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## **An Asset Risk Theory of Share Tenancy**

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# An Asset Risk Theory of Share Tenancy

Marc F. Bellemare\*      Christopher B. Barrett†

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## Abstract

Reverse share tenancy, wherein poorer landlords rent out land to richer tenants on shares, is a common phenomenon. Yet it does not fit existing theoretical models of sharecropping and has never before been modeled in the economics literature. We explain share tenancy contracts using an asset risk model that incorporates Marshallian inefficiency and thereby provides a credible explanation for share tenancy more broadly, reverse tenancy included. When choosing the terms of an agrarian contract, the landlord considers the impact of her choice on the probability that she will retain future rights to the rented land. Thus, this model captures the effect of tenure insecurity and property rights on agrarian contracts. Among the main testable implications of the theoretical model are that, as property rights become more secure, reverse tenancy tends to disappear and that kin contracts tend to make share tenancy more likely.

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# 1 Introduction

Sharecropping, an agrarian contract by which a landlord leases out land to a tenant in exchange for a share of the crop, has long been studied by social scientists in general and by economists in particular. The canonical explanation for the existence of sharecropping, following Cheung (1969) and Stiglitz (1974), is that share tenancy matches a relatively richer landlord in a better position to absorb production risk with a tenant who, as a residual claimant on the output, has the proper incentives not to shirk. Sharecropping could thereby dominate both fixed rent contracts that were considered too risky by the tenant and wage contracts that would predictably lead to underprovision of effort by the tenant.

Of course, not every sharecropping contract fits the above stylized facts. We are especially interested in situations of reverse share tenancy, in which a relatively poorer landlord contracts with a relatively richer tenant. These situations do not fit the canonical model of sharecropping because the poorer landlord no longer holds comparative advantage in risk bearing over the tenant. Indeed, none of the extant published models of sharecropping are consistent with the oft-observed phenomenon of reverse share tenancy. Note that we distinguish “reverse share tenancy” from “reverse tenancy”, the latter term being somewhat confusing since it could refer to both fixed rent and sharecropping contracts.

In this paper, we present a theoretical model of reverse share tenancy as it is being practiced in Madagascar. Since the poorer landlord can neither sell her land nor exploit it herself, she rents out to a richer tenant on a share tenancy contract. We hypothesize that imperfectly secure land rights motivate reverse share tenancy. As under the canonical sharecropping model, if the landlord were to hire the tenant on a wage labor contract, moral hazard would lead to labor shirking. The innovation we introduce is that if the landlord were to rent out her land on a fixed rent contract, she would face an increased probability of losing her claim on the land. In much of rural Madagascar, local custom holds that taking possession of the fruits of the land ensures continued access to the land, much as direct cultivation of the land does under more traditional Lockean property rights. Under such conditions, the incentive to reduce asset risk motivates reverse tenancy sharecropping, replacing the traditional incentive that arises due to the landlords superior capacity to

bear yield risk. This asset risk explanation could explain any sharecropping in areas with insecure land rights, not just reverse share tenancy.

The rest of the paper is organized as follows. In section 2, we briefly review the literatures on sharecropping and on reverse share tenancy. Section 3 develops the theoretical model and presents the main results. In section 4, we discuss our model in relation to property rights in Madagascar. Section 5 concludes.

## 2 Literature Review

### 2.1 The Literature on Sharecropping

The sharecropping literature dates back to Adam Smith's *An Inquiry into the Nature and Causes of the Wealth of Nations* (1776, 1957), who observed that share tenancy was an unsatisfactory arrangement between slavery and the English (or fixed rent) system, that tenants had virtually no incentive to make improvements to the land under a sharecropping contract, and that issues of moral hazard were likely to arise. It then took close to a century and a half for economists to "discover" sharecropping again. Marshall (1920), in the eighth and last edition of his *Principles of Economics*, applied a rigorous, diagrammatic, marginal analysis to the phenomenon and concluded that, given the prohibitive cost to the landlord of enforcing the tenant's effort, tenants will equate the marginal product of their labor to the marginal income they get from their share of the crop. Thus, Marshall argued that the landlord could do strictly better by signing a fixed rent contract by which she extracts the entire surplus. This kind of moral hazard is referred to as "Marshallian inefficiency".

