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Further development of flexible parametric models for survival analysis

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Abstract. Royston and Parmar (2002, *Statistics in Medicine* 21: 2175–2197) developed a class of flexible parametric survival models that were programmed in Stata with the `stpm` command (Royston, 2001, *Stata Journal* 1: 1–28). In this article, we introduce a new command, `stpm2`, that extends the methodology. New features for `stpm2` include improvement in the way time-dependent covariates are modeled, with these effects far less likely to be over parameterized; the ability to incorporate expected mortality and thus fit relative survival models; and a superior `predict` command that enables simple quantification of differences between any two covariate patterns through calculation of time-dependent hazard ratios, hazard differences, and survival differences. The ideas are illustrated through a study of breast cancer survival and incidence of hip fracture in prostate cancer patients.

Keywords: st0165, `stpm2`, survival analysis, relative survival, time-dependent effects

1 Introduction

The first article in the first volume of the *Stata Journal* presented the `stpm` command, which enabled the fitting of flexible parametric models (Royston and Parmar 2002), as an alternative to the Cox model (Royston 2001). A further command, `strsrcs`, extended the methods to incorporate expected mortality and thus fit relative survival models (Nelson et al. 2007). Here we present a new command, `stpm2`, that combines the standard and relative survival approaches, improves on the modeling of time-dependent effects, and has much improved postestimation commands. Also, `stpm2` is much faster than `stpm` (sometimes over 10 times as fast).

Briefly, the flexible parametric approach uses restricted cubic spline functions to model the baseline cumulative hazard, baseline cumulative odds of survival, or some more general baseline distribution in survival analysis models. These models enable proportional hazards, proportional-odds, and probit models to be fit but can be extended to model time-dependent effects on each of these scales. The advantages of this approach over the Cox model are the ease with which smooth predictions can be made, the modeling of complex time-dependent effects, investigation of absolute as well as relative effects, and the incorporation of expected mortality for relative survival models.

2 Methods

2.1 Flexible parametric models

A common parametric model for survival data is the Weibull model. The Weibull model is a proportional hazards model but is often criticized for lack of flexibility in the shape of the baseline hazard function, which is either monotonically increasing or decreasing. The survival function, $S(t)$, for a Weibull distribution is

$$S(t) = \exp(-\lambda t^\gamma)$$

If we transform to the log cumulative hazard scale, we get

$$\ln\{H(t)\} = \ln[-\ln\{S(t)\}] = \ln(\lambda) + \gamma \ln(t)$$

Thus, on the log cumulative hazard scale, we get a linear function of log time. If we add covariates, we have

$$\ln\{H(t | \mathbf{x}_i)\} = \ln(\lambda) + \gamma \ln(t) + \mathbf{x}_i \boldsymbol{\beta}$$

Thus the baseline log cumulative hazard function is $\ln(\lambda) + \gamma \ln(t)$, with covariates additive on this scale. This parameterization differs slightly from **streg**, where $\ln(\lambda)$ is incorporated as an intercept in $\mathbf{x}_i \boldsymbol{\beta}$ and $\ln(\gamma)$ is estimated as an ancillary parameter. The basic idea of the flexible parametric approach is to relax the assumption of linearity of log time by using restricted cubic splines.

So why do we model on this scale? First, under the proportional-hazards assumption, the covariates can still be interpreted as (log) hazard ratios because proportional hazards also imply proportional cumulative hazards. Second, the cumulative hazard as a function of log time is generally a stable function; for example, in all Weibull models, it is a straight line. It is easier to accurately capture the shape of more stable functions. Third, it is easy to transform to the survival and hazard functions.

$$S(t) = \exp\{-H(t)\} \quad h(t) = \frac{d}{dt} H(t)$$

The hazard and survival functions are needed to feed into the likelihood when estimating the model parameters.

The models we describe are parametric, and thus it is easy to obtain predictions. However, through the use of splines, they are more flexible than standard parametric models.

2.2 Restricted cubic splines

Splines are flexible mathematical functions defined by piecewise polynomials, with some constraints to ensure that the overall curve is smooth. The points at which the polynomials join are called knots. The fitted function is forced to have continuous 0th, 1st, and 2nd derivatives. The most common splines used in practice are cubic splines. Regression splines are useful because they can be incorporated into any regression model with a linear predictor.

`stpm2` uses restricted cubic splines (Durrleman and Simon 1989). These have the restriction that the fitted function is forced to be linear before the first knot and after the final knot. Restricted cubic splines with K knots can be fit by creating $K - 1$ derived variables. For knots k_1, \dots, k_K , a restricted cubic spline function can be written as

$$s(x) = \gamma_0 + \gamma_1 z_1 + \gamma_2 z_2 + \dots + \gamma_{K-1} z_{K-1}$$

The derived variables, z_j (also known as the basis functions), are calculated as follows:

$$\begin{aligned} z_1 &= x \\ z_j &= (x - k_j)_+^3 - \phi_j(x - k_1)_+^3 - (1 - \phi_j)(x - k_K)_+^3 \quad j = 2, \dots, K - 1 \end{aligned}$$

where $\phi_j = (k_K - k_j)/(k_K - k_1)$.

The derived variables can be highly correlated, and by default, `stpm2` orthogonalizes the derived splines variables by using Gram–Schmidt orthogonalization.

2.3 Flexible parametric models: Incorporating splines

Because the models are on the log cumulative hazard scale, we can write a proportional hazards model

$$\ln\{H(t | \mathbf{x}_i)\} = \ln\{H_0(t)\} + \mathbf{x}_i \boldsymbol{\beta}$$

A restricted cubic spline function of $\ln(t)$, with knots \mathbf{k}_0 , can be written as $s\{\ln(t) | \boldsymbol{\gamma}, \mathbf{k}_0\}$. This is then used for the baseline log cumulative hazard in a proportional (cumulative) hazards model:

$$\ln\{H(t | \mathbf{x}_i)\} = \eta_i = s\{\ln(t) | \boldsymbol{\gamma}, \mathbf{k}_0\} + \mathbf{x}_i \boldsymbol{\beta} \quad (1)$$

For example, with four knots, we can write

$$\ln\{H(t | \mathbf{x}_i)\} = \eta_i = \gamma_0 + \gamma_1 z_{1i} + \gamma_2 z_{2i} + \gamma_3 z_{3i} + \mathbf{x}_i \boldsymbol{\beta}$$

We can transform to the survival and hazard scales:

$$S(t | \mathbf{x}_i) = \exp\{-\exp(\eta_i)\} \quad h(t | \mathbf{x}_i) = \frac{ds\{\ln(t) | \boldsymbol{\gamma}, \mathbf{k}_0\}}{dt} \exp(\eta_i)$$

The hazard function involves the derivatives of the restricted cubic splines functions. However, these are easy to calculate:

$$s'(x) = \gamma_1 z'_1 + \gamma_2 z'_2 + \dots + \gamma_{K-1} z'_{K-1}$$

where

$$\begin{aligned} z'_1 &= 1 \\ z'_j &= 3(x - k_j)_+^2 - 3\phi_j(x - k_{k_1})_+^2 - 3(1 - \phi_j)(x - k_{k_k})_+^2 \end{aligned}$$

