Y to 2 U		~-	しけ	0.0000000		07.0715348	0.0000	INF
- 47	J.C.L.			LB	- 0.000000u		2750.0000000	0.0000	INE
ن 4	162		-	لالا	0.00000000		2340.00000000	0.0000	INF
49	YCB			LB	0.0000000		1960.0000000	0.0000	INF
ა	YL4	~		Li	 0.0000000		1650.0000000	0.0000	INF
51	YC5			Lö	0.0000000		1350.0000000	0.0000	INF
5%	Y C 6			드라	0. 00000000		1060.0000000	0.0000	INF
5 ₃	Y C 7			L 13	 - 0.0000000		840.0000000	0.0000	- INF
54	YCB			Lo	0.00000000		650.0000000	0.0000	INF
ხე	169			Lb	0.0000000		450.00000000	0.0000	INF
ა	YC10 -			LB	 0•0000000		- 300.0000000	0.0000	INF
57	YC11			LB	0.0000000		180.0000000	0.0000	INF
ప్ర	YC1Z			LB	0.0000000		90.0000000	0.0000	INF
	1613			LB	 - 0.0000000		50.0000000	0.0000	INF
ບິດ	YC14			じ	.7104305		0.0000000	0.0000	INF
οj	YC15			ដ	• 2835095		0.0000000	0.0000	INF
u <u>z</u> -	YClo -			·· LB ·	 0.0000000		- 50.0000000	0.0000	- INF
رن	YC17		~~ ~~	Ld	0.0000000		90.0000000	0.0000	INF
04	YCIO			LB	0.0000000		160.0000000	0.0000	INF
იე	SLACK	D	1	. LB	 0. 0000000	•	13.6315923	-0.0000	INF
じと	SEACK	U=	2	본	29.9991284		0.0000000	0.0000	INF
01	SEACK	U**	ئ	Li	0.00000000		5.0000000	0.0000	INF
o _o	SLACK	∪	4	- L6 ··	O•0000000		15.4315923	- 0.0000	· : · · INF
ပ်ပ	SLACK		5		0.0000000		9.0000000	0.0000	INF
٥į	AKTIF	IJ →	5		0.0000000		-9.0000000	0.0000	INF
/ u	SLACK	U-	Ġ		 -0.0000000	-	91+1767587	0.0000	·· INF
1	SLACK	U-	7	′ Lບ	0.00000000		2.0000000	0.0000	INF
12	SLACK	U-	8	-	0.0000000		15.4315923	0.0000	INF
/3	SLACK		ç) LB	 . 0. 0000000		9.0000000	0.0000	· · · INF
ರಕ್ರ	AKIIF -	U-	9		0.0000000		-9.0000000	0.0000	INF
14	SLACK	U=	10	i Luu	0.0000000		50.7923163	0.0000	INF
. 15	SLACK		. 11	. Ld	 0.0000000		9.0000000	0.0000	INF
57	AKTIF	D -	11	ناسا	0.0000000		-9.0000000	0.0000	INE
10	SLACK	٦-	12	≟ ≟ ಟ	0.0000000		2730.0000000	0.0000	INF

MAXIMUM VALUE OF THE OBJECTIVE FUNCTION = 3192.758883

CALCULATION TIME WAS .2200 SECONDS FOR 30 ITERATIONS.

DATA STORAGE MEMORY =002465(OCTAL) TOTAL MEMORY = 050000(OCTAL) TOTAL TIME FOR THIS PROBLEM WAS .991 SECONDS

Problem Two Dual

For problem 2, the dual values are taken from the computer output and listed below:

λ6 - dual row 6 - pr	oducer surplus $^{ m Y}$	91.18
$\lambda 10$ - dual row 10 - p	roducer surplus Y	30.79
λ11 - dual row 11 - p	rice of Y -	9.00
λ 12 - dual row 12 - c	onsumer surplus Y	- 2730.00

VI. HEADER CARDS

Three groups of JCL header cards are given. The first is to generate maximum output for troubleshooting. The second is to utilize a previously compiled program and to generate only output pertinent to problem solving. The third is to address APEX-1.

1. Maximum output, No LP output

NAME, T10.

ACCOUNT, GQM1111, PASSWORD.

BIN CARD IF NECESSARY

RFL(77000)

ACQUIRE(MGAO).

FETCH (MINNLIB/V=MNF)

MNF(I=MGAO, B=CMG)

RETAIN, CMG/CT=PU.

CBR(INPUT, TAPE5)

R, TAPE5.

SETTL(20)

CMG.

COST.

7 8₉

Data Deck

⁷89

6780

⁶7₈₉

2.	Reduced out	put using	compiled	deck,	CMG,	with	LP	output					
	NAME, T10.												
	ACCOUNT, GQM	1111,PASS	WORD.										
	RFL(77000)												
	FETCH (MINNL	IB/V-MNF)											
	ACQUIRE,CMG	•											
	CBR(INPUT, T	APE5)											
	R, TAPE5.												
	SETTL(20)												
	CMG.												
	R, TAPE1.												
	COPYSBF, TAP	E1,OUTPUT	•										
	R,TAPE1.												
	MPOS (TAPE1)												
	COST.												
	⁷ 8 ₉												
	Date Deck	Date Deck											
	⁷ 8 ₉												
	⁶ 7 ₈₉												
	6 ₇ 80							•					

3. APEX-1

In order to access APEX, the following cards are inserted between the MPOS(TAPE1) and COST cards in deck 2.

R,APXFIL.

COPYSBF(APXFIL,OUTPUT)

RETURN, TAPE1.

R,APXFIL.

RENAME, TAPE1=APXFIL.

APEX(SOLV-----)

VII. FINAL COMMENTS

This computer program has not been fully tested and problems may be found. However, initial testing and use indicate that the program could be extremely useful in solving certain types of problems. The fortran program itself is rather straight forward and appears to be organized in a way that would facilitate user provided modification.

Some comments regarding the use of MGAO with APEX are in order.

Currently, only APEX-I one is operable. APEX-II may be accessed, however format errors are incurred. If the user accesses APEX-I directly, parametric and/or ranging procedures are difficult if not impossible to perform.

An alternative is to use MGAO to punch out the data deck and then put together a completely new problem specification for the APEX problem. This may be done with cards or through the use of permanent files and interactive terminals.

The user should not be limited by the mathematical forms of the functions as currently read. One need only to change the format and the read statements to fit different needs and problems.

Bibliography

- [1] Program developed by Terry L. Roe and Paul Chang
- [2] Multi Purpose Optimization System User's Guide Version 3, Claude Cohen and Jack Stein, Manual No. 320, Copyright 1976, Voeglback Computing Center, Northwestern University, Evanston, Illinois 60201.

APEX-1 Reference Manual

- [3] Intrilligator Michael D., Mathematical Optimization and Economics Theory, 1971, Prentice-Hall, Inc., p. 72.
- [4] Intrilligator, p.44.
- [5] Duloy, John H. and Roger D. Norton, "Prices and Incomes in Linear Programming Models," American Journal of Agricultural Economics, Volume 57, Number 4 (November 1975) pp. 591-600.

Klein, Harold E. and Terry L. Roe, "Agriculture Sector Analysis Model Design: The Influence of Administrative Infrastructure Characteristics," in Planning Processes in Developing Countries: Techniques and Achievements, eds. W.D. Cook and T.E. Kuhn (Amsterdam-London: North-Holland, 1982) pp. 273-308.

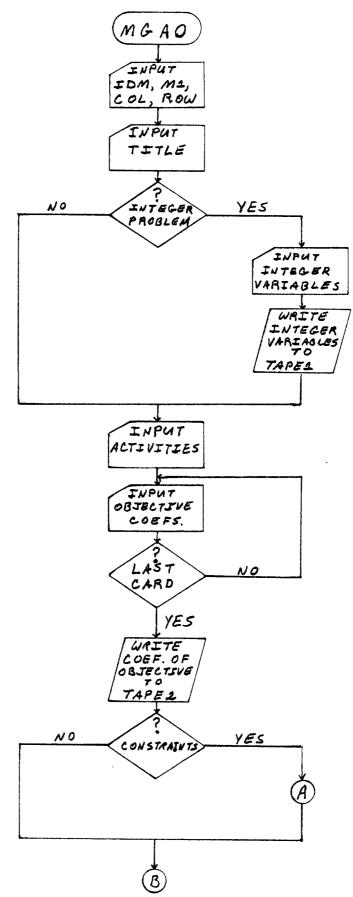
- [6] Klein and Roe, pp. 297-299.
- [7] Duloy, John H. and Roger P. Norton, "The CHAC Demand Structures, Chapter 3 in Programming Studies for Mexican Agricultural Policy, eds. Roger D. Norton and Leopoldo M. Solis, forthcoming.
- [8] Roe, Terry, "Modelling of Nonlinear Functions into a Linear Programming Format," Staff Paper P75-9, June 1975, Dept. of Ag. and Applied Econ., U of M, St. Paul.