Cheung (1968) noted that the tenant's surplus observed in a Marshallian equilibrium was inconsistent with the notion of a competitive equilibrium. He thus took a different view, assuming that the tenant's effort was costlessly enforceable. He also assumed that landlords choose the number of tenants with whom they contract, which allows the former to bind the latter to their reservation utility. Cheung (1969) then discussed without much formalism that, in presence of both agricultural risk and transaction costs, sharecropping might emerge as the dominant tenurial arrangement. Stiglitz (1974) picks up where Cheung (1969) had left off by focusing on risk-sharing and the incentive ef-

fects of sharecropping. By exploring in turn what happens when the labor supply is inelastic and when the labor supply can vary, he obtains a series of results, two of which are striking: (i) under certain circumstances, i.e., when both parties can mix contracts, sharecropping becomes redundant; and (ii) under other, particular circumstances, effort will not be underprovided, i.e., there is no Marshallian inefficiency, and sharecropping contracts are efficient.

Newbery's (1977) contribution takes Stiglitz (1974) a step further by focusing solely on the risk-sharing effects of sharecropping contracts. He demonstrates that sharecropping is irrelevant when agricultural risk is the only risk that exists, but that when another type of risk enters the picture (a plausible assumption as regards agriculture in developing countries), sharecropping becomes the dominant tenurial arrangement. Our model follows in the spirit of Newbery by introducing multiple sources of risk, in our case asset risk in addition to production yield risk.

The above key references, like the rest of the economic-theoretic literature on sharecropping, cannot explain the emergence of reverse share tenancy. Assuming agents do not exhibit increasing absolute risk-aversion, the conjectured dominance of sharecropping in the canonical, Cheung-Stiglitz-Newbery tradition depends fundamentally on a relatively rich landlord who has a comparative advantage in risk-bearing or credit access and a relatively poorer tenant who has a comparative advantage in labor supervision due to moral hazard. Based on this, the economic-theoretic literature on sharecropping inherently fails to explain reverse share tenancy.<sup>1</sup>

## 2.2 The Literature on Reverse Tenancy

The literature on reverse share tenancy is small and purely empirical, consisting almost solely of case studies. Lawry (1993) presents a case study of land tenure in Lesotho, Lyne and Thomson (1995) review land use in KwaZulu, South Africa, and Colin and Bouquet (2001) discuss the *a medias* (or fifty-fifty) arrangement in the Mexican Sierra Madre. There is likewise scattered evidence that the phenomenon of reverse share tenancy is on the rise in

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<sup>1</sup>The reader interested in more complete reviews of the literature on sharecropping can consult Singh (1989) and Otsuka, Chuma and Hayami (1992).

India (most notably Punjab and Haryana<sup>2</sup>, but also in West Bengal) and in the Philippines (Roumasset, 2002). Two focal points seem to emerge of Lawry (1993) and Lyne and Thomson (1995): landlord households are typically headed by a single, older woman, i.e., a woman that is either divorced or widowed, and tenant households are typically headed by a younger man.<sup>3</sup> But none of these studies provide a sound theoretical explanation for the reverse share tenancy phenomenon. All of them are merely descriptive in nature and extant agrarian contract theory would predict reverse fixed rent tenancy, not share tenancy.

Given the seeming frequency with which reverse share tenancy occurs and the absence of any clear theory to explain its existence, there seems to be value in providing a theoretical model of reverse sharecropping that is consistent with the phenomenon of reverse share tenancy. This way, agrarian policy on a reasonably common phenomenon might be founded on a clear understanding of the institution's *raison d'être*. Such an understanding is essential if policymakers are to anticipate correctly how changes in key exogenous parameters, such as the legality of share contracts, access to rural credit, or security of land tenure, are likely responses to affect agricultural production and the welfare of poorer farmers.