When choosing the location of the knots for the restricted cubic splines, it is useful to have some sensible default locations. In `stpm2`, the default knot locations are at the centiles of the distribution of uncensored log event times as shown in table 1.

| Knots | Degrees of freedom (df) | Centiles |
|-------|-------------------------|--|
| 1 | 2 | 50 |
| 2 | 3 | 33, 67 |
| 3 | 4 | 25, 50, 75 |
| 4 | 5 | 20, 40, 60, 80 |
| 5 | 6 | 17, 33, 50, 67, 83 |
| 6 | 7 | 14, 29, 43, 57, 71, 86 |
| 7 | 8 | 12.5, 25, 37.5, 50, 62.5, 75, 87.5 |
| 8 | 9 | 11.1, 22.2, 33.3, 44.4, 55.6, 66.7, 77.8, 88.9 |
| 9 | 10 | 10, 20, 30, 40, 50, 60, 70, 80, 90 |

Table 1. Default positions of internal knots for modeling the baseline distribution function and time-dependent effects in flexible parametric survival models. Knots are positions on the distribution of uncensored log event times.

2.4 Likelihood

The contribution to the log likelihood for the i th individual for a flexible parametric model on the log cumulative hazard scale can be written as

$$\ln L_i = d_i (\ln [s' \{\ln(t_i) \mid \gamma, \mathbf{k}_0\}] + \eta_i) - \exp(\eta_i)$$

where d_i is the event indicator. The likelihood can be maximized (using a few tricks) with Stata's optimizer, `ml`. The main trick is to define an additional equation for the derivatives of the spline function and constrain the parameters to be equal to the equivalent spline functions in the main linear predictor. This is how the implementation of `stpm2` differs from `stpm`. In `stpm`, there was a separate `ml` equation for each spline parameter. Two advantages of `stpm2` are the increased speed and the fact that more parsimonious modeling of time-dependent effects can be performed.

2.5 Extending to time-dependent effects

One of the main advantages of the flexible parametric approach is the ease with which time-dependent effects can be fit. In the proportional (cumulative) hazards model in (1), the baseline log cumulative hazard is modeled using restricted cubic splines. To

make effects time dependent, we can just form interactions with the spline terms and the covariates of interest. In `stpm`, any time-dependent effects had to have the same number of knots at the same locations as the baseline effect. This tended to over-parameterize the time-dependent effects because, generally, the underlying shape of the baseline hazard is more complex than any departures from it. Thus, in `stpm2`, time-dependent effects are allowed to have fewer knots and have these knots at different locations than for the baseline effect. If there are D time-dependent effects, then we can write

$$\ln \{H_i(t | \mathbf{x}_i)\} = s \{\ln(t) | \boldsymbol{\gamma}, \mathbf{k}_0\} + \sum_{j=1}^D s \{\ln(t) | \boldsymbol{\delta}_k, \mathbf{k}_j\} x_{ij} + \mathbf{x}_i \boldsymbol{\beta}$$

The default knot locations for a specified number of degrees of freedom (df) are the same as those listed for the baseline hazard in table 1. The number of spline variables for a particular time-dependent effect will depend on the number of knots, \mathbf{k}_j . For each time-dependent effect, there is an interaction between the covariate and the spline variables. The model is allowing for nonproportional cumulative hazards, and there will be a bit of work to convert this to the hazard-ratio scale.

2.6 Hazard ratios

The most common method of summarizing differences between two groups is the hazard ratio. When the hazard ratio becomes a function of time, it is generally best to plot it, with 95% confidence intervals, as a function of time. Because the models described so far are on the (log) cumulative hazard scale and we want to quantify difference on the (log) hazard scale, we have to perform a nonlinear transformation of the model parameters.

Consider a model with one dichotomous covariate, x_1 , taking on the values 1 and 0 and that has a time-dependent effect. The log hazard-ratio comparing $x_1 = 1$ with $x_1 = 0$ at time t_0 can be written as

$$\begin{aligned} \ln(\text{HR}) = & \ln [s' \{\ln(t_0) | \boldsymbol{\gamma}, \mathbf{k}_0\} + s' \{\ln(t_0) | \boldsymbol{\delta}_1, \mathbf{k}_1\}] - \ln [s' \{\ln(t_0) | \boldsymbol{\delta}_1, \mathbf{k}_1\}] \\ & + s \{\ln(t_0) | \boldsymbol{\delta}_1, \mathbf{k}_1\} + \beta_1 \end{aligned}$$

Because this is a nonlinear function of the parameters, the standard error (and thus the confidence interval) of the log hazard-ratio at time t_0 is obtained with the delta method by using the Stata `predictnl` command, where the derivatives are calculated numerically. This is a further enhancement over `stpm`.

2.7 Other predictions

`stpm2` also enables other useful predictions for quantifying differences between groups. The first of these is the difference in hazard rates between any two covariate patterns. The second is the difference in survival curves between any two covariate patterns.

Confidence intervals are obtained by applying the delta method by using `predictnl`. It is also possible to calculate and compare centiles of the survival distribution. This involves an iterative process using the Newton–Raphson algorithm.

2.8 Delayed entry

`stpm2`, like most Stata `st` commands, can incorporate delayed entry. This means that some subjects become at risk at some time after time $t = 0$. This is also known as left-truncation. A common example in epidemiology is when age is used as the time scale, so subjects become at risk at the age they were diagnosed with the disease under study (Cheung, Gao, and Khoo 2003). A further example, used in relative survival models, is when using period analysis where up-to-date estimates of survival are obtained by artificially left-truncating the time scale so that only the most recent data are used to estimate survival (Brenner and Gefeller 1997). Delayed entry is also needed when incorporating time-dependent covariates or piecewise time-dependent effects similarly to the Cox model (Cleves et al. 2008).

2.9 Modeling on other scales

Royston and Parmar (2002) discuss the use of models on other scales. These include flexible proportional-odds models, probit models, and a more general model that involves transformation of the survival function based on a suggestion by Aranda-Ordaz (1981). All these models are available in `stpm2`.

2.10 Relative survival

Relative survival is a common method used in population-based cancer studies. In these studies, mortality associated with the cancer under study is of the most interest. However, cause of death information is often not available or is otherwise considered to be unreliable. Therefore, mortality associated with the disease of interest is estimated by incorporating expected (or background) mortality, which can usually be obtained from national or regional life tables. In relative survival, the all-cause survival function, $S(t)$, can be expressed as the product of the expected survival function, $S^*(t)$, and the relative survival function, $R(t)$:

$$S(t) = S^*(t)R(t)$$

Transforming to the hazard scale gives

$$h(t) = h^*(t) + \lambda_d(t)$$

where $h(t)$ is the all-cause hazard (mortality) rate, $h^*(t)$ is the expected hazard (mortality) rate, and $\lambda_d(t)$ is the excess hazard (mortality) rate associated with the disease of interest. Thus the mortality rate is the sum of two components: the background mortality rate and the excess mortality rate associated with the disease. The flexible

parametric modeling approach was extended to relative survival and implemented in the `strsrcs` command available from the Statistical Software Components archive.

