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Consumer Demand for Food Commodities in the United States With Projections for 1980

P.S. George and G.A. King

Department of Agricultural and Resource Economics University of California, Davis



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This study analyzes the demand for food commodities in the United States in the postwar period using both time-series and cross-section data. Income-consumption relationships are based on data from the 1955 and 1965 USDA household food consumption surveys.

The analysis of cross section data emphasized: (1) effects of grouping observations, (2) choice between expenditures and quantities as the dependent variable, (3) effects of household size on income-consumption relationships, (4) shifts in the regression coefficients (intercepts and income elasticities) between 1955 and 1965, and (5) regional variations in the income-consumption relationships.

A demand interrelationship matrix was developed for 49 commodities or commodity groups at the retail level. Commodities were classified into 15 separable groups and all direct and cross elasticities for commodities within a group were estimated directly. The cross elasticities corresponding to commodities outside a given group were estimated through assumptions of cardinal separability. The synthesis of demand interrelationships was achieved by the use of restrictions on demand equations for an individual consumer as suggested by Frisch (1959) and quantified by Brandow (1961). Consideration also was given to the measurement of time trends on consumption. Marketing margins were analyzed and demand interrelationships were developed at the farm level.

Projections of 1980 consumption per capita were developed for individual commodities and group aggregates. These projections are based on a specification of constant real prices, exogenous projections of real income per capita, and continuation of past time trends for certain commodities.

THE AUTHORS:

P. S. George is on the faculty of the Indian Institute of Management, Ahmedabad, India.

G. A. King is Professor of Agricultural Economics and Agricultural Economist in the Experiment Station and on the Giannini Foundation, University of California, Davis.

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CONSUMER DEMAND FOR FOOD COMMODITIES IN THE UNITED STATES WITH PROJECTIONS FOR 1980⁴

INTRODUCTION

A NUMBER OF STUDIES have estimated demand characteristics and explained the factors that influence consumer behavior. Individual farm commodifies such as beef, corn, cotton, potatoes, sugar, and wheat have been the subject of investigation. Most of these studies are partial analyses without considering the complete interdependent nature of demand. A notable exception is Brandow's (1961) study of the demand interrelationships among all food commodities. One basic reason for the absence of a large number of studies in this area seems to be the gap between the theory of demand and empirical analysis using statistical procedures of estimation. Kuznets (1963) observes, "..., to obtain confrontation between theory and fact. large bodies of micro data are needed which refer directly to decision units whose economic behavior is the object of the study. Such data are costly and we have much to learn about how to collect and analyze this information." Recent advances in economic theory. statistical procedures of estimation, and testing hypotheses have overcome some of these problems. The present study reviews a few approaches to bridge the gap between theory and empirical analysis.

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[1]

These concepts are used to measure income-consumption relationships, demand interrelationships at the retail level, and the nature of price spreads between retail and farm levels.

A demand relationship obtained as a result of maximizing consumer's satisfaction subject to a budget restraint, is expressed as a function of prices of the commodities and consumer income. To analyze the effects of prices and income on the quantity consumed, it is necessary to isolate the effects of other non-, economic elements such as psychological, sociological, cultural, and regional factors that determine the level of consumption of a given commodity.

Generally, prices remain unchanged during a short period of time and, therefore, data obtained from cross-section surveys provide a basis for obtaining the effects of income on consumption free from price effects. However, within a cross section, it is difficult to keep the psycho-socio-cultural factors constant and, therefore, the effects of these factors on the income coefficient have to be determined before deciding on the reliability of the income coefficient obtained from cross-section data. Unfortunately, it is often difficult or even impossible to quantify the effects of many noneconomic factors. Household consumption survey data for the United States can be used to obtain the effects of household size and region on the income-consumption relationship. Also, changes in income coefficient over time can be evaluated using cross-section data from two points in time, and the effects of redistribution of income on food consumption can be analyzed.

The effect of a change in the price of one commodity will influence the consumption of all commodities in the consumer's choice relationship. Often policy decisions require estimates of demand interrelationships and estimates of the probable level of consumer demand in the future. Recent contributions in the area of economic theory and statistical methods of estimation and testing hypotheses have made it possible to improve procedures used in estimating demand interrelationships. In particular, the assumptions of want independence and neutral want association can be used to separate the commodities in the utility function to obtain separable groups. The estimates obtained for particular groups can be used to synthesize a demand interrelationship matrix showing all the direct- and cross-price elasticities corresponding to the commodities entering the utility function.

Retail prices are determined as an outcome of the decisions made at different levels in the marketing system. In many cases, only a small percentage of the retail prices go to the producers of raw materials, and the difference between prices realized at the retail level and at the farm level can be treated as charges for the marketing services. Such charges are often known as price spreads or marketing margins. It can be hypothesized that certain relationships exist between price spreads and prices at the retail or farm levels. It is possible to derive the elasticities at the farm level from the elasticities at the retail level based on the relationship assumed between price spreads and actual prices.

Considering the above factors, the objectives of the present study can be summarized as follows:

1. To estimate the effects of different factors that influence the consumption of food items in the United States through the use of cross-section data. In particular, attempts are made to estimate the effects of income, household size, and region on quantities consumed. Also, the income elasticities obtained from 1955 and 1965 cross-section data are compared, considering the effects of income redistribution during this period.

2. To estimate demand interrelationships among the major items in the family food budget at the retail level. Here, the different commodities are classified into separable groups and the demand coefficients within a group are estimated independently. The restraints provided by demand theory are imposed upon the coefficients to synthesize the demand interrelationship matrix.

3. To specify a relationship between price spreads and retail prices and to derive the demand interrelationship at the farm level from corresponding estimates for the retail level. It was specified that a linear relationship exists between price spreads and retail prices. (This specification incorporates the commonly assumed absolute spread and the percentage spread.)

4. To specify procedures for projecting consumption levels in the future and derive estimates, by commodity, for 1980. The projections are based on the assumption of prices held at the 1962–1966 level.

The overall objective of this study is

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to contribute toward the understanding of demand characteristics for food commodities in the United States and to estimate the effect of various factors on the consumption of commodities included in the analysis.

I. ECONOMIC AND STATISTICAL FRAMEWORK Basic Concepts in Demand Theory

The economic framework for the study of consumer behavior generally is through the theory of utility-maximizing individuals (Stigler, 1965), while some recent studies have attempted to make certain generalizations based on observed consumer behavior (see Houthakker, 1961). The purpose of this section is to emphasize theoretical developments of importance for empirical research in the present context. Therefore, some aspects are omitted here, especially those related to welfare economics. Following the general practice in static consumption theory, the beginning point will be the choice problems of an individual consumer with given tastes, attempting to purchase the most preferred combination of commodities subject to a budget restraint.2 We shall trace out the consumer theory from an axiomatic point of view and show the derivation of demand functions and the constraints imposed upon them by the assumptions made in orthodox economic theory. This is followed by a brief description of the revealed preference approach, to show the formal equivalence of the two approaches.

Preference axioms

The static theory of consumer behavior begins with a choice problem facing an individual consumer with given income, prices, tastes, and preferences. The consumer is confronted with a set of goods from which he is supposed to make a choice of items. His choice will be governed by certain behavioral factors, the most important among them being that he is "assumed to choose among the alternatives available to him in such a manner that the satisfaction derived from consuming commodities (in the broadest sense) is as large as possible" (Henderson and Quandt, 1958, p. 6). The extent of satisfaction derived from a given set of goods is assumed to depend upon the individual's preference relationship. Economists often refer to this preference relationship as a utility indicator. Because utility has been a central point of controversy in the theory of consumer behavior, we shall briefly describe this concept.

According to Chipman (1960, p. 221). "Utility in its most general form is a lexicographic ordering represented by a finite or infinite dimensional vector with real components unique only up to an isotone (order preserving) homogeneous transformation, and these vectors (lexical numbers) are ordered lexicographically like decimal numbers or words in a dictionary." However, the historic significance attached to utility is not exactly the same as the above definition. For example, Bentham, who brought the principle of utility into a prominent position, assumed it to be a cardinal measure of pleasure. (See Stigler, 1965, and Dorfman, 1964). The founders of

² We maintain Arrow's (1958, p. 1) distinction between "choice" and "decision making." "Decision making" is usually applied only when "conscious reflective choice is involved." However, it is possible to have selection of commodity bundles with unconscious or unreflective choices. Therefore, the term, "choices," will be used instead of decision making.

the utility theory (Jevons, Walras, and Menger) accepted the existence of utility as a fact of "common experience" and they spoke of utility as an absolute magnitude. (See Stigler, 1965, p. 85; also Samuelson, 1966, pp. 90–96). The early authors considered that the utility derived from the consumption of a commodity was a function of the quantity consumed alone. Thus, if q_1, q_2, \dots, q_n are *n* commodities belonging to a commodity bundle, the utility function is explicitly written as

$$U = U_1(q_1) + U_2(q_2) + \cdots + U_n(q_n),$$

The cardinal nature of the utility function was relaxed by Fisher (1892) and Pareto (1896). They realized that, if a utility function reaches a maximum with a certain basket of commodities, then any order-preserving transformation of that function also reaches a maximum at that particular basket. In other words. the above maximum involves only ordinal properties. In most of the recent works, this ordinal property of the utility indicator is used to avoid the restrictive assumptions of a cardinal utility approach. Therefore, here it is not required that the consumer assigns units or measurements of utility associated with the possession and use of individual commodities. However, it is required that the preference relationship of the individual satisfy the following axioms (Debreu, 1965; Wold, 1952; and Uzawa, 1959).

Axiom 1. Ability to rank (axiom of comparability, see Newman, 1965, p. 10).

This axiom asserts that the consumer

facing different commodity bundles in a given commodity space³ is able to rank⁴ the bundles according to his order of preferences. Given two bundles q^0 and q^1 , the individual is capable of making one of the following three choices:

- (a) q^0 is preferred to q^1 , or $(q^0p q^1)$,
- (b) q^0 and q^1 are equally sastisfac- (1) tory, or $(q^0I q^1)$, and
- (c) q^0 is not preferred to q^1 , or $(q^0 \vec{p} q^1)$.

There is no specification as to the extent to which q^0 is preferred to q^1 or otherwise—only that one is preferred to the other or that both are equally preferred.

Axiom 2. Antisymmetry

This axiom avoids any ambiguity in the preference ordering.

If
$$q^{0}p q^{1}$$
, it is not possible that (2)
 $q^{1}p q^{0}$ holds simultaneously.

Axiom 3. Consistency of Ranking (Transilivity)

Suppose that there are three bundles $(q^0, q^1, and q^2)$ and that the following conditions hold:

(a)
$$q^{b}p q^{1}$$
 and
(b) $q^{1}p q^{2}$.

The axiom of consistency asserts that a set of preference relationships satisfying (3) will satisfy the relationship $q^{0}p q^{2}$. Newman (1965) points out two cases where this axiom may not hold: First, there are certain threshold effects where "the combination of two gaps

³ Following Debreu (1965, p. 32), the term "commodity" is used to denote "a good or a service completely specified physically, temporally and spatially." The existence of only a finite number of commodities is assumed. The quantity of any one of the commodities can be any real number. A subset of elements belonging to the commodity space is referred to as a "commodity bundle."

⁴ A given individual does not need to rank all items, but just those of relevance to his experience.

each of which is below the individual's threshold (of preference perception), might itself be above that threshold." Second, the relevant bundles may contain numerous commodities whose preference relationships are such that comparison among the bundles may not be possible.

The axioms of comparability, antisymmetry, and transitivity are necessary and sufficient conditions for a complete ordering of the commodities in the commodity space.

Axiom 4. Monotonicity

This axiom assures that the consumer has not achieved satiation. In the preference ordering, if the commodity bundles are ranked in an increasing order of preference, the preference relationship remains monotonically increasing.

Axiom 5. Convexity

The consumption set is convex (see Dorfman, pp. 396-97) if, for any two bundles, q^0 and q^1 belonging to the set, their weighted average $tq^0 + (1 - t)q^1$ where 0 < t < 1, also belongs to the same set. A fundamental property of the (ordinal) utility indicator is that the indifference curves represent convex sets, and the minimal property of all utility indicators is quasi-concavity. The assumption of quasi-concave utility indicators is important. Arrow and Enthoven (1961, p. 792) have shown that if the utility function is quasi-concave and monotonic, the usual first-order conditions are necessary and sufficient for obtaining a solution for a constrained maximization problem.

To sum up, the preference axioms mentioned in this section enable us to define an order-preserving, quasi-concave utility indicator which is monotonic and continuous.

Concept of demand

The concepts of demand, as stated in the middle of the nineteenth century by Cournot and Dupuit, were popularized by Marshall. (See Hicks, 1962). Marshall's theory focusing on the quantityprice relation for a single commodity. holding income and all other prices constant, provided a demand function uncompensated for income effects. The work of Pareto and Walras focused on the more general case in which all prices and income are variable. However, the basic theory was clarified by Hicks (1939), in his famous mathematical appendix, which explicity links utility theory with demand analysis. His work drew on the article written in 1915 by Slutsky (1952) who distinguished between income and substitution effects due to a price change and between a compensated and uncompensated demand function.

Earlier, it was shown that the axioms on the preference relationship of an individual consumer lead to the existence of a monotonic order-preserving utility indicator which, by assumption, is a function of quantities of commodities belonging to the commodity bundle chosen. (See also Kalman, 1968). The behavioral axioms of the individual consumer are such that he makes his choices of the commodity bundle in order to obtain the maximum satisfaction subject to this budget limitation.

Suppose that a consumer with a given income, y, makes a choice of quantities, q_1, q_2, \dots, q_n , from a commodity space with n elements. Then the utility function can be specified as

$$U = U(q_1, q_2, \cdots, q_n). \tag{4}$$

If p_1, p_2, \dots, p_n represent the unit prices of these commodities, $p_1q_1 + p_2q_2 + \cdots$ $+ p_n q_n$ will be the total expenditure and this should not exceed the income; or

$$p_1q_1 + p_2q_2 + \cdots + p_nq_n \leq y.$$
 (5)

So the choice problem reduces to finding a maximum of $U(q_1, q_2, \dots, q_n)$ subject to the restriction (5). When we retain the inequality sign in restriction (5), the usual calculus method of finding constrained maximum becomes complicated and, therefore, we have to resort to programming techniques (see Dantzig, 1963; Hadley, 1964). Quadratic utility indicators were used in a few studies (Wegge, 1968). However, for explaining the theoretical concepts, it is sufficient to retain the equality sign in (5).

The consumer's choice of q_1, q_2, \cdots, q_n will correspond to the quantities consistent with maximization of

$$U(q_1, q_2, \cdots, q_n) + \lambda(y - p_1q_1 - \cdots - p_nq_n).$$
(6)

Differentiating with respect to q_1 , q_2 , \cdots , q_n and λ , we get the following normal equations:

$$\begin{cases} U_{j}(q_{1}, q_{2}, \cdots, q_{n}) - \lambda p_{j} = 0, \\ (j = 1, \cdots, n) \end{cases} (7) \\ y - p_{1}q_{1} - p_{2}q_{2} - \cdots - p_{n}q_{n} = 0, \end{cases}$$

where

$$U_j = \frac{\partial U}{\partial q_j}.$$

The system (7) provides (n + 1) equations in (n + 1) variables (q_1, q_2, \dots, q_n) and λ when all the prices and income are given. Therefore, under given prices and income, we can solve for the quantities that provide the individual with the highest possible level on his preference

relationship. The solutions will be of the form

$$q_{j} = q_{j}(p_{1}, p_{2}, \cdots, p_{n}, y).$$

(j = 1, 2, \dots, n) (8)

The quantity purchased of each commodity is expressed as a function of its price, price of other commodities, and income; hence, the relationships in (8) represent a set of demand functions.

The demand functions (8) obtained from (7) should satisfy the second-order condition of utility maximization. Here the quasi-concavity assumption of utility indicators plays its role. The conditions expressed in (7) only assures that the consumer is neither on the uphill nor the downhill side of the preference function; rather, it leaves him at a stationary point, which may correspond to either a maximum or a minimum point of satisfaction. The necessary conditions, as expressed in (7) are sufficient if $U(q_1, q_2, \cdots, q_n)$ is a twice differentiable quasi-concave function in the neighborhood of the optimum. This condition can be elaborated to show the restrictions on the marginal rate of substitution. Here we shall use the properties of concave and quasi-concave functions. The Hessian matrix, H of U, can be written as

$$H = \begin{bmatrix} U_{11}, U_{12}, \cdots, U_{1n} \\ \vdots, \vdots, \cdots, \vdots \\ U_{n1}, \cdots, \cdots, U_{nm} \end{bmatrix}$$
(9)

where

$$U_{ij} = \frac{\partial^2 U}{\partial q_i \partial q_j}$$

For a quasi-concave function, the bordered Hessian matrix (bordered with 4

the marginal utilities $\partial U/\partial q_i$) will have alternating principal minors starting with negative. Therefore,

$$(-1)^{t}D_{r} \geq 0 \quad (r = 1, 2, \cdots, n) \quad (10)$$

where

$$D_r = \begin{bmatrix} U_{11} \cdot \cdots \cdot U_{ir}U_1 \\ U_{n1} \cdot \cdots \cdot U_{rr}U_r \\ U_1 \cdot \cdots \cdot U_r 0 \end{bmatrix}$$

Ł.,

and where

$$U_j = \frac{\partial U}{\partial q_j}, \quad (j = 1, \dots, n)$$

In particular, when n = 2,

$$\begin{bmatrix} U_{11} & U_{12} & U_1 \\ U_{21} & U_{22} & U_2 \\ U_1 & U_2 & 0 \end{bmatrix} > 0.$$
(11)

If we consider any movement along a given indifference curve, the following must hold:⁶

$$U_{1}dq_{1} + U_{2}dq_{2} = 0$$

and the slope of the line tangent to this curve is defined as:

$$\frac{dq_2}{dq_1} = -\frac{U_1}{U_2}.$$
 (12)

The change in the slope of the indifference curve is given by

$$\frac{d\left(\frac{-U_{1}}{U_{2}}\right)}{dq_{1}} = -\frac{\left(U_{11} + U_{12}\frac{dq_{2}}{dq_{1}}\right)U_{1} - \left(U_{21} + U_{22}\frac{dq_{2}}{dq_{1}}\right)U_{1}}{U_{2}^{2}},$$

$$= \frac{-U_{11}U_{2}^{2} + U_{12}U_{1}U_{2} + U_{21}U_{1}U_{2} - U_{22}U_{1}^{2}}{U_{2}^{3}}.$$
(13)

Here the numerator is the same as the 14 matrix in (11). Using the relationship, (11), the sign of (13) depends on the sign of U_2 alone. The relationship, (13), is positive if $U_2 > 0$ and it is negative if $U_2 < 0$. Also, when the marginal utilities are positive, from the relationships (11), (12), and (13), we have the indifference curves downward sloping and convex to the origin. This convexity of indifference curves assumes diminishing marginal rate of substitution. The marginal rate of substitution is diminishing when we have diminishing marginal utility. Therefore, concavity of utility

function (diminishing marginal utility) is sufficient for diminishing marginal rate of substitution. However, this is not necessary, because the sign of the rate of change of the marginal rate of substitution depends only on the sign of U_2 as long as condition (11) holds. It is possible for (11) to be true even if U_{12} or U_{22} or both may be positive. Therefore only diminishing marginal rate of substitution is necessary for assuring a maximum of solution in (8).