Our work is motivated by field observations in Madagascar, where sharecropping was declared illegal in the early 1970s based on the perception that it led to agreements between relatively rich landlords and relatively poor tenants, and that this in turn could lead to exploitation in the context of what Breman (1974) refers to as a “patron-client” relationship. Sharecropping nonetheless continues in Madagascar, comprising more than half of all land rentals, according to the most recent available data (Minten and Razafindraibe, 2003). Moreover, anecdotal evidence and our own visits to numerous small farms in rural Madagascar confirm the presence of reverse share tenancy and limited survey evidence suggests that landlords are, on average, less educated, poorer and more likely female than tenants. Jarosz (1991), referring to the Lac Alaotra, Madagascar's main rice-producing region, notes that “(...) sharecroppers are not solely landless or nearly landless peasants; members of the wealthy

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<sup>2</sup>India's *Economic and Political Weekly* has mentioned this a few times. We thank Kei Otsuka for pointing this out.

<sup>3</sup>The same focal points seem to be true in India. We thank Clive Bell for pointing this out.

and middle classes also sharecrop the land of others. These landowners are generally smallholders, poor or middle-class farmers who are indebted, elderly, female or the descendants of former slaves”. Jarosz also notes how landowners who enter sharecropping agreements are often married women who have inherited land near their ancestral villages and then have moved away to live near their husband’s village, divorced women, widows, etc. She also adds that poor landlords who own land will have middle-income or rich farmers as tenants, or even urban people. This is because landlords typically lack the financial or physical capital to cultivate their land themselves.

The theory that follows is thus motivated by the reasonably widespread practice of reverse share tenancy in a nation where the overwhelming majority of the poor are small farmers, the poor systematically have weaker property rights in land than the rich (Randrianarisoa and Minten, 2001; Minten and Razafindraibe, 2003), and stimulating agricultural productivity is universally recognized as crucial to poverty reduction. One needs a coherent theory of the reverse share tenancy phenomenon in order to answer practical policy questions such as whether a ban on share tenancy is relevant, what are the likely consequences of land tenure changes, and how might the welfare of poor land-owning households be increased?

### 3 The Model

Let  $h_t$  denote the landlord’s land holding at time  $t$ ,  $\alpha \in [0, 1 - \epsilon]$  be the share of the crop that goes to the landlord as part of the sharecropping agreement,  $\beta \in \mathbb{R}$  be a side payment from the richer tenant to the poorer landlord, and  $\delta \in (0, 1)$  be the landlord’s discount factor.<sup>4</sup> We assume  $\alpha = 1$  to be impossible, which is equivalent to assuming that the landlord cannot borrow interseasonally in order to become an owner-operator and hire tenants – wage laborers – at a fixed wage. In this setting, we want to know when a poorer landowner will rent out her land to a richer tenant on shares instead of a fixed rent contract.

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<sup>4</sup>The parameter  $\epsilon$  is a (potentially very small) positive number in the  $(0, 1)$  interval included for purely technical reasons to bound the results in order that we can use a simpler model that excludes the fixed wage contract option.

Further, we assume that the landlord cannot sell her land. This is empirically motivated by the fact that very often in Madagascar and elsewhere, the poor have incomplete or insecure claims over land held under customary tenure. Because rights are incomplete or insecure, land sales are uncommon and assumed away in this analysis. This model is appropriate only for places with some degree of tenurial insecurity such that land sales are effectively infeasible.

As regards land, we make

**Assumption 1** *Let the expected law of motion for land be  $E(h_{t+1}) = \rho(\alpha)h_t$ .*

In Assumption 1, the function  $\rho(\alpha)$  is an asset security parameter. Equivalently,  $1 - \rho(\alpha)$  is the risk of asset-loss due to tenure insecurity in the land. Small farmers in several different sites in rural Madagascar have told us over the past decade that if their claim to a parcel of land is at all insecure, in the sense that it could be repossessed by the community and given to a different farmer or that they could lose their land to a squatter in a dispute, then their customary claim to the land is enhanced if they are observed to receive and retain part of the crop from the parcel. This seems to reflect some sense of the household's dependence on the parcel for its food security – and communities are loathe to damage members' food security – a quasi-Lockean property right, wherein receiving the fruit of the land is treated similarly to working it directly, or both. The origin and motive of this perception are not the object of our study. We take these as given. We therefore make

**Assumption 2** *Let  $\rho'(\alpha) > 0$ , i.e., asset security (risk) is strictly increasing (decreasing) in the share of the output received as rent.*

Note that tenure insecurity, observed in conjunction with reverse share tenancy, is seemingly not exclusive to Madagascar. The proceedings of an IFPRI (2002) conference also mention that “[a]t present, the laws in most Indian states do not permit tenancy of that type. Reverse tenancy is taking place without solid legal backing. Those who lease out land are at risk of losing ownership of that land”.