All the models and postestimation features described so far can be extended to relative survival. This means adapting the likelihood function. The general likelihood function for a relative survival model can be written as

$$\ln L_i = d_i \ln\{h^*(t_i) + \lambda_d(t_i)\} + \ln\{S^*(t_i)\} + \ln\{R(t_i)\}$$

$S^*(t_i)$ does not depend on the model parameters and can be excluded from the likelihood. This means that to fit these models, the user needs to merge in the expected mortality rate, $h^*(t_i)$, at time of death, t_i . This is important because many of the other models for relative survival involve fine splitting of the time scale or numerical integration (Lambert et al. 2005; Remontet et al. 2007). With large datasets, this can be computationally intensive. The relative survival models fit using `stpm2` are much quicker to fit than some of the standard models.

3 stpm2

3.1 Syntax

```
stpm2 [varlist] [if] [in], scale(scalename) [df(#) knots(numlist)
      tvc(varlist) dftvc(df_list) knotstvc(numlist) knscale(scale)
      bknots(knotslist) noorthog bhazard(varname) noconstant stratify(varlist)
      theta(est|) alleq eform keepcons level(#) showcons constheta(#)
      initttheta(#) lininit maximize_options]
```

You must `stset` your data before using `stpm2`; see [ST] `stset`.

3.2 Options

Model

`scale(scalename)` specifies on which scale the survival model is to be fit.

`scale(hazard)` fits a model on the log cumulative hazard scale, i.e., the scale of $\ln[-\ln\{S(t)\}]$. If no time-dependent effects are specified, the resulting model has proportional hazards.

`scale(odds)` fits a model on the log cumulative odds scale, i.e., $\ln[\{1 - S(t)\}/S(t)]$. If no time-dependent effects are specified, then this is a proportional-odds model.

`scale(normal)` fits a model on the normal equivalent deviate scale, i.e., a probit link for the survival function $\text{invnorm}\{1 - S(t)\}$.

`scale(theta)` fits a model on a scale defined by the value of θ for the Aranda-Ordaz family of link functions, i.e., $\ln[\{S(t)^{(-\theta)} - 1\}/\theta]$. $\theta = 1$ corresponds to a proportional-odds model, and $\theta = 0$ corresponds to a proportional cumulative-hazard model.

`df(#)` specifies the df for the restricted cubic spline function used for the baseline hazard rate. `#` must be between 1 and 10, but a value between 1 and 5 is usually sufficient. The knots are placed at the centiles of the distribution of the uncensored log times as shown in table 1. Using `df(1)` is equivalent to fitting a Weibull model when using `scale(hazard)`.

`knots(numlist)` specifies knot locations for the baseline distribution function, as opposed to the default locations set by `df()`. The locations of the knots are placed on the scale defined by `knscale()`. However, the scale used by the restricted cubic spline function is always log time. Default knot positions are determined by the `df()` option.

`tvvc(varlist)` specifies the names of the variables that are time dependent. Time-dependent effects are fit using restricted cubic splines. The df is specified using the `dftvc()` option.

`dftvc(df_list)` specifies the df for time-dependent effects. The potential df is between 1 and 10. With 1 degree of freedom, a linear effect of log time is fit. If there is more than one time-dependent effect and a different df is required for each time-dependent effect, then the following syntax can be used: `dftvc(x1:3 x2:2 1)`, where `x1` has 3 df, `x2` has 2 df, and any remaining time-dependent effects have 1 df.

`knotstvc(numlist)` specifies the location of the internal knots for any time-dependent effects. If different knots are required for different time-dependent effects, then this option can be specified as follows: `knotstvc(x1 1 2 3 x2 1.5 3.5)`.

`knscale(scale)` sets the scale on which user-defined knots are specified. `knscale(time)` denotes the original time scale, `knscale(log)` denotes the log time scale, and `knscale(centile)` specifies that the knots are taken to be centile positions in the distribution of the uncensored log survival times. The default is `knscale(time)`.

`bknots(knotslist)` is a two-element list giving the boundary knots. By default, these are located at the minimum and maximum of the uncensored survival times. They are specified on the scale defined by `knscale()`.

`noorthog` suppresses orthogonal transformation of spline variables.

`bhazard(varname)` is used when fitting relative survival models. `varname` gives the expected mortality rate at the time of death or censoring. `stpm2` gives an error message when there are missing values of `varname`, because this usually indicates that an error has occurred when merging the expected mortality rates.

`noconstant`; see [R] **estimation options**.

`stratify(varlist)` is provided for backward compatibility with `stpm`. Members of *varlist* are modeled with time-dependent effects. See the `tvvc()` and `dftvc()` options for `stpm2`'s way of specifying time-dependent effects.

`theta(est| #)` is provided for backward compatibility with `stpm`. `est` requests that θ be estimated, whereas `#` fixes θ to `#`. See `constheta()` and `inittheta()` for `stpm2`'s way of specifying θ .

Reporting

`alleq` reports all equations used by `m1`. The models are fit using various constraints for parameters associated with the derivatives of the spline functions. These parameters are generally not of interest and thus are not shown by default. Also, an extra equation is used when fitting delayed-entry models; again, this is not shown by default.

`eform` reports the exponentiated coefficients. For models on the log cumulative-hazard scale, `scale(hazard)`, this gives hazard ratios if the covariate is not time dependent. Similarly, for models on the log cumulative-odds scale, `scale(odds)`, this option will give odds ratios for non-time-dependent effects.

`keepcons` prevents the constraints imposed by `stpm2` on the derivatives of the spline function when fitting delayed-entry models from being dropped. By default, the constraints are dropped.

`level(#)` specifies the confidence level, as a percentage, for confidence intervals. The default is `level(95)` or as set by `set level`.

`showcons` lists in the output the constraints used by `stpm2` for the derivatives of the spline function and when fitting delayed-entry models; the default is to not list them.

Max options

`constheta(#)` constrains the value of θ ; i.e., it is treated as a known constant.

`inittheta(#)` specifies an initial value for θ in the Aranda-Ordaz family of link functions.

`lininit` obtains initial values by fitting only the first spline basis function (i.e., a linear function of log survival time). This option is seldom needed.

maximize_options: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `shownrtolerance`, `tolerance(#)`, `ltolerance(#)`, `gtolerance(#)`, `nrtolerance(#)`, `nonnrtolerance`, `from(init_specs)`; see [R] **maximize**. These options are seldom used, but `difficult` may be useful if there are convergence problems when fitting models that use the Aranda-Ordaz family of link functions.

4 stpm2 postestimation

stpm2 is an estimation command and thus shares most of the features of Stata estimation commands; see [U] **20 Estimation and postestimation commands**. The range of predictions available postestimation when using **stpm2** has been much extended compared with the range available for **stpm**. The predictions available are briefly described below.