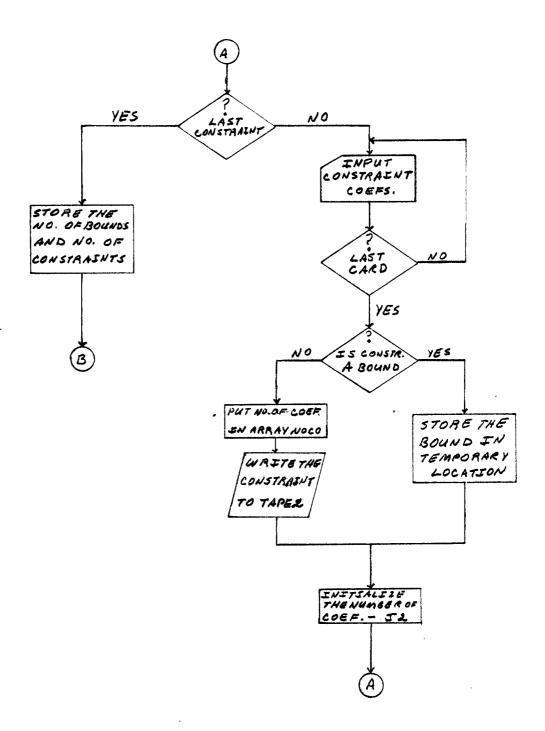
Appendix A. Variable Name

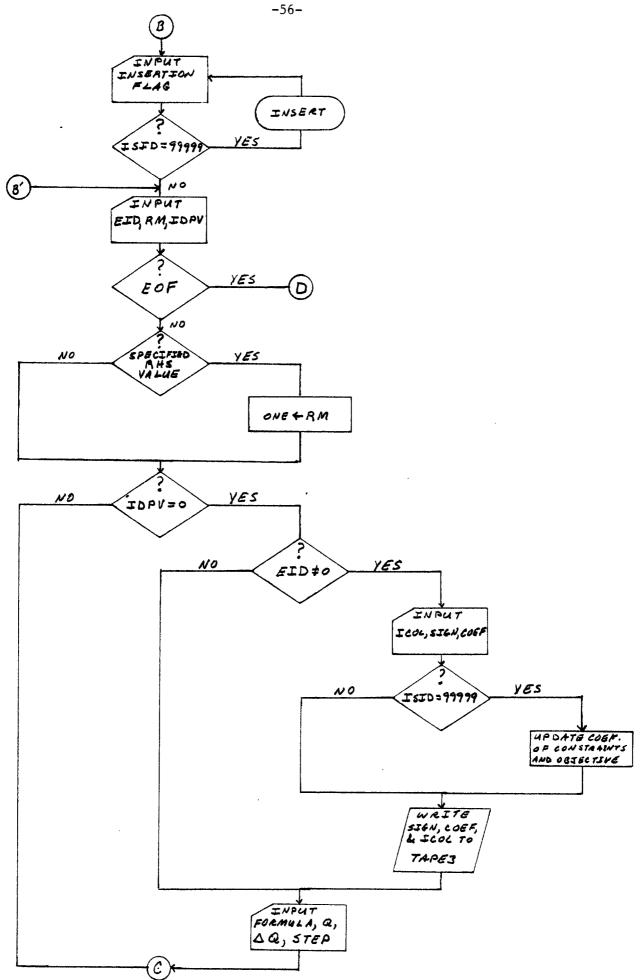
```
** METHO(M1) CONTAINS THE 12 ALGORITHMS WHICH ARE USED IN M.P.O.S.
      M1 = 01
                    #REGULAR#, 2-PHASE SIMPLEY
**
                                                    (L.P.)
      M1 = 02
* *
                    ≠REVICED## REVISED SIMPLEY
                                                    (L.P.)
      M1 = 03
                    ≠DUAL#, DUAL SIMPLEX
                                                    (L.P.)
      M1 = 04
                                                    (L.P.)
**
                    #MINIT# PRIMAL-DUAL ALG.
* *
      M1 = 05
                    #BBMIP#, BRANCH AND BOUND MIXED INT. PROGRAM. (I.P.)
**
      M1 = U5
                    #DSZ11P#, DIRECT SEARCH 0_1 INTEGER BROGRAM. (I.P.)
* *
      M1 = 07
                    #GOMORY#, GOMORY#5 CUTTING PLANE
                                                                    (I.P.)
                    #WOLFE#, WOLFE#S QUARDRATTC SIMPLEX (Q.P.)
#REALF#: BEALE#S ALGORITHM (Q.P.)
**
      M1 = 0_{\rm R}
      M1 = 09
**
      M1 = 10
                    #LEMKF# LEMKE#S COMPLEMENTARY PIVOT ALG. (O.P.)
**
                    #APEX1# MPOS-APEX DATA FILE INTERFACE (GENERAL)
**
      M1 = 11
      M1 = 12
**
                    #APEX2#, MPOS-APEX DATA FILE INTERFACE (GENERAL)
**
**
   VARS(N1) ARE THE RESERVED WORDS USED BY #SPOS#+
**
      N1 = 1
                    TITLE
      N1 = 2
* *
                    INTEGER
**
      N1 = 3
                    VARIABLES
      N1 = 4
                    MAXIMIZE
      N1 = 5
**
                    MINIMIZE
      N1 = 6
* *
                    CONSTRAINTS
**
      N1 = 7
                    BOUNDS
      N1 = 8
**
                    PRINT
      N1 = 9
**
                    OPTIMIZE
**
      N1 = 10
                    ENDAPEX
* *
      N1 = 11
                    BNDALL
**
      N1 = 12
                    BNDINT
* *
      N1 = 13
                    RNGOBJ
**
      N1 = 14
                    RNGRHS
      N1 =
**
           15
                    TOLERANCE
      N1 = 16
**
                    EPSILOY
      N1 = 17
**
                    BNDOBJ
      N1 = 18
**
                    LIMIT
      N1 = 19
                    NOSCALE
      N1 = 20
                    CHECK
      N1 = 21
**
                    QCHECK
* *
      N1 = 22
                    GO
* *
      N1 = 23
                    STOP
      N1 = 24
                    RESCALE
**
**
      N1 = 25
                    MAXCM
**
      N1 = 26
                    MAXECC
**
**
  GFL (M2)
                    CONTAIN #.LE.#, #.EQ.#, #.GE.#
**
         =-1n0
                    MEANS LESS THAN OR EQUAL TO
                    MEANS EQUAL TO MEANS GREAT THAN OR EQUAL TO
         =-200
**
* *
         =+3n0
* *
```

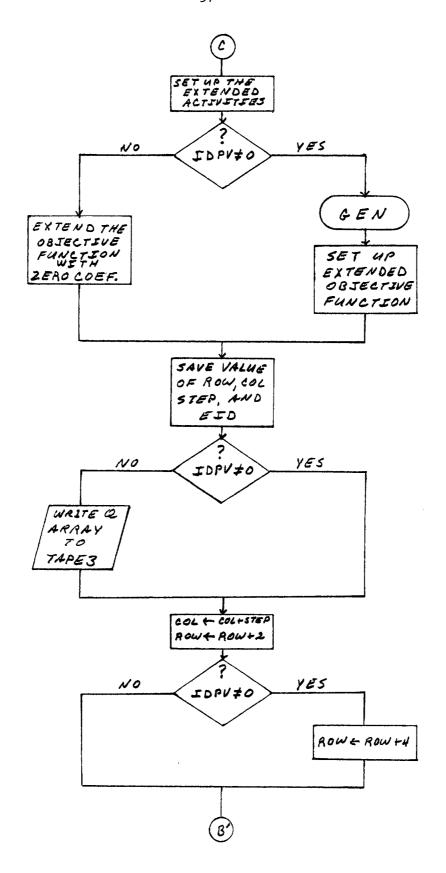
```
** CWRIJE
                        AN ARRAY STORE THE COEF. OF MATRIX TO BE DUMPED
** EID
                        EXYEDING MODEL FLAG
**
           .EQ. 0
                        EXTENDING THE MODEL WITHOUT READING THE COEF.
**
                        (CNA) AVAIB SHO GCA YING)
* *
           .NE. 0
                        EXTENDING THE MODEL WITH
                                                         READING THE COEF.
                        (PUNCH THE NO. OF COEF. WHICH WILL BE ADDED.)
    1DM
                        MAX. OR MIN. IDENTIFIER
           = 0
                        MEANS MAXIMIZE
* *
           = 1
                       MEANS MINIMIZE
   IDPV
           = 99999
                        2 INDEP. VAR. FUNC. EXTENSION
           = 0
                       OTHER CASE
**
   ISIO
                       INSERTION FLAG
**
                       NO NEW ACTIVITIES ARE TO RE ADDED.
**
           = 99999
                       NEW ACTIVITIES ARE TO BE INSERTED.
                        DUMP WAIRIX TABLE FLAG
**
    IWRITE
                       DONAL DUMP THE TABLE
**
**
           = 1
                       DUMP THE TABLE
                       DUMP PART OF THE TABLE
**
           = 2
** ACT
                       ACTIVITIES
** AACT
                       NEW ACTIVITIES
                       COEF. OF THE FORMULA
ABSOLUTE VALUE OF THE COEFFIENT.
COLUMN NO. OF THE MATRIX(NO. OF FNTRIES)
** CC
** COEF
** CoL
                       DELTA Q
** DELTAQ
** ICOL
                       COLUMN COORD. OF THE ACTIVITY
** IEXP
                       EXPONENT OF EACH ITEM OF THE FORMULA
** lJ
                       NO. OF ITEMS OF THE FORMULA.
AL **
                       NO. OF EXTENDING PROCEDURES.
                       NO. OF INTEGER VARIABLES FOR I.P.
NO. OF ACTIVITIES NEEDS TO BE INSERTED
** N2
**
   NAA
                       TOTAL NO. OF NON-ZERO COEF.
THE PLACEMENT OF NEW ACTIVITIES WILL BE INSERTED
** NBB
** NINS
                       ARRAY STORE THE VELUES OF COL OF EXTENDING ARRAY STORE THE VELUES OF EID OF EXTENDING
** NCOL
** NEID
                       NO. OF BOUNDS
** NOBU
                       NO. OF CONSTRAINTS
** NOCD
                       ARRAY STORE THE VELUES OF NOCO OF EXTENDING ARRAY STORE THE VELUES OF ROW OF EXTENDING ARRAY STORE THE VELUES OF STEP OF EXTENDING
** NOCO
** NROW
** NSTEP
** ONE
                       #1#, CONSTANT ONE.
** 4(1)
                       INITIAL VALUE OF 9
** ROW
                       ROW NO. OF THE MATRIX
                       THE SPECIFIED R.H.S VALUE DIFFERENT FROM DEFAULT ONE*
** RM
                       SIGN OF THE ACTIVITY
** STGN
** STEP
                       STEPS
** TACT
                       TEMP. LOC. STORES THE ACTIVITIES OF BOUNDS
                       TEMP. LOC. STORES THE ABSOLUTE VALUES OF BOUNDS
** 100EF
** TITLE
                       TITLEOF THE PROBLEM (RESTRICTED ONE CARD )
                       TEMP+ LOC+ STORES THE SIGN OF BOUNDS
TEMP+ LOC+ STORES THE RELATIONS OF BOUNDS
** TSIGN
** TT1
                       TEMP. LOC. STORES THE SIGH OF R.H.S.
** TT2
                       TEMP+ LOC. STORES THE ABSOLUTE VALUE OF R+H-S. THE VALUES OF THE FORMULA WITH PUTTING Q VALUES THE STONS OF W ARRAY
** TT3
** 4
** WSIGN
** XGIGN
                       ###, MINUS SIGN.
** YSIGN
                       ###, pLUS SIGN.
                       #U#! CONSTANT ZERO
```