To sum up, quasi-concave functions guarantee that if the necessary firstorder conditions are satisfied at a certain

⁵ Indifference curve, in cardinal analysis, represents the locus of points in the commodity space which provide the same level of satisfaction. For our purpose, it is enough to assume that two commodity bundles fall on the same indifference curve if the consumer is indifferent towards these two bundles in an ordinal sense, (q^{0}, q^{1}) . It is not necessary to introduce any cardinal utility assumption in this section.

point, it corresponds to a point of maximum satisfaction (see proofs in Arrow and Enthoven, 1961; Wold and Jureen, 1964). There will be a maximum for a quasi-concave function even if it exhibits increasing marginal utility without violating the property of diminishing marginal rate of substitution. Incidentally, this property helps us to release the preference relationship from a restrictive assumption of diminishing marginal utility.

Restrictions on demand functions

The demand functions satisfy a number of important relationships. Hicks (1962), Wold and Jureen (1964), Frisch (1959), Brandow (1961), and Pearce (1961) have summarized the properties of the demand functions. These conditions follow from differentiation of the first-order conditions.

Homogeneity Condition (row restraint)—The first-order conditions in (7), from which demand functions are derived, imply that if prices and income are changed by the same proportion, the quantity demanded remains the same. In the case of two commodities, the firstorder conditions are

$$\begin{cases} U_1 - \lambda p_1 = 0 \\ U_2 - \lambda p_2 = 0 \end{cases}$$

$$(14)$$

$$[y - p_1 q_1 - p_2 q_2 = 0.$$

This leads to a condition that

$$\frac{U_1}{U_2} = \frac{p_1}{p_2}$$

When income and prices are changed by the same proportion (say k), the first

⁶ Elasticities are defined by $e_{ij} = (p_j/q_i)(\partial q_i/\partial p_j)$, and $e_{iy} = (y/q_i)(\partial q_i/\partial y)$.

order conditions become

$$\begin{aligned} U_1 - \lambda k p_1 &= 0, \\ U_2 - \lambda k p_2 &= 0, \\ k y - k p_1 q_1 - k p_2 q_2 &= 0, \text{ or } \\ y - p_1 q_1 - p_2 q_2 &= 0. \end{aligned}$$
(15)

Equations (15) also lead to the conditions

$$\frac{U_1}{U_2} = \frac{p_1}{p_2}$$
 and $y = p_1q_1 - p_2q_2 = 0$.

Since the first order conditions essentially remain the same, the optimum commodity bundle is unaltered. This property is known as the homogeneity condition, implying that demand functions are homogeneous of degree zero in prices and income. Consider the demand function for a single commodity i:

$$q_i = q_i(p_1, p_2, \cdots, p_n, y).$$
 (16)

Using Euler's theorem for homogeneous functions of degree zero, we have

$$p_{1} \frac{\partial q_{i}}{\partial p_{1}} + p_{2} \frac{\partial q_{i}}{\partial p_{2}} + \cdots$$

$$+ p_{n} \frac{\partial q_{i}}{\partial p_{n}} + y \frac{\partial q_{i}}{\partial Y} = 0.q_{i}.$$
(17)

Converting (17) into elasticities by dividing throughout by q_1° , we obtain

$$e_{i1} + e_{i2} + \cdots + e_{in} + e_{in} = 0.$$
 (18)

This implies that the direct- and crossprice elasticities and income elasticities add to zero.

$$(i, j = 1, 2, \dots, n)$$

Engel aggregation.—The budget restraint is denoted by

 $p_1q_1+p_2q_2+\cdots+p_nq_n=y.$

The effect of a change in income on consumption can be obtained by differentiating (19) with respect to y to obtain

$$p_1 \frac{\partial q_1}{\partial y} + p_2 \frac{\partial q_2}{\partial y} + \cdots + p_n \frac{\partial q_n}{\partial y} = 1$$
 or (20)

$$\frac{p_1 q_1}{y} \cdot \frac{y}{q_1} \frac{\partial q_1}{\partial y} + \cdots + \frac{p_n q_n}{y} \cdot \frac{y}{q_n} \frac{\partial q_n}{\partial y} = 1.$$
(21)

It will be convenient to express (21) in terms of budget proportions and elasticities as

$$W_1e_{1y} + W_2e_{2y}$$

$$+ \cdots + W_ne_{ny} = 1$$
(22)

where

 $W_i = (p_i q_i) / y$ represents the share of

expenditures (budget proportions) on i^{th} commodity.

Equation (22) implies that the income elasticitics weighted by the respective expenditure proportions add to one.

Cournot aggregation.—The effect of a change in the price of j^{ih} commodity, with all prices remaining the same, can be obtained by differentiating the budget restraint (19) with respect to p_{ii} or

$$p_{1} \frac{\partial q_{1}}{\partial p_{j}} + p_{2} \frac{\partial q_{2}}{\partial p_{j}} + \dots + q_{j} + p_{j} \frac{\partial q_{j}}{\partial p_{j}} + \dots + p_{n} \frac{\partial q_{n}}{\partial p_{j}} = 0 \quad \text{or}$$

$$p_{1} \frac{\partial q_{1}}{\partial p_{j}} + p_{2} \frac{\partial q_{2}}{\partial p_{j}} + \dots + p_{j} \frac{\partial q_{j}}{\partial p_{j}} + \dots + p_{n} \frac{\partial q_{n}}{\partial p_{j}} = -q_{j}.$$
(23)

Expressing (23), in terms of elasticities and budget proportions, we have

(19)

$$\frac{p_1q_1}{p_jy}\frac{p_j}{q_1}\frac{\partial q_1}{\partial p_j} + \cdots + \frac{p_nq_n}{p_jy}\frac{p_j}{q_n}\frac{\partial q_n}{\partial p_j} = -\frac{q_j}{y}, \qquad (24)$$

$$\frac{p_1q_1}{y}\frac{p_j}{q_1}\frac{\partial q_1}{\partial p_j} + \dots + \frac{p_nq_n}{y}\frac{p_j}{q_n}\frac{\partial q_1}{\partial p_j} = -\frac{p_jq_j}{y} \text{ or}$$

$$W_1e_{1i} + W_2e_{2i} + \dots + W_ne_{ni} = -W_j.$$
(25)

Thus, the weighted sum of the elasticities in the j^{th} column is equal to the negative of the expenditure proportion on the j^{th} commodity.

Slutsky condition.—The Slutsky (1952) relationship incorporates a fundamental relationship between changes in quantities and the marginal utility of income. The effects of simultaneous changes in prices and income can be obtained by taking total derivatives of the first-order conditions in (7). As developed in a later section, a change in the consumption of the i^{th} commodity as a

result of a change in j^{th} commodity price can be represented as

$$\frac{\partial q_i}{\partial p_j} = \left(\frac{\partial q_i}{\partial p_j}\right)_{U=\text{const}} - q_j \left(\frac{\partial q_i}{\partial y}\right) \quad (26)$$
$$= k_{ij} - q_j \frac{\partial q_i}{\partial y}.$$

The first term on the right-hand side (k_{ij}) is the substitution effect and the second term is the income effect.

It is also shown that the compensated cross-price derivatives are symmetric.

$$\frac{\partial q_i}{\partial p_j} + q_j \left(\frac{\partial q_i}{\partial y} \right) = \frac{\partial q_j}{\partial p_i} + q_j \left(\frac{\partial q_j}{\partial y} \right). \quad (27)$$

Converting (27) into elasticities,

$$e_{ij} = \frac{w_j}{w_i} e_{ji} + w_j (e_{jy} - e_{iy}).$$
 (28)

When the price changes of the same commodity are considered, the substitution effect, $k_{ii} = \partial_{q_i}/\partial_{p_i} + q_i(\partial_{q_i}/\partial y)$, will be negative.

The demand restrictions, expressed in terms of elasticities, are summarized in table 1.

Other aspects of demand theory

A few other aspects of demand theory are summarized briefly to round out the discussion. Such aspects as multiperiod consumption decisions are not used in this study. The concept of separability used in the study is discussed in a later section.

Indirect utility indicator.—Many of the classical properties of the demand functions discussed can be derived from a dual representation of the utility indicator, often known as the indirect utility indicator. The notion of duality has become popular in recent years, especially in the framework of linear program-

TABLE 1 MATRIX OF DEMAND ELASTICITIES

	1 26							
q;	<i>p</i> 1	Pi	pa		P. a	*		
ga	£1:	617	<10		din.	¢13		
ga	¢11	612	613		#2n	629		
91 • •	6al	675	632	•••	63m	£34		
- Pn	e.,	cn.	α,		f	5 m g		

Row Restraint (Homogeneity Condition

Row Restrant (floringenerity Condition)

$$P = \sum_{j}^{i} e_{ij} + e_{iy} = 0$$
(for $i = 1$) $e_{11} + e_{12} + e_{1x} + \cdots + e_{1n} + e_{1y} = 0$
Encle Aggregation

$$\sum_{i}^{i} w_{i}e_{iy} = 1$$
($w_{i}e_{iy} + w_{2}e_{1y} + w_{2}e_{1y} + \cdots + w_{n}e_{ny} = 1$
Courned Aggregation

$$\sum_{i}^{i} w_{i}e_{ij} = -w_{i}$$
(for $j = 3$) $w_{i}e_{ij} + w_{2}e_{2} + w_{2}e_{2} + \cdots + w_{n}e_{nz} = -w_{2}$
Situlaty
 $e_{ii} = e_{ij}(w_{i}/w_{j}) + w_{i}(s_{iy} - e_{iy})$
(for $j = 3, i = 2$) $e_{2} = e_{23}(w_{2}/w_{2}) + w_{3}(e_{2y} - e_{3y})$
Substitution Effect
 $e = e_{ii} < 0$
 $e_{ii} + w_{i}e_{ij} < 0$

ming. The utility indicator, as defined earlier, is a function of quantities of commodities consumed. Also from (8), the quantity consumed of a given commodity is a function of its price, price of other commodities, and income.

$$U = U(q_1, q_2, \cdots, q_n) q_i = q_i(p_1, p_2, \cdots, p_n, y)$$

Therefore,

$$U = U[q_1(p_1, p_2, \cdots, p_n, y), q_2(p_1, p_2, \cdots, p_n, y), \cdots, q_n(p_1, p_2, \cdots, p_n, y)] = \phi(p_1, p_2, \cdots, p_n, y)$$

which is known as the indirect utility indicator. Though the existence of an utility indicator dependent upon prices and income was pointed out by Hotelling (1932), its full implications were explored only later by Court (1941), Houthakker (1952), and Samuelson (1960). The function ϕ is a dual representation of U. The properties of demand functions can be obtained from ϕ by obtaining the minimum level of expenditures necessary to reach a given level of individual satisfaction, say ϕ . That is, obtain

$$\begin{array}{ll} \underset{p}{\operatorname{Min.}} p_1 q_1 + p_2 q_2 + \cdots + p_n q_n + \\ \underset{p}{\lambda[\phi(p_1, p_2, \cdots, p_n, y) - \phi]} \\ q_i = -\lambda(\partial \phi / \partial_{p_i}) & (i = 1, 2, \cdots, n) \end{array}$$

give the first order conditions.

Considering two commodities q_i and q_{ii}

$$q_i = -\lambda \frac{\partial \phi}{\partial p_i}$$
 and
 $q_j = -\lambda \frac{\partial \phi}{\partial p_j}$.

Therefore,

$$\frac{q_i}{q_j} = \frac{\partial \phi}{\partial p_i} \bigg/ \frac{\partial \phi}{\partial p_j}$$

Samuelson (1965) provides a proof for the complete e quality of direct and indirect utility indicators.

The theory of revealed preference.— An alternative to the utility approach to demand theory is revealed preference, as originally suggested by Samuelson (1966). The consumer with a given income is placed in a market situation and his choices of baskets at different market conditions are observed. These observations reveal the consumer's preferences which serve as the basis for arriving at certain conclusions regarding the choice function of the individual.

Suppose that in a price situation $p^{0}(p_{1}^{0}, p_{2}^{0}, \dots, p_{n}^{0})$, the consumer buys

a commodity bundle q^0 . The commodity bundle q^0 is said to be preferred to an alternative bundle q^1 if, $p^0q^1 \ge p^0q^0$. In the price situation p^1 in which q^1 is bought, the q^0 basket must be at least as expensive. Therefore, $p^0q^1 \leq p^0q^0$ implies $p^{i}q^{i} \leq p^{i}q^{0}$. This is known as the weak axiom of revealed preference. Samuelson (1938) asserts that the postulates of weak axiom "is logically equivalent to the reformulation (of consumer theory) of Hicks and Allen." Arrow (1959) has demonstrated the complete equivalence of the weak axiom of revealed preference with the existence of an ordering from which the choice function can be derived.

The results of homogeneity of the demand functions of degree zero and the negativity of the substitution term (k_{ij}) can be obtained from the weak axiom. However, to prove the symmetry of the substitution term $(k_{ij} = k_{ji})$, the weak axiom has to be extended to what is known as the strong axiom of revealed preference (Houthakker, 1950). In fact, the weak axiom deals with only pairwise choices, while the strong axiom incorporates the consistency idea that if $q^0p q^1$ and $q^1p q^2$, then $q^0p q^2$. This can be extended to any number of commodity bundles. A consumer whose choices are governed by these axioms will always possess an indifference map. Further, Debreu (1965) has shown that if the preference ordering is reflexive, transitive, and the "no worse than" and "no better than" sets are closed, a continuous utility function exists. In fact, Houthakker has established the formal equivalence of the revealed preference and utility function approaches to the theory of consumer behavior by showing that "a theory based on semi-transitive revealed preference entails the existence of ordinal utility, while the property of semi-transitivity itself was derived from utility consideration."⁷ Though a few corrections are provided for Houthakker's proof, his result is still valid.

Multiperiod consumption decisions.-The choice problems discussed in the previous sections were based on decisions made for a single period of time. For the consumption of food items it may be true that the amount demanded adjusts itself within each period to the changes in prices, income, and other variables affecting demand in that period. However, for many durables adjustments may not be complete during the same period because of such factors as inertia expectations about future prices and income, and the influence of past incomes (see Stone 1954a, p. 272). Also, in the framework of a static analysis, sayings are just like any other item of expenditure, while a dynamic framework requires the introduction of borrowings and lendings which alters the individual's distribution of income over the different periods. It is possible to extend the static theory of consumer choices to a dynamic framework by introducing a multi-period utility index and budget restraint (Tintner, 1938). In this case, a multiperiod ordinal utility index can be assumed to be dependent upon the planned consumption of each commodity over the entire planning horizon. With n commodities and t time periods, the utility function can be written as

$$U = U(q_{11} \cdots q_{n1}, q_{12} \cdots q_{n2}, \dots, q_{1t} \cdots q_{nt}),$$

where

 q_{it} represents the consumption of i^{th} commodity in period t.

The consumer maximizes his utility subject to a budget restraint to obtain a demand function (Henderson and Quandt, 1958, pp. 229-234):

$$q_{jt} = D_{jt}(p_{11}\cdots p_{nt}, i_1\cdots i_{t-1})$$

where

- p_{it} is the price of i^{th} commodity during period t and
- i_t is the interest rate during period t.

Choices under uncertainty.-The choice problems discussed so far are based on the assumption that prices and income were known with certainty. However, when purchases of many durables are based on multiperiod decision processes, it may not be possible to know future prices and income with certainty. Consumer choices under stochastic situations also can be analyzed systematically using the Von Neumann and Morgenstern (1947) approach. (Also, see Friedman and Savage (1948), Luce and Raiffa (1957), and Samuelson (1952). Here, we are interested in determining the choice pattern of consumers under uncertain situations. If an individual is consistent in his preference ordering, it is possible to construct an index which describes his preference numerically. Henderson and Quandt (1958, pp. 34 -38) provide five axioms that allow construction of an ordinal utility index which can also be used to predict choices in uncertain situations. The utility numbers associated with each possible stochastic component is determined as expected values. However, choices under uncertainty involve some elements of cardinal utility, although strict cardi-

⁷ Uzawa (1959) has shown the equivalence of these two approaches, and also that the strong axiom of revealed preference can be replaced by the weak axiom if the demand functions satisfy a regularity condition. As Houthakker (1961, p. 713) points out, "The economic meaning of this (regularity) condition has not been spelled out."

nality could be avoided by taking two arbitrary starting points and successively confronting the consumer with other choice situations in order to evaluate them on a relative basis. Instead of the strict cardinal measure of utility, this involves only an operational measure of satisfaction associated with different risky situations. The marginal utility that can be derived from the utility index obtained in this manner is similar to the marginal rate of substitution.

Empirical Models of Consumer Demand

While the theory of consumer demand was being developed through the utility approach, demand characteristics based on observed consumer behavior were analyzed. In certain cases, this empirical analysis was used to test the conclusions based on the utility approach and in others to obtain meaningful theories of consumer behavior. Here are some significant highlights of these studies.

The effects of income and prices on consumption have been analyzed in many studies. One of them, using family budgets to analyze the differences in consumption by poor and rich families, led Engel to his proposition that "The poorer a family, the greater the proportion of its total expenditure that must be devoted to the purchase of food." (Stigler, 1965, p. 203). Long before data on quantity and prices were available on market performance over time, data on quantities harvested and prices prevailing at harvest period were used to arrive at an inverse relationship between these two factors.8 However, statistical analysis of demand became popular only in the current century after the pioneering attempts of Moore (1917) and Lehfeldt (1914). Stigler (1962, p. 1) points out that "Mathematical analysis became increasingly common after Walras's first edition . . . but statistical economics, the name given by Henry Moore, is the one important modern development. Henry

Moore was its founder . . . Moore's basic contribution was not to invent this field. but he made statistical estimation of economic functions an integral part of modern economics." Working's study of potatoes (1922) prompted a series of studies on individual commodity demand functions. Schultz (1938) combined a review of economic theory with a large number of empirical studies. The objective of most studies have been (1) to develop equations that can be used to forecast prices or quantities and (2) to approximate the demand curves of economic theory. Empirical studies have been facilitated by developments in data availability, improved data-processing facilities and developments in econometric theory.