4.1 Syntax

```
predict newvar [if] [in] [, at(varname # [varname # ...])
    centile(#|varname) ci cumhazard cumodds density hazard
    hdiff1(varname # [varname # ...]) hdiff2(varname # [varname #
    ...]) hrdenominator(varname # [varname # ...]) hrnumerator(varname
    # [varname # ...]) martingale meansurv normal sdiff1(varname #
    [varname # ...]) sdiff2(varname # [varname # ...]) stdp survival
    timevar(varname) xb xbnobaseline zeros centol(#) deviance dxb
    level(#)]
```

4.2 Options

Main

at(varname # [varname # ...]) requests that the covariates specified by *varname* be set to #. This is a useful way to obtain out-of-sample predictions. If **at()** is used together with **zeros**, then all covariates not listed in **at()** are set to zero. If **at()** is used without **zeros**, then all covariates not listed in **at()** are set to their sample values.

centile(#|varname) requests the #th centile of survival-time distribution, calculated using the Newton–Raphson algorithm (or requests the centiles stored in *varname*).

ci calculates a confidence interval for the requested statistic and stores the confidence limits in *newvar_lci* and *newvar_uci*.

cumhazard predicts the cumulative hazard function.

cumodds predicts the cumulative odds-of-failure function.

density predicts the density function.

hazard predicts the hazard rate (or excess hazard rate if **stpm2**'s **bhazard()** option was used).

hdiff1(*varname* # [*varname* # ...]) and **hdiff2**(*varname* # [*varname* # ...]) predict the difference in hazard functions, with the first hazard function defined by the covariate values listed for **hdiff1**() and the second, by those listed for **hdiff2**(). By default, covariates not specified using either option are set to zero. Setting the remaining values of the covariates to zero may not always be sensible. If # is set to missing (.), then *varname* has the values defined in the dataset.

Example: **hdiff1**(**hormon** 1) (without specifying **hdiff2**()) computes the difference in predicted hazard functions at **hormon** = 1 compared with **hormon** = 0.

Example: **hdiff1**(**hormon** 2) **hdiff2**(**hormon** 1) computes the difference in predicted hazard functions at **hormon** = 2 compared with **hormon** = 1.

Example: **hdiff1**(**hormon** 2 **age** 50) **hdiff2**(**hormon** 1 **age** 30) computes the difference in predicted hazard functions at **hormon** = 2 and **age** = 50 compared with **hormon** = 1 and **age** = 30.

hrdenominator(*varname* # [*varname* # ...]) specifies the denominator of the hazard ratio. By default, all covariates not specified using this option are set to zero. See the cautionary note in **hrnumerator**() below. If # is set to missing (.), then the covariate has the values defined in the dataset.

hrnumerator(*varname* # [*varname* # ...]) specifies the numerator of the (time-dependent) hazard ratio. By default, all covariates not specified using this option are set to zero. Setting the remaining values of the covariates to zero may not always be sensible, particularly on models other than those on the cumulative hazard scale or when more than one variable has a time-dependent effect. If # is set to missing (.), then the covariate has the values defined in the dataset.

martingale calculates martingale residuals.

meansurv calculates the population-averaged survival curve. This differs from the predicted survival curve at the mean of all the covariates in the model. A predicted survival curve is obtained for each subject, and all the survival curves in a population are averaged. The process can be computationally intensive. It is recommended that the **timevar**() option be used to reduce the number of survival times at which the survival curves are averaged. Combining **meansurv** with the **at**() option enables adjusted survival curves to be estimated.

normal predicts the standard normal deviate of the survival function.

sdiff1(*varname* # [*varname* # ...]) and **sdiff2**(*varname* # [*varname* # ...]) predict the difference in survival curves, with the first survival curve defined by the covariate values listed for **sdiff1**() and the second, by those listed for **sdiff2**(). By default, covariates not specified using either option are set to zero. Setting the remaining values of the covariates to zero may not always be sensible. If # is set to missing (.), then *varname* has the values defined in the dataset.

Example: **sdiff1**(**hormon** 1) (without specifying **sdiff2**()) computes the difference in predicted survival curves at **hormon** = 1 compared with **hormon** = 0.

Example: `sdiff1(hormon 2) sdiff2(hormon 1)` computes the difference in predicted survival curves at `hormon = 2` compared with `hormon = 1`.

Example: `sdiff1(hormon 2 age 50) sdiff2(hormon 1 age 30)` computes the difference in predicted survival curves at `hormon = 2` and `age = 50` compared with `hormon = 1` and `age = 30`.

`stdp` calculates the standard error of prediction and stores it in `newvar_se`. `stdp` is available only with the `xb` and `dx` options.

`survival` predicts survival time (or relative survival if the `bhazard()` option was used).

`timevar(varname)` defines the variable used as time in the predictions. The default is `timevar(_t)`. This is useful for large datasets where, for plotting purposes, predictions are needed for only 200 observations, for example. Some caution should be taken when using this option because predictions may be made at whatever covariate values are in the first 200 rows of data. This can be avoided by using the `at()` option or the `zeros` option to define the covariate patterns for which you require the predictions.

`xb` predicts the linear predictor, including the spline function.

`xnobaseline` predicts the linear predictor, excluding the spline function, i.e., only the time-fixed part of the model.

`zeros` sets all covariates to zero (baseline prediction). For example, `predict s0, survival zeros` calculates the baseline survival function.

Subsidiary

`centol(#)` defines the tolerance when searching for the predicted survival time at a given centile of the survival distribution. The default is `centol(0.0001)`.

`deviance` calculates deviance residuals.

`dx` calculates the derivative of the linear predictor.

`level(#)` specifies the confidence level, as a percentage, for confidence intervals. The default is `level(95)` or as set by `set level`.

5 Examples

For the initial models, we use data from the public-use dataset of all England and Wales cancer registrations between 1 January 1971 and 31 December 1990 with follow-up to 31 December 1995 (Coleman et al. 1999). Covariates of interest include the effect of deprivation—defined in terms of the area-based Carstairs score (Coleman et al. 1999)—age, and calendar period of diagnosis. There are five deprivation groups ranging from the least deprived (most affluent) to the most deprived quintile in the population. For the initial analysis, we will concentrate on women aged under 50 at diagnosis, who were diagnosed with breast cancer between 1986 and 1990, and we will compare the five deprivation groups. Follow-up is restricted to 5 years after diagnosis. All-cause mortality is the outcome, although given their age, most of the women who die will die from the cancer. There are 24,889 women included in the analysis.

5.1 Proportional hazards models

A Cox proportional hazards model comparing the effect of deprivation group (with the most affluent group as the baseline) is shown below:

```
. stcox dep2-dep5, noshow nolog
Cox regression -- Breslow method for ties
No. of subjects =      24889      Number of obs   =      24889
No. of failures =       7366
Time at risk    =   104638.953
Log likelihood   =   -73302.997      LR chi2(4)      =      62.19
                                      Prob > chi2     =      0.0000
```

| _t | Haz. Ratio | Std. Err. | z | P> z | [95% Conf. Interval] | |
|------|------------|-----------|------|-------|----------------------|----------|
| dep2 | 1.048716 | .0353999 | 1.41 | 0.159 | .9815786 | 1.120445 |
| dep3 | 1.10618 | .0383344 | 2.91 | 0.004 | 1.03354 | 1.183924 |
| dep4 | 1.212892 | .0437501 | 5.35 | 0.000 | 1.130104 | 1.301744 |
| dep5 | 1.309478 | .0513313 | 6.88 | 0.000 | 1.212638 | 1.414051 |

The hazard ratios for the deprivation group indicate that the mortality rate increases with increasing deprivation group, with the most deprived group having a mortality rate 31% higher than the most affluent group.