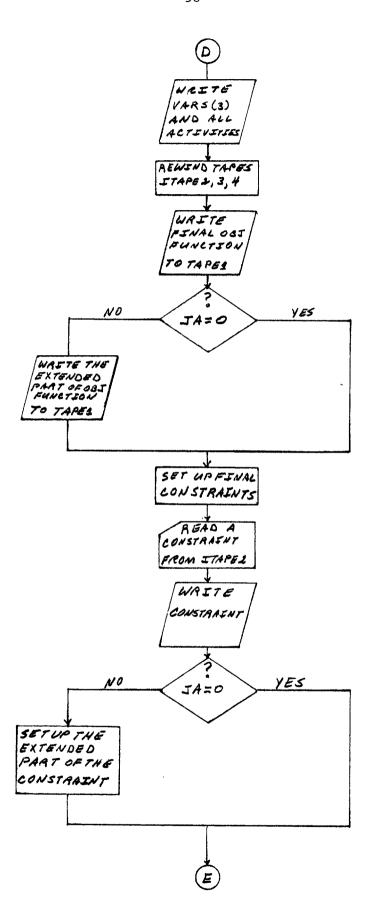
Appendix B. Flow Chart

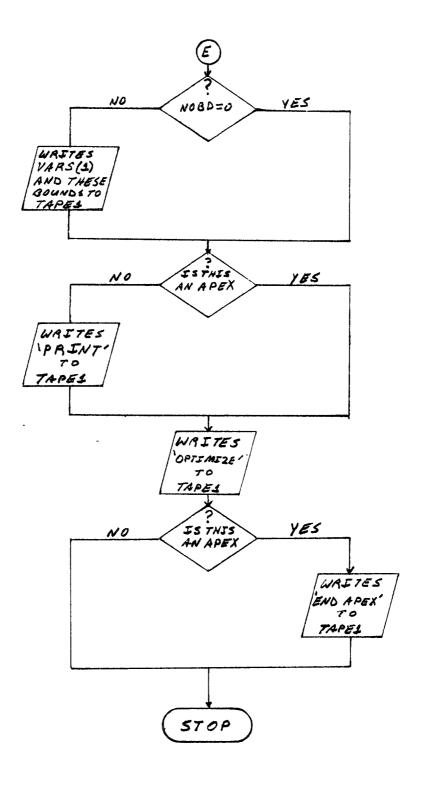


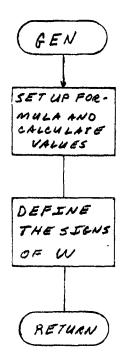


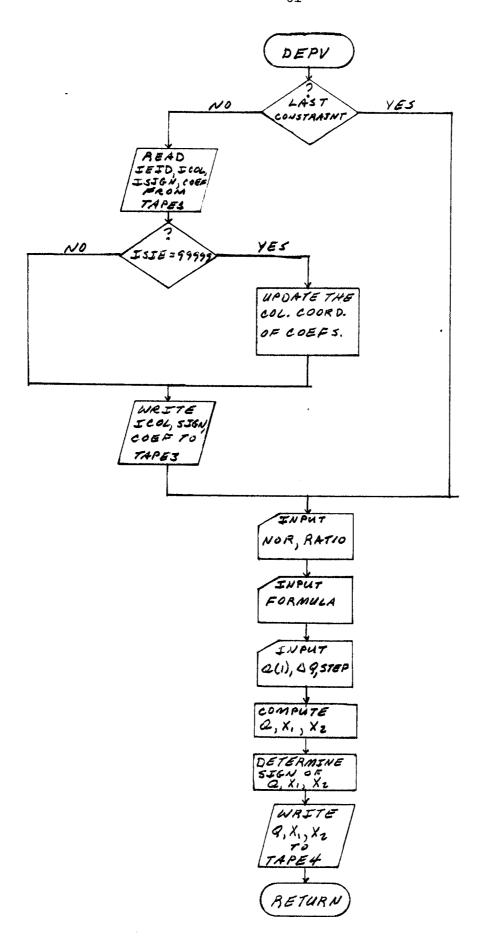














Appendix C. Program Listing

```
MATRIX GENERATOR AND OPTIONALS
    Mushic
李爷亲说,我有什么不不不要的,我们就是我们的自己的自己的,我们的自己的,我们的自己的人,我们的自己的人,我们的自己的人,我们的自己的人,我们的自己的人,我们就会
            THE FUNCTION OF THIS ROUTINE IS TO
            READ A SET OF DATA CARDS IN SPECIFIED FORMATS.
            SET UP AN M.P.O.S. MODEL OR EXTED THE MODEL BY
            CALLING AN APPROPRIATE SUBROUTINE (GEN).
            THACUGH MAPAGASA , WE CAN GET THE SOLUTIONS.
* METHO (31) CONTAINS THE 12 ALGORITHMS WHICH ARE USED IN M.P.O.C.
    M1 = U.
               FREGULARE. 2-PHASE STUPLEY
                                             (L.P.)
    in1 = un
                 *REVISED#, REVISED SIMPLEY
                                               (L.P.)
    Wil = U4
                 #DUALE DHAL SIMPLEX
                                               (I.P.)
    Fel = 0...
                 #MINITE. PRIMAL-DUAL ALG.
                                              (| .P.)
    41 = Ua
                 #BRAIR#, BRAUCH AND BURND MIVED INT. PROGRAM. (T.P.) *
                 #MSZITP#: DIRECT SEARCH 0-1 INTEGER PROGRAM. (T.P.) *
    M1 = U,
                 #GOMORY# . GOMORY#S CUTTING PLANE
    MI = 0 -
                                                             (T.P.) *
    MI = Un
                 #WOLFF#, WOLFF#S QUARDRATIC SIMPLEX (Q.P.)
    15.1 I Um
                 #REALF#. REALF#S ALGORITHM
                                                    (n.P.)
                 #LEMKF#. LEMKF#S COMPLEMENTARY PIVOT ALG. (Q.P.)
    841 = 1A
    int = 1.
                 #APEXIA. MPOS-APEX DATA FILE INTERFACE (GENERAL)
    MI = 1.
                 *APEX2#: MPGS-APEX DATA FILE INTERFACE (GENERAL)
 VANS(M1) ARE THE RESERVED WORDS USED BY #APOS#.
    N1 = 1
               TITLE
    W1 = 2
                 INTEGER
    1,1 = 3
                 VARIABLES
   -N1 =-4 -
                -- MAXIMTZF----
    N1 = 5
                 MINIMIZE
    141 = 6
                 COMSTRATATS
    141 = 7
                 SOUNUS
    N1 = 8
                 PRINT
    1.1 = 9
                 OPTIMIZE
    N1 = 1.
                 ENDAPEX
    (4) = 1.
                 BNOALL
    N1 = 1.
                 BINDLINT
    111 = 1 -
                 RMGORG
    141 = 1...
                 RNORHS
    141 = 10
                 TOLERANCE
    N1 = 1,
                 EPSILON
    N) = 1-
                 BNOOKL
    N1 = 1a
                 LIMIT
    N1 = 10
                 NOSCALE
    Nx = 20
                 CHECK
    N1 = 2.
                 QCHECK
    N1 = 2.
                 GO
                 STOP
    N1 = 2.
    1.1 = 2.
                 RESCALE
    111 = 20
                 MALCIN
    1.1 = 2.
                 MALECS
GEL (M2)
                 CONTAIN F.LE.T. F.EQ. # F.GE. #
       =-1...
                 MEANS LESS THAM OR EQUAL TO
       2000
                 MEANS EDUM: 10
       =-3.0
                 MEANS GREAT THAM OR ENHAL TO
```

```
* [....]] [
                   AN ARRAY STORE THE COSE. OF MATRIX TO BE DUMPED
 Elin
                   EXTENTION VODEL FLAG
                   EXTENDING THE MODEL WITHOUT WEADING THE COEF. (ONLY ADD ONE BLANK CARD)
         · Ew
                   EXTENDING THE MODEL WITH
                                                 READING THE COEF.
         · NE
                   (PUNCH THE NO. OF COEF. WHICH WILL HE ADDED.)
  1100
                   MAX. OR WIN. TOENTIFIER
                   MEANS MAXIMIZE
        = 11
        = 1
                   MEANS MINIMIZE
 LINEV
        Z 9.00u
                   2 THUFP. VAR. FUNC. EXTENSION
                   OTHER CASE
        ~ U
  ISID
                   INSERTION FLAG
        = U
                   NO NEW ACTIVITIES ARE TO BE ADDED.
        = 9,499
                   NEW ACTIVITIES ARE TO BE INSERTED.
  I lain [] F
                   DUMP WATRIX TABLE FLAG
                   DOISET DUMP THE TABLE
        = 1
                   DUMP THE TABLE
                   DUMP PART OF THE TABLE
                   ACTIVITIES
 AUCT
                   NEW ACTIVITIES
                   COEF. OF THE FORMULA
* CC
                   ABSOLUTE VALUE OF THE COEFFIENT.
 COFF
  CUL
                   COLUMN NO. OF THE MATRIX (NO. OF ENTRIES)
* DEL FAQ
                   DELTA O
                   COLUMN COORD. OF THE ACTIVITY
* ICOL
                   EXPONENT OF EACH ITEM OF THE FORMULA"
* IFxP
* I.1
                   NO. OF ITEMS OF THE FORMULA.
 شال
                   NO. OF FATENDING PROCEDURES.
 112
                   NO. OF INTEGER VARIABLES FOR I.P.
                   NO. UF ACTIVITIES NEEDS TO BE INSERTED
                   TOTAL NO. OF MON-ZERO COEF.
                   THE PLACEMENT OF NEW ACTIVITYES WILL BE INSERTED
 MINS
                   ARRAY STORE THE VELUES OF COL OF EXTENDING
 MC OL
                   ARRAY STURE THE VELUES OF EID OF EXTENDING
                   NO. OF ROUNDS
                   NO. OF CUMSTRAINTS
 NOCE
                   ARRAY STORE THE VELUES OF NOCO OF EXTENDING
  NOCO
                   ARRAY STURE THE VELUES OF ROW OF EXTENDING ARRAY STORE THE VELUES OF STEP OF EXTENDING
  No MA
  NSTEP
 ONE
                   #1#, CONSTAUL ONE.
                   INITIAL VALUE OF Q
  3111
                   ROW NO. OF THE MATRIX
 18.11.
                   THE SPECIFIED R.H.S VALUE DIFFERENT FROM DEFAULT ONF*
                   SIGN OF THE ACTIVITY
  STail
                   STEPS
  SILP
                   TEMP. LOC. STORES THE ACTIVITIES OF ROUNDS
TEMP. LOC. STORES THE ABSOLUTE VALUES OF ROUNDS
  TACT
  TODEF
                   TITLENE THE POORLEM (RESTRICTED ONE CARD )
  TITLE
  TSIGN
                   TEMP. LOC. STORES THE SIGN OF BOUNDS
  171
                   TEMP. LOC. STORES THE RELATIOUS OF BOUNDS
  Tio
                   TEMP. LOC. STORES THE SIGN OF R.H.S.
  TTA
                    TEMP. LOC. STORES THE ARSOLUTE VALUE OF R.H.S.
                   THE VALUES OF THE FORMULA NITH PUTTING Q VALUES
                   THE STOWS OF W ARRAY
  WSIGN
                   F-F: MINUS SIAN.
  XS15W
* YS10N
                   # FFF - Lits SLAH.
                   $04, COMSTANT ZERO
```

```
PROGRAL MANO(INPUT:NUTPUT:TAPF1:TAPF2:TAPF3:TAPF4:TAPF5:TAPF6=OHT
APUT, THUE T, TAPELLI
 REAL METHIN, 18 XP, L
 INTEGE. AICOL, AFWCOL, AFWROW
 INTEGER COLLINOW FIDISTEP
 COMMON /T111/0(1000).w(1000).CC(10).TEVP(10) .wsIgw(1000)
 COMMON ZTELEZOFLTAG, CUL, RUW, FID, STEP, I 1, 10M, MI, NZ, NOBO , NOAB
 COMMON /:113/Tille(8).6EL(3).ACT(1200).ICOL(1200).SIGN(1200).
          CUFF (1200) . METHO (15) . VARS (26)
 NOMMOD
          /1114/TACT(100), Tip(100), TT3(100)
 COMMON
          71115/NSTFP(50)+NOCO(500)+NROW(50)+NCOL(50)+NEID(5a)
 COMMON
         /illo/Y(20.100)
 COMMON
          /T118/RACTO(100):c(1000):L(1000):100V(50)
 COMMON
           /Til9/[Ein(100).CSIGN(1000).LsIGN(1000).oSIGN(1000)
 COMMON
           /T120/ASIGN.YSIGN.ZERO.ONF.JA.JB.JC.NRR.TTAPE1.ITAPE2
 COMMON
         /TIPI/ISID: NAA: NdB: NINS: AACT(2n) . AICOL(2n) . ASIGN(2n) . ISIF.
          ACOFF (20) . AEWROW (50) . AFWSIGN (50) . AEWCOFF (50) . AFWCOL (50)
 DATA -FRUIFIDIISIF/0.0:-1.0/
 DATA X-IGN, YSIGN, ONE, JA, JB. JC/t-t, ++1,1.0.0.0,1/
DATA METHOZZREGULAR
                         # # #KEVISED
                                        #.≠DUAL
                                                      #.#MINIT
*≠BMIP
                                          #.#WOLFF
             #+#DSZ11P
                           ≠,±GOMORY
                                                         * * FREALE
                                                                       I.
*ILFMKE
             I, IAPEXI
                           # . + APEX2
                                          11
 DATA G-1/4 .LE. +++ .EA. ++ + .GE. +/
DATA VARSZITITLE
                        ###INTEGER ###VARIABLES ###MAXIMIZE
*#MINIM.ZE #.#CONSTRAINT#.#BOUNDS
                                          #. PRINT
                                                        # # #OPTIMT7F
* FENDAP-X
                                          #.#RNGORJ
                                                                       Į,
             TITHINUAL L
                           #++BNDTNT
                                                        ±, ≠RNGRHC
*#TOLER.NCF # ##FP511 ON
                                          #.#LIMIT
                           4+±BNOOBJ
                                                        ±+#NOSCALE
                                                                       #,
**CHFCK
             # # # SCHECK
                           # . #GO
                                          #.#STOP
                                                        + + #RESCALE
                                                                       t.
##MAXCML
             *+ *MAXEYS
 DATA DFPV.NORO/# #.U/
 DATA
       -AC1.TT2.T13/200*# #.100*0.0/
DATA
       /Y(1,MA),MA=1,1U0)/4YA1
                                      #, ±YAo
                                                            #. #YAu
                                                 +, +YA3
*#YA5
         t.
       -YA6
                I. + Y 47
                           I. ±YA8
                                       F. #YA9
                                                  ###YAIN
                                                             # / # Y 1 1
       -YA12
                           I.TYA14
                                       TITYA15
                                                  #1#YA16
                                                             INTYA17
                II+YA13
                                                                        ±.
                                                    #YAD1
       -YAIR
                I. IYA19
                           TITYARA
                                                             #1#Y122
                                                                        ±.
       -YA23
                                       t. tYA26
                                                  1. LYA27
                                                             #1#YA28
                            ± . + Y . 25
                E. LYAZU
                                                                        ±.
                                       #1 #YA32
                                                  ###YA33
       -YA29
                # . FY 430
                            ICAYX . I
                                                             ###YA34
                                                                        ±.
                                       I. IYABA
                                                  IIIVA30
                                                                        t.
       -YA.55
                I. IYU3h
                           IIIXAS7
                                                             エリオイルはひ
                            #+#YA43
                                      # + # Y 444.
       ... t . t Y A 45 ....
                                                             totYaus-
                                                                        t.
       4YA47
                I. FYA4A
                           #, #YA4a
                                       # #YA50
                                                  * . #YAS1
                                                             #1#Y652
                                                                        t.
                                       #, #YA56
       -YA53
                #. FY454
                           4, +YASS
                                                  #, #YAK7
                                                             I, IYASA
                                                                        ±.
                                       #1#Y462
                                                  I, IYAA3
       #YA54
                # . FYABO
                           ###YA61
                                                             #1 # Y A 64
                                                                        t.
       -YAns
                                       t. TYAGA
                                                  totyagn
                I. FYUGA
                            #. tYA67
                                                             t. IYA70
                                                                        ±.
       -YA71
                1. EYA70
                            # , # Y'A 7 3
                                       t. LYA74
                                                  LILYA75
                                                             ###YA76
                                                                        ±.
                                       ###Y490
       -YA77
                # + FYATR
                            T. IYA70
                                                  LITYAAT
                                                             #1#YAR2
                                                                        Í.
       LYAHR
                # + # Y & 84
                            #++YA85
                                       #+ LYARS
                                                  ±1≠YAH7
                                                             ###YARB
                                                                        t,
                                       1.1YA92
                                                  ###YAQZ
       -YANG
                IIIIAYA90
                            t.tYA91
                                                             t, tYAQU
                                                                        Í.
                112449K
                                       L. LYAGA
                                                  1, LYAU9
       LYAME
                            £114497
                                                             ###YA100
                                                                        1./
 DATA
       /Y(2,MA),MA=1,100)/4YB1
                                      # . #YB2
                                                 キャキYR3
                                                            キ・キャらに
```

```
*#YB5
          Į,
        a Yisin
                  I. LYU7
                              Z. LYAR
                                          1.1144
                                                      IF#YB1n
                                                                  I+ IYR11
                                                                              t.
        -YH12
                                          1, 1YR15
                  I. IYR13
                              2, #YB14
                                                      INTYRIA.
                                                                  ###Y017
                                                                              Í.
        .. YE18
                  # . FYR19
                              #+#Y820
                                                        #YB21
                                                                  #+#Y1122
                                          £ .
                                                                              Í.
        ~YB23
                  #1+Y224
                              # , #YH25
                                          IIIXXX25
                                                      キャキYR27
                                                                  ###Y1128
                                                                              t.
        LYAPA
                              #++YB31
                                          #+#Y032
                 #+#YH30
                                                      キャギソけるろ
                                                                  #1#Y034
        4 YA35
                  # . # YH3A
                              I. tYR37
                                          11 1Y 13 3 8
                                                      III EYR30
                                                                  *+ #Y040
                                                                              t.
        .YR41
                  # . #YH42
                              1.+YH43
                                          I. 1. YA44
                                                      #,#Y845
                                                                  ###YWUR
                                                                              t.
        4YB47
                 I. LYRHA
                             I. IYH49
                                          1, #YA50
                                                      キャエYBS1
                                                                  エナキYロ52
                                                                              I.
        +YF153
                 1. #YR54
                              # . + YB55
                                          4, 2YA55
                                                      t.IVBG7
                                                                  ###YR58
                                                                              1.
        -Y659
                 #+ #YR60
                              #, #YH61
                                          5.1YR62
                                                      # , # YB63
                                                                  エレキソロムは
        -Yanh
                 #+#YH66
                              1+±Y867
                                          I + I YASA
                                                      ###YBAn
                                                                  ###YA70
                                                                              I.
                                                      1+1Y875
                                                                  ###YR76
        +YB71
                 # . 4Y272
                              # . + YG73
                                          t. tYa74
                                                                              I.
        4Y877
                 I, LYH7A
                              #1#Y879
                                          DPRYTET
                                                      #+#YBA1
                                                                  # # # YAR2
                                                                              I.
        -YBA3
                  # # # YARL
                              #1#Y885
                                          4. #YRR6
                                                      ###YBA7
                                                                  ###YRRR
                                                                              I.
        -YAHO
                  LITYR91
                              ###YA91
                                          I. IYRG2
                                                      ###YBOZ
                                                                  #1#YEQ4
                                                                              t.
        4YB95
                  TITYH96
                              #,+YA97
                                          71 1749R
                                                      I. I yRaa
                                                                  # # # Y 10 100
                                                                             ±/
DATA
        ,Y(3,WA),MA=1,100)/#YC1
                                         #, #YCo
                                                     ###YC3
                                                                 #. #YCu
                                                                             Į,
*#YC5
          1.
        -YCn
                 INFYC7
                              #1+YC8
                                          to #YC9
                                                      #+#YC1N
                                                                  ###Yr11
                                                                              z.
                                                      I, IYC1a
        4YC12
                  F.FYC13
                              #11YC14
                                          #+ 4 YC 15
                                                                  #+#Yr17
                                                                              ±.
        .YCIA
                  #+#YC19
                              ###YC2n
                                                        ≠YC21
                                                                  1+ #Yr22
                                          10
                                                                              ±,
        -YC23
                  4.4YC24
                              #+#YC25
                                          £11YC25
                                                      エ・キャピップ
                                                                  エナキYc28
                                                                              i.
        44C24
                 ###YC3n
                              # . 1YC31
                                          1. ±YC32
                                                      #11YC33
                                                                  #+#YC34
                                                                              t.
        4Y635
                 #+ FYC36
                              キャセYC37
                                          #+#YC38
                                                      ±+#YC3n
                                                                  キャキソクなり
                                          1, ±YC44
                                                      #1#YC45
        ..YC41
                  #+#YC42