The developments in the field of statistics and econometrics have made substantial contributions to demand analysis. Correlation and curve-fitting techniques have made it possible to estimate the parameters of a postulated functional relationship among prices, income, and quantities. Statistical testing procedures provide the framework for testing various hypotheses regarding the behavior of these variables. Early studies, based on least-squares estimation procedures using time-series data, were handicapped by problems like autocorrelation, multicollinearity, heteroskedasticity, and simultaneous equation

⁸ This is often recognized as Gregory King's Law that, "... a defect in harvest may raise the price" (of corn).

bias. The dilemma of applying ordinary least-squares analysis to time-series data was expressed by Working (1927) and Haavelmo (1943) but improvements have overcome at least some of these problems. Others remain in spite of advances in econometric methods.

Often studies using macro data to estimate the relationship among demand variables (quantities, price, income, and other attributes) make an implicit assumption that demand relationships, applicable to a "representative consumer" in a given area and time period, are a true representation of the consumption pattern in that area and for that period. Both time-series and crosssection data will be used in this study to analyze demand characteristics.

Cross-section analysis

Cross-section data relate to the consumption behavior of a given sample of the population at a given period of time. Early studies, based on household food consumption data from cross-section surveys, were used for estimating income elasticities. In most cases, published data on consumption patterns give the quantities of food items consumed or expenditures on these items by certain income classes. Based on these grouped data, it is possible to obtain weighted regressions to estimate the aggregate income elasticity.º A systematic application of this procedure is available in Wold and Jureen (1964, p. 216). They had four family-size groups, and each group was divided into four income classes according to annual income per consumer unit or the family unit standardized according to size and age distribution. Assuming constant income elasticity E, a regression equation of the form, $d = C y^{x}$ was fitted. (Here, d = quantity consumed and y = annual income.) Using a linear logarithmic regression, the income elasticity for the *i*th family-size group can be obtained as

$$E^{i} = \frac{\Sigma H_{*}(X_{*} - M_{z})y_{*}}{\Sigma \pi_{*}(X_{*} - M_{z})^{2}}$$
(29)

where

$$M_x=\frac{\Sigma U_v X_*}{\Sigma U_v}.$$

All summations run over four income classes,

 $N_{*} = \text{total number of households in}$ V^{th} income class,

 $C_v =$ consumer units per household,

 $U_v = N_v C_v = \text{total number of con-}$ sumer units,

- $X_* =$ logarithm of income per consumer unit, and
- $Y_* =$ logarithm of food expenditure per consumer unit.

After obtaining elasticity coefficients for the four groups, the aggregate elasticity was found, using the formula

$$E = \frac{\Sigma \mathbf{K}^{i} E^{i}}{\Sigma K^{i}} \tag{30a}$$

where

 $K^i = \Sigma H_v^i y_v^i$ and $y_v = \text{food expenditure per consumer}$ unit.

Stone's (1954) analysis of British family budgets was based on the assumption that all income changes were in the same proportion. (See also Prais and Houthakker, 1955). If q_{ir} represents the quantity of the *i*th commodity consumed by the *r*th individual and *y*, the income

⁴ For a discussion on weighted regressions see Draper and Smith (1966, pp. 77-81) and Johnston (1963, pp. 207-211). Instead of using weighted regression, it is possible to use simple regression on group averages to obtain an unbiased estimate, though the variance will differ (see Malinvaud, 1968, pp. 242-46).

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of the r^{th} individual, and if the relationship between the logarithms of q_{ir} and y_r is linear with slope b, market income elasticity is obtained by

$$\frac{b}{q_i} \sum_r q_{ir} \frac{\partial y_r}{\partial y} \frac{y}{y_r}.$$
 (30b)

Most of these studies were based on the assumption that the elasticity was constant over the whole range of observations and that income and quantities were the only relevant variables. To overcome these drawbacks, a number of modifications have been suggested. One of these is to construct a general model incorporating additional variables like family size and composition, urbanizations, regions, and other qualitative variables. Herrmann's (1964) analysis of 1955 U.S. consumption data shows that the most important variables in explaining food expenditure patterns in their order of importance are income, urbanizations, region, life-cycle stage, education of homemaker, and social class.

Another approach to explain variations of the type mentioned above is to obtain regression equations for each subgroup separately. (See Sosnick, 1962, and Foytik, 1951, for use of this procedure in estimating seasonal demand functions). The equality of these regression coefficients can be tested, using standard tests of significance. However, in many cases, when it is required to test the equality of regression coefficients for factors like regions, seasons, and urbanizations, individual regression equations may not always be appropriate because of multiplicity of equations and small number of degrees of freedom associated with each equation. Analysis of covariance techniques are useful to handle such problems.

Time series analysis

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Demand theory specifies that the

quantity consumed of a particular commodity is a function of its price, prices of other commodities, and income. This static theory of demand for the individual, with all income spent on commodities including savings, takes prices and income as "given." As will be discussed in the second part of this study, the move from the individual to market demand requires simplified assumptions to maintain essentially the same model for empirical estimation. For example, the assumption of prices as predetermined variables may be appropriate for the individual but not for the market. Stone (1954a) in the United Kingdom utilized a model paralleling the classic model mentioned above, arguing that prices were essentially determined in the world markets. On the other hand, commodity analysts in the United States have argued that, for many agricultural products, quantities available at the end of the harvesting season are essentially exogenous and that prices at farm and retail are functionally related to quantities and income-shift variables. Even for the analysis of a single commodity, it is often necessary to specify multiequation models to account for export demand, domestic demand, and stocks. The approach adopted by the analyst of time-series data depends on a great variety of questions relating to the scope of the model and problems of estimation. Here are some considerations of direct importance to the present study with its emphasis on estimation of demand at the retail level.

Single equation models.—Consider the estimation of demand function parameters for a simple model in which one commodity can be singled out for analysis. Theoretically, the following model might be specified as a first approximation:

$$q_{il} = f_i(p_{il}, z_{il}, y_i, u_{il})$$
 (31a)

where

- $q_{it} = \text{per capita consumption of the}$ i^{th} commodity,
- P_{ii} = price of the *i*th commodity,
- z_{it} = other factors affecting demand (assumed exogenous),
- $y_t = \text{per capita disposable income},$ and
- $u_{ii} = a$ random disturbance.

A number of problems arise from the estimation of the desired parameters:

Error specification. Estimation by ordinary least squares requires that the error term is not correlated with prices and income, the absence of autocorrelation, constant variance over time, and, in addition, sufficient observations in relation to the number of parameters to be estimated. When these conditions are not met, more complex formulations are required, as is discussed in texts on econometrics such as Johnston (1963), Goldberger (1964), or Malinvaud (1966).

Multicollinearity. Often prices and income move together over time, resulting in problems of multicollinearity which, in the extreme case, results in a singular matrix. In the case of income and prices, writers have suggested combining timeseries data with income slopes or elasticities estimated from cross-section data. With high multicollinearity among prices, problems exist as to the significance of coefficients. Where the goal is to approximate a complete demand matrix, other methods must be introduced.

Relevant variables. In the more general models, quantity consumed is related to all commodity prices and income which is an impossible task, when time-series data are used. The concepts of separable utility functions provide guides for meaningful methods to simplify the estimation procedures. Mathematical form of the equation. No a priori guideline exists for the functional form of the relationship among quantity, prices, and income that is appropriate in all cases. Time-series data provide only samples from a limited range of observations. Some of the commonly used functions belong to one of the following:

Linear: q = a + by + cp + u,

Semi-logarithmic:

 $q = a + b \log y + c \log p + u$, Double-logarithmic:

 $\log q = a + b \log y + c \log p + u$, or Inverse-logarithmic:

 $\log q = a + by + cp + u.$

Static versus dynamic functions. A static model, as specified in equation (31a), may be incorrect in several ways. Shifts in consumers' tastes may affect the slope or position of the demand curve; past levels of consumption may affect consumption patterns; or levels of inventory of consumer goods may be important although this is probably of minor importance for food commodities. The analyst must choose among alternative approaches, realizing the limitations inherent in any given approach.

Simultaneous equation models. In a theory of general equilibrium, the quantities consumed arc equated to the quantities produced. Similarly, the quantity consumed of a given commodity is functionally related to all commodity prices and income (or factor prices). Concentration on a demand matrix alone limits a realistic analysis of individual commodity markets. This is unfortunate but necessary within the scope of this study. However, even within the demand matrix, simultaneous relationships that are recognized are difficult to estimate.

Demand theory asserts that consump-

tion of all commodities are interrelated. But, in a single-equation approach, it is not possible to incorporate this simultaneous nature of the demand relationship and, therefore, the coefficients obtained from the single equation method will be subject to possible bias.

Different estimation procedures, like two-stage least squares, full information maximum likelihood, limited information maximum likelihood, and threestage least squares, are available for handling simultaneous estimation problems. Though a number of problems associated with simultaneous estimation procedure have been solved, there is still some doubt regarding the advantages of simultaneous equations over single equation procedures (see Christ, 1960).

The most important problem of using simultaneous equation methods for estimating demand coefficients is not one of estimation procedures but, rather, the problem of defining an identifiable model (see Hood and Koopmans 1953, Fisher 1966, and Wegge 1965). Suppose that there are *n* endogenous variables, y_1 , y_2 , \cdots , y_n and *m* exogenous variables, z_1, z_2, \cdots, z_m . A structural equation can be represented as

$$BY + CZ = U.$$

The reduced form is given by

$$Y = -B^{-1}CZ + B^{-1}U.$$

The problem of identification is one of

deducing the value of the parameters of

the structural relations from a knowledge of the reduced-form parameters. The order condition of identifiability states that the number of variables excluded from each equation must be at least as great as the number of endogeneous variables in the model less one. Therefore, in the present example, the maximum number of variables that can appear in any equation is

$$[n + m - (n - 1)] = m + 1$$

As far as the system of demand equations for all commodities are concerned, it is difficult to meet this identification criteria.

Dynamic models of demand

A number of attempts have been made to modify the static formulation of demand functions.¹⁰ Distributed lag models and recursive systems have been especially useful to incorporate some of the dynamic elements. A distributed lag model may be estimated, using any of the following three methods:

(1) Make no assumption as to the relationship among regression coefficients. Tinbergen (1951) suggested the typical form of the demand equation to be

$$q_{i} = a + b_{0}p_{i} + b_{1}p_{i-1} + \cdots + b_{i}p_{0}$$
(31b)
$$= a + \sum_{p=0}^{\infty} b_{i}p_{i-1}$$

where

- q_t is the quantity demanded in period t and
- P_{t-i} is the price in period (t i).

Here, we do not make any assumption

¹⁰ Bieri (1966) classifies different approaches to incorporate time into demand analysis as: (1) models introducing the time dimension through dating of the variables in the utility function (Henderson and Quandt, 1958; Modigliani and Brumberg, 1954; and Strotz, 1956; (2) models introducing dynamic aspects into demand function (Houthakker and Taylor, 1966; Nerlove, 1958b; and Farrell, 1952; and (3) models introducing dynamic aspects into the utility function (Cramer, 1957; Stone, 1954; Stone, et al., 1964; Basmann, 1956; and Tsujimurs and Sato, 1964).

regarding the relationship among b_i . No restriction is imposed on the distribution of the lag effect of past prices on the quantity demanded. In practice, lagged prices will be added successively to the least-squares regression of quantity on prices until the coefficients become insignificant or the signs become erratic. (2) Assume a general form for the distribution of lag and estimate the parameters. Fisher (1925) and Koyck (1954) have suggested that the form of the distribution of the lag may be approximately assumed and then the specific characteristics of the distribution may be estimated. If time is treated as a continuous variable, the demand relationship is

$$q_{\iota} = a + \int_{0}^{\infty} b(u) P(t-u) du. \qquad (32)$$

Koyck calls the distribution of b(u) the "time shape of an economic reaction" and the cumulative distribution of b(u)"the adjustment path." The distribution of b(u) can be assumed; for example, Fisher assumed a logarithmic normal distribution. (3) Develop an explicit dynamic model which implies the distributed lag only incidentally. This approach is basically similar to Nerlove's (1958b) static expectation model. The current quantity consumed will change in proportion to the long-run equilibrium quantity and current quantity.

$$q_i - q_{i-1} = \gamma(\bar{q}_i - q_{i-1})$$
 (33)

where

 q_t is the quantity consumed in period t, \bar{q}_t is the quantity demanded in longrun equilibrium, and

 γ is a constant of proportionality.

Nerlove (1958b, p. 308) compares these three approaches as follows:

"Because of the finite length of, and degree of auto-correlation in most economic time series, the first approach where nothing is assumed is not always feasible. On the other hand, the second approach must necessarily contain a somewhat arbitrary assumption concerning the form of the distribution of lag. The third approach leads to a direct interpretation of the distribution of lag in terms of producer or consumer behavior and, therefore, in terms of the difference between short- and long-run elasticities of supply or demand."

Models combining cross-section and time-series data

Because both time-series and crosssection analysis have certain inherent disadvantages, attempts have been made to supplement one method with the other. The "conditional regression analysis" used by Wold and Jureen (1964) and The "extraneous estimators" used by Stone (1954a) are based on the utilization of income elasticities obtained from budget studies in conjunction with time-series data.¹¹ Goureux's (1960) analysis of consumption behavior, based on data derived from household surveys and time series of national averages, consisted of three kinds of comparisons: (1) household surveys, consumption of households at a given period; (2) international comparisons, average consumption in different countries at a given period : and (3) time series, change in the average consumption over the last decade. To estimate regional and sectoral demand characteristics, analysis of covariance can be used effectively. Hoch (1962), Mundlak (1961 and 1963), and Paris and Hoch (1966) have used this approach for estimating productionfunction parameters. Balestra and Nerlove (1966) and Ben-David and Tomek

¹¹ Durbin (1953) explains a procedure for handling extraneous information. Kuh and Meyer (1957) warn against giving undue importance to extraneous estimation procedures. Also see Kuh (1959).

(1965) have applied similar approaches for estimating demand functions.

Mundlak model.—Assume that there are observations on quantity, price, and income from m regions for t periods. If the regression coefficients in all regions are the same and if regional characteristics can be isolated, the demand function can be written as

$$q_{t}^{(r)} = B_{0} + B_{l}P_{1t}^{(r)} + \cdots + B_{k}P_{kt}^{(r)} + B_{\nu}Y^{(r)} + CR^{(r)} + er^{t}$$
(34)

where

 $q_t^{(r)} =$ quantity demanded in region r during period t, $p_{it}^{(r)} =$ price of commodity, i, in region r during period t, $R^{(r)} =$ regional effect in region r, (commodity) $i = 1, 2, \dots, k$, (region) $r = 1, 2, \dots, m$, and (period) $t = 1, 2, \dots, t$.

The usual procedure in cross-section data is to fit a regression to data collected for regions at a period of time, ignoring the contribution of regional factors, $CR^{(r)}$. When we are interested in regional variations also, we obtain the estimates by minimizing the sum of squares

$$S = \sum_{r} \sum_{t} (q_{t}^{(r)} - B_{0} - B_{1}P_{1t}^{(r)} - B_{k}P_{kt}^{(r)} - B_{k}Y_{kt}^{(r)} - B_{y}Y^{(r)} - A^{(r)})^{2}$$
(35)

where

$$A^{(r)} = CR^{(r)}.$$

If the demand function is complete,

$$\hat{C} = 1 - \sum_{j} \hat{\beta}_{j}$$
. Therefore, $\hat{R}_{i} = A^{(r)} / \hat{C}$, which gives an estimate of regional effect.

Ben-David and Tomek model.—If the regression coefficients take different values for different regions, the following model can be used:

$$q_{t}^{(r)} = a_{0} + \sum_{j=1}^{m} a_{j} D_{jt}^{(r)} + b_{0} P_{t}^{(r)} + \sum_{j=1}^{m} b_{j} S_{jt}^{(r)} + U_{t}^{(r)}$$
(36)

where

$$r = j = 1, 2, \dots, m,$$

$$t = 1, 2, \dots, t,$$

$$q = \text{endogenous variable,}$$

$$P = \text{exogenous variable,}$$

$$D_j = \text{intercept-shifting variable}$$

with

$$p_j^{(r)} = \begin{cases} 1, \text{ when } r = j, \\ 0, \text{ when } r \neq j, \end{cases}$$

$$S_j = \text{slope containing dummy variables, with}$$

$$S_{ji}^{(r)} = D_{ji}^{(r)} P_i^{(r)} = \begin{cases} P_i^{(r)}, \text{ when } r = j \\ 0, \text{ when } r \neq j \end{cases}.$$

The above equation can be estimated, using certain assumptions, and the equality of regression coefficients can be tested. Also, these models can be generalized to handle variations in both slopes and intercepts of demand over different regions.

Shifts over time

The time-series analysis assumes that the structure of demand and the values of coefficients remain stable over the period under consideration. It is possible that the structure over time may gradually change. The effect of such shifts on demand coefficients have been recognized (see Daly, 1956). If the change in structure is clearly identifiable, a shift variable can be introduced in the regression equation. One possible method of identifying shifts may be through a preliminary graphical analysis. Shift variables could be introduced in the demand function through dummy variables whose values are one and zero, depending upon the period of observation. According to Rojko (1961, p. 44), another way to handle changes in structure is to break the period into subperiods during which no change in structure has occurred. One difficulty with this approach is that the number of observations per subperiod may be small for statistical analysis.

Introducing time as an explicit variable in the demand equation is another feasible approach. The coefficient of time may absorb most of the unexplained variations and an interpretation of the coefficient may become difficult. Sometimes, time-series and cross-section data may be combined to analyze the secular and cyclical changes of demand. (For example, see Douglas, 1967.)

Foytik (1951) suggests two alternative methods that could be used to allow for systematic shifts in the regression coefficients over time. The first approach is essentially the same as fitting separate demand functions for each period and the second approach considers all weekly observations together and estimates an equation of the form:

$$P_{i} = a + (b + b'w)Q_{i} + (C + C'w)D_{i}$$
$$+ (d + d'w)Q_{i-1}$$
$$+ (e + e'w)W \qquad (37)$$
where

i = w = week of season, P = price,

Q = quantity sold, and

D =consumer income.