A flexible parametric proportional-hazards model is also fit and shown below:

(Continued on next page)

```
. stpm2 dep2-dep5, df(5) scale(hazard) eform nolog
```

```
Log likelihood = -22502.633          Number of obs   =       24889
```

| | exp(b) | Std. Err. | z | P> z | [95% Conf. Interval] | |
|-------|----------|-----------|-------|-------|----------------------|----------|
| xb | | | | | | |
| dep2 | 1.048752 | .0354011 | 1.41 | 0.158 | .9816125 | 1.120483 |
| dep3 | 1.10615 | .0383334 | 2.91 | 0.004 | 1.033513 | 1.183893 |
| dep4 | 1.212872 | .0437493 | 5.35 | 0.000 | 1.130085 | 1.301722 |
| dep5 | 1.309479 | .0513313 | 6.88 | 0.000 | 1.212639 | 1.414052 |
| _rcs1 | 2.126897 | .0203615 | 78.83 | 0.000 | 2.087361 | 2.167182 |
| _rcs2 | .9812977 | .0074041 | -2.50 | 0.012 | .9668927 | .9959173 |
| _rcs3 | 1.057255 | .0043746 | 13.46 | 0.000 | 1.048715 | 1.065863 |
| _rcs4 | 1.005372 | .0020877 | 2.58 | 0.010 | 1.001288 | 1.009472 |
| _rcs5 | 1.002216 | .0010203 | 2.17 | 0.030 | 1.000218 | 1.004218 |

The `df(5)` option implies using 5 df (4 internal knots) at their default locations. The `scale(hazard)` option states that the model is being fit on the log cumulative hazard scale. The estimated hazard ratios and their 95% confidence intervals are very similar to the Cox model, and in fact, there is no difference up to four decimal places. We have yet to find an example of a proportional hazards model where there is a large difference in the estimated hazard ratios between these two models.

The advantage of using the parametric approach is the ease of obtaining predictions. The following code obtains the predictions for the linear predictor, the survival function, and the hazard function. Confidence intervals can be obtained by adding the `ci` option.

```

predict xb, xb
predict s, survival
predict h, hazard

```

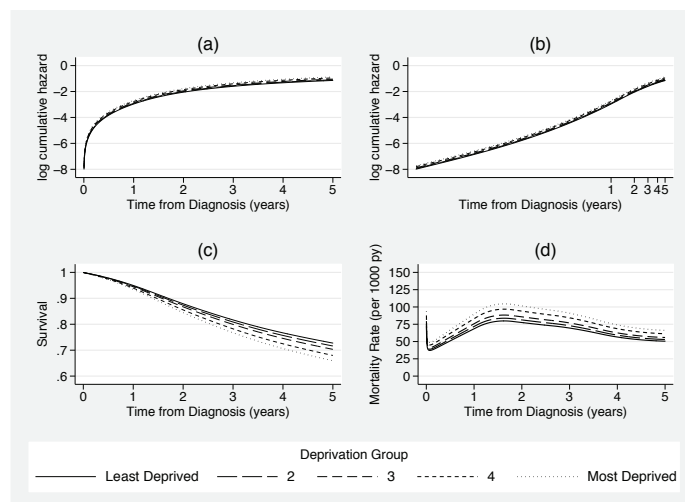


Figure 1. Predictions from proportional hazards model for breast cancer data

Figure 1(a) shows the predicted log cumulative hazard function. This is the scale we are modeling on. Figure 1(b) also shows the predicted log cumulative hazard function, but now it is plotted against log time. This shows the reason why the splines are a function of log time; the curve is generally much more stable on this scale. Figure 1(c) shows the predicted survival curves for the five deprivation groups. This shows that survival is worse as deprivation increases. Finally, figure 1(d) shows the predicted hazard function. The hazard function has been multiplied by 1,000 to give the mortality rate per 1,000 person-years. There is an initial sharp decrease in the hazard rate, followed by an increase until about 1.5 years. Because these fitted values come from a proportional hazards model, these lines are all proportional.

5.2 Time-dependent effects

One option to fit time-dependent hazard ratios is to use `stsplit` to split the time scale and fit piecewise hazard ratios. See [Cleves et al. \(2008\)](#) for examples of how to do this for a Cox model. However, we will concentrate on continuous time-dependent effects using restricted cubic splines.

For simplicity, we have dropped the three middle deprivation groups and are just comparing the most deprived group with the most affluent group. The following code allows the effect of deprivation group 5 (`dep5`) to be time dependent:


```
. stpm2 dep5, df(5) scale(hazard) tvc(dep5) dftvc(3) nolog
```

Log likelihood = -8751.407 Number of obs = 9721

| | Coef. | Std. Err. | z | P> z | [95% Conf. Interval] | |
|------------|-----------|-----------|--------|-------|----------------------|-----------|
| xb | | | | | | |
| dep5 | .3002046 | .0400425 | 7.50 | 0.000 | .2217228 | .3786865 |
| _rcs1 | .7910193 | .0208548 | 37.93 | 0.000 | .7501446 | .8318939 |
| _rcs2 | -.030325 | .0163107 | -1.86 | 0.063 | -.0622933 | .0016433 |
| _rcs3 | .0533712 | .0076102 | 7.01 | 0.000 | .0384555 | .068287 |
| _rcs4 | .0074654 | .00348 | 2.15 | 0.032 | .0006448 | .014286 |
| _rcs5 | -.00016 | .0016231 | -0.10 | 0.921 | -.0033412 | .0030212 |
| _rcs_dep51 | -.0970786 | .0306738 | -3.16 | 0.002 | -.1571981 | -.0369591 |
| _rcs_dep52 | .0196886 | .0230924 | 0.85 | 0.394 | -.0255717 | .064949 |
| _rcs_dep53 | .0012426 | .0098037 | 0.13 | 0.899 | -.0179723 | .0204574 |
| _cons | -1.480394 | .0240537 | -61.55 | 0.000 | -1.527539 | -1.43325 |

The `tvc(dep5)` option states that the `dep5` variable is to be time dependent. The `dftvc(3)` option requests that the time dependence be modeled using restricted cubic splines with 2 internal knots. The baseline is still being modeled using 5 df. Thus there are five derived spline variables for the baseline log cumulative hazard (`_rcs1`–`_rcs5`) and three derived spline variables for the time-dependent effect of `dep5` (`_rcs_dep51`–`_rcs_dep53`).

Figure 2 shows the estimated hazard rates for the two deprivation groups from this model together with the estimated hazard rates from a proportional hazards model. This clearly shows that the hazard rates become closer over time and that the time-dependent effects are noticeably different from those from the proportional hazards model.