                              *++YC43
                                                                  111Y046
                                                                              I.
        -YC47
                 I. IYC48
                              1.1YC4a
                                          # + # Y C 50
                                                      #+#YCS1
                                                                  #1#Y052
                                                                              Í.
        -YC53
                 # . #YC54
                              #++YC55
                                          ###Y056
                                                      ###YC57
                                                                  ###Y058
                                                                              t. .
        +YC5a
                 #1#YC60
                              #,#YC61
                                          #+#YC62
                                                      #+#YCK3
                                                                  ###YOR4
                                                                              I.
        -YCh5
                 111YC66
                              #++YC67
                                          ###YC6A
                                                      #+#YCAn
                                                                  ナ・キャーフリ
                                                                              t.
        -YC71
                  ###YC72
                              #, #YC73
                                          INTYC74
                                                      #1 #YC75
                                                                  #1#Y076
                                                                              Ź.
        4YC77
                  ###YC7A
                              #, #YC79
                                          4. #YC80
                                                      # # #YCA1
                                                                  #+#YCA2
                                                                              t.
        4YCK3
                  ###YC84
                                          # # #YOBS
                              #, +YC85
                                                      エルギYCハフ
                                                                  ###YCRR
                                                                              ŧ.
        4 YCAG
                  #+#YC90
                              # . #YC91
                                          #, #Yra2
                                                      # , tyCaz
                                                                  #1#YC94
                                                                              Í.
        +YC95
                  ###YC96
                                          #. #YC98
                              # + ± YC97
                                                      #+#YCoa
                                                                  #!#Yr100
                                                                              #/
DATA
        /Y(4, MA), MA=1,100)/#YD1
                                         1.2YD2
                                                     #*#YD3
                                                                 ≠,≠Y7u
                                                                             Į,
*#YD5
         I.
        +Y06
                  # . FYN7
                              4, #YD8
                                          ###YN9
                                                      ###YD1n
                                                                  #1#Yn11
        +Y(110
                              #1+YD14
                  1. IY113
                                          # . # YD15
                                                      1, EYD1a
                                                                  41 #Yn17
                                                                              ±.
        ...Y()1A
                  # . #YD19
                              #+±YD2n
                                                        #YD21
                                                                  #1#Yn22
                                          I.
                                                                              ±.
        +YD23
                  #+ #Y1124
                              #, ±Y025
                                          # . # Yn26
                                                      キ・キYn27
                                                                  ###Yn28
                                                                              Í.
        4Y029
                  チャチャの30
                              # + + Y 131
                                          #+#Y032
                                                      キャギYD33
                                                                  ###Yn34
                                                                              t.
        +YD35
                  ###YN3A
                              # + ±Y037
                                          1+#Y038
                                                      #1#YD39
                                                                  #+#Y040
                                                                              Ź.
        +Y1741
                  キャナメリサン
                              #+#YD43
                                          1140Att
                                                      I. IYDus
                                                                  #1#Yn46
                                                                              t.
                                          4. #Yn50
                  #+#YM4A
        4YD47
                              #, tY1)49
                                                      #1#YD51
                                                                  #1#Yn52
                                                                              t.
        +Y053
                  ###YN54
                              #+#Y055
                                          111Yn55
                                                      #+#YDS7
                                                                  キナキイの58
                                                                              ŧ.
        4YD59
                  #+#Y060
                              ###Yn61
                                          29U1 1 + +
                                                      ###YDK3
                                                                  4+4YDBA
        +YDn5
                              # + + Y N 67
                                          II #YOSB
                                                      # . LYDAG
                                                                  #, #Yn70
                                                                              ± .
        4YD71
                  #++Y072
                              # . ± Y1773
                                          1. #Y074
                                                      #, #Y()7K
                                                                  ±1 キャハフら
                                                                              t.
        4Y077
                  ###YD78
                              #++YA7a
                                          # # #Y080
                                                      ###YOR1
                                                                  ###YOR2
                                                                              ±.
        ∓Y083
                  ###YN84
                              # . xYD85
                                          1 + 1 YORK
                                                      IIII LYDAT
                                                                  ###YOAR
                                                                              # •
                  #14Y090
        4YDN4
                              キょまYの91
                                          T. TYD95
                                                      ###YDa3
                                                                  ###Y504
                                                                              J. .
        +Y1945
                  FITY1196
                              キ, ±Y1197
                                          t. tYnga
                                                      # + LYDaa
                                                                  # # # Y 5 1 0 0
                                                                              #/
IMIA
        14 (5.MH) . MA=1+1001/44F1
                                         #, #YES
                                                     1.4YE3
                                                                 1, #YF (1
                                                                             ‡.
* 4 YF 5
         7.
```

```
###YESB
        - Y+ 6
                  1 + 4 Y = 1
                               ++ITTH H
                                            111TEU
                                                                     #1#Ye11
                  #++YF13
        4YF12
                               1. tYF14
                                            4.2YF15
                                                        I. IYF1K
                                                                     11 t Y = 17
                                                                                  1 .
         -YFIR
                  11+YF19
                               #+ #YE 20
                                                           #YE 21
                                                                     ±1 ± 4 = 22
                                                                                  i.
                                            I.
        -YF23
                  # # # YF 24
                                            IIIYF26
                                                         LILYFOT
                               #+±YF25
                                                                     ###Y#28
                                                                                  t.
        -YF24
                  #14YE30
                               #++YF31
                                            # . #Y # 32
                                                        IIIYF 33
                                                                     11 #Y=34
                                                                                  t.
                                            1,1YF38
                                                        #+#YF30
        ~YF35
                  414YF36
                               #11YF37
                                                                     LITYEUD
                                                                                  I.
         -YF41
                                            # . # Y = 4 4
                                                                     41#YE46
                  I. LYEUD
                               I. tYFU3
                                                        t. LYFUS
                                                                                  Í.
         +YE47
                  LIFYF4R
                               # , + YF40
                                            4. #YF50
                                                        #+ #YEn1
                                                                     エナキャセラク
                                                                                  z.
        →YF53
                  F. FYF54
                               #, 14F55
                                            #1#Y#56
                                                        エノエYFニフ
                                                                     #1#YE58
                                                                                  1.
                                            #1#YF62
        +YE59
                               ###YF61
                  I.IYF60
                                                        ###YFAR
                                                                     エ・エソビムは
                                                                                  Z. .
        -YF65
                  #1#YF66
                               1.1YF67
                                            ###YF68
                                                        t + #YFK4
                                                                     #17YF70
                                                                                  ± .
        ~YF71
                               # + ± YF 73
                                            # . #YF74
                                                        1, #YE75
                                                                     #1#YE76
                  LIFYE72
                  IIIIYF7A
         -YF77
                               # + tYF79
                                            ###YF81
                                                        ###YEW1
                                                                     # # #YERP
                                                                                  ±.
                                            ###YEB6
        -YFB3
                  I.FYF84
                               # , + YF85
                                                        ###YFA7
                                                                     ±11YEAA
                                                                                  1.
                  #1#YF90
                               1. ±YF91
                                            ###YF92
                                                        #1#YEQZ
                                                                     ###YE94
                                                                                  # .
        LYFNG
        4YE45
                  LILYF9A
                               #+#YF97
                                            ###YF9R
                                                                     ###Y⊏100
                                                        # # TE aa
DATA
         /Y(8,MA),MA=1,100)/#YF1
                                           #,#YFo
                                                        4. #YF3
                                                                    # . #YF /
**YF5
           ‡.
         -YF6
                                            I, IYF9
                                                        # # #YFin
                  エ・エソドフ
                               I . EYEA
                                                                     #1#YE11
                                                                                  I.
        _YF12
                  #+#YF13
                               # * ± YF14
                                            # # # YF 15
                                                        t, #YFIL
                                                                     ###Y=17
                                                                                  t.
                  # . FYF19
                               #++YF20
                                                           #YF21
                                                                     ###Y#22
                                                                                  z,
         +YF1A
                                            £.
        LYF23
                               #, ±YF25
                                            # , #YE26
                                                         ±+4YF27
                                                                     #+#Y=28
                                                                                  t.
                  # . # YF24
        -YF29
                  #1#YF30
                               t, ± YF31
                                            1. #Y#32
                                                        オナキャデスス
                                                                     2+ #Y=34
                                                                                  ±.
*
                                                        # . # YF 30
                                            x1 ± Y = 38
                                                                                  ±.,
         _YF35
                  # . LYF36
                               #++YF37
                                                                     ±1 ±Y=40
         4YF41
                  # . AYF42
                               ###YF43
                                            I, IYEU4
                                                        1, TYFAR
                                                                     1 . 1 Y = 46
                                                                                  I.
        +YF47
                  #+#Y#4A
                               #1 ± YF49
                                            # + #YF50
                                                        キャキYF5も
                                                                     ナナキャビ52
                                                                                  z.
                               # , #YE55
                                            # , #Y#56

ま,≠YF57
                                                                     #1#YE58
        -YF53
                  4+7YE54
                                                                                  #.
        4.YF59
                  #. FYF60
                               ###YFo1
                                            I, #YF62
                                                         LILYFAR
                                                                     オナギソ#64
                                                                                  t.
         -YFns
                               t, tYF67
                                            ###YESB
                                                        ###YFAQ
                                                                     エナキソニフロ
                                                                                  ŧ.
                  1, 17 F66
         4YF71
                                            # . ± Y = 74
                                                        #+#YF75
                               ###YF73
                                                                     ###Y=76
                                                                                  ±.
                  ###YF72
         -YF77
                  # + FYF7A
                               L, ±YF79
                                            #+#YF90
                                                         t+ tYFA1
                                                                     #1#YER2
                                                                                  t.
                  I. FYF84
                               #++YF85
                                            #1#Y#96
                                                         t, tYFR7
                                                                     I . IYEAR
         -YFA3
                                                                                  I.
         -YFR9
                  I. FYF91
                               t, tYF91
                                            #1#YF92
                                                         #, #YFaz
                                                                     # # # Y # Q #
                                                                                  T .
                               #, #YF97
         ...YF45
                                            #, #Y=9A
                                                                     ###Y=100
                  1.FYF96
                                                        ±, #Y.Faq
                                                                                  11
         ,Y(7,MA),MA=1,1U0)/4YG1
                                           # . #YG2
                                                                    # # #YGu
                                                       # . # YG3
 DATA
                                                                                 t.
*#YG5
           # ,
         "YGn
                  I. IYGT
                               ≠, +YGA
                                            #. #YG9
                                                        # # #YG1n
                                                                     # + # Y a 1 1
                                                                                  t.
                                            # . #YG15
                                                        #, #YG1 %
         -Y612
                               # , #YG14
                                                                     tetYc17
                  #147G13
                                                                                  ±.
         -YGIA
                  # . #YG14
                               # . y YG2n
                                            1.
                                                           #YG21
                                                                     #+#YG22
                                                                                  t.
         -Y623
                  #++YG24
                               # . ±YG25