To find out whether the demand equation changed systematically over time, the coefficients b', c', d', and e' were tested to see whether they differed significantly from zero.

Though the above approaches can be "used to study the shifts over time of a single commodity, they may not be sufficient to analyze stochastic elements in consumer behavior. Barten (1966) has specified a model which takes into account the shifts in utility function over time. Rosenberg (1968) provides different approaches to incorporate stochastic variations among parameters during the period of observation. However, certain conceptual and empirical problems are yet to be solved before such procedures can be applied to a large number of commodities.

The Gap Between Demand Theory and Empirical Analysis

In theoretical development, we specify certain postulates and deduce the behavior of the variables through logic. In contrast, empirical studies deal with quantifiable phenomena. Often theoretical developments and empirical analysis complement each other—empirical analysis can be used to verify the validity of certain theories. Sometimes certain theories are reached by starting from an empirical analysis. In the field of demand analysis, econometricians have often built empirical models based on the significance of economic variables like prices and quantities, and justified their findings through economic theory. On the other hand, some models in consumption theory are not subject to

empirical verification because of deficiencies in data or in statistical procedures. As a result of this, we are faced with a situation of ". . . insufficient predictive power, inappropriate basis for empirical analysis, and difficulties in establishing empirical confrontation . . ." (deJanvry, 1968, p. 4) which is often referred to as "the gap between theory and empirical analysis." This section describes attempts to bridge this gap and, also, points out certain difficulties encountered in the process. The discussion of concepts of separability owes much to the excellent treatment in deJanvry's (1966) award-winning thesis.

The fact that, according to economic theory, consumption of a particular commodity is dependent upon its price. prices of other commodities, and income. suggests that the demand for all commodities are interrelated and that any empirical study should consider the demand for all commodities simultaneously. If there are n commodities, this involves $(n \times n)$ price elasticities and n income elasticities for a total of n(n + 1)parameters to be estimated. For the model to be estimable by known techniques, the number of observations should be at least equal to the number of parameters to be estimated which, in this case, is n(n + 1). When a large number of commodities are considered. this condition cannot be satisfied and we run into the so-called "problem of degrees of freedom." (For further discussion, see deJanvry and Bieri, 1968; Clarkson, 1963; Mishan, 1961; and Boutwell and Simmons, 1968.) If we impose the restrictions on consumer demand, the number of parameters to be estimated directly can be reduced. The symmetry condition provides n[(n-1)/2]restrictions, the homogeneity condition provides n restrictions, and the Engel aggregation provides one restriction for a total of $n[(n-1)/2] + n + 1 = (n^2 + n + 2)/2$ restrictions. Therefore, the number of parameters to be estimated independently is reduced to

$$n(n + 1) - \frac{(n^2 + n + 2)}{2} = \frac{1}{2}(n^2 + n - 2)$$

which still remains to be a big number to permit direct estimation of a system of equations involving large numbers of commodities. Realizing this difficulty, two different approaches have been adopted—a single commodity or a subsector analysis, and the "integrationist's approach" (Boutwell, 1965, p. 8).

Single commodity or sector models

A single equation is formulated for a commodity to estimate the direct price and a few other cross-price elasticities. The effect of all other omitted variables is implied to be zero. The choice of other prices to be included is often based on subjective judgments of researchers. Also, the number of parameters to be included in each equation depends upon the required number of degrees of freedom which can be increased either through increasing the number of observations or through decreasing the number of parameters in the equation. The number of observations can be increased by extending the period of observation or reducing the interval between successive observations in the case of time series data, and enlarging the sample space in the case of cross-section data, In general, the effect of using enlarged time-series and cross-section data is to increase the variability in the data and it may be important to test whether any structural change or heterogeneity has occurred in the process of enlargement. The number of parameters in the model can be reduced by defining composite

commodities. Although the estimation problem can be solved by aggregating commodities, this procedure introduces a number of "aggregation problems." Also, for policy analysis, often information on individual commodities is required and an aggregate derived from heterogeneous items may not reflect the characteristics of individual commodities belonging to the set.

The "integrationist's approach"

The integrationist's approach recognizes the interrelationships among all commodities. To overcome the problems of degrees of freedom and identification, a number of assumptions regarding the interaction of commodities and the nature of utility functions are introduced. Also, attempts are made to incorporate the theoretical restrictions into the statistical model. Strotz' (1957. 1959) utility tree and Houthakker's (1960) additive preferences and various forms of separability ideas belong to this group. Frisch (1959) in a pioneering article, proposed that the demand relationships derived from utility theory could be used in computing all direct price and cross elasticities under an assumption of want independence.

Frisch model.--Frisch considers the implications for estimation of a matrix of demand coefficients for the case in which the utility of some or all commodifies are independent of the quantity of others. The idea of want independence is explained by Frisch (1959, p. 178) by referring to commodities where, for example, ". . . the marginal utility of using more electricity in the home can safely be regarded as independent of the quantity of Swiss cheese consumed." Similarly, he discusses the case where commodity groups may be want independent, but dependence is assumed among commodities within a group. The major argument is for the case of want-independent commodities and can be compared with the classical case in which the Slutsky relation is given as

$$e_{ij} = e_{ji} \frac{w_j}{w_i} + w_j (e_{iy} - e_{iy}).$$
 (38)

The Frisch statement of this relation expresses price elasticities (e_{ij}) as a function of want elasticity (σ_{ij}) , budget proportions (w_i) , income elasticities (e_{iy}) , and the flexibility of the marginal utility of income with respect to income (ϕ) .

$$e_{ij} = \sigma_{ij} - w_j e_{ij} - \frac{1}{\phi} w_j e_{ij} e_{ij} \qquad (39)$$

where

$$\sigma_{ij} = \frac{\partial q_1(u_i, u_2, \cdots, u_n)}{\partial u_j} \cdot \frac{u_j}{q_i} \quad \text{(want elasticity) and}$$

$$\phi = \frac{\partial \lambda}{\partial y} \cdot \frac{y}{\lambda} \quad (\text{money flexibility}).$$

For income elasticities, the conventional row restraint, or Slutsky-Schultz condition, is that the elasticities for prices and income sum to zero, or

$$-e_{iy} = \sum_{j} e_{ij} \qquad (40)$$
$$(i, j = 1^{-} \cdots, n)$$

The Frisch statement in terms of want elasticities and the money flexibility coefficient is

$$e_{ig} = \phi \sum_{j} \sigma_{ij} . \qquad (41)$$

Consider the case where a good is want

independent of all other goods, or where income clasticities may then be ex- $\sigma_{ij} = 0$ for all $i \neq j$. The cross-price and pressed as

$$e_{ij} = -w_j e_{iy} - \frac{1}{\phi} w_j e_{jy} e_{iy},$$
 (42)

$$= -e_{iy}w_j\left(1 + \frac{e_{jy}}{\phi}\right), \quad (\text{cross-price elasticity}), \text{ and}$$
(43)

 $e_{in} = \phi \sigma_{ii}$ (income elasticity).

To obtain the direct price elasticity σ_{ii} in equation (43), substitute the term under want independence, we solve for in equation (42), and obtain

$$e_{ii} = \frac{e_{iy}}{\phi} + w_i e_{iy} - \frac{1}{\phi} w_i e_{ig} e_{ig},$$

$$= -e_{ig} w_i - \frac{1 - w_i e_{iy}}{\phi}$$
 (own price elasticity). (44)

Under want independence, we may solve for ϕ , or

$$\phi = \frac{e_{iy} - w_i e_{iy} e_{iy}}{e_{ii} + w_i e_{iy}} \quad \text{(money flexibility)}. \tag{45}$$

If a value of ϕ is known, equation (42) may be used to obtain estimates of cross elasticities under the assumption of want independence ($\sigma_{ij} = 0$). Money flexibility may be estimated from equation (45) for any commodity where the directprice and income elasticity coefficients are known. Further, estimates for various commodities or commodity groups should provide similar values of ϕ if the assumption of want independence is valid. Thus, if we know all income elasticities, expenditure weights, and directprice elasticities for a single commodity, all the remaining parameters can be derived.

The assumption of want independence for all commodities implies complete additivity of the direct utility function, or

$$u(q_1, q_2, \cdots, q_n) = u_1(q_1)$$

$$+ u_2(q_2) + \cdots + u_n(q_n).$$
(46)

Houthakker (1960) refers to this case of independent utilities as "direct additivity" and shows that the cross derivatives of demand are proportional to the derivatives with respect to income. Thus, under independent utilities, the commodities are still related through the budget restraint but with demand interrelationships of a much less complex form than with conventional theory when complete dependence is allowed. Barten (1964, 1967) suggests a model incorporating a weaker assumption on the utility function, with complete additivity replaced by conditions of "almost additive preferences." For a detailed comparison of the Hicks, the Frisch, and the Barten models, see Appendix B.

Barten model.—The essential contribution of Barten's model is to develop methods of estimating demand functions with somewhat less restrictive conditions being imposed on the preference function. Consider the Hessian matrix U in which elements are $U_{ij} = \partial^2 U/(\partial q_i \partial q_j)$. For the Frisch case of want independence for all commodities, the Hessian matrix has zeros except for diagonal elements. The Hicks matrix would allow values in all cells. Barten would limit values to diagonal elements plus certain nondiagonal elements of a nature that the consumer's preferences are "almost additive." The term for a cross-price elasticity for Barten is of the form

$$e_{ij} = \frac{p_j}{q_i} U_{ij}^{-1} - w_j e_{ij} \left(1 + \frac{e_{ij}}{\phi} \right).$$
 (47)

For Frisch, the first term on the right of the equality is σ_{ij} ; otherwise, the equations are identical. Barten's formulation incorporates a term (U_{ij}^{i}) that is invariant under transformations whereas the Frisch term (σ_{ij}) is not. For practical considerations, these two derivations can be considered as equivalent as pointed out by Ayanian (1969).

For estimation purposes, Barten specifies a regression equation of the form

$$\Delta \log q_i^{(t)} = \alpha_i + \sum_{j=1}^n \left(\epsilon_{ij} - \frac{1}{\phi} e_{ij} e_{jj} w_j - e_{ij} w_j \right) \Delta \log p_j^{(t)} + e_{ij} \Delta \log y(t) + u_j(t)$$

$$(48)$$

where the constant term represents trend due to changes in tastes or other factors, ϵ_{ij} represents that part of the substitution effect that is directly related to the interaction of commodities in the utility function, the compound term (money flexibility, budget proportion, and income elasticities) represents the remaining substitution effects, e_{iy} the income elasticity, and u_i a random error term. The first difference of logarithmic specification is justified on pragmatic grounds. Details of the estimation procedures are available in Barten (1964).

A different approach to the complete additivity assumption used in Frisch's formulation and to the almost additivity assumption used in Barten's formulation is obtained by introducing different concepts of separability, developed from the "utility tree" concept discussed by Strotz (1957, 1959).

The role of separability in demand analysis

The concept of a utility tree.-The

basic idea is that the elements belonging to the commodity bundle can be partitioned into different groups (similar to the branches of a tree). It is assumed that consumers follow a budget allocation process in such a way that, in the first stage, the total expenditure is divided into different subgroups and then, at the second stage, the amount allotted to each subgroup is allotted to individual commodities belonging to that subgroup. In other words, consumers follow a two-stage budgeting process by which total expenditure is first split into group expenditures at the first stage and then each group expenditure is split into individual commodity expenditures at the second stage. According to this procedure, it is possible to calculate all the parameters involved in the system of demand equations from a knowledge of certain parameters.

To permit the use of the two-stage allocation process, the utility function must satisfy certain properties. Strotz starts with the classical utility function $U(q_1, q_2, \cdots, q_n)$ and assumes that it is separable in the branches 1, 2, \cdots , s if it can be written as¹²

$$U = F[U^{1}(q^{1}) + U^{2}(q^{2}) + \cdots + U^{4}(q^{4})]$$
(49)

where

$$U^{i}(q^{i}) = U^{i}(q_{1}^{i}, q_{2}^{i}, \cdots, q_{n_{i}}^{i})$$

 n_i = number of commodities in the i^{th} group such that $n_1 + n_2 + \cdots + n_s = n.$

As usual, maximizing this utility function subject to the budget restriction

$$\sum_{i=1}^n p_i q_i = y^i,$$

$$q_{j}^{(i)} = \alpha_{j}^{(i)} + \sum_{i \in I} \beta_{ji}^{(i)} P_{i}$$

$$+ \sum_{k \in I} \beta_{jk}^{(i)} P_{k} + \gamma_{j}^{(i)} y \qquad (50)$$

where

- $q_j^{(i)} = j^{\text{th}}$ commodity belonging to the i^{th} commodity group,
 - $j = 1, 2, \dots, n_i$, and $i = 1, 2, \dots, s$.

Taking two commodities belonging to the same group, the relationship can be written as

$$q_{j_{k}}^{(i)} = \alpha_{j_{k}}^{(i)} + \sum_{i \in I} \beta_{j_{k}i}^{(i)} P_{i} + \sum_{k \in I} \beta_{j_{k}k}^{(i)} P_{k} + \gamma_{j_{k}}^{(i)} y$$

$$q_{j_{k}}^{(i)} = \alpha_{j_{k}}^{(i)} + \sum_{i \in I} \beta_{j_{k}i}^{(i)} P_{i} + \sum_{k \in I} \beta_{j_{k}k}^{(i)} P_{k} + \gamma_{j_{k}}^{(i)} y$$
(51)

for any such two commodities belonging to a group, the coefficients $\beta_{j,k}^{(i)}$ and $\beta_{j,k}^{(i)}$ will be in fixed proportion for k not in branch *i*. Strotz has shown that the ratio of such price slopes is equal to the ratio of income slopes, $\gamma_{i_1}^{(i)}/\gamma_{i_1}^{(i)}$. Therefore,

$$\frac{\boldsymbol{\beta}_{j_1k_1}^{(i)}}{\boldsymbol{\beta}_{j_2k_1}^{(i)}} = \frac{\boldsymbol{\beta}_{j_2k_2}^{(i)}}{\boldsymbol{\beta}_{j_2k_1}^{(i)}} = \frac{\boldsymbol{\beta}_{j_2k_2}^{(i)}}{\boldsymbol{\beta}_{j_2k_2}^{(i)}} = \frac{\boldsymbol{\gamma}_{j_1}^{(i)}}{\boldsymbol{\gamma}_{j_2}^{(i)}} \qquad (k_1, k_2, \cdots, gI).$$
(52)

Using the relationship (52), a number of parameters in the system of demand equations can be calculated with the knowledge of income coefficients and at least one other interbranch coefficient.

Concepts of separability.—To separate commodities in the utility function, the ratio of marginal utilities of a pair

of commodities i and j is assumed to be unaffected by the level of consumption of a third commodity k. In other words, it can be assumed that

$$\frac{\partial \frac{U_i}{U_j}}{\partial q_k} = 0 \text{ for } k \neq i, j$$
(53)

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¹⁷ This is the "strong" definition of a separable utility function. Strotz admitted that, in his original formulation, he had defined a weak form of separable utility function, though his results were derived based on this strong form of separability (see Strotz, 1959). Expressing the utility function in this manner implies additivity among groups.

holds for at least some of the goods. While the concept of complete additivity used by Frisch assumes that the marginal utilities of i and j are unaffected, the concept of separability assumes that the marginal utilities are changed equally because of a change in the consumption of the k^{th} commodity. Depending on the assumptions, four types of separability can be defined.

Weak separability. This concept implies that the utility function can be divided into subgroups such that the marginal rate of substitution between two commodities i and j from the same group (g) is independent of the quantities of commodities not belonging to group g. That is

$$\frac{\partial \frac{U_i}{U_j}}{\partial q_k} = 0 \tag{54}$$

for all $i, j \in \text{group } g$ and $k \notin \text{group } g$. Goldman and Uzawa (1964) have shown that the utility function $U(q_1 \cdots q_n)$ is weakly separable with respect to a grouping of the n commodities into a class of s mutually exclusive and exhaustive subgroups (with n_1, n_2, \cdots, n_r commodities in each of the s groups respectively) if, and only if, the utility function is of the non-additive form

$$U(q_{1} \cdots q_{n}) = F[U^{1}(q^{1}),$$

$$U^{2}(q^{2}), \cdots, U^{4}(q^{4})]$$
(55)

where

$$U^{i}(q^{i}) = U^{i}(q_{1}^{i}, q_{2}^{i}, \cdots, q_{n_{i}}^{i}); i = 1, 2, \cdots, s; \text{ and } n_{1} + n_{2} + \cdots + n_{i} = N_{i}$$

Weak homogeneous separability. Green (1964) adds one property to the weak separability concept—that each subgroup is homogeneous of degree one. In other words,

$$U(q_1^i, q_2^i, \cdots, q_n^i)$$

is homogeneous of degree one for all i.

Strong separability implies that the utility function can be partitioned into subgroups such that the marginal rate of substitution between two commodities i and j from two different subsets does not depend upon the quantities of commodities that do not belong to the same groups as i and j.

$$\frac{\partial U_i}{U_j}{\partial q_k} = 0 \tag{56}$$

for all $k \in \text{group } g$; *i* from group *m*, and *j* from group *s*.

Strong separability is applicable only to those utility functions which are additive among groups.

$$U(q_{1}\cdots q_{n}) = F[U^{1}(q^{1}) + U^{2}(q^{2}) + \cdots + U^{*}(q^{*})].$$
(57)

Earlier it was shown that strong separability was required for the establishment of the concept of a utility tree.

Pearce separability. Pearce introduced the concept of neutral association which has been later referred to as "Pearce Separability" by Goldman and Uzawa (1964). Pearce defined the existence of neutral want association between goods i and j and good k if the marginal rate of substitution between two commodities i and j from the same subset is independent of the quantities of all other commodities.

$$\frac{\partial \frac{U_i}{U_j}}{\partial q_k} = 0; \qquad (58)$$

 $i, j \in \text{group } g \text{ and } k \neq i, j.$

$$U(q_{1} \cdots q_{n}) = U\{U^{i}[f_{1}^{i}(q_{1}^{i}) + \cdots + f_{n_{i}}^{i}(q_{n_{i}}^{i})] + \cdots + U^{i}[f_{1}^{i}(q_{1}^{i}) + \cdots + f_{n_{i}}^{i}(q_{n_{i}}^{i})]\}.$$
(59)

From the description of Pearce separability, it is evident that it includes both weak separability and strong separaability.