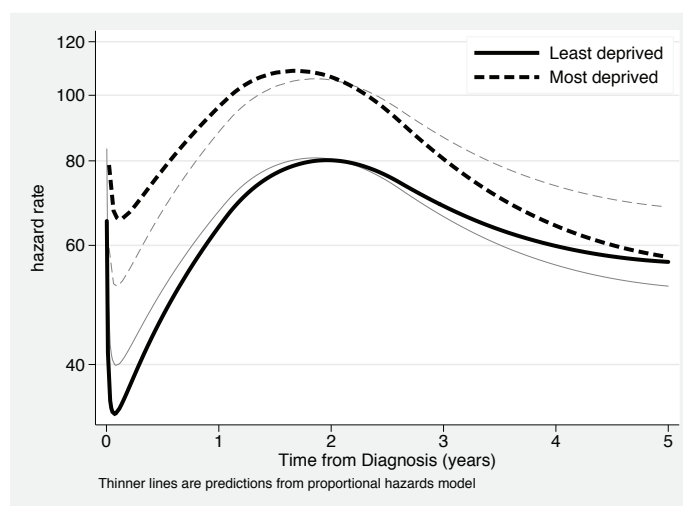


Figure 2. Hazard rates for most deprived versus most affluent group from model with time-dependent effects

It is useful to quantify differences between groups, but each parameter estimated from the above model is fairly meaningless taken on its own, and so it is best to obtain predictions for functions of interest by using the `predict` command:

```
. predict hr, hrnum(dep5 1) hrdenom(dep5 0) timevar(timevar) ci
. predict hdiff, hdiff1(dep5 1) hdiff2(dep5 0) timevar(timevar) ci
. predict sdif, sdif1(dep5 1) sdif2(dep5 0) timevar(timevar) ci
```

The time-dependent hazard ratio is obtained with the `hrnum()` and `hrdenom()` options. These options are fairly general and can be used to obtain the estimated hazard ratio for potentially any two covariate patterns, but this simple model is just comparing the hazard ratio for when `dep5 = 1` with when `dep5 = 0`. Alternative comparisons can be made by calculating the difference in the hazard rates by using the `hdiff1()` and `hdiff2()` options and for the difference in survival functions by using the `sdif1()` and `sdif2()` options.

Figure 3(a) shows the time-dependent hazard ratio with 95% confidence intervals. The deprived group has a mortality rate about twice that of the affluent group at the start of follow-up. The ratio decreases as follow-up time increases. After about 3.5 years, the hazard rates are very similar, which we can see because the hazard ratio is approximately 1. Figure 3(b) shows the difference in hazard rates between the two groups. In the first year of follow-up, there are approximately 40 more deaths per 1,000 person-years in the deprived group when compared with the affluent group. This difference decreases over time, and from about 3.5 years, there is very little difference between the two groups. Figure 3(c) shows the estimated survival curves from the two groups, which clearly show a difference that is quantified in figure 3(d). At 3

years postdiagnosis, there is an approximate 6% difference in survival, which stays approximately constant to the end of follow-up at 5 years.

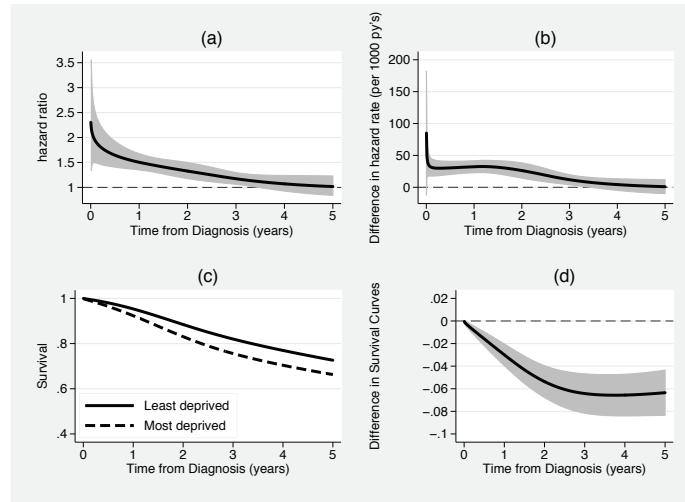


Figure 3. Comparison of affluent and deprived groups: (a) hazard ratio, (b) hazard difference, (c) survival curves, and (d) difference in survival curves

It is useful to investigate how changing the number of knots impacts the estimated hazard ratio. Figure 4 shows the estimated hazard ratio for a model using 5 df for the baseline hazard and between 1 and 5 df (using the `dftvc()` option) for the time-dependent effect of deprivation group. The lowest Akaike's information criterion and Bayesian information criterion are for the model with 1 df, indicating that the time-dependent effect can be expressed as a linear function of log time. However, the four other models have very similar fitted values, with some evidence of over-fitting with 5 df.

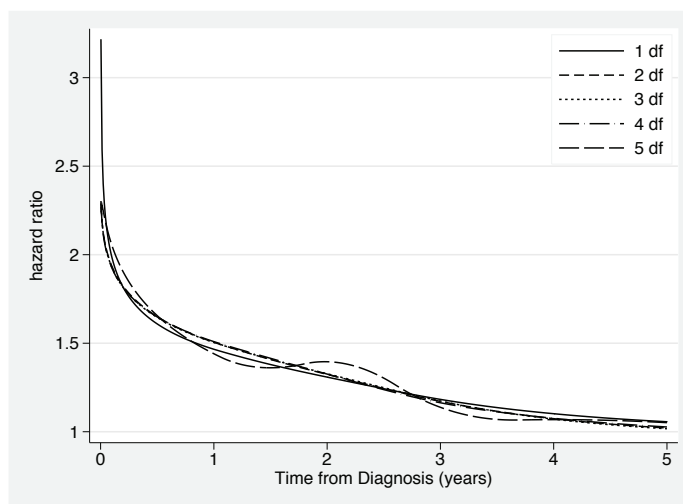


Figure 4. Comparison of time-dependent hazard ratios for models with 5 df for baseline effect and between 1 and 5 df for time-dependent effect

A disadvantage of modeling on the log cumulative hazard scale when compared with the more standard modeling on the log hazard scale is that when there are two variables with time-dependent effects, the hazard ratio for the first variable can be dependent on the level of the second variable. This is shown in figure 5 where year of diagnosis has been added to the model as a time-dependent effect. The hazard ratio, and its 95% confidence interval, for deprivation group has been calculated at 1986 and 1990. Although there is close agreement between the two hazard ratios, they are not identical as they would be when modeling on the log hazard scale.

(Continued on next page)

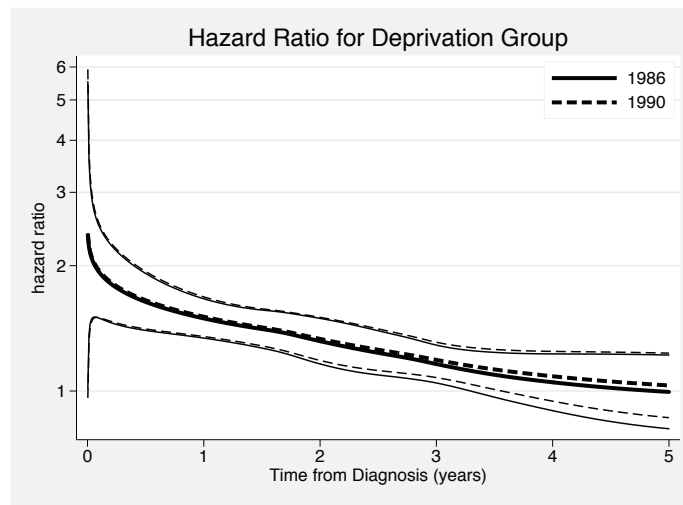


Figure 5. Comparison of time-dependent hazard ratio for deprivation group for different levels of a second time-dependent covariate

5.3 Age as the time scale

We now switch to a different dataset to show how to model with age as the time scale. The study compares incidence of hip fracture of 17,731 men diagnosed with prostate cancer treated with bilateral orchiectomy with 43,230 men with prostate cancer not treated with bilateral orchiectomy and 362,354 men randomly selected from the general population (Dickman et al. 2004). The outcome was femoral hip fractures. The risk of fracture is likely to vary by age, and thus age is used as the main time scale. With age as the time scale, the hazard rate gives us the age-specific incidence rates.