                                            ###YG26
                                                        エ・キャGクマ
                                                                     #1#YG28
                                                                                  ±.
         ~YG29
                  #+#YG30
                               # + + YG31
                                            #1#Y432
                                                        #1#Y633
                                                                     エノエソルス4
                                                                                  T.
                                            # + # YG39
                                                                     #1#Y640
        -YG35
                  ILLYG36
                               ###YG37
                                                        III IYG39
                                                                                  t.
                                            1.14G44
        + YG+1
                  # + #YG42
                               ##+YG43
                                                        I, IYGUK
                                                                     #1#Y046
                  # , # Y G 4 A
                               # , + YG4Q
                                            #. #YG50
                                                        t, tYG51
                                                                     #1#Y052
                                                                                  t.
        +YG47
         4Y653
                  #+#YG54
                               キャキYG5ら
                                            #, #YG56
                                                        ま, まYG57
                                                                     #1#Y058
                                                                                  £,
                                            # . # YE62
                                                                     ###YER4
         .YG59
                   I. FARREU
                               ###YGŐ1
                                                        111YG63
                                                                                  t.
                                                        t, tYGA9
                                                                     #1 #YG70
                               # . + YG67
                                            #1#Yasa
                                                                                  z.
                  #++YG66
         ~YGn5
         -Y671
                  I.FYG72
                               # . + YG73
                                            t. ±YG74
                                                         ###YG7K
                                                                     ###YG76
                                                                                  ±.
         -YG77
                  ホェムYは7段
                               キャエYGフロ
                                            ###YGRN
                                                        ###YGA1
                                                                     #1#YGRP
                                                                                  I.
                                                        ###YGA7
                                            I. IYAR6
                                                                     # # #YGAR
         ∡YGH3
                  # . FYG84
                               キャナYG35
                                                                                  t.
         4YGHQ
                  # + 4YG911
                                            #1#Y592
                                                         ###YGQ3
                                                                     11 #Y = 94
                                                                                  ‡ •
                               #1#YG91
                   1,44694
                                            # , # YG98
                                                         LILYGOD
                                                                     ###Ya100
         4Y695
                               エチェイクタフ
                                                                                  #1
 DATA
         · Y ( A . MA ) . MA=1 + 1 (10) / 4 Y H 1
                                           さいより付っ
                                                       # . # YH3
                                                                    よ。キY州ル
```

```
_Yhn
                   LIZY117
                               #+#YH3
                                            I + TYWO
                                                         #+#YHin
                                                                      ###Yu11
                                                                                  ‡. •
                  4.4Y=13
        -YH12
                               # , IYHI4
                                            #1#YH15
                                                         LIXYHIG
                                                                      エナギYu17
                                                                                  I.
        LYHIR
                  #, #YH10
                               エ・エイは2n
                                                           ‡YH21
                                                                      キナキャコクス
                                            10
                                                                                  Į.
                                            SSHYLLA
        --YH23
                   オナキギリンム
                               712YH23
                                                         土」ま丫Hつフ
                                                                      #1#YW28
                                                                                  #.
        TAH50
                  #1#YH31
                               ###YH31
                                            #1+TY432
                                                         エレナYH33
                                                                                  Į.
                                                                      #1#Y434
        +YH.55
                               #1+YH37
                  ILLYH3A
                                            112 Y 438
                                                         I . IYHZO
                                                                      # # # Y LL U
                                                                                  ±.
        47H41
                  #+#YH42
                               #1 ± YH43
                                            101Y444
                                                         エ・エYHムス
                                                                      # + #YIJUG
                                                                                  t.
        +YH47
                               #, #YH49
                                            ###Y#50
                   キャチャルり月
                                                         1+ 1YH51
                                                                      #+ #Y 1152
                                                                                  z.
        4YH53
                   £ . 4 Y H 5 4
                               ###YH55
                                            # 1 # Y H 56
                                                         t, tYHG7
                                                                      #1#Y458
                                                                                  t.
        ~YHDO
                   # . # Y HIGH
                               #++YH61
                                            20mY # 1 #
                                                         エ・エYHらス
                                                                      11 #YUR4
                                                                                  t.
        +YHOS
                  # + # Ymón
                               # . ± YH67
                                            LI ±Y=ióR
                                                         I. IYHAD
                                                                      ###YW70
                                                                                  t.
                                            1, ±Y474
        4YH71
                   1.1YH72
                               #++YH73
                                                         エ・エYHフ片
                                                                      Į,
        4YH77 --
                  4+4Y47A
                               #+±YH79
                                            #1#YUA0
                                                         ###YHA+
                                                                      #1#YU82
                                                                                  ±.
        →YHH3
                  # . IYHB4
                               #++YH85
                                            # . # YH86
                                                         LILYHAT
                                                                      ###YUAR
                                                                                  t.
        -YHHO
                  #, #Y49n
                               #, ±YH91
                                            #1 # Y 1492
                                                         # # #YHG3
                                                                      エナボアロ94
                                                                                  1.
        -YH45
                  #+#YH9K
                               # 1 # YH98
                                                         #1#YHGO
                                                                      #1#Y4100
                                                                                  11
DATA
        IIYIV(OUT + TEAM + (AM + P)
                                           #.#YI2
                                                        #.#Y13
                                                                     I, IYIn
                                                                                 Į,
*≠YI5
          7. .
        +YIn
                   1, #Y 17
                               #, ±YI8
                                            1, tYT9
                                                         ###YIIn
                                                                      1+ 1 Y 7 1 1
                                                                                   z.
        ~Y112
                   ###YT13
                               # . #Y114
                                            #, #YT15
                                                         # # # Y I 1 K
                                                                      エナキYナ17
                                                                                  #.
        AFIY.
                   # . #YT19
                               # + + Y 1211
                                            i.
                                                           #YI21
                                                                      #1#Y122
                                                                                   # .
        エYLンス
                   #1#Y124
                               # . tY 125
                                            ZIXYT26
                                                         キャよYIクフ

ナナ
ギ
ナナ
ナナ
アナク
8
                                                                                  t.
        41129
                   t. FYT30
                                            £1#YT32
                               ###YI31
                                                         ###Y133
                                                                      エナキャナ34
        -Y135
                   #14YT36
                               tetY137
                                            #+#Y139
                                                         #+#YI39
                                                                      #1#Y740
                                                                                  I.
        -Y 1 4 1
                  エ・エソエリン
                               ギョ 生YT4ス
                                            #+#YIUE
                                                                      #1#Y146
                                                                                  Į.
        +Y147
                   I. LYTHH
                               F, #YI49
                                            1. 1Y150
                                                         ###Y15+
                                                                      ホナキャナ52
                                                                                  Į.
        +Y153
                  #1#Y154
                               #, #Y155
                                            tetY155
                                                         ###YTE7
                                                                      ###Y+58
                                                                                  I.
        4Y159
                   ###YT611
                               # # #YTa1
                                            titYth2
                                                         tetY163
                                                                      to track
                                                                                  t.
        +Y165
                   #+#Y166
                               # + tY 167
                                            ###YTS8
                                                         # # #YTA9
                                                                      #1#Y170
                                                                                  Į.
        4Y171
                   キ・エYTフク
                               キャセY173
                                            ###YT74
                                                         ###YI75
                                                                      ** #YT76
        4Y177
                   4.4Y17A
                               1. ±Y179
                                            t. tYIRO
                                                         #, #YIA1
                                                                      ###YTA2
                                                                                  I.
        4Y 1 133
                   #+#YT84
                               # + tYIAS
                                            11 tYTRG
                                                         t+ #YIR7
                                                                      ###YYAR
                                                                                  t.
        +Y189
                  ###Y190
                               # . tY [91
                                            #+#Y192
                                                         I, IYIQz
                                                                      111Y+04
                                                                                  t.
        4Y145
                  #1#Y19h
                               I. tyla7
                                            t. #YTGR
                                                         t. tylaa
                                                                      #+#YT100
                                                                                  #1
DATA
        .Y(10,MA),MA=1,100)/±YJ1
                                            #, #Y.12
                                                         t, tYJR
                                                                      #1#Y.14
                                                                                  t.
*#YJ5
          7.
        4 Yuln
                  # . 4Y . 17
                               # . + Y.18
                                            # + # Y . 19
                                                         t+ #YJ1n
                                                                      # > # Y, 11 1
                                                                                  I.
        4YJ12
                  # . FY. 113
                               # + + Y J 14
                                            # , #Y.115
                                                         t, #YJ16
                                                                      #+#Y.117
                                                                                  z.
        ATUYA
                  # + #Y.ILQ
                               115UY++*
                                                                      #+#Y,122
                                            11
                                                           #YJ21
                                                                                  t.
        エYリンろ
                   #+#Y.124
                               キ・±YJ25
                                            # # # Y.126

ままま
ソ
リ
つ
フ
                                                                      #1#Y.128
                                                                                  t.
        ن مرل ۲ م
                  ###YJ38
                               #1#YU31
                                            #, #Y, 132
                                                         エノエY リスス
                                                                      #1#Y.134
                                                                                  Į,
                                            I+ £Y.138
        ~ YU.55
                  #12Y.136
                               1, +Y.137
                                                         #1#YJ30
                                                                      #+#Y,140
                                                                                  t.
        4YJ41
                   エ・チャ.142
                               キャナYJ43
                                            1. ±Y,144
                                                                      #1#Y 146
                                                         # + #YJU5
                                                                                  ±.
        4YJ47
                  # + # Y . 14 A
                               ≠,±YJ4a
                                            #, #Y.150
                                                         1,2VJ51
                                                                      #1#Y.152
        →YJ53
                  #+#Y.154
                               # . ± Y J55
                                            4, #Y. 156
                                                         エナキY JS7
                                                                      #+#Y 158
                                                                                  z.
        ...YU59
                  #+#YJI60
                               # + # Y J 61
                                            # # # 162
                                                         t, tYJKz
                                                                      #1#Y 164
                                                                                  t.
        aYUN5
                  #1 #YJBn
                               キャエY いろフ
                                            1+ ± Y. 158
                                                         PALYJAG
                                                                      ###Y.170
                                                                                  t.
        +YJ71
                  #+ 4Y.172
                               I. +Y.173
                                            # . #Y . 174
                                                         エノキソリフち
                                                                      ###Y.176
                                                                                  t.
        4.YJ77
                  #+#Y.17H
                               # , ± Y J 79
                                            ###Y.180
                                                         taLY# tt
                                                                      #+#Y.182
                                                                                  ±.
        4 Y U13 3
                  4+4Y.184
                               786YIII
                                            # . #Y.IRh
                                                         I, TYJA7
                                                                      #+#Y 188
                                                                                  ‡.
        +YJH9
                  #+#YJ190
                               #+ # Y J 91
                                            ## 2 Y . 192
                                                         I + #YJQz
                                                                      # 1 # Y 104
                                                                                  ±.
                   ±+44.196
        44.145
                               キ・エY 197
                                            # 1 4 Y 198
                                                         POLYTIT
                                                                      #+#Y 1100
```