The two-stage maximization process.—Imposition of the assumption of separability reduces the number of parameters to be estimated directly. Suppose that there are *n* commodities belonging to *s* separable groups. In the first stage, the total expenditure *y* has to be alloted among the *s* commodity groups. Let y_1, y_2, \dots, y_s represent the amounts spent on different groups $(y = y_1 + y_2 + \dots + y_s)$. Therefore, the first stage is to determine y_1, y_2, \dots, y_s such that the utility is maximized. That is,

$$U(y_1, y_2, \cdots, y_n) = \lambda(\sum_{i=1}^n y_i - y)$$

should be a maximum. As usual, the first order conditions are

$$\frac{\partial U}{\partial y_i} - \lambda = 0 \quad \text{and} \qquad (60)$$

$$\sum_{i=1}^{r} y_i - y = 0 \qquad (i = 1, 2, \cdots, s).$$

Equations (60) presumably can be solved to obtain the group expenditures y_1, y_2, \dots, y_s . But expenditures for a particular group is a function of the group price indices P_1, P_2, \dots, P_s . Therefore, the solutions obtained from (60) can be written as a function of group price indices and income

This implies that any two commodities from the same group should be in neutral want association with all other commodities in that group. Under Pearce separability, the utility function $U(q_1)$

 $\cdots a_n$) should be separated into a form

$$y_{i} = y_{i}(P_{1}, P_{2}, \cdots, P_{s}, y)$$

$$(i = 1, 2, \cdots, s).$$
(61)

Thus, at the end of the first stage, the group expenditures are expressed as a function of price indices of all groups.

In the second stage,

$$U^i(q_1^i, q_2^i, \cdots, q_{n_i}^i)$$

is maximized for all groups *i* subject to the restriction that group expenditures equal the amount determined at the first stage. That is,

$$U^{i}(q_{1}^{i}, q_{2}^{i}, \cdots, q_{n_{i}}^{i}) + \lambda_{i} (\sum_{j=1}^{n_{i}} P_{j}^{i} q_{j}^{i} - Y_{i})$$

should be maximized. Taking the first order conditions and solving for the quantities,

$$q_{j}^{i} = q_{j}^{i}[P_{1}^{i}, P_{2}^{i}, \cdots, P_{n_{i}}^{i},$$

$$y_{i}(P_{1}, P_{2}, \cdots, P_{n}, y)]$$
for all $j = 1, 2, \cdots, n_{i}$
 $i = 1, 2, \cdots, s.$
(62)

Thus all the demand equations can be specified.

Under certain conditions the twostage maximizations of a separable utility function provide the same equilibrium solutions as direct maximization. Gorman (1959) and Green (1964, p. 22). have provided the conditions under which two-stage maximization is consistent. Accordingly, two-stage maximization of a utility function will be consistent if the weak separability conditions are satisfied together with any one of the following conditions: (1) only two groups exist, (2) strong separability exists, (3) weak homogeneity conditions are satisfied, (4) all functions U^i except one (say the first) are homogeneous and U can be written as

$$U = U[U^{1}, \phi(U^{2}, U^{3}, \cdots, U^{s})];$$
 and

(5) the functions U^i beyond *m* are homogeneous and *U* can be written as

$$U = U[U^{1} + U^{2} + \dots + U^{m} + H(U^{m+1}, \dots, U^{t})].$$

When the two-stage maximization is consistent, the maximum levels of utility reached by direct and two-stage maximization should be the same. It is possible to extend the concept of twostage maximizations to a number of stages, if necessary.

Identifying separable groups.—So far it was assumed that it will be possible to identify separable groups. In actual practice, it will not be possible to look upon the marginal utilities to determine the nature of separability; deJanvry has demonstrated the use of factor and cluster analysis to identify homogeneous groups. However, the grouping obtained through factor analysis may not be unique because the criteria for obtaining the groupings are, to some extent, based on value judgments.

Practical considerations

Attempts to bridge the gap between demand theory and empirical work have often run into difficulties because of the restrictive assumptions used in the theory and the inadequate nature of the data. More specifically, we run into difficulties regarding the concept of demand, its time dimension and aggregation problems, marketing margins, and the nature of recorded data, all of which are discussed below.

Concept of demand.—As Baumol (1965, p. 210) points out, "Demand functions, as they are defined in economic analysis are queer creatures, somewhat abstract, containing generous elements of the hypothetical and, in general, marked by an aura of unreality." Although the Walras-Pareto-Hicks concept of demand serves as a basis for defining demand in pure economic theory, it is not adapted to the measurement of demand for statistical analysis.

The relationship between price and quantity through demand functions provides answers to questions like, "What would consumers do if price were different from the present level?" In static analysis, a demand relationship is specified for a particular period of time. In practice, each time an observation is made, we get one point on a demand curve and, by the time another observation is made, the curve might have shifted because consumer tastes have changed or for other reasons influencing demand. These shifts may influence the nature of functions obtained from timeseries analysis and, at times, it will be difficult to isolate the effects of such shift variables from purely economic variables such as prices and income. Sometimes this difficulty may lead to the conclusion that economic variables may not be significant factors in explain-

ing demand. An example of this type is obtained in Prest's (1949) analysis of consumption patterns in the United Kingdom for 1870-1938 where only 1 per cent of the variance of the consumption of tea and tobacco was explained by income and price. Farrell (1952) explains Prest's results in terms of irreversible demand functions. He assumes, "That a man who has been induced by a rise in income or a fall in the price of tobacco to take up smoking, or to smoke heavily, will form a habit, and will not, when prices or income returns to its former level, cut his consumption to the former level." Often irreversibility will tend to be a matter of differential lags. For example, Goodwin, et al. (1968) derive irreversible demand functions for beef with different lagged-response coefficients for the increasing and decreasing phases of a consumption cycle.

Aggregation.-According to Green (1964, p. 1), "Aggregation is a process whereby a part of the information available for the solution of a problem is sacrificed for the purpose of making the problem more easily manageable." Most of the demand relationships specified earlier apply to an individual consumer with a given income facing given market conditions. But, in empirical work, the behavior of a single consumer (in a perfectly competitive market) is not interesting; we study the behavior of the market which is an aggregation of all individual consumers. Therefore, we are faced with the question of deriving theories on aggregate (macro) relationships based on individual (micro) relationships. In particular, it is necessary to specify a consistent procedure for aggregation and then determine the nature of the aggregation bias involved in the procedure adopted. Green (1964, p. 1) defines aggregation to be consistent,

"... when the use of information more detailed than that contained in the aggregates would make no difference to the results of the analysis of the problem at hand." On aggregation bias, Grunfeld and Griliches (1960, p. 1) argue that aggregation may sometimes reduce the specification error and thus bring some gain in accuracy. According to them,

"... in practice we do not know enough about micro behavior to be able to specify micro equations perfectly. Hence empirically estimated miero relations, whether those of individual consumers or of individual producers, should not be assumed to be perfectly specified either in an economic sense or in a statistical sense. Aggregation of economic variables can, and in fact, frequently does, reduce these specification errors. Hence, aggregation does not only produce an aggregation error, but may also produce an aggregation gain."

Theil's (1954) work on linear aggregation is one of the early systematic approaches adopted. Allen (1964, Ch. 20) discusses the case of (1) aggregation over individuals, (2) aggregation over individuals and commodities. Theil (1959, p. 14) points out that, ". . broadly speaking, if linear micro relations are aggregated in terms of linear aggregates to a linear macro relation, the resulting macro parameters are weighted sums of all micro parameters." Here, we shall illustrate this problem using some simple examples.

Aggregation over individuals. Earlier it was deduced that an individual's demand for a commodity is a function of the price of the commodity, price of other commodities, and income. Assuming a linear relationship, the demand for a commodity for the j^{th} individual can be written as

$$q_{ij} = a_{ij} + \sum_{i} b_i p_i + c_j y_j$$
 (63)

where

 q_{ij} = quantity of *i*th commodity demanded by *j*th individual, p_i = price of *i*th commodity, and y_j = income of *j*th individual.

In a given market situation, it can be assumed that the price is the same for all individuals and that only income is variable. Under this simplifying assumption, (63) can be written as

$$q_{ij} = a_{ij} + c_j y_j.$$
 (64)

If we specify an aggregate relation of the form

$$q_i = a_i + cy \tag{65}$$

between aggregate demand q_i and aggregate income y, the problem of aggregation is to find a consistent method of relating (64) and (65).

Summing (64) over all individuals,

$$\sum_{j=1}^{n} q_{ij} = \sum_{j} a_{ij} + \sum_{j} c_{j} y_{j}.$$
 (66a)

To establish a relationship between yand individual incomes, let us define the mean value of micro slopes (marginal propensity to consume) as

$$\bar{c} = \frac{1}{n} \Sigma c_j. \tag{66b}$$

Now let us define the aggregate income y as the sum of individual marginal propensity to consume multiplied by individual income, divided by the mean value of the micro slopes, or

$$y = \frac{1}{\bar{c}} \sum_{j}^{c} c_{j} y_{j}. \tag{67}$$

$$y = \frac{n}{\Sigma c_j} \Sigma c_j y_j$$
 (from 66b and 67). (68)

From (65) and (68), we obtain

 $q_i = a_i + \frac{c}{\bar{c}} \sum_j c_j y_j. \tag{69}$

Comparing (66) and (69), we get a consistent aggregation if

$$q_{i} = \sum_{j=1}^{n} q_{ij}$$

$$a_{i} = \sum_{j} a_{ij}, \text{ and } \qquad (70)$$

$$\frac{c_{i}}{\bar{c}} = 1, \text{ or } c = \bar{c} = \frac{1}{n} \Sigma c_{j}.$$

From (70), it is clear that the aggregate quantity is the sum of individual quantities, the intercept of the aggregate relationship is the sum of individual intercepts, and the aggregate marginal propensity to consume is the average of individual marginal propensities. Aggregate income is defined as a weighted average of individual incomes, the weights being proportional to the individual marginal propensities and, therefore, the aggregate income, as defined here, will differ from commodity to commodity. However, this is only one form of aggregation-other approaches are available in Allen (1964), Stone (1954), and Wold and Jureen (1964).

Aggregation over commodities. Often it will be required to aggregate individual commodities to commodity groups or it may be that a given commodity appears in different forms or varieties and it will be difficult to handle all varieties separately. In such cases, it is necessary to aggregate over commodities. To consider a simple example, suppose that there is only one individual in the market facing k varieties of a given commodity. The demand relationship, ignoring other prices for simplification, can be written as

$$q_j = a_j + b_j p_j \tag{71}$$

where

 $q_j =$ quantity of j^{th} variety demanded and

$$p_i = \text{price of } j^{\text{th}} \text{ variety.}$$

When different varieties of the same commodity are considered, quantity and prices are in comparable units and they can be aggregated, as in the case of different individuals in the previous example. The only difference is that, instead of summing over individuals, here, summation is over varieties.

When it is necessary to add up a mixed bag of commodities, the homogeneity property is no longer valid and it is not possible to add up the quantities or prices. In this case, a standard approach is to construct index numbers of quantities and prices with respect to some basic quantities and prices (say q_{j0} and p_{j0}). With reference to the base value, (71) can be formulated as

$$\frac{q_j}{q_{j0}} = a_j + b_j \frac{p_j}{p_{j0}}.$$
 (72)

Using a transformation of variables applicable when using Laspeyres index numbers,

$$q_j^* = rac{w_{j0}}{\Sigma w_{j0}} rac{q_j}{q_{j0}}$$
 and

$$p_j^* = \frac{w_{j0}}{\Sigma w_{j0}} \frac{p_j}{p_{j0}}$$

where

$$w_{j0} = p_{j0}q_{j0}$$

(72) can be written as

$$\frac{\Sigma w_{j0}}{w_{j0}} q_j^* = a_j + b_j \frac{\Sigma w_{j0}}{w_{j0}} q_j^*$$

Dividing by

$$\frac{\sum w_{j0}}{w_{j0}}$$

$$q_{j}^{*} = a_{j} \frac{w_{j0}}{\sum w_{j0}} + b_{j} p_{jj}^{*} \qquad (73)$$

where

$$a_j = \frac{w_{j0}}{\Sigma w_{j0}} a_j.$$

 $=a_i^*+b_ip_i^*$

If an aggregate relationship

$$q = a + bp \tag{74}$$

is specified between q and p, the results in (70) can be applied to (73) and (74) to arrive at the aggregates as

$$a = \sum_{j=1}^{k} q_{j}^{*},$$

$$\sum_{j=1}^{k} \frac{w_{j0}}{\Sigma w_{j0}} \frac{q_{j}}{q_{j0}}$$

$$= \frac{\Sigma w_{j0}}{\Sigma w_{j0}} \frac{q_{j}}{q_{j0}}, \text{ and}$$

$$= \frac{\Sigma p_{j0} q_{j}}{\Sigma p_{j0} q_{j0}}.$$
(75)

Also, using (68), p can be obtained as

$$p = \frac{k}{\Sigma b_j} \Sigma b_j p_j^*$$
$$= \frac{k}{\Sigma b_j} \Sigma b_j \frac{w_{j0}}{\Sigma w_{j0}} \frac{p_j}{p_{j0}}, \quad (76)$$

$$= \frac{k}{\Sigma b_j} \frac{\Sigma b_j q_j p_j}{\Sigma p_{j0} q_{j0}}$$

As before, it is possible to modify these aggregation procedures by using other assumptions.

Aggregation over individuals and commodifies. In this case, the simple treatment presented in the previous two cases is no longer applicable. The presence of cross effects make it difficult to obtain the aggregate relationship as a sum of individual relationships. Allen (1964, pp. 714-15) shows that it is not permissible to write the extended Kevnesian consumption function of the form q = ay + dybp + c as the result of simple aggregation over individuals and commodities from a similar micro form. He suggests that "the alternatives open are to ignore micro theory, taking the consumption function (q = ay + bp + c) as the basic construction or, on the other hand, to stick to micro theory and to avoid macro relations like (q = ay + bp + c) except as a rough approximation or as appropriate to particular circumstances in particular time periods."

Marketing margins.-The choice of price and quantities entering demand relationships is an important consideration. Though often consumers make their purchasing decisions based on prices at the retail level, the product has to go through a number of channels before it. reaches the consumer. In fact, modern markets are undergoing rapid changes from a period when the consumer used to bake the bread for home consumption to now when a number of intermediaries exist between the producer and the ultimate consumer. Normally, consumer reactions at the retail level will be transmitted to the producers through the intermediaries. 19 The prices at the farm level and at the retail level will be separated through marketing margins,

the magnitude of which will be dependent upon the nature of the product, the number of intermediaries, and other related factors. As Waugh (1964, p. 20) points out, a complete theory of demand would have to explain the factors that influence retail prices and price spreads between farmers (producers) and consumers. For the sake of exposition, the term "marketing group" is used here to denote all the intermediaries.¹⁴ In this case, it is possible to identify four types of behavioral relationships: (1) the consumer demand, (2) marketing group's supply, (3) marketing group's demand, and (4) producer supply. To provide an economic model of these behavioral relationships, we shall use the following symbols:

- $q^r =$ quantity consumed at the retail level,
- $q^f =$ quantity produced at the farm level,
- $p^* = \text{price at retail level},$
- $p^{\prime} = \text{price at farm level},$
- $M = p^r p^r$, charges realized by the marketing group, and

$$y =$$
consumer income.

Ignoring all other factors influencing the behavior of different groups involved, the following implicit relations can be specified:

$$F_1(q^r, p^r, y) = 0 \tag{77}$$

(consumer demand),

$$F_2(q^r, p^r, M) = 0$$
 (78)

$$F_3(q^r, p^r, M) = 0$$
(79)

¹⁸ Producers will use this information to modify their product. This is why modern theories of marketing management give great importance to consumers, in contrast to the old belief that "supply creates its own demand." See Kotler (1967, Ch. 1) or a discussion of this "new concept of marketing."

¹⁴ The number of stages identified explicitly will partly depend upon the purpose of the analysis (see Hildreth and Jarrett, 1955, p. 107).

 $F_4(q^f, p^f) = 0$ (80) (producer supply—supply at farm level).

Because M is a function of p^r and p^r , it is possible to eliminate M from (78) and (79) and write these relationships as

$$F_2(q^r, p^r, p^f) = 0$$
 and
 $F_3(q^f, p^r, p^f) = 0.$

Some of the variables defined above can be adjusted to eliminate certain variables and to arrive at what is known as derived demand relationships. Also, it is possible to make certain assumptions regarding the relationship between farm prices and retail prices and derive the relationships between elasticities at different levels as will be demonstrated later.

Nature of recorded data (demand and supply interactions).—There has been much controversy regarding the significance of the prices shown in the records and whether this price level corresponds to the intersection of supply and demand. The experimental markets of Chamberlin (1957, pp. 226-249) and Smith (1962) have shown that the supply and demand do no more than place bounds on quantity and price. According to the Cournot-Walras theory of general equilibrium, there exists a tendency that the total quantity purchased by the consumers (market demand) is equal to the total quantity produced by entrepreneurs (market supply), Often consumption and production are not in equilibrium in the short run. The notions of supply and demand should be kept apart and, for demand analysis, quantities should refer to quantities purchased. When consumption data are not available, adjustments have to be made in production data to incorporate exports, imports, and changes in stock levels.

II. EMPIRICAL ANALYSIS OF DEMAND Demand Interrelationships at the Retail Level

The model

Here, an attempt is made to obtain a demand interrelationship matrix for 49 major food commodities (or commodity groups) in the United States. Also, an attempt is made to obtain estimates of the linear effects of time on consumption of a number of commodities.

Relation to the Brandow study.— Brandow (1961) took 24 food items and obtained the complete structure of demand relationships in terms of direct and cross-price elasticities and income elasticities in a synthesized model. To construct the retail demand model, Brandow used the direct elasticities obtained from a number of studies and invoked most of the theoretical restrictions on demand coefficients. Although the estimates obtained from Brandow's study are not claimed to be precise, he has demonstrated the use of Frisch's (1959) procedure to obtain all the direct and cross-price elasticities. However, the estimates can be modified in a number of respects:

(1) Brandow derived most of his direct elasticities from "statistical estimates obtained from other studies" and, as such, they do not follow a consistent pattern of estimation procedures. Different studies may have used data belonging to different periods and obtained from various sources. Also, the estimation procedures used may vary. Thus, it is difficult to obtain consistency in different studies which is also reflected in the estimates.

(2) With 24 commodities or commodity groups, it is necessary to have a considerable degree of aggregation. Because wide variations exist among commodities of a group and we may be interested, for policy purposes, in a single commodity rather than in a commodity group, it is desirable to obtain a detailed breakdown of commodity groups according to individual commodities belonging to a group. Variations that exist for a given commodity as to grade, size, and other characteristics are of recognized importance, but are not considered in this study.