Delayed entry is defined using the `stset` command, and `stpm2` then has exactly the same syntax as that for a standard analysis. For example, in the code below, the date of hip fracture or censoring is stored in the variable `dateexit`, the date of cancer diagnosis is stored in the variable `datecancer` and the date of birth is stored in the variable `datebirth`. With use of the `enter()`, `origin()`, and `exit()` options, we can declare that a subject becomes at risk on the date he or she was diagnosed with cancer and stops being at risk on the day he or she had a hip fracture or was censored (death, migration, or end of study) or reached the age of 100. We then fit proportional and nonproportional hazard models for the effect for subjects without an orchiectomy (`noorc`) and for subjects with an orchiectomy (`orc`).

Figure 6(a) shows the incidence rate of hip fracture as a function of age from a proportional hazards model with 5 df for the baseline hazard. This shows how the incidence rate of hip fracture increases with age. There appears to be a difference in the incidence rate between the three groups with a hazard ratio of 1.37 (95% CI: 1.28 to 1.46) for prostate cancer patients without orchiectomy and 2.10 (95% CI: 1.93 to 2.28) for patients with orchiectomy. However, there is strong evidence of nonproportionality of the incidence (hazard) rates in these data, and figure 6(b) shows the estimated incidence rates as a function of age with 3 df used for the time-dependent effect. There appears to be a greater difference in the hazard rates (on the log scale) for younger patients. Figure 6(c) quantifies this difference with a time-dependent hazard ratio comparing those receiving an orchiectomy with the control group. There is a twentyfold difference in the incidence of hip fracture for the youngest men. For those aged 85 and over, the relative increase in risk is lower but is still double that in the control group. However, the large increase in risk at a young age is actually less important in terms of the number of individuals affected. Figure 6(d) shows the difference in the incidence rates between those receiving a bilateral orchiectomy and the control group. The difference at younger ages, where the relative increase is greatest, is lower than at older ages. This is due to the incidence rate being so low at younger ages.

```
stset dateexit, fail(frac = 1) enter(datecancer) origin(datebirth) ///
      id(id) scale(365.25) exit(time datebirth + 100*365.25)
stpm2 noorc orc, df(5) scale(h) eform
stpm2 noorc orc, df(5) scale(h) tvc(noorc orc) dftvc(3)
```

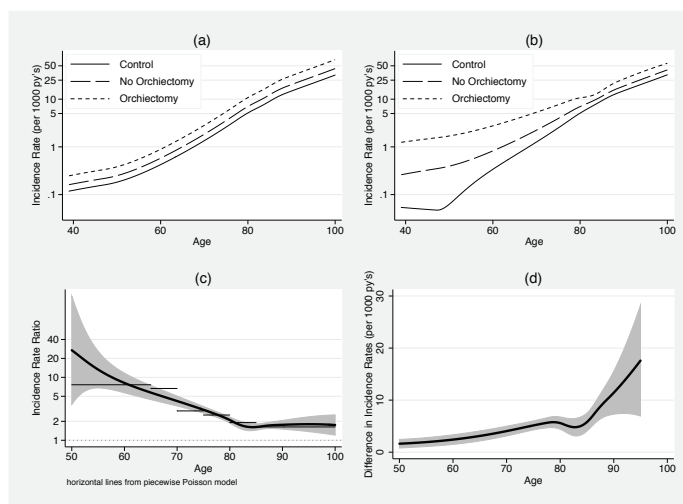


Figure 6. Analysis of orchiectomy data using age as the time scale: (a) predicted incidence rates as a function of age from a proportional hazards model, (b) predicted incidence rates as a function of age from a nonproportional hazards model, (c) incidence-rate ratio as a function of age for orchiectomy versus control, and (d) difference in hazard rates for orchiectomy versus control

5.4 Multiple time scales

There are in fact two time scales of interest in the orchietomy study. Not only is the age of the patient of interest but also is the time since orchietomy. Multiple time scales are usually modeled using Poisson regression (Carstensen 2004). In `stpm2`, a second time scale can be modeled using `stsplrit` and including dummy covariates for each time interval. Thus one time scale is modeled continuously, and the other is modeled using categories.

```
. stsplrit fu, at(1 2 3 4 5 7 10 15) after(datecancer)
(1475609 observations (episodes) created)

. xi: stpm2 i.fu noorc orc year_diag, df(5) scale(hazard) nolog eform
i.fu          _Ifu_0-15      (naturally coded; _Ifu_0 omitted)
note: delayed entry models are being fitted
Log likelihood = -16475.169              Number of obs   =   1898907
```

| | exp(b) | Std. Err. | z | P> z | [95% Conf. Interval] |
|-----------|----------|-----------|-------|-------|----------------------|
| xb | | | | | |
| _Ifu_1 | 1.022544 | .0363008 | 0.63 | 0.530 | .9538148 1.096226 |
| _Ifu_2 | 1.004172 | .0371311 | 0.11 | 0.910 | .9339707 1.079649 |
| _Ifu_3 | 1.007609 | .038827 | 0.20 | 0.844 | .9343118 1.086656 |
| _Ifu_4 | .9785442 | .0398745 | -0.53 | 0.595 | .9034311 1.059902 |
| _Ifu_5 | .992808 | .0357086 | -0.20 | 0.841 | .9252304 1.065321 |
| _Ifu_7 | .9951544 | .0370239 | -0.13 | 0.896 | .9251715 1.070431 |
| _Ifu_10 | .9931954 | .0427913 | -0.16 | 0.874 | .9127694 1.080708 |
| _Ifu_15 | .9449704 | .0652245 | -0.82 | 0.412 | .8254027 1.081858 |
| noorc | 1.36563 | .047332 | 8.99 | 0.000 | 1.275942 1.461623 |
| orc | 2.100881 | .0888205 | 17.56 | 0.000 | 1.933813 2.282382 |
| year_diag | .9980222 | .0018848 | -1.05 | 0.294 | .9943349 1.001723 |
| _rcs1 | 2.314448 | .1905098 | 10.19 | 0.000 | 1.969619 2.719648 |
| _rcs2 | .8731181 | .0237939 | -4.98 | 0.000 | .8277064 .9210213 |
| _rcs3 | 1.023806 | .0050983 | 4.72 | 0.000 | 1.013862 1.033847 |
| _rcs4 | 1.00204 | .0023906 | 0.85 | 0.393 | .9973658 1.006737 |
| _rcs5 | 1.003079 | .0013675 | 2.25 | 0.024 | 1.000402 1.005762 |

This is a proportional hazards model. The `_rcs#` terms model the baseline (log) cumulative hazard (as a function of attained age). The `_Ifu_#` terms are dummy variables for years since diagnosis, where the coefficients are (log) hazard ratios comparing all intervals with the reference (0–1 years). There appears to be little effect of follow-up, as was found in the original article. Time-dependent effects could be added for age by using the `tvc()` and `dftvc()` options. Time-dependent effects for years since diagnosis could be added by incorporating interactions between the exposure covariates (`noorc` and `orc`) and the `_Ifu_#` terms.