:

- *** InPUT +- FINGS+ and OF CULTURES AND ROLS.
 READ (-- Sud) Indem1. COL. Roll
- *** INPUT THE TITLE OF YOUR PROBLEM.
 READ (#1501) TITLE
- *** WRITE AUT THE ALGORITHM#S MAME AND TITLE WRITE , 1,100) METHO(MI), VAOS(1), TITLE
- *** TEST WOFTHER THIS IS AN I.P. PROBLEM.
 IF IT -S AN I.P. PHOBLEM, READ THE INT. VARS AND WRITE TO TAPE 1.

 O.W. CANTINHE THE PROCESS.
 IF ((M. .+1.5) .UH. (M) .GT. 7)) GO TO S
 READ (-.503) NP.(ACT([1]).[1=1:N2)
 WRITE .1:701) VARS(2): (ACT([1]).[1=1:N2)
 S CONTINUE
- *** READ I.TO ALL OF THE ACTIVITIES READ (~.505) (ACTITA) IA=1.COL)
- **** REAU ILTO THE COEFFIFNTS OF OBJECT FUNCTION. ULTI
- 10 CONTINUE

 READ (-.50A) (ICUL(IR).SIGN(IB).COFF(IR).18=U1.U1.01.01

 LO 15 (C=U1.U1+4

 IF (ICUL(IC) .EG. -999) GO TO 20
- 15 CUNTINGF 01=U1+-00 TO .n
- *** NOOB 1- THE NO. OF NON-ZERO COFF. OF ORJECTIVE FUNCTION.