(3) Demand coefficients of many commodifies may have changed between the postwar and the prewar period. Although inclusion of the prewar period may provide more variation in the data compared to the relatively stable consumption pattern during the postwar period. it is doubtful whether the estimates obtained from a long time series, without considering structural changes in the variables, is useful for policy analysis in a future period. At present, we have more than 20 observations of annual data for the postwar period, and thus can obtain estimates from the postwar demand structure alone.

In the present study, the coefficients were obtained using a uniform estimation procedure; the data of the 49 commodities relate to the postwar period; and estimates from other studies, especially Brandow's, were used only when data were not available for estimating the coefficients independently.

Nature of assumptions.—As mentioned, the assumptions of Frisch and Barten imply cardinal utility and those of Strotz and Pearce ordinal utility. As Hallberg (1968, pp. 378–79) states "... if the proper combination of commodi-

ties are involved, either of these propositions (neutral-want association of Pearce and want-independence of Frisch) will probably be acceptable as reasonable approximations to actual consumer behavior." Also, Pearce (1961) points out that, under certain conditions, it is possible to derive the conclusions obtained by Frisch from both neutralwant association and the want-independent assumptions. For an empirical analysis of the type considered here, identification of proper commodity groups and estimation procedures requires more attention than choosing between neutralwant association and want independence. While using the assumption of ordinally separable utility indicators (neutral-want association), it may often become necessary to estimate parameters from a nonlinear system and the methods available for their estimation may become very complicated when commodities are numerous. Therefore, for practical considerations, we had to adopt a procedure which implied elements of want independence and neutral-want association as follows:

(1) Because of their large number, we grouped the commodities into different separable commodity groups.

(2) Following the principle of two-stage maximization, the demand equation for a single commodity within a group was specified as a function of prices of all commodities within the group, prices indices for other groups, and income.

(3) It was assumed that commodities belonging to a particular group were want independent of commodities belonging to another group so we could use the procedure suggested by Frisch to obtain the cross elasticities corresponding to all commodities outside a given group. Considering the cardinality assumptions involved in want independence, we would have preferred to avoid it so that we could deal with ordinal assumptions alone. However, the estimation problems associated with handling large numbers of commodities was such that we had to impose the assumptions of want independence for all commodities outside a given group.

Choice of commodities.—Our choice of commodities was based on two major considerations:

(1) The commodity included should account for at least .3 per cent of the food budget, based on U.S. Bureau of Labor Statistics (1963). Since total food expenditures account for 22.79 per cent of all expenditures, included commodities should occupy at least .68 per cent of total expenditures. However, we made exceptions for onions, carrots, and sweet potatoes, which accounted for only .263. .263, and .175 per cent, respectively, because data were available for these items. (2) Commodities were included where data were available on prices, quantities consumed, and an income-consumption pattern. In general, time-series data on prices were taken from U.S. Bureau of Labor Statistics (1963) reports, quantities consumed from Hiemstra (1968), and cross-section data on food consumption was from 1955 and 1965 food consumption survey reports (see Appendix A.)

Among the 49 selected commodities we have five commodity groups—"other fresh fruit," "other fresh vegetables," "other canned fruits and vegetables," "bread and other cereal products," and "other beverages." These groups were included because it was difficult to obtain individual commodities within these groups satisfying the above criteria, while their combined effects were not negligible.

Determination of expenditure weights.- The expenditure proportions of different items are derived from both time-series and cross-section data. Hiemstra (1968, p. 172) reports the expenditure proportions¹⁵ on major commodity groups in December of 1963 and 1966, Because these proportions included meals eaten away from home also, they were adjusted to remove this effect and then these two periods were averaged to obtain group expenditure proportions. To obtain the budget proportions for individual commodities included in this study, the group proportions were calculated as above and a breakdown, according to the expenditure proportions, was obtained from the 1965 household foodconsumption survey. For example, the adjusted time-series estimate of the budget proportions for dairy products accounted for 3.8277 per cent of total expenditures. According to the 1965 food consumption survey, butter, fresh milk, evaporated milk, cheese, and ice cream accounted for 8.451, 58.873, 2.817, 17.465, and 12.394 per cent, respectively, of the total dairy products. Therefore, the budget proportions for butter, fresh milk, evaporated milk, cheese, and ice cream are obtained as .003235 (i.e., .038277 × .08451), .022535 (i.e., .038277 × .58873), .001078, .006685, and .004744, respectively. The expenditure proportions for all the other commodities are calculated in the same manner (table 2). To facilitate comparison with other studies, table 2 also gives the budget proportions used in Brandow's study. (Brandow used weights for 1955-1957, obtained by adjusting 1947-1949 data.)

Choice of regression equations.—The demand for a commodity, expressed in terms of all prices and income, is repre-

¹⁶ These proportions were originally derived by the Bureau of Labor Statistics. The quantity weights used in the derivation of these figures were based on the spending pattern of wage earner and clerical worker families as derived from the 1960-1961 Surveys of Consumer Expenditures.

TABLE 2 EXPENDITURE PROPORTIONS

Commodity and group*		ions expressed as per- age of	Brandow propertions
	Food expenditures	All expenditures	of all expenditures
Mest, poultry, and fish (group 1)			
Beef	11.555	2.6337	2.834
Yeal	. 880	.2005	422
Pork	13.228 .880	3.0149 .2005	2.194
Chicken.	3.818	.8703	.919
Turkey.	. 789	. 1799	,229
Fiah	2,701 33,861	.6155 7.7158	.553 7.831
Egge (group 2)	3.875	. 8833	1.128
Pote and oils (groups 3, 4, and 5)			
Butter	L.\$19 .299	.3235	-398
Lard	. 299	.0681 .3133	.138 .261
Margaride	.638	.1225	.158
Salad dressing	L,135	. 2585	.320
Total,	4,766	1.0863	1,261
Dairy products (groups 6 and 7) Freeh milk	9,887	2.2535	3.786
Fresh milk. Evaporated milk	.473	1 .1076	172
Checee	2,933	. 6685	.375
Ice cream. Total (ascluding butter).	9.081 16.374	.4744 3.5042	.590 3,923
Potatoss (group 8)			
White	1.226	.2795	
Total	.175 1.401		. 469
Supertenses, excluding noncalorics (group 9)			ļ
Sugar.	2.573	. 5861	
Corn syrup	L.009 3.58L	.2300	1.649
	0.001	,0104	1.098
Fruit (group 10) Fresh	4,645	1 1046	
Canned	1.690	1.1045	
Frosen	.746	.1700	
Dried	.373	.0850	
Total	8.182	1.8848	1.839
Vegelablee (group 11) Freeh	4.285	.9721	
Canzed	3.002	.6842	
Frosen	. 746	. 1700	
Dried Total	.373 8.386	.0850	
1	5.300	1,9113	2.335
Cereal and bakery products (group 12) Rice	. 588	1333	
Wheat flour.	1.039	.1333 .2369	
Breakfast percelle	2.859	6516	
Corn meal Bread and other bakery products	.390 9.746	.0889	
Total	9,746 L4,623	2.2212 3.3319	1.819
Beverages and soup (groups 13, 14, and 15)		l	
Collee	2.445	, 5573	
Nonalcoholic beverages	1.963	. 4475	
Soupe Total	1,008 5,963	. 3538 1.3586	1.031
TOTAL ALL FOOD	100,00	22.79	23.177
TOTAL NONFOOD	ļ	77 01	76 000
IOTAL RONFOOD	1	77.21	76.823

See text for discussion of commodity groups. See table 5, last row, for expenditure proportions for certain individual items in the fruit and vegetable categories.
 † Includes dry beans, peas, and nuts of .392.

sented by

$$q_i = q_i(p_1, p_2, \cdots, p_n, y).$$
 (81)

Taking total differentials of (81),

$$dq_{i} = \frac{\partial q_{i}}{\partial p_{1}} dp_{1} + \frac{\partial q_{i}}{\partial p_{2}} dp_{2}$$
$$+ \cdots + \frac{\partial q_{i}}{\partial p_{n}} dp_{n}. \tag{82}$$

$$+ \frac{\partial q_i}{\partial y} dy.$$

Dividing (82) by q_{i_i}

$$\frac{1}{q_i} dq_i = \frac{1}{q_i} \frac{\partial q_i}{\partial p_1} dp_1 + \cdots + \frac{1}{q_i} \frac{\partial q_i}{\partial p_n} dp_n + \frac{1}{q_i} \frac{\partial q_i}{\partial y} dy.$$

(83)

But

$$\frac{d(\log q_i)}{dq_i} = \frac{1}{q_i},$$

therefore,

$$\frac{dq_i}{q_i} = d(\log q_i),$$

$$\frac{1}{q_i} \frac{\partial q_i}{\partial p_j} dp_j = \frac{p_j}{q_i} \frac{\partial q_i}{\partial p_j} \frac{dp_j}{p_j}$$

$$= e_{ij} d(\log p_j).$$

Similarly,

$$\frac{1}{q_i}\frac{\partial q_i}{\partial y}dy = e_{iy}d(\log y).$$

Substituting these results in (83), we have

$$d(\log q_i) = e_{i1} d(\log p_1) + \cdots$$
$$+ e_{in} d(\log p_n) \qquad (84)$$
$$+ e_{iy} d(\log y).$$

When we take only finite differences, the differentials in (84) can be replaced by first differences and, therefore, equation (84) can be written as

$$\Delta \log q_i = e_{i1} \Delta \log p_1 + \cdots + e_{in} \Delta \log p_n \qquad (85)$$
$$+ e_{iy} \Delta \log y.$$

While using time-series data,

$$\Delta \log q_i = (\log q_{il-1} - \log q_{il})$$

whereas, using equation (85) for crosssection data, price changes vanish and, therefore,

$$\Delta \log q_i = e_{iy} \Delta \log y. \tag{86}$$

The present study makes extensive use of equations of type (85) and (86). The use of first differences may reduce the effect of serial correlation if the serial correlation coefficient is approximately one. However, in some cases, a double logarithmic function gave statistically better estimates than the first difference equation and, in such cases, we have selected the estimates with better statistical properties.

Grouping of commodities into separable groups.—To obtain a regression equation similar to (85), it is necessary to restrict the number of commodities to be included in any given equation. Grouping of commodities according to certain characteristics permits us to obtain a consistent estimate through twostage maximization. From the previous section, we have a demand equation for the j^{th} commodity belonging to group *i*, expressed as

$$q_{j}^{i} = q_{j}^{i}[p_{1}^{i}, p_{2}^{i}, \cdots, p_{n_{j}}^{i}] \\
 y_{i}(p_{1}, p_{2}, \cdots, p_{n_{j}}, y)]$$
(87)

for

$$j = 1, 2, \dots, n_i; i = 1, 2, \dots, s$$

where

- p_1, p_2, \cdots, p_n^i represent the individual commodity prices,
- P_1, P_2, \cdots, P_s represent group price index, and

 y_i is the expenditure on the i^{th} group.

Equation (87) can also be expressed as

$$q_{j}^{i} = q_{j}^{i}(p_{1}^{i}, p_{2}^{j}, \cdots, p_{n}^{j}, P_{1},$$

$$P_{2}^{i} \cdots P_{n}^{j}, y).$$
(88)

To use this two-stage maximization procedure, we had to classify our 49 commodities into a number of separable groups. Instead of depending on arbitrary groupings, we adopted a grouping developed by deJanvry (1966, p. 112). DeJanvry took the price elasticities, income elasticities, and budget shares used in Brandow's study and developed the proportionality factors¹⁶ represented by

$$\theta_{ij} = \frac{y}{e_{iy}} \frac{e_{iy}}{w_j e_{iy}} + 1$$

Using the proportionality factors, separable groups were identified such that the between group θ_{ik} 's are maximally equal for all $i \in I$ and $k \in K$. Eventually, the following 15 groups were established:

- 1. Beef, veal, pork, lamb, chicken, turkey, fish
- 2. Eggs
- 3. Butter
- 4. Lard
- 5. Shortening, margarine, salad dressing and cooking oil
- 6. Milk, evaporated milk
- 7. Cheese, ice cream
- 8. Potatoes, sweet potatoes
- 9. Sugar, corn syrup
- Apples, bananas, oranges, other fresh fruits, canned peaches, canned pineapple, frozen fruits
- 11. Lettuce, tomatoes, beans, onions, carrots, other fresh vegetables, canned peas, canned corn, canned tomatoes, dry vegetables, frozen vegetables, other canned fruits, and vegetables
- 12. Rice, wheat flour, breakfast cereals, corn meal, bread, and other cereals
- 13. Coffee
- 14. Soup
- 15. Other beverages

The list of all 49 commodities are contained in table 5 on page 46.

Estimation of the demand matrix

Having grouped the 49 commodities into 15 groups, a demand equation similar to (88) was used for each commodity in a given group. The functional form of the demand equations, in many cases, was similar to (85) so that we were using the first difference of variables. In many cases, the coefficients of the group prices turned out to be highly insignificant and, therefore, in actual estimation, we have omitted a number of price indices. Also,

¹⁶ DeJanvry used the proportionality factors to arrive at groupings based on factor analysis. "The criteria for the allocation of variables to composites will be that these reproduce for each variable its intercorrelations with the other variables. This corresponds to the building of cluster of variables that have maximal correlations in terse and maximally proportional correlations with outside variables." (1966, p. 57)

both annual and quarterly data were used, where available, to estimate the demand coefficients. Thus, for many commodities, there were a number of equations using both annual and quarterly data and, also, using logarithmic form and the first difference of logarithms of variables. Demand equations were specified with quantities as dependent variables and prices of all commodities belonging to the same group, together with price indices of other groups and income, as the independent variables. Therefore, it was possible to obtain the direct price elasticity and cross-price clasticities with respect to all the commodities in the same group from a given demand equation.

A number of equations existed for the same commodity, and one coefficient had to be chosen. In most cases, the criteria for selection of coefficients were based on the statistical properties such as the fit of the equation (as determined by the multiple correlation coefficient), the significance of the individual coefficients (determined by the *t*-statistic), and the existence of serial correlation (determined by the Durbin-Watson test statistic). The theoretically anticipated sign of the regression coefficient was also considered when we had estimates satis-

fying more or less the same statistical properties. All the estimates of direct and cross-price elasticities for commodities belonging to the same group are obtained in this manner. However, the cross-elasticity coefficients were adjusted to satisfy the symmetry condition. Quantity and price data on five commodities (turkey, fish, frozen fruits, frozen vegetables, and bread) were not available on a comparable basis. Therefore, we used estimates obtained from other sources for the direct price elasticities of these commodities.¹⁷

Synthesis of demand interrelationships.—We have seen how the direct and cross-price elasticities for all commodities belonging to each group are determined. The section on income and consumption shows how various measures of income elasticities are obtained. Using these figures and the restrictions imposed upon an individual's demand coefficients by the theory of consumer behavior, we can calculate all the other remaining coefficients. All nonfood items are treated in one category. The demand interrelationships are represented in table 3.

We can summarize the restrictions on demand coefficients specified in table 1 as follows:

(a) Row Restraint (Homogeneity Condition)

$$e_{i1} + e_{i2} + \dots + e_{i49} + e_{i50} + e_{ig} = 0 \qquad (i = 1, 2, \dots, 50)$$
(89)

(b) Symmetry

$$e_{ij} = w_{ij} e_{ji} - w_j (e_{ij} - e_{jy}) \qquad (i, j = 1, 2, \cdots, 50)$$
(90)

(c) Cournot Aggregation

 $w_{1}e_{1j} + w_{2}e_{2j} + \cdots + w_{49}e_{40j} + w_{50}e_{50j} = -w_{j} \qquad (j = 1, 2, \cdots, 50)$ (91)

(d) Engel Aggregation

$$w_{1e_{1y}} + w_{2e_{2y}} + \dots + w_{4y} + w_{50} + w_{50} = 1$$
(92)

¹⁷ Brandow's estimates were used for turkey, fish, and bread. The direct price elasticity estimate for frozen vegetables was based on an unpublished study of Ben C. French, Department of Agricultural Economies at Davis.

<u> </u>						<u> </u>	
		Comme	odities				_
	1,	2.	,	49	. All food	Nonfood	Income
t	e i i	fiz		ē1.4	er.)	¢1,10	£1,y
2	421	6m		¢.a	6.7	51,60	63, 3
		i .	•		. I		
•			•••	•		•	•
49	e#.1	6 4 9,3	•	80.0	ea.,	e 10,10	¢m.r
All food	6/.1	£1,2		t/.a	er 3	¢5.36	57.a
Nonfood	410,1	¢10,1		₹60.st	¢10.1	¢40,40	6a 4 .3
Expenditure weight	101	103		ts er	wj	wю	. 1
I		1			1		

TABLE 3 DEMAND INTERRELATIONSHIP MATRIX

NOTE : Subscripte 1-49 denote the 49 food items, "50" denotes nonfood, "/" denotes all food, and "y" denotes income,

(e) Frisch Equations

$$e_{ij} = -\frac{1}{\phi} e_{ij} e_{jj} w_j - e_{ij} w_j \text{ for } i \neq j, \text{ and}$$
(93)

$$e_{ii} = -e_{iy}w_i - \frac{1 - w_i e_{iy}}{\phi}$$
(94)

These restrictions were used in the following manner to obtain all the elements in the demand interrelationship matrix.

(a) Our starting point is the estimates of direct-price elasticity (e_{ii}) , income elasticity (e_{ii}) , and expenditure proportions (w_i) for all commodities. We have already explained the estimation procedure adopted in obtaining all these elements. Also, we have seen that the cross elasticities for commodities belonging to the same food group basically are obtained through direct estimation process. The particular coefficients used in this analysis were chosen from a large number of estimates, using certain desirable properties of the estimates and some element of intuitive judgment.

(b) Income elasticity for all food (e_{fy}) is obtained as a weighted average of the

income elasticities for individual commodities, the weights being the expenditure proportions, or

$$e_{f_{V}} = \frac{w_{1}e_{1_{V}} + w_{2}e_{2_{V}} + \dots + w_{4_{V}}e_{4_{9_{V}}}}{w_{1} + w_{2} + \dots + w_{4_{9}}}$$

$$= \frac{w_{1}e_{1_{V}} + w_{2}e_{2_{V}} + \dots + w_{4_{9}}e_{4_{9_{V}}}}{w_{f}}$$
(95)

because the expenditure weight of all food is the sum of expenditure weights for individual food items. The elasticity obtained in this manner was .176265. Although this estimate is lower than Brandow's (.25667), it compares favorably with independent estimates of income elasticities for all food in other studies. For example, Hiemstra (1968, p. 29) obtained the following equations by fitting annual data for the 1948-1966 period through the use of the single equation least-square model.

$$x_{1} = 2.227 - 0.182 x_{2}$$
(.093)
$$+ 0.174 x_{3} - 0.104 x_{4}$$
(.060)
(.125)
$$(R^{2} = .733)$$
here

wh

- $x_1 = \log \text{ per capita food consumption}$ index.
- $x_{z} = \log$ retail food price index,
- $x_3 = \log$ per capita disposable personal income index, and
- $x_4 = \log$ consumer price index (all items less food). All the indices are with reference to the base period, 1957 - 1959 = 100.