We then make

**Assumption 3** *Let the landlord's utility function  $u(\pi_t)$  be a bounded, strictly increasing, strictly concave and twice continuously differentiable function of profit at time  $t$ ,  $\pi_t$ .*

The concavity assumption implies that the landlord is risk averse. The sharecropping literature typically assumes that the landlord is risk neutral and the tenant risk averse. It seems reasonable to assume that the landlord is indeed risk averse, irrespective of the wealth ordering between landlord and tenant. The landlord's profit at time  $t$  is a function of land, such that:

$$\pi_t = \alpha_t f(k_t, \ell_t, h_t) + \beta_t - c_t, \quad (1)$$

where  $f(k_t, \ell_t, h_t)$  is the agricultural output as a function of capital, labor and land at time  $t$ , respectively, such that  $f'(\cdot) > 0$ ,  $f''(\cdot) < 0$  and  $f$  is bounded; The parameter  $\beta_t$  is the side payment – the fixed rent if it is positive or, if negative, a cash wage – from the tenant to the landlord; and  $c_t \geq 0$  subsumes the various costs borne by the landlord. For simplicity, we assume that the landlord possesses no input other than land, i.e., the tenant possesses both capital and labor inputs, as seems typical from the extant literature. In order for the reverse tenancy sharecropping contract to be individually rational, the landlord must derive non-negative profit from the agreement.

In order to account for moral hazard we make

**Assumption 4** *Let  $\ell_t = \ell(\alpha_t)$ , where  $\ell'(\cdot) < 0$  and  $\ell''(\cdot) > 0$ . That is, there is Marshallian inefficiency.*

This does not mean that the tenant's labor input is a choice variable of the landlord via her choice of crop share. Rather, we use this as a shortcut to capture the agency problem associated with a tenant's discretionary allocation of imperfectly observable labor effort without having to model that choice as well. In practice, the landlord might just be aware that her choice to take a greater share of harvest as rent will generally decrease the tenant's labor effort.

Note that for simplicity, we only assume traditional moral hazard instead of

assuming both traditional and technical moral hazard.<sup>5</sup> This does not make much difference, as our main results would only be strengthened by assuming both traditional and technical moral hazard.

Thus, the landlord's problem is to

$$\max_{\{\alpha_t, \beta_t\}_{t=0}^{\infty}} E_t \sum_{t=0}^{\infty} \delta^t u(\pi_t) \text{ s.t. } E(h_{t+1}) = \rho(\alpha)h_t \text{ given } h_0 > 0. \quad (2)$$

The Bellman equation for equation (2), or its dynamic programming version, is such that:

$$V(h) = \max\{u(\pi) + \delta EV(h')\} \text{ s.t. } E(h') = \rho(\alpha)h \text{ given } h > 0. \quad (3)$$

We drop the subscript in equation (3) given that the sequential problem is reduced to only two periods – now and tomorrow – by the principle of optimality. Thus,  $h$  denotes the landlord's land now and  $h'$  denotes the landlord's land in the future. Let us now assume that the landlord's utility function or returns function, in dynamic programming terms, takes the canonical DARA/CRRA form:

**Assumption 5** *Let  $u(\pi_t) = \ln(\pi_t) = \ln[\alpha_t f(k_t, \ell(\alpha_t), h_t) + \beta_t - c_t]$ .*

Given that the landlord's profit is bounded by assumption<sup>6</sup>, the function  $u(\cdot)$  is also bounded, and we have assumed that it is continuous, strictly increasing, strictly concave and twice continuously differentiable. Thus, the landlord's dynamic programming problem is

$$\begin{aligned} V(h) &= \max_{\alpha, \beta} \{ \ln[\alpha f(k, \ell(\alpha), h) + \beta - c] + \delta EV(h') \} \\ &\text{s.t. } E(h') = \rho(\alpha)h, h > 0. \end{aligned} \quad (4)$$

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<sup>5</sup>Traditional moral hazard refers to situations where the agent underprovides labor or, more generally, effort. Technical moral hazard refers to situations where the agent underprovides capital or chooses a production technique which is not optimal from the principal's point of view.