 20 CONTINUE
 NOOB = 10 1
- *** WRITE AUT THE COEF. OF OBJ. FUNCTION TO PERMENANT FILE (TADE 2) WRITE ,2,201) (Sign(TD),COFF(ID),ICOL(TD),10=1,NOn=)

```
*** TEST IN THERE IS NO ANY CONSTRAINT IN NON-ARBUMENTED
   CONSTRAINT MATRIX.
   IF (RU., .F.). (1) GO TO 43
*** READ 1.. TO THE CUFFFIFNTS OF CONSTRAINTS.
   32=1 % K1=0 %[Ev=0 -
25 CONTINUE
   10 50 -F=1,ROW
27 CUNTINGE
   READ (=.50A) (ICOL(IF):SIGN(IF):COFF(IF):IF=J2:J2:4)
   DO 30 -GEU2+U2+4
   IF (ICAI (16) .LT. 11) 60 TO 40
30 CONTINUE
   J2=J2+~
   60 TO -7
40 CONTINUE
*** TEST In THIS ROW CONTAINS ONLY ONE COEF. WITH #LF# RELATION.
   IF YES, THEN PUT IT IN TEMP. LAC.
   GTHERWISE CONTINUE THE PRUCESS.
   TP (16 .67. 2) HO TO 45
   16 (10a) (1a) .1 % -100 ) GO TO 45
   Kl=Kl+.
   TACT(K.) = ACT(ICOL(1))
   TT2(K1,=Stan(Ia)
   TT3(K1,=Coff(IG)/ChEf(1)
   60 TO 48
45 CONTINUE
*** NOCO CANTAINS THE MO. OF NON-ZERO COFF. OF CONSTRAINT.
   IEW=IE...+1
   NOCO(1-w) = IG - 1
*** WRITE JUT THE COEF. AND R.H.S. OF FACH COUSTRAINT.
   wRITE ,2,201) (SIGN(IH),CUFF(IH),ICON(IH),IH=1,MOCO(IEW))
   ISFL=1,OL(TG)/(-100)
   WRITE ,2,202) GEL(IGFL),SIGN(IG),COEF(IG)
   48 CONTINUE
   1251
50 CONTINUE
*** NOBD CANTAINS THE NO. OF HOULDS.
*** WOOD CANTAINS THE MO. OF CONSTRAINTS.
   NURD = R1 5 NOCU = ROW-NORD
```

```
43 CONTINE
*** TEST In These ARE SOME NEW ACTIVITIES WEED IN BE INSERTED INTO
    THE #U. D. HATRIX. (1810 = 99909)
    IF YES, THEN CALL SURROUTINE FINSERTAL
    OTHERWISE, CONTINUE THE NUMBAL PROCESS.
    LOOP = 1
    ITAPER = >
 44 CONTINUE
    READ ( ... SI1) ISTO
    IF (EU-(5) .NE. U.) GU TO 65
    IF (IS:0 - GF. 99999) 60 TU 52
    ILGOP = LUCP/2 #1100P=ILUOP+2 SITAPE1 = 2 FITAP=2 = 7
    IF (ILAOP .NE. LUOP) 60 TO 44
    ITAPE1 = 7 SITAPE2 = 2
 40 CONTINUE
    CALL THISFRE
    60 TO 1.4
 52 CONTINUE
*** TEST In THE PROBLEM NEEDS TO BE EXTENDED (CHECK EDE)
 54 CONTINUE
    JAEJA+.
    READ ( .. Sta) EIDARM . LOPV( IA)
    IF (EU-(5) .NE. U.) GU TO A5
    IF (Ab-(Ha) .LF. 10.**(-10)) GO TO 54
    ONE = AM
54 CONTINUE
*** TEST in This is an extention of Two DEP. VAR. FUNCTIONS
    IF YES THEN CALL GUAROUTINE FREPVA
    O.W. CANTIBUE THE PROCESS.
    WRITE ,3,507) FID.ONE
    if (10~V(un) .Fu. n) 60 To 55
    CALL SEPV
    60 TO 1.7
 SK CONTINUE
    IF (EIM .FO. 0) GO TO 56
    READ (A.SUA) (ICON (IT).SIGN(II).COFF(IT).TITT.ETD)
*** UPDATE THE COL. COORD. OF MON-ZERO COEF. IF COL. .ST. MINS.
    IF (IS.F .GF. 99990) 60 TO 46
    00 42 - T=1.FID
    IF (ICAL(IT) .G(. MINS) ICOL(IT)=ICOL(TT)+NAA
40 CONTINUE
 44 CONTTIALF
    WRITE ,3,201) (S160(II), COFF(II), ICOL(YI), IT=1,FIN)
 56 CONTINUE
```

- *** PROCESH THE EXTENDING PROJECURE.

 REAU INTO THE FORMULA

 READ (H.SUR) IU.(CC(TK).)EVP(IK).1K=1.1J)
- *** READ THE INITIAL VALUE OF OF DELTA O AND STEPS.
 READ (2.509) O(1).0ELTAR.STEP
- *** SET UP THE NEW ACTIVITIES.
- 57 CONTINUE DO 58 WA=1.5TEP ACT(KA.COL)=Y(JA.KA)
- SA CONTINUE
- *** CALL THE SHRKOHTINE GEN TO GENERATE THE VALUES OF A AND W. IF (IUHV(UA) -NE. A) GO TO 62 CALL BEN
- *** EXTENDING THE ORDECT FUNCTION:

 10=1

 10 60 P= COL+1: COL+STEP

 SIGN(1A)=WRIGN(1D)

 COFF(1A)=WRIGN(1D)

 10=10+:

 60 CONTINUE
 GO TO >4
- 62 CONTINUE

 10=1

 DU 63 P=COL+1.COL+STEP

 51GN(1..) = ±+#

 COFF(1..) = 0.0 «ICOL(IP) = COL+TO

 10 = 1.41

 63 CONTINUE
- *** STORE WHE VALUES OF ROW (COL) AND STEPS

 BY CONTINUE

 NROW(Ux)=ROW SNCOK(UA)=COL SNSTEP(JA)=STEP SNFID(UA)=EID
- *** EXTENU-NG THE CONSTRAINTS:

 IF (ID W(DA) -NF. n) GO TO 66

 WRITE ,3-500) (W(IT)-IT=1+\STEP(JA))

```
*** IPHATE THE VALUES OF COL AND ROW.
 On CUNITIVER
    COLECUI +STEP - ROW = ROW+2
    IF (106V(04) \cdot ME \cdot n) ROW = ROW+4
    GU 10 -3
 BE CONTINUE
    ひんこびんー,
*** SET UP THE VARIABLES.
    WRITE /1+103) VAKS(3)
     WRITE (1:504) (ACT(UN): UN=1:COL)
*** REVINU THE 3 PERMENANT FYLES (ITAPE2.TAPE3.TAPE4)
    REWIND ITAPF2
    REWIND 3 - -
                             REWINU 4
*** SET UP THE FINAL DRUFCT FUNCTION.
    IDM=Io..+a
    WRITE (1, 103) VARS(IDM)
    READ ( TAPE > 201) (SIGN(10) COFF(10) I TOL(10) ID=1 NOOB)
    weite(...in2) (SiSm(ID),COEF(ID),ACT(ICAL(ID)),ID=1,NOOR)
    IF (JA .FW. 11) GU TO BB
    WRITE /1:102) (SIGM(TD):COFF(ID):ACT(InOL(ID)):TD=NCOL(I)+::COL)
*** SET UP THE FINAL CONSTRAINTS.
 AR CONTINUE
    wRITE (1:183) VARS(6)
    DO 70 (C=1.NOCh
    READ (+TARE2+201) (SIGN(TH)+COFF(TH)+TODE(TH)+THE1.NOCO(UC1)
    wkITE(., 102) (SIGN(IH), COEF(IH), ACT(TCOL(TH)), IH=1, NOCO(UC))
    READ (.TAPES, 202) TITL, TITLS, TITS
    WRITE(...2012) TTT11.TTT2.TTT3
 70 CONTINUE
    IF (JA .FW. a) 60 TO 85
    IAW = ...COL (1)
    DO 80 K=1.JA
    READ /3/5/7/ FID/ONE
    IF (10 -V (UK) .FN. n) 60 TO 74
    DO 840 [3=1.FID]
    READ (3:511) IF (0:13)
    115 = .FID(13) + 1
    READ (... Sun) (1604 (I1), Stan([1), COFF([1), T]=1, [TE)
    willE /1, in2) (stool(11), COFF(I1), ACT(IcOL(I1)), I1=1, IEID(Ta))
```

```
ICT = -COL(TIE)/(-100)
    READ (4.590) (CS(AN(IR),C(IR),IR=1; )STEP(UK))
WHITE (1.102) (CSIAN(IR),C(IR),ACT(CO) (12)+TB
           11.1021 (CSIGN(IR), C(IR), ACT (CO) (UK)+18), TamingTEP(UK))
    WRITE (1,202) GEL((CT),SIGN([IF),COEF(TIE)
RUM CONTINUE
    00NE = 1.0
    WRITE (11.102) ((STGN: NONE: ACT (NCOL (UK)+1)): 12=1: MSTEP (UK))
    WRITE ,1.202) GFL(1). YSTG.I. ONE
    05 TO 20
 74 CUNTINGE
    IF (E1~ .FS. 0) SO TO 75
READ (...201) (SESN(II).COE=(II).ICOL(II).II=1.EID)
    SKITE(... 102) (STON(IT), COEF(II), ACT(ICOL(II)), IT=1.FID)
    KEAD /3/300) (WCIT), IT=1/MSTED(UKI)
    WRITE(...102)(XSIGN.Q(IT-NCOL(UK)) .ACT(II).II=NCOL(UK)+1.NCOL(UK)+
   *MSTEP( K))
    1 V=3
    IWW=145-FP(JK)/2 + 1 +IWW
    if (SI_N(IWW) .FW. #+#) GU TO 77
    1 v = 1
 77 CONTINUE
    INW = +WW+NSTEP(UK1/2-1
    WRITE(... 2012) GFL(IV), YSIGN, ZFRO
    wkITE(...102) (YS160,00F,ACT(II),II=NCO((UK)+1,NCO((UK)+NST&P(UK))
    WRITE (1.202) GEL(1).YSIGN.ONE
Bu CONTINUE
*** IF NOBA FWHAL TO HE THEN THERE IS NO BAUMO EXITS.
    ELSE PAINT OUT THE VERB #HOUND# AND SET UP THE ROUND SECTION.
 AS CONTINUE
    IF (NO.D .FO. D) GO TO 90
    WRITE (1+103) VARS(7)
    DU A8 UR=1.NOBD
    WRITE , 1, 104) TACT (KR), GFL (1), TT2 (KR), TT3 (KH)
 AR CONTINUE
 911 CONTINUE
*** PRINT AUT THE VERH FORTIMIZET.
    WRITE (1,103) VARS(9)
*** IF IT IS FOR MPOS-APEX. THEN PRINT #FNOAPEX# AND STOP
    FLSE SHOP.
    IF ((M. .WF. 11) .AND. (MI '.NE. 12)) STOP
    WRITE ,1,103) VAKS(10)
```

*** FURMATA.

```
FURNAL (ATHINALHINATA)
ũũ
     FORMAT (APRIZACAZIAX))
U I
     FURMAT (3(41,818.5.47))
U #
03
     FORMAT (ALD)
     FURMAL ( ... / . A | U . A | . F | n . 5)
04
UI
     FURMAL (StateFin.S.In))
     FURNAT (Almini,Fin.5)
UZ
00
     FURHAL (RE16.2)
     FORMAT (11,12,215)
00
     FORMAL (AAID)
U1
     FORMAT (FL., 2)
02
     FORMAL (13,11A7/(3x,11A7))
0.3
U4
     FURNAT (ALBXIA7))
     FORMAT (34.11A7)
05
     FURMAT (5(14.41.511.2))
06
     FORMAT (IN.F16.5)
07
0B
     FURMAT (15.5(F10.4.F5.0))
ü9
     FURMAL (2F10.4,15)
10
     FORMAT (15.F10.2:16)
11
     FURMAT (15)
99
     FURRAT (5(A1,F15.3))
     STOP
     END
     SUBROUGHTHE GEN
     INTEGER CULLINUW FITD STEP
     REAL MATHURTEXPIL
     COMMON /T111/w(1una).w(10un).Cc(10).jExP(10) + #SIGN(1000)
     COMMON /T112/OFLIAM: COL: ROW: FIM: STEP: I.J. IMM: M1: N2. WOOD : NOOR
 *** SET UP AMM CALCULATE THE FORMULA
     00 8 I. =1.STEP
     will)=~.0
     00 3 i =1.1J
   w(TE) = w(TE) + CC(TM)*O(TE)**tEXP(TM)*CONTINGE
     G(IL+1, =O(II)+OFLTAG
   A CONTINUE
 *** DEFINE THE SIGHS OF W.
     00 13 .N=1.STEP
     ">1011(N) #4+#
     IF (alan) .Gr. H.H GO TO 13
     ASIGN(+N)=1-4
  13 CONTINUE
     RETURGI
     END
```