For the period 1948–1962, Waugh (1964, p. 16) obtained a regression equation

$$\begin{array}{rcl} x_1 = 2.19 - 0.24 \ x_2^* + 0.14 \ x_3 & (97) \\ (.15) & (.50) \end{array}$$

where the variables are as defined above except that x_2 and x_3 are deflated by the consumer price index to obtain x_2^* and x_3^* , respectively. Thus, the estimate, .176265 (obtained in this study) can be compared with .174 in (96) and .14 in (97). However, income elasticity obtained from 1965 cross-section data using expenditure as the dependent variable was .277111 (see table 13). The estimate of .176265 corresponds to quantities and, therefore, it is consistent with the general notion that income elasticity with expenditure as the dependent variable is higher than the corresponding estimate with quantity as the dependent variable.

(c) Income elasticity of nonfood (e_{b0y}) . From equation (92), we know that the weighted sum of all the income elasticities is unity. We have already estimated all the expenditure weights and the income elasticities for commodities other than nonfood. Therefore, in equation (92), only e_{50y} is unknown.

$$e_{50y} = \frac{1 - (w_1 e_{1y} + w_2 e_{2y} + \dots + w_{4y} e_{4yy})}{w_{50}}$$
(98)

Using equation (95), this can be written 88

$$e_{\delta 0y} = \frac{1 - w_f e_{fy}}{w_{\delta 0}}.$$
 (99)

Using (99), the income elasticity of nonfood is estimated as

$$\frac{1 - (.227918)(.176265)}{.772082} = 1.243165.$$

This estimate is fairly consistent with Brandow's estimate of 1.22426.

(d) Direct elasticity for all foods (e_{II}) . Using (94), we can write e_{ff} as

$$e_{ff} = -e_{fy}w_f - \frac{1 - w_f e_{fy}}{\phi}.$$
 (100)

On the right-hand side of (100), all the terms except the value of the money flexibility coefficient (ϕ) are known. Since the value for equation (99) approximates that of Brandow, it seems to be appropriate to use Brandow's estimate of ϕ at -.86. Thus, from equation (100), the value of e_{ff} is -.236845, which comparcs favorably with results obtained independently. Using the results obtained by Girshick and Haavelmo (1947), Buchholz, et al., (1962) have calculated the elasticity of food consumption with respect to retail prices to be -.25. In (97), Waugh had obtained the value of e_{tt} as -.24. Considering the rounding of decimals in Waugh's results, the figure obtained from our estimation procedure is consistent and we are justified in taking the value of ϕ at -.86. Brandow (1961, p. 18), himself, agrees that his estimate of -.34137 "appears on the basis of time-series analysis to be slightly too high."

(e) Direct elasticity for nonfood $(e_{60,60})$ is also obtained in a procedure similar to that of direct elasticity of all food.

$$e_{50, 50} = -e_{50y}w_{50} - \frac{1 - w_{50}e_{50}y}{\phi}$$
$$= -1.243165 \ x \cdot 818796$$
$$= -1.017898.$$

This estimate is consistent with -1.02556 from Brandow's study.

(f) Cross elasticity of all food with re-

spect to nonfood prices $(e_{\beta 0})$ is obtained using the homogeneity restraint that

$$e_{fb0} + e_{ff} + e_{fy} = 0. \tag{101}$$

From steps (b) and (d), we obtained e_{fy} and e_{ff} as .176265 and - .236845, respectively. Therefore, from equation (101),

$$e_{760} - .236845 + .176265 = 0.$$

Thus, we obtain an estimate of e_{f50} as .060580, which is considerably lower than Brandow's corresponding figure (.08470). However, our estimate is greater than at least one independent estimate with the coefficient, .052, reported in Brandow (1961, p. 18).

(g) Cross elasticity of nonfood with respect to food prices (e_{50f}) . Using the symmetry relations in equation (90)

$$e_{s0f} = \frac{w_f}{w_{s0}} e_{f50} - w_f (e_{50y} + e_{fy})$$

= $\frac{.227918}{.772082} (.060580) - .227918 (1.243165 - .176265)$
= $-.225266.$

(h) Cross elasticities showing the effects of nonfood prices on consumption of individual foods (e_{i50}) for $i = 1, 2, \cdots$, 49. From equation (93) we have

$$e_{ij} = -\frac{1}{\phi} e_{ij} e_{jj} w_j - e_{ij} w_j$$
$$= -e_{ij} w_j \left(1 + \frac{e_{jj}}{\phi}\right).$$

Assuming j to be nonfoods, we have

$$e_{i50} = -e_{iy}w_{60}\left(1 + \frac{e_{50y}}{\phi}\right)$$

Therefore,

$$\frac{e_{i50}}{e_{iy}} = -w_{50} \left(1 + \frac{e_{50y}}{\phi}\right). \quad (102)$$

Here, it is implied that each food is want independent of nonfood items. The righthand side of (102) is independent of i, which implies that the ratio of cross elasticities showing the effect of nonfood prices on consumption of an individual food item and the income elasticity of the same food do not vary from commodity to commodity. In particular, if we consider the total food, using the results from (f) and (b), the ratio e_{f50}/e_{fy} becomes .060580/.176265 = .343687. We have assumed that the common ratio e_{is0}/e_{iy} , for all *i* to be the same as e_{fi0}/e_{fy} . Therefore,

$$e_{i50} = .343687 \ e_{iy}$$

(103)
 $(i = 1, 2, \cdots, 49).$

Thus, the cross elasticities showing the effects of nonfood prices on the consumption of individual foods is 34.3687 per cent of the corresponding income elasticities. Brandow obtained the corresponding percentage as 33.

(i) Cross elasticities showing the effects of individual food prices on non-food quantity (e_{50i}) for $i = 1, 2, \dots, 49$. Since we have obtained e_{i50} from (h), we can use the symmetry relationship in (10) to obtain e_{50i} as

$$e_{50i} = \frac{w_i}{w_{50}} e_{i50} - w_i (e_{50y} - e_{iy}) \quad (104)$$

for $i = 1, 2, \dots, 49$. From (a), (c), and (b), all the coefficients on the right-hand side of (104) are known and, hence, the values of e_{50i} can be calculated.

(j) Cross clasticities showing the effect of all food prices on the consumption of individual foods (e_{ij}) , $i = 1, 2, \dots, 49$.

From the homogeneity restraint (89), we have $e_{i1} + e_{i2} + \cdots + e_{i49} + e_{i40} + e_{i9} = 0$. But the sum, $e_{i1} + e_{i2} + \cdots + e_{i49}$ represents e_{i7} . Therefore,

$$e_{if} + e_{i30} + e_{iy} = 0$$

(*i* = 1, 2, ..., 49)
or
 $e_{if} = -(e_{iy} + e_{i50}).$ (105)

Both terms on the right-hand side are known from (a) and (h). Therefore, the cross elasticities showing the effect of all food prices on the consumption of a given commodity is obtained as the negative of the sum of the income elasticity and the cross elasticity showing the effect of nonfood prices on the consumption of that commodity.

(k) Cross elasticity showing the effect of individual commodity prices on food consumption (e_{fi}) , $i = 1, 2, \dots, 49$. From the Cournot aggregation in (91), we have

$$w_{1}e_{1i} + w_{2}e_{2i} + \dots + w_{49}e_{49i} + (106)$$
$$w_{50}e_{50i} = -w_{i}.$$

If we define e_f, as

$$e_{fi} = \frac{w_1 e_{1i} + w_2 e_{2i} + \dots + w_{i9} e_{49i}}{w_1 + w_2 + \dots + w_{i9}},$$

$$w_i e_{1i} + w_2 e_{2i} + \dots + w_{49} e_{49i} = (w_1 + w_2 + \dots + w_{49}) e_{fi}$$
(107)

Substituting (107) in (106)

$$e_{fi}w_{f} + e_{b0i}w_{b0} = -w_{ii}$$

$$e_{fi} = -\frac{w_{i} + w_{b0}e_{b0i}}{w_{i}}.$$
(108)

From (a) and (i), all the terms on the right-hand side of (108) are known.

 $= w_f e_{fi}$

(1) Cross elasticity showing the effect of individual commodity prices on the commodities outside the group (e_{ij}) $i \neq j$, $i \in I$, and $j \notin I$. Suppose that we are considering the i^{th} commodity. We have already estimated the direct elasticity, cross elasticities with respect to commodities in the same group, and income elasticity, using (a). The nonfood cross

elasticity is obtained from (h). Thus, using the homogeneity restraint, we can obtain the sum of the remaining unknown coefficients in the same row. For convenience, if we assume that the first k commodities belong to a group, for any commodity belonging to that group, e_{i1} , $e_{i2}, \dots, e_{ik}, e_{ik0}$, and e_{iy} are known. Since we have

$$(e_{i1} + e_{i2} + \dots + e_{ik}) + e_{ik+1} + \dots + e_{i49} + e_{i40} + e_{ij} = 0,$$

the sum of the cross elasticities corresponding to the commodities outside the group is $-(e_{i1} + \cdots + e_{ik} + e_{i9} + e_{i9})$, which is the negative of the sum of all known coefficients. Let us denote this sum by R_i . Having known the value of R_i , our next job is to see how this value is distributed over the individual commodities. In (93), we have seen that the cross elasticities can be obtained as

$$e_{ij} = -e_{iy}w_j\left(1 + \frac{e_{iy}}{\phi}\right).$$

Since all the values on the right-hand side are known, we can calculate the remaining (49-k) cross elasticities showing the effects of their prices on the consumption of the i^{th} commodity. It is possible that the sum of the coefficients obtained in this manner will not add to R_i . So we will have to adjust the individual coefficients such that their sum adds to R_i . Thus, the cross elasticities are taken only as proportional to $-e_{iy}w_j(1 + e_{iy}/\phi)$, without assuming strict equality. By the time we complete this step, all the coefficients in the i^{th} row are known.

In practice, we start with the first row and obtain all the coefficients in that row, then, using these figures and the symmetry relationship, we can calculate the remaining elements in the first column. Now, we complete the second row and obtain the remaining elements of the second column, using symmetry relationship. Thus, continuing a row and column operation, we can obtain all the unknown coefficients in the demand interrelationship matrix (table 5). The steps taken in obtaining the demand interrelationship matrix are given in table 4.

Linear effects of time on consumption

The specification of demand functions in terms of prices and income excludes any possible continuous systematic variations in the demand as a result of factors other than those specified. Often, in demand analysis, such variations are handled by incorporating time as a variable with linear or nonlinear effects. If the purpose of the analysis is only for making projections, inclusion of time may result in more reliable projections than when time is excluded. However. it may be possible that variables such as income and prices are highly correlated with time so that introduction of time as a variable may result in estimation problems. An estimate of the coefficient associated with time may often be an overcstimate because most unexplained variations might be absorbed by this coefficient in addition to the effect of time. Further, it will be hard to provide an interpretation for the coefficient associated with time. Considering these factors, we have avoided the practice of using time as a variable in our demand equations.

Use of the first difference of the variables in the demand equations provides an opportunity to test the presence of any linear effect of time. If we add a constant to the demand equation in (85),

Comm	odity		Commodity gro	мр		All food	Nonfood	Income
Group	Item	I,	п,	,	xv	All 100d	Noilloon	Income
		1, 2,, 21	1, 2,, #2		1, 2,, 194	6)	(b)	(a.)
	1 2	(a.)	(1)	(4)	(1)	6)	(b)	(6)
t		(,	47		(4)
	· ·							
	#1							
	•						ļ	
	1 2	(1)	(a)	(0	(6)	(i)	(h)	(4)
11	1 .	(0)	(4)	(6)	(*)	G)	(1)	1447
	· ·		1					
	, 11.7							
	· [·					
		(4)	(3)	(a)	(1)	6)	(h)	(a)
		,						
	1							
	2	(2)	(8)	(1)	(a.)	6)	(h)	(a)
XV								
	*11							
food		(k)	(k)	(k)	(k)	(d)	0	(b)
afood					(i)	(g)	(e)	(c)
penditure v	weight	(a)	(a)	(a.)	(a)	(1)	(.)	(1)

TABLE 4 SYNTHESIS OF DEMAND INTERRELATIONSHIPS (SUMMARY)

Norm: The letters in the boxes represent the steps mentioned in the text.

specified in terms of the first difference of the variables, it can be written as

$$\Delta \log q_i = a_i + e_{i1} \Delta \log p_1 + e_{i2}$$

$$(109)$$

$$+ e_{in} \Delta \log p_n + e_{iy} \Delta \log y.$$

When the independent variables (prices and income) do not change over the years, (109) reduces to $\Delta \log q_i = a_i$. If the value of a_i is significantly different from zero, it implies that some change in consumption will take place from the preceding year even if there was no change in prices and income. Thus, when first differences of variables are used in the demand equation, the constant term in the regression equation represents the linear effect of time. We have used first difference equations similar to (109) for 39 commodities and the constant term was significantly different from zero at the 5 per cent level for ten commodities eggs, butter, lard, evaporated milk, ice cream, sweet potatoes, beans, canned peas, wheat flour, and soup. At the 10 per cent level, the coefficients of six more commodities—cheese, canned peaches, dried fruit, carrots, corn meal, and coffee—became significantly different from zero (see Appendix table A-6).

Foote (1958, p. 43) suggests that the percentage effect of time in each year can be obtained by taking the anti-

TABLE DEMAND INTERRELATIONSHIPS

	Commodifies	Beef	Veal	Pork	Lamb	Chicken	Turkey	Fish	Eggs
Columa		I	2	3	& mutton	5	6	7	8
Row			 		· _	-	-		
1	Beef	-0.643800	0.027953	0.082609	0.046433	0 067560	0.007525	0.003128	0.0010
2	Veal	0.359295	-1.717737	0,197665	0.066017	0.173564	0.0138(0	0.003125	0.0013
3	Pork	0.076284	0.014062	-0.413013	0.060153	0.035251	0.005037	0.004630	0.0025
4	Lamb and						0.000	0.001000	/ 0.00460
	mutton	0.589451	0.066057	0.891362	-2.625500	0.233588	0.015092	0.002\$10	0.0039
5	Chicken	0.197067	0.043577	0.120758	0.054601	-0.777830	0.083745	0.003722	0.0022
6 7	Turkey Fish	0.097590	0.014702	0.065260	0.017800	0.400000	-1 555329	0.001078	0,0021
8	Ecc	0.020910 0.010179	0.002203	0.026578	0.002052 0.001940	0.006780	0.001690	-0.230000	0.0109
ě	Butter	0.001944	0.001671	0.000304	0.001116	0.003325 0.000315	0.001720	0.007339	-0.3182
LÖ	Lard	0.013438	0.003164	0.015359	0.002264	0.004603	0.001972	0.008938	0.0076
11	Shortening	0.010978	0.002849	0.012144	0.002019	0.003605	0.001809	0.007729	0.0149
12	Margarine	0.011888	0.002966	0.013319	0.002110	0.003935	0.001855	0.008184	0.0162
13	Salad			1					-····
14	dressing	0.003481	0.002014	0.002750	0.001332	0.000948	0.002229	0.004891	0.0103
14 15	Fresh milk Evaporated	0.006400	0.002138	0.004993	0.001474	0.001604	0.001250	0.005007	0.0107
	milk	0.011764	0.002915	0.013001	0.002083	0.003867	0.001040	0.007047	
18	Cheese	0.004107	0.001954	0.003150	0.001332	0.003387	0.001843 0.001272	0.007945	0.0157
17	Ice cream	0.001525	0.001817	-0.000239	0.001073	0.000138	0.001078	0.002995	0.0094
18	Potatoes	0.008248	0.002492	0.012071	0.001746	0.002603	0.001198	0.006372	0.0130
19	Sweet								0.0.00
	potatoes	0.008064	0.001364	0.004981	0.001242	0.001793	0.001430	0.000847	0.0163
20 21 i	Sugar	0.010892	0.002838	0.012026	0,002011	0.003572	0.001782	0.007695	0.0153
32	Corn syrup	0.003489	0.002260	0.005218	0.001667	0.001945	0.001448	0.005475	0.0118
23	Варадаа	0.007522 0.007528	0.002390 0.002398	0.007607	0.001669 0.001673	0.002334	0.001529	0.007659	0.0124
24	Oranges	6,003504	0.001604	0.002131	0.001241	0.002339	0.001529	0.005997	0.0124
25	Other fresh fruit.	0.000622	0.001337	-0.003058					0.0082
26	Canned peaches				0.000860	-0.000649	0.000917	0.001929	0,00\$3
37	Ceaned	0.001230	0.001581	-0.000626	0.001087	0.000033	0.000950	0.002\$50 :	0.0069
28	pineapples Dried fruits.	-0.002098 0.001998	0.001141	-0.005017	0.000710	-0.001196	0.000600	0.001104	0.0041
29	Frozen fruita	-0.008793	0.001683	0.000407	0.001124 0.000042	0.000323	0.001116	0.003255	0.0076
30	Lettuce	0.007286	0.001338	0.007312	0,001650	0.002283	0.000363 0.001514	-0.002146 0.005875	-0,0016 0,0122
31	Tomatoes	0.006565	0.002321	0.006372	0.001679	0.001989	0.001456	0.005526	0.0116
32	Beans	0.011887	0.002630	0.013344	0.002114	0.003947	0.001857	0.009176	0.0162
33	Onions .	0.011777	0.002953	0.013143	0.002096	0.003892	0.001845	0.008176	0.0102
34 36	Carrota Other freah	0.001906	0.001630	0.000234	0.001111	0.000268	0.001108	0.003197	0.0076
	vegetables	0.007203	0.002357	0.007190	0.001842	0.002221	0.001604	0.005649	0.0121
38	Canned peas	0.010902	0.002953	0.012042	0.002013	0.003579	0.001782	0.007709	0.0154
37 38	Canned corn Canned to-	0.011151	0.002868	0.012358	0.002036	0.003664	0.001800	0.007812	0.0155
39	matoes Dry vege-	0.006445	0.002258	0,006208	0.001566	0.001948	0.001447	0.005432	0.0114
40	tables Frozen vege-	0.005114	0.001923	0.004438	0.001433	0.001445	0,001346	0.004809	0.0103
4	tables Other	0.007383	0.000390	0.011909	0.000185	0.003128	0.000408	-0.001450	~0.0004
"	canned fruite and								
	vegetables	0.005689	0.002153	0.005143	0.001492	0.001447	0.001000	0.005045	0 0100
42	Rice	0,010145	0.002745	0.011059	0.001493	0.001647 0.003301	0.001387 0.001727	0.005067 0.006467	0.0108 0.0146
43 44	Wheat flour. Breakfast	0.009293	0.002631	0.009942	0.001853	0.002987	0.001662	0.006890	0,0139
	cereals	0.010089	0.002733	0.010974	0.001931	0.003260	0.001721	0.007000	A
45 46	Corn meal. Bread and	0.010063	0.002786	0.007379	0.001034	0.003282	0.001321	0.007289 0.007279	0.0145 0.0146
F U	other								
47	Coffee	0.011894	0.002969 9.002778	0.013339	0.003111	0,003941	0,001857	0.008198	0.0163
48	Boup	0.010417 0.004499	0.002778	0.011380 0.003655	0.001964	0.003402	0.001746	0.007455	0.0149
49	Other bever-	1			0.001372	0.001230	0.00130I	0.001191	0.0096
50	All food	0.001697	0.002030 	0.003914 0.025047	0.001391	0.001300	0.001316	0.004590	0.0099
51	Nonfood	-0.021707	-0.000780	-0.020047	-0.005958 -0.000838	-0.008140	-0.006247	-0.001207	-0.0039
62	Erpenditure propor-		- • . ••••100	-0.001000	-v. vuuooa	0.006074		-0,00/617	0.0102