5.5 Relative survival

Relative survival (or excess mortality) models can be fit simply by adding the `bhazard()` option. Estimation and predictions continue as for standard models. This is one of the key advantages of `stpm2` in that it brings standard survival and relative survival models into the same framework. We return to the breast cancer data, but we now include women aged over 50 years. We will compare five age groups: <50, 50–59, 60–69, 70–79, and 80+. The analysis of all-cause mortality can be misleading because the older a woman becomes, the more likely it is that she will die of other causes. Relative survival models overcome this by incorporating the expected mortality due to other causes. The expected hazard rate at the time of death or censoring needs to be merged into the dataset. The easiest way to do this is to create the relevant updated merge variable after using `stset`, as follows.

```
stset survtime, failure(dead == 1) exit(time 5) id(ident)
gen age = int(min(agediag + _t,99))
gen year = int(yeardiag + _t)
sort sex region caquint year age
merge sex region caquint year age using "../Data/popmort_UK", nokeep
```

An all-cause flexible parametric model including age group can be seen below.

```
. stpm2 agegrp2-agegrp5, df(5) scale(hazard) eform nolog
Log likelihood = -139425.46          Number of obs   =      115331
```

| | exp(b) | Std. Err. | z | P> z | [95% Conf. Interval] | |
|---------|----------|-----------|--------|-------|----------------------|----------|
| xb | | | | | | |
| agegrp2 | 1.116145 | .0183245 | 6.69 | 0.000 | 1.080801 | 1.152644 |
| agegrp3 | 1.284454 | .0195326 | 16.46 | 0.000 | 1.246736 | 1.323313 |
| agegrp4 | 1.979577 | .029436 | 45.92 | 0.000 | 1.922716 | 2.038119 |
| agegrp5 | 4.155234 | .0631771 | 93.68 | 0.000 | 4.033236 | 4.280922 |
| _rcs1 | 2.452246 | .010547 | 208.56 | 0.000 | 2.431661 | 2.473005 |
| _rcs2 | .9542421 | .0027479 | -16.26 | 0.000 | .9488715 | .9596432 |
| _rcs3 | .9695571 | .0015477 | -19.37 | 0.000 | .9665283 | .9725953 |
| _rcs4 | 1.015823 | .0009726 | 16.40 | 0.000 | 1.013918 | 1.017731 |
| _rcs5 | .9996703 | .0005226 | -0.63 | 0.528 | .9986466 | 1.000695 |

Not surprisingly, there is a large effect of age with older women being at increased risk. However, it is not known which of these deaths are due to breast cancer and which are due to other causes. We thus fit a relative survival model by using the `bhazard()` option:

(Continued on next page)


```
. stpm2 agegrp2-agegrp5, df(5) scale(hazard) bhazard(rate) eform nolog
```

| | | |
|-----------------------------|---------------|-----------|
| | Number of obs | = 115331 |
| | Wald chi2(4) | = 3267.44 |
| Log likelihood = -133915.41 | Prob > chi2 | = 0.0000 |

| | exp(b) | Std. Err. | z | P> z | [95% Conf. Interval] | |
|---------|----------|-----------|--------|-------|----------------------|----------|
| xb | | | | | | |
| agegrp2 | 1.051428 | .0182859 | 2.88 | 0.004 | 1.016192 | 1.087886 |
| agegrp3 | 1.072864 | .0181672 | 4.15 | 0.000 | 1.037842 | 1.109069 |
| agegrp4 | 1.411935 | .0250603 | 19.44 | 0.000 | 1.363662 | 1.461917 |
| agegrp5 | 2.651379 | .0510765 | 50.62 | 0.000 | 2.553137 | 2.753401 |
| _rcs1 | 2.342038 | .0111471 | 178.80 | 0.000 | 2.320292 | 2.363988 |
| _rcs2 | .9607407 | .0030349 | -12.68 | 0.000 | .9548108 | .9667075 |
| _rcs3 | .9697656 | .0017879 | -16.65 | 0.000 | .9662677 | .9732762 |
| _rcs4 | 1.022492 | .0011734 | 19.38 | 0.000 | 1.020195 | 1.024794 |
| _rcs5 | 1.000382 | .0006277 | 0.61 | 0.543 | .9991522 | 1.001613 |

In a relative survival model, we get excess hazard ratios as opposed to hazard ratios. The excess hazard ratios are lower than the hazard ratios because the latter incorporate mortality due to both breast cancer and mortality due to other causes.

All the topics covered so far are easily extended to relative survival. Thus we can fit models with smooth estimates of the baseline excess hazard. We can estimate excess hazard ratios and time-dependent excess hazard ratios. We can model on the proportional-odds and other scales. We can use age as the time scale. We can use multiple time scales. We can easily obtain predictions of the baseline excess hazard, relative survival, time-dependent excess hazard ratios, difference in excess hazard rates, etc.

One useful summary is to report centiles of the survival function. The table below shows the time at which the relative survival function = 0.75, i.e., an estimate of the time at which 25% of women have died of breast cancer, with 95% confidence intervals.

```
. tabdisp agegrp, cellvar(c25 c25_lci c25_uci) format(%4.2f)
```

| agegrp | c25 | c25_lci | c25_uci |
|--------|------|---------|---------|
| 1 | 3.94 | 3.83 | 4.05 |
| 2 | 3.41 | 3.31 | 3.51 |
| 3 | 2.89 | 2.81 | 2.97 |
| 4 | 1.75 | 1.70 | 1.80 |
| 5 | 0.48 | 0.45 | 0.51 |

5.6 Further possibilities

There are other possibilities from these models that have not been covered in this article. These include obtaining average and adjusted survival curves by using the `meansurv` option, obtaining up-to-date estimates of survival by using period analysis ([Brenner and Gefeller 1997](#)), dealing with multiple events, and estimating the net and

crude probabilities of death from relative survival models, to mention but a few. We aim to write further articles for the *Stata Journal* on some of these topics.

6 Conclusion

The Cox model is perhaps overused in medical and other research. For a proportional hazards model, the estimates you get from a Cox model and the flexible parametric approach will be very similar. However, with the flexible parametric approach, you get several advantages associated with parametric models. The new Stata `stpm2` command takes the methodology a step further, and we hope that these models will become a useful tool in medical and other research.

7 Acknowledgments

We thank Chris Nelson and Paul Dickman for helpful comments on `stpm2` and the latter for access to the orchiectomy data. Part of this work was carried out while Paul Lambert was on a secondment at the Department of Medical Epidemiology and Biostatistics, Karolinska Institutet, Stockholm, Sweden, a visit funded by the Swedish Cancer Society (Cancerfonden) and the Swedish Research Council.

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