SUAROUNTINE DEAV INTEGEN COH INOW IFTD. STEP REAL MOTHINIEXPIL CULMON /T1(1/Q(lunn).a(lunn).CC(lu), [ExP(10) .uSIay(lun0) COMMON /TITE/DELIAM, COL, ROW, FIG. STEP, I, J. IOM, MI.NZ. MOBD , MODA COMMUN /1113/TITLEF(8).GEL(3).ACT(1200).ICOL(1200).SIGN(1200). CUFF (1200) . METHO (10) . VaRS (26) COMMON /[118/kAij0(100).c(1000).L(1000).i)pv(50) COMMON /T119/IETh(100).CsIGN(1000).LsIGH(1000).nsIGN(1000) COMMON /Tipi/ISin.Naa.NBu.NING.AACT(2n).alCCL(2n).ASIGN(2n).ISIF. ACOFF(20) + 4EWROW(50) + AFWSIGN(50) + AEWCOFF(50) + AFWCOL (50) *** READ INTO THE NO. OF NON-ZERO COEF. OF EACH ROW DO 800 13=1.EID READ (-.507) IE13(13) READ (**506) (ICOL(II)*5168(II)*COFF(II)*II=1*IEIn(I3)*I) *** UPDATE THE COL. COORD. OF NON-ZERO COEF. IF COL. .GT. MINS. IF (IS:F .NF. 99999) 60 TO 701 66 700 11=1, IEID(14) IF (ICAL(II) .GF. MINS) ICDL(II)=ICOL(II)+NAA 700 CUNTINGE 701 CONTINUE *** WRITE AUT TO PERMENANT FILE (TAPE 3) WRITE (3:507) IF10(13) write (3.506) ((COL(11).SIGN(I1).COFF(T1).I1=1.7FT5(I3)+1) 8an CONTINUE *** READ 1.TO THE NO. OF RATIOS DESIRED (NOR) AND RATIOS (RATIO) READ (= +584) NOR+(RATIO(12)+12=1+NGR) *** READ 1..TO THE FORMILA. READ (-,585) AA, ALPHI, ALPHO AXX = AIPH1 + AIPH2

*** READ 15TO THE INITIAL VALUES OF O. DELTA A. AND STEPS. READ (2.504) 0(1).DELTAG.STEP

XXA = ./Xxx XXH = _ALPH1/Xxx

```
*** COMPUTA THE VALUES OF A. L. AND C.
     00 806 IS=1.NOR
     DU 805 INELISTEP
     III = +6+STEP*IS-STEP
     G(III+.) = G(III)+DELIAD
     L(III) = (\square(II_1) *** *XA) * (AA **(-XXA)) * (RATIO(IS) *** (XXB))
     C(III) = MATIO(15) *L(III)
 BUS CONTINGE
     G(111+.) = G(1)
 AUM CONTINUE
 *** DETERMINE THE STOILS OF ARRAYS J.C. AND L.
     NAR = ..OR*STEP
     DO 820 THE1.NRR
     GSIGN(+N) = #+#
    CSIGN(+N) = #+#
     LSIGN(+N) = #+#
     IF (0(+14) .SE. 0.) GO TO H16
     G(711) = #=#
 814 CONTINUE
     IF (C(VN) .GE. 0.) GO TO 817
     C(IN) _ #-#
 817 CUNTINGE
     IF (L(3H) .GE. H.) GO TO 818
     L(14) - 7-1
BIR CUNTINGE
- 820 CONTINUE
     STEP = NAK
 *** WRITE AUT TO PERMENAUT FILE (TAPE 4)
     ARITE (4.599) (CSIAN(18).C(IA).I8=1.NRq)
     wRITE ,4,500) (LSTEN(19),L(19),19=1,MRR)
```

WRITE , 4,549) (USIGN(11), 10(11), 11=1, NRR)

```
*** FURMATA.
     FORMAT (3(41) F16.5.471)
02
     FURMAT (ALII)
0.3
01
     FURMAT (5(A1)F18.5.14))
02
     FORMAT (ATH.A1.F16.5)
     FURMAT (34,1147)
05
     FORMAT (5(14, A1, F11.2))
liń
     FORMAI (15)
09
     FORMAT (2F18.4.15)
     FURMAT (13,11F7.2/(3x,11F7.2))
84
     FURMAT (3F10.2)
65
     FURMAL (5(41) F15.31)
     RETURN
     Eino
     SUBROU-INE INSERT
     INTEGER COLORON OF IDISTEP
     INTEGER
               ATCOL AFMCOL AENDON
     COMMON /T112/OFL (AG:CUL:RUW:FID:STEP.I.):InM:M1:N2:NOBD :NODB
     COMMON /T113/T1T(F(A).GEL(3).aCT(1200).IcoL(1200).SIGN(1200).
              COFF (1200) . MFTHD (15) . VARS (26)
             //115/NSTPP(50).NO/O(500).NROW(50).NCOL(50).NETD(50)
     COMMON
     COMMON
              /T120/x51gN,YSIGH,ZFRO,ONF,UA,UB,UC,NRR,TTAPF1,ITAPE2
     COMMON
              /T121/ISID:NAA.NBB.MINS.AACT(2a).aICOL(20).ASIGN(2a).ISIF.
              AUDFF (20) . AEWROW (50) . AFWSIGH (50) . AEWCOFF (50) . AFWCOL (50)
 *** READ INTO THE PLACEMENT OF HEW ACTIVITIES (NINS) IN
     OLD MARRIX, NAMES OF NEW ACTIVITIES (AACT). AND COFF.
     OF OBJECTIVE FUNCTION.
     ISIE = 99999
     READ (-,511) NINS
     REAU ( ... 503) NAA ( AACT ( IA) . IA=1 . NAA)
     READ (-, SOA) (ALCOL (TB), ASTGN(TB), ACOEF (IR), IB=1, NAA)
 *** READ INTO THE COEF. OF CONTRAINTS.
     READ (~, 511) NBB
     READ (2.512) (REWROW(IX) + AFWCOL(IX) + AEWSIGN(IX) + AFWCOEF(IX) + IX=
    *1 PMBB)
```

```
*** INSERT THE HEN ACTIVITIES INTO FOLD + OAD. FUCTION.
    00 30 01=1.CUL
    18 (NINS .HF. KI) GO TO 40
 30 CONTINE
 4n CONTINUE
   10 45 J2=1, CUL-NING
    KAD=CUL +NHA+1-K2
    KAFICU, +1-42
    ACT (KAK) = ACT (KAE)
 45 CONTINUE
    DO 47 62=1.NAA
    KAC=N1..5+K2
    ACT (KAA) =AACT (K2)
 47 CONTINGF
*** OPPLATE THE NO. OF ACTIVITIES.
    COL=CO, +NAA
*** READ 1..TO THE FULDE OBJECTIVE FUNCTION FROM TTAPE1.
    KEWINU ITAPFI
    READ (.TAPE1.201) (SIGN(ID).COFF(ID).ICOL(ID).ID=1.NOOR)
*** START TO INSERT THE NEW ACTIVITIES INTO THE OLD OR I. FUNC.
    00 50 JIEL NOOR
    IF (NILS .GF, ICOL(K1) .AND. NINS .LT. ICOL(K1+1)) 60 TO 5E
 SA CONTINUE
    60 TO 23
 55 CONTINUE
    00 60 JAR =1.8005-WINS
    kAD = ..00n + VAA + 1 + kAB
    KAE = ...000+1+KAH
    SIGN(KAD) = STUN(KAF)
    COEF (KAD) = COEF (KAF)
    ICOL (K.D) = 1 COL (KAF) + NAA
 BO CONTINUE
 63 CONTINUE
   00 65 02 = 1.NAA
    KAC = LINS + KA
    SIGN(KAC) = ASIGN(K2) - COFF(KAC) = ACOFF(K2) - ICOL(KAC) = ATCOL(K2)
 AS CUNTINGF
*** UPBATE THE NO. OF COFF. OF OBJ. FUNC. (MODA)
    AAM+NOON = BOOM
```

*** WRITE AUT THE ENEME ONJ. FUNC. TO ITAPES.

write(-lapes, 2011 (Ston(ID), COFF(LD), ICOL(LD), ID=1, NOOA)

```
*** DU THE INSERTION FOR CONSTRAINTS.
    NO BU FEEL RUN
     READ (Flame 1,201) (SIGN(Im), COFF(Im), ICOL(IM), IN=1, NOCO((F))
     READ ( TAPFI 1202) TTT1 1 TT ( 5 TT T3
 *** OPDATE THE COL. COORD. OF MON-ZERO COEF. IF COL. .ET. NINS.
    00 71 .1=1.NUCO(1F)
     IF (ICAL(II) +GT+ MINS) ICOL(II)=ICOL(II)+NAA
 71 CONTINUE
     00 70 -D#1.588
    1F (AE. ROW(10) .NF. 1E) GO TO 70
    110 67 F = 1 NOCO(TE)
    IF (AEUCOL(10) .9F. ICOL(1F) .4ND. AFWOOL(ID) .HT. ICOL(IF+1)) GO
    * TO 68
 67 CONTINEE
    60 TU -5
  BH CONTINUE
    DO 69 FG#1.MOCO(IF)-IF
     IN # NACOUFFIFIER
    SIGN(1..+1) = SIGN(TH)
     COFF(IN+1) = COEF(IH)
     ICOL(1..+1) = ICOL(TH)
  AU CONTINUE
  75 CONTINUE
     SIGN(1++1)=AFXSIGN(ID)
     COFF (I .. +1) #AEWCOFF (ID)
     ICOL(1-+1)=AFWCUL(10)
 *** UPDATE THE NO. OF COFF. OF CONSTRAINT.
    NOCO(I-) = NOCO(IE)+1
 -70 CUNTINGF
 *** WRITE BUT THE FINEWE CONSTRAINTS TO ITAGES.
     WRITE (ITAPE2:201) (SIGN(IH):COEF(IH):TCOL(TH):THE::NOCO(TE))
     WRITE ITTAPESIONS TTT1.TTZ.ITT3
 RA CONTINUE
 *** REWIND THE PERMENNAT FILE (ITAF2)
     REWIND ITAPES
 *** FURMATA.
01
     FORMAT (5(a1,Fin.S.I4))
     FORMAT (almalifia.5)
02
    FORMAT (13,1147/(3x,1147))
0.3
     FURMAT (5((4.A).F11.2))
     FURMAT (15)
11
     FURMAL (4(213, A1, F13.2))
12
     RETURN
     Figh
```