<sup>6</sup>Assuming that the agricultural output is bounded, then the landlord's profit is bounded.

Note that because  $\beta$  enters the landlord's profit linearly, by strict monotonicity of her preferences, she will always seek to set  $\beta$  at the highest possible value, while still satisfying the tenant's individual rationality constraint, which we omit here in the interest of brevity.<sup>7</sup>

Thus,  $\beta = \beta(\alpha)$ , where  $\beta'(\cdot) < 0$  and  $|\beta'(\alpha)| < f(k, \ell(\alpha), h)$ . That is, the contract trades off cash for in kind rent and rent cannot exceed the value of the crop, otherwise the contract would not be optimal.

The problem can then be reduced to:

$$\begin{aligned} V(h) = \max_{\alpha} \{ & \ln[\alpha f(k, \ell(\alpha), h) + \beta(\alpha) - c] + \delta EV(h') \} \\ \text{s.t. } & E(h') = \rho(\alpha)h, h > 0. \end{aligned} \quad (5)$$

The first-order condition for equation (5) implies that under the optimal contract

$$\frac{f(k, \ell(\alpha^*), h) + \alpha^* f'(k, \ell(\alpha^*), h) \ell'(\alpha^*) + \beta'(\alpha^*)}{\alpha^* f(k, \ell(\alpha^*), h) + \beta(\alpha^*) - c} = -\delta EV'(h') \rho'(\alpha^*) h \quad (6)$$

In light of the assumptions we have made thus far, the value function  $V(\cdot)$  is strictly increasing. Consequently, the value of owning a plot of size  $h$  for a landlord who behaves optimally from now on is strictly increasing in the amount of land owned. Therefore, the right-hand side of equation (6) is strictly negative, which allows us to state the following:

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<sup>7</sup>We use an implied principal-agent formulation here for the sake of simplicity and consistency with the extant sharecropping literature. As Bell (1989) notes, it is likely that tenants also enjoy welfare gains from sharecropping contracts. This may be especially true when tenants are wealthier, and thus probably more powerful than, landlords. The intuition and qualitative results of our model carry over to the more complex bargaining theoretic framework necessary to derive mutual gains from sharecropping.

**Proposition 1 (Existence)** *Under Assumptions 1 through 5, sharecropping emerges as the optimal contract. That is,  $\alpha^* > 0$  and  $\beta = \beta(\alpha^*)$  is set so as to maximize the landlord's profit from the contract while maintaining the tenant at his reservation utility level.*

**Proof 1** *Suppose not, i.e., suppose  $\alpha^* = 0$ . Then, evaluating equation (6) at  $\alpha^* = 0$  yields*

$$\frac{f(k, \ell(0), h) + \beta'(0)}{\beta(0) - c} = -\delta EV'(h')\rho'(0)h \quad (7)$$

*But then, the right-hand side of equation (7) is negative given our assumptions, and the numerator on the left-hand side is necessarily positive. Since the denominator must be nonnegative for this to be an optimal contract,  $\alpha^* > 0$ .*

We can also state the following as regards the comparative statics of the model, which gives us the usual testable implications:

**Conjecture 1 (Comparative Statics)** *Under Assumptions 1 through 5, the share of the crop that goes to the landlord should be increasing in the cost borne by the landlord. That is,  $\frac{\partial \alpha}{\partial c} \geq 0$ .*

We conjecture this rather than include it in the following proposition given that it is not immediately obvious that  $\frac{\partial \alpha}{\partial c} \geq 0$ . To see this, note that

$$\frac{\partial \alpha}{\partial c} = \frac{\delta EV'(h')\rho'(\alpha)h}{f(k, \ell(\alpha), h)\delta EV'(h')\rho'(\alpha)h + f'(k, \ell(\alpha), h)\ell'(\alpha)}. \quad (8)$$

In the above equation, the numerator is strictly positive, but the denominator is not necessarily positive given that the second term is negative. Intuitively, the share of the crop that goes to the landlord as rent should be increasing in the cost borne by the landlord, but proving this would require a technical assumption which would be difficult to justify.

**Proposition 2 (Comparative Statics)** *Under Assumptions 1 through 5, the share of the crop that goes to the landlord is strictly decreasing in the amount of capital provided by the tenant. Further, the output is decreasing in the crop share. That is,  $\frac{\partial \alpha}{\partial k} < 0$ , and  $\frac{\partial f}{\partial \alpha} < 0$ .*

**Proof 2** *We prove this directly using the partial derivatives of  $\alpha$  with respect to  $k$  and of  $f(\cdot)$  with respect to  $\alpha$ :*

$$\frac{\partial \alpha}{\partial k} = \frac{-f'(k, \ell(\alpha), h)}{[f(k, \ell(\alpha), h)\delta EV'(h')\rho'(\alpha)h + f'(k, \ell(\alpha), h)\ell'(\alpha)]^2}$$

$$\frac{-[f'(k, \ell(\alpha), h)\delta EV'(h')\rho'(\alpha)h + f''(k, \ell(\alpha), h)\ell'(\alpha)]}{[f(k, \ell(\alpha), h)\delta EV'(h')\rho'(\alpha)h + f'(k, \ell(\alpha), h)\ell'(\alpha)]^2} < 0 \quad (9)$$

Further,

$$\frac{\partial f}{\partial \alpha} = f'(k, \ell(\alpha), h)\ell'(\alpha). \quad (10)$$

Proposition 2 confirms familiar, intuitive results. The optimal share and falls as the tenant's capital contributions,  $k$ , grow, and since the tenant's labor effort decreases in the share of the crop accruing to the landlord, output,  $f(\cdot)$ , necessarily moves inversely with  $\alpha$ .

This moral hazard effect is standard in the literature. Yet it may not be as serious a problem as commonly thought if the landlord and tenant interact repeatedly over time — a standard folk theorem result — or if the tenant feels altruistically toward the landlord. Both factors may prevail in kin-based contracts.<sup>8</sup>

If kin-based contracts (denoted by the superscript  $o$ ) obviate Marshallian inefficiency, i.e. if we no longer impose Assumption 4, we get

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<sup>8</sup>Sadoulet, de Janvry and Fukui (1997) find that moral hazard plays much less of a role in contracts among kin than in non-kin contracts. Survey evidence suggests that as much as 40 percent of sharecropping contracts are kin-based in Madagascar, and we intend to test for this in our upcoming research.

**Proposition 3 (Kin Contracts)** *Under Assumptions 1, 2, 3 and 5, i.e., in kin-based contracts, since Marshallian inefficiency is obviated, sharecropping becomes more likely. That is,  $\alpha^* < \alpha^o = 1 - \epsilon$ .*

**Proof 3** *Because there is no Marshallian inefficiency under kin-based contracts,  $f(k, \ell(\alpha^o), h) > f(k, \ell(\alpha^*), h)$ , which implies that a landlord holding her tenant to his reservation utility level will take the whole of gain, necessarily implying an increase in the optimal share.*

This model hinges on the existence of insecure land rights that are affected by the distribution of the harvest. This implies that tenure security will affect the existence of reverse share tenancy contracts. This leads to

**Proposition 4 (Property Rights)** *As property rights become secure, i.e., under Assumptions 1, 3, 4 and 5 with  $\rho(\alpha) = 1$  and  $\rho'(\alpha) = 0$ , the landlord will switch from a sharecropping agreement to a fixed rent contract in non-kin contracts, thus moving from a second- to a first-best solution. That is, when  $\rho(\alpha) = 1$ ,  $\alpha = 0$ . In kin-based contracts, when property rights are secure, fixed rent and sharecropping contracts are both first-best, thus making sharecropping irrelevant.*

**Proof 4** *This is simply a Newbery-type result: when there exists only one type of risk, in this case moral hazard, then sharecropping agreements become irrelevant. To see this, note that if  $\rho(\alpha) = 1$ , then a risk averse landlord does strictly better by leaving all of the crop to the non-kin tenant and extracting the whole surplus by setting  $\beta(\alpha) = \beta(0)$  at the value which will maximize her profit while maintaining the tenant at his reservation level of utility. In the kin-based contract with no moral hazard, there is no longer any risk or inefficiency, so the form of payment (cash or kind) does not matter.*

In sum, Proposition 1 establishes mathematically the existence of reverse share tenancy, i.e., that under our assumptions, sharecropping between a poorer landlord and a richer tenant emerges as the dominant tenurial arrangement. Conjecture 1 and Proposition 2 provide the empirically testable implications of our theoretical model in the presence of cross-sectional data among a population characterized by reverse tenancy sharecropping. Proposition 3 establishes that, if we assume that kin contracts obviate the moral hazard problem, then the share of the crop that goes to the landlord is strictly greater in a kin contract than in a non-kin contract, providing a final

testable implication. Finally, proposition 4 establishes that as property rights get stronger, reverse tenancy sharecropping tends to disappear, providing a key empirically testable proposition that will require longitudinal data for proper testing.

## 4 Discussion

Given the model of the preceding section, it appears that sharecropping contracts, which are still illegal in Madagascar but often take the form of reverse share tenancy, emerge from the joint presence of asset risk and Marshallian inefficiency. In so far as sharecropping's illegality impedes reverse tenancy contracting, the legal restriction injures poor, landed households by inducing them to choose a suboptimal form of contracting out their land. Furthermore, as property rights become more secure, reverse tenancy sharecropping will tend to disappear, with poorer land owners benefiting from reduced Marshallian inefficiency as a result of endogenously changing agrarian contracts. Thus, there seems to be a good reason for the State to address the issues of sharecropping and property rights enforcement.

The relevance of property rights questions is made greater by empirical evidence that poor landowners may be most affected by insecure property rights. Randrianarisoa and Minten (2001) mention that in 1993, percent of owned land was titled among the richest income quintile but only 20 percent was for the poorest quintile. Minten and Razafindraibe (2003) note that this inequity becomes more acute when one looks at gender differences, with a man's land more than three times more likely to be titled than a woman's. Poor and female landowners thus appear to be the ones whose property rights are the weakest, and so they are most likely the ones who could most benefit from a strengthening of property rights. Randrianarisoa and Minten (2001) also mention that "while an improvement of secure property rights that can be established in a cheap way might benefit agricultural productivity and efficiency in some regional settings, increasing attention should be paid to include the poor in this titling process. It is shown that the rich hold relatively more secure titles to land than do the poor and some studies have shown that the rich might even get titles to the detriment of the poor."

In this sense, if property rights are endogenous, an effort should be made to

make them secure and therefore exogenous. Besley (1995), studying the link between land rights and individual investment decisions in Ghana, similarly argued that property rights could be endogenous but he concluded that one should not necessarily see developing land rights as a universal panacea. Platteau (1996) also argues that the beneficial effects of establishing private property rights are overestimated, and that it would be better to rely on informal mechanisms at the community level. Note that we are not arguing for a particular institutional mechanism for making property rights secure — e.g., titling by the State or community enforcement of customary access rules — merely for securing property rights in order that poor landowners do not choose relatively inefficient production arrangements as a means to insure against asset loss. Our model introduces the important possibility of endogenous change in the form of contract governing agricultural production. In this setting, it appears that establishing such rights may well improve the situation of poor but landed households.

## 5 Conclusion

Using a dynamic argument which combines the risk of asset loss with Marshallian inefficiency associated with labor shirking by an imperfectly supervised tenant, we establish that sharecropping contracts will be chosen by the landlord and derive comparative statics that are consistent with the stylized facts of reverse tenancy sharecropping.

Our model also implies that reverse share tenancy will tend to disappear as property rights get stronger. First, the State should make sharecropping contracts legal, for even though the ban on share tenancy is not strictly enforced, it still creates some uncertainty for the households that are party to such agreements. Second, the State should address the question of land rights for all land owners, perhaps especially the poor.

This paper introduces a more encompassing theory of sharecropping that can explain oft-observed reverse share tenancy, a phenomenon that defies the canonical model of Cheung, Stiglitz, Newbery and their successors. As such, it introduces a theory of sharecropping that could explain the institution's existence wherever property rights are insecure.

While this model explains the stylized facts well enough, there is still much to be done on reverse share tenancy. For one, our model should be taken to data and tested against other plausible explanations for the existence of reverse share tenancy. For instance, Bellemare (2003) offers a preliminary model of reverse share tenancy based on limited liability. Given apparent widespread practice of reverse tenancy in different legal, political and economic environments, a general explanation of this phenomenon based on sound theory and empirical validation should be sought.

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