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AT THE RETAIL LEVEL

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						<u> </u>			·
Bolter	Lard	Shortening	Margarino	Salad dressing	Freeh	Evapora- ted milk	Cheese	Ice cream	Potatoes
•	10	11	12	13	14	16	18	cream 17	16
					•• ·· · ·	· · ·			
0.000830	0.000138	0.000489	0.000198	0.000329	0.002782	0.000169	0.000768	0.000471	0.000391
0.001813	0.000638	0.002691	0.001089	0.001907	0,015300	0.000930	0,004226	0.002898	0.002148
0.000630	0.000222	0.000935	0.000378	0.000628	0.005315	0.000323	0.001469	0.000901	0.000746
0.000982	0.000346	0.001467	0.000590	0.000979	0.008286	0,000604	0.002\$88	0.001404	0.001163
0,000060	0.000197	0.000831	0.000238	0.000558	0.004722	0.000287	0.001304	0.000800	0.000663
0.000638	0.000169	0.000835 0.004012	0.000323	0.000536	0.004587	0.000275	0.001252	0.000769	0.000537
0.002708	0.000952 0.001279	0.005394	0.001625 0.002184	0.002699 0.003629	0.022826 0.030686	0.001387 0.001854	0,006301 0,008471	0.003864 0.005198	0,003206
-0.562435	0.000302	0.001271	0.160500	0.000655	0,007233	0.000439	0.001997	0.001225	0.004313
0.002625	-0.400000	0.280000	0.100479	0.000832	0.002613	0,000171	0.000776	0.000476	9.000395
0,002247	0.080333	-1.015830	0.082285	0.170090	0.102349	0.006415	0.026274	0.017884	9.014378
0.424534	0.055758	0.133704	-0.846801	0,115826	0.009069	0.000567	0.002600	0.001684	0.001271
0.009149	-0.000241	0.205108	0.054520	-0.694401	0.002461	0.000155	0.000680	0,000417	0.000346
0.001400	-0.000088	0.013882	0.000243	0,000498	-0.345545	0.010047	0.000673	0.000418	0.000343
0.002347	0.000074	0.018785	0,000645	0,001109	0.214688	-0.319806	0,001236	0,000759	0.000484
0.001190	-0.000124	0.012582	0.000163	0.000356	0.001250	-0.019305	-0,400142	0.005526	0.000626 0.002337
0.000798	-0.000191	0.010514	-0.000010	0.000107	0.000915	-0.000185	0,007235	-0.527608	0.001484
0.001829	-0.000009	0.015842	0.000414	0.000758	0.004718	0.000116	0.006473	0.003535	-0.308562
									1
0.002399	0.000079	0.018740	0.000545	0.001107	0.007606	0.000284	0,009278	0.004485	0.420164
0,002236	0.000061	0.017938	0.000610	0.001011	0.006937	0.000235	0.007674	0.004226	0.000896
6.001853	-0.000064	0.014423	0.000301	0.000584	0.003221	0,000036	0.005662	0.003078	0.000138
0.001697 0.001715	-0.000036 -0.000036	0.015263	0.000368	0.000685	0.004107	0.000084	0.006144	0.008349	0.000348
0.001038	-0.000140	0,012274	0.000370 0.000130	0.000322	0.004127 0.000947	0.000085	0.006185 0.004431	0.003354	0,000249
0.001000	0.000410	0,011011	0,000100		0,000aa	-0.000000	0.001101	0.002000	-0.000144
0.000462	-0.000247	0.006813	-0,000148	0.000169	-0,002717	-0.000281	0.002450	0.001234	-0.000592
8.000747	0.000199	0.010981	-0.000098	0.000680	-0.001162	-0.000199	0.003291	0.001714	-0.000401
0,000226	-0.000285	0.007644	-0.000239	-0.000242	0.005113	-0.000348	0.001777	6,000648	-0.000744
0.000669	-0.000178	0.010906	0.000022	0.000156	-0.000500	-0.000162	0.008654	0.001923	-0.000318
-0.000795	-0.000414	0.002330	-0.000562	-0.000888	-0.009574	-0.000548	-0.001264	-0.000694	-0.001437
0.001678	-0.000042	0.016089	0.000355	0.000664	0.008990	0.000074	0.005041	0.003290	0.000235
0.001569	0.000061	0.014509	0.000308	0.000595	0.003310	0.000041	0.008711	0.003100	0.000522
0.002385	0.000077	0.016736	0.000860	0.001110	0.007776	0.000981	0.008181	0.001187	0.000625
0.002375 0.000968	0,000074	0.013628	0.000637	0.001097	0.007643	0.000272	0.006072	0.001116	0.000668
0.000908	-0.000181	0.011382	-0.000335	0.000157	-0.000600	-0.000189	0.003792	0.001981	-0.000319
0.001667	-0.000044	0.015014	0.001819	0.000685	0.003546	0.000070	0.006000	0.003266	0.000316
0.002239	0.000051	0.017937	0.000787	0.001011	0.005938	0.000236	0.007676	0.004227	0.000696
0.002275	0.000658	0.018151	0.000608	0.001037	0.007189	0.000347	0.007795	0.004294	0.000623
		•							
0.001545	-0.000064	D. 014639	0.000302	0.000584	0.003226	0.000036	0.005671	0,003078	0.000187
0.001347	-0.000098	0.013354	0.000024	0.000456	0,002087	-0.000025	0.005050	0.003726	0.00001
0.000678	-0.000422	0.003448	-0.000572	-0.000782	-0.008393	-0.000686	0.000625	-0.000526	-0.001291
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0.001427	-0,000085	0.018773	0.000250	0.000504	0.002533	0.000000	0.065289	0.009889	0.000050
0.002119	0.000032	0.018773	0.000200	0.000941	0.002533	0.000203	0.007845	0.004309	0.000053
0.001989	0.000010	0.016674	0.000481	0.000857	0.005598	0.000163	0.000040	0.003811	0.000420
0.003111	0.000031	0.017305	0.000531	0.000933	0.006267	991000.0	0.007812	0.004017	0,000518
0.003198	0.000030	0.017295	0.000530	0.000934	0.006278	0.000301	0.007829	0.004014	0.000518
		[1				1
0,009389	0.000077	0.018735	0.000645	0.001108	0.007761	0.000280	0.000131	0.004466	0.000599
0,003365	0.000039	0.017564	0.000552	0.000968	0.006841	0.000216	0.007469	0.004102	0.000547
0.001251	0.000114	0.012873	0.000178	0.000395	0.001881	-0.000051	6.004773	0.002564	-0.000004
0.091281	0.000109	0.015028	0,000191	0.000414	0.001743	-0.000043	0.004863	0.002515	-0.000064
-0.005609	0.000139	-0.000999	-0.000381	-0.004065	-0.024682	-0.000100	-0.000324	-0.008531	-0.002090
-0.003534	-0.000923	-0.003763	-0.001824	-0.002182	-0.021888	-0.001340	-0.005908	-0.003696	-0.003089
0.008235	0,000681	0.003183	0.001226	0.003588	0.023888	0.001078	0.006588	0.004744	0.002795
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TABLE 5

	Commodities	Sweet polatoes	Sugar	Corn syrup	Apples	Bananas	Oranges	Other fresh fruits
olumn		19	20	21	22	23	24	25
Row				·				
1	Beef	0.000065	0.000913	0.000297	0,000325	0.000189	0.000393	0.00029
2	Veal.	0.000355	0,005021	0.001633	0,001788	0.001040	0.002160	0.00164
3	Pork	0.000124	0.001745	0,000567	0.000620	0.000361	0.000750	0,0005
4	Lamb and mutton	0.000193	0.002719	0.000884	0.000987	0.000383	0.001170	0.0005
6	Chicken	0.000110	0,001550	0.000504	0.006551	0.000321	0.000667	0.00050
6	Turkey	0.000108	0.001489	0.000484	0.000530	0.000309	0.000641	0.0004
7 8	Fish	0.000533	0.007491	0.002437	0.002687	0.001551	0.003224	0.00241
	Eggs.	0.000717	0.010070	0.003276	0.003585	0.002085	0.004335	0.0032
	Butter	0.000169	0.002374	0.000772	0.000845	0.000491	0.001022	0.00073
10	Lard	0.000066	0.000923	0.000300	0.000329	0.000191	0.000397	0.00030
11 12	Shortening	0.002375	0.033576	0.010926	0.011938	0.006975	0.015741	0.01101
12	Margarine		0.002969	0.000966	0.001055	0.000617	0.001392	0,00097
13	Salad dressing Fresh milk	0.000057	0.000808	0.000263	0.000287	0.000168	0.000379	0.00026
14 15	Evaporated milk	0.000057	0.000799	0.000260	0.000284	0.000168	0.000875	0.0002
10 16		0.000105	0.001487	0.000478	0.006522	0.000305	0.000689	0,00048
17	Cheese	0.000385	0.005458	0.001778	0.001941	0.001134	0.002669	0.00170
18		0.000246	0.003466	0.001128	0,001233	9.000720	0.001625	0.00113
19	Polatoes	0.059934	0.000753	0.000245	0.000268	0.000158	0.000353	0,0002
20	Sweet potatoes	-0.520414	0.001401	0.000458	0.000499	0.000291	0.000667	0.00046
20 21	Sugar	0.000062	-0.241858	0.052022	0.001392	0.000813	0.001835	0.00128
22	Corn syrup	0.000010	0.131678	-0.442900	0.000425	0,000248	0.000560	0.00039
23	Apples	0.000027	0.002773	0.000456	-0.720000	0.124629	0,255814	0.00302
24	Bananas.		0.002780	0.000487	0.213601	-0.614937	0.000460	0.00303
25	Oranges.	0.000036	0.001496	0.000140	0.101204	0.000000	-0.663184	0,00303
28	Other fresh fruits	-0.000107	0.000020	-0.000260	0.001339	0.000862	0.002800	-0.60000
27	Canned peaches	-0.000076	0.000648	-0.000090	0.003542	0.029481	0.030882	0,00698
28	Canned pineapples Dried fruits	-0.000131	-0.000478	-0.000396	0.122799	0,000000	0.000000	0,00663
29		-0.000063	0.000913	-0.000017	0.000000	0.111765	0,000000	0.00707
20 30	Frozen fruite	-0.000241	-0.002747	-0.001008	0.003004	0.001767	0.005254	0.00587
31	Lettuce	0.000024	0.002697	0.000465	0.000182	0.000603	0.005030	0,00238
32		0.000011	0.002462	0.000398	0.000119	0.000665	0.004793	0.00223
88	Beans	0.000099	0.004252	0.000686	0.000575	0.000942	0.006530	0.00317
34	Carrote	0.000097	0.004212	0.000873	0.000564	0.000930	0.006493	0.00311
35	Other fresh vegetables	-0.000052	0.000997	-0.000012	-0.000270	0.000241	0.003437	0.00146
36	Canned peas	0.000022	0.002668 0.003916	0.000457	0.000198	0.000601	0.005001	0.00234
37	Canned corn	0.000083		0.000796	0.000490	0.000824	0.006209	0.00299
38	Canned tomatoes.	0.000009	0.004007 0.002420	0.000818	0.000511	0.000887	0.006296	0.00304
39	Dry vegetables	-0.000013	0.001958	0.000390 0.000268	0.000111	0.000548	0.004763	0,00221
40	Frozen vegetables	-0.000218	0.002268	-0.000366	-0.000004	0.000337	0.004316	0.00197
41	Other canned fruits and	-0.000218	0,008208	-0.000880	-0.001121	-0.000465	0.000224	-0.00023
	vegetables	-0.000004	0.002137	0.000313	6.000040	0.000488	0.004498	0.00206
42	Rice	0.000070	0.003555	0.000728	0.000437	0.000816	0.005969	0.00286
43	Wheat flour	0.000058	0,003375	0.000648	0.000333	0.000752	0.005687	0.00271
44	Breakfast cereals	0.000069	0.003544	0.000721	0.000421	0.000810	0.005947	0.00265
45	Corn meal	0.000069	0.003640	0.000722	0.000420	0.000610	0.005946	0,00285
45	Bread and other cereals.	0.000099	0,004249	0.000887	0.000675	0.000941	0.006538	0.00317
47	Coffee	0.000075	0,003755	0.000751	0.000449	0.000884	0.006654	0.00291
48	Soup	-0.000023	0.001753	0.000200	-0.000057	0.000405	0.004117	0.00186
49	Other beverages	-0.000019	0.001820	0.000227	-9,000040	0.000420	0.004181	0.00190
50	Ail food	-0.000071	-0.001963	-0.002328	-0.002084	-0,001198	-0.005508	-0.00785
51	Nonfood	-0.000496	-0.007014	-0.002293	-0.002494	-0.001457	-0.003288	-0.00230
52	Expenditure propertions.	0.000399	0.005881	0.002301	0,002396	0.001398	0.003794	0.00346

(Continued)

Canned peachea	Canned pine- apples	Dried fruite	Frozen fruite	Lettuce	Tomatoca	Beans	Onione	Carrote	Other fresh vegetable
26	27	28	29	30	31		33 	34	35
0,000138	0.00088	0.000087	0.000054	0.000187	0.000233	0.000129	0.000097	0,000081	0.00066
0.000762	0.000482	0.000479	0.000349	0.001031	0,001282	0,000712	0.000531	0.000334	0,00332
0.000264	0.000167	0.000186	9.000122	0.000358	0.000446	0.000247	0.000184	0.000116	0.00115
0.000412	0.000281	0.000259	0.000189	0.000558	0.000695	0.000386	0.000287	0.000181	0.00180
0.000235	0.000149 0.000143	0,000148 0,000142	0,000108	0,000318 0,000205	0.000396	0.000220	0.000164 0.000167	0.000108	0.00102
0.000226	0.000722	0.000714	0.000525	0.001534	0.001912	0.001058	0.000796	0.000099	0.00098
0.001522	0.000971	0,000960	0.000706	0,002063	0 002870	0,001423	0.001070	0.000073	0.0066
0.000359	0.000229	0.000225	0.000166	0.000486	0.000806	0.000335	0.000252	0,000159	0.0015
0.000139	0.000089	0.000088	0.000085	0.000189	0.000236	0.000130	0.000098	0.000062	0.0006
0.005088	0.003238	0.003202	0.002339	0.006898	0.008578	0.004755	0.003547	0.002350	0,0222
0.000450	0,000286	0.000283	0.000207	0,000610	0.000758	0.000420	0,000314	0.000208	0.0019
0.000123	0.000078	0.000077	0.000057	0.000166	0.000207	0.000115	0.000086	0.000087	0.0005
0.000121	0.000077	0.000076	0.000056	0,000164	0,000204	0.000113	0.000084	0.000056	0.0005
0.000222	0,000141	0.000140	0.000103	0.000301	0.000375	0,000209	0.000154	0.000103	0.0009
0.000827	0.000526	0.000521	0.000380	0.001121	0.001394	0.000773	0.000677	0.000382	0.0038
0.000525	0.000\$34	0.000331	0.000241	0.000712	0.000885	0.000401	0.000366	0.000243	0.0022
0.000114	0,000073	0.000072	0.000052	0.000155	0.000192	0,000107	0,000050	0.000053	0.0004
0,000212	0.000136 0.000378	0.000134 0.000373	0.000097 0.000273	0.000289 0.000804	0.000367 0.001000	0.000199	0.000149	0.00098	0.0009
0,000181	0,000118	0.000114	0.000084	0.000245	0.000305	0.000169	0.000126	0.000084	0.0007
0.002437	0.038416	0.000149	0.009036	0.000115	0.000144	0.000080	0.000000	0.000040	0,0003
0.030145	0.000319	0.068117	0.003036	0.000519	0.000769	0.000427	0.000318	0.000211	0.0019
0.011621	0,000212	0.000047	0.003036	0,001695	0.002108	0,001109	0,000972	0.000578	0.0054
0.002776	0.002222	0.001666	0.003332	0.000601	0.000747	0.000414	0.000309	0.000205	0.0019
-0.769157	0.125909	0.064183	0.018497	0.000990	D, 001231	0.000682	0.000509	0.000837	0.0031
0.155849	-0.826206	0.000000	0.001153	0.000066	0,000082	0.000046	0,000034	0.000023	0.0002
0.106957	0.000150	-0.655307	0.007920	0.000329	0.000409	0.000227	0.000169	0.000112	0,0010
0.013910	0.000526	0.003866	-1.000000	0.002389	0.002970	0.001647	0.001229	0.000814	0.0077
0,001277	0.000394	0,000343	0.003750	-0.141400	0.040788	0.031481	0.000000	0.008715	0.0081
0.001211	0.000366	0.000317	0.003645	0.036367	-0.384600	0.000000	0.000172	0.007044	0,0065
0.001691	0.000572	0.000509	0.004829	0.055288	0.000305	-0.255000	0.000003	0.003038	0.0007
0.001879	0,000568	0.000340	0.001609	0,000199 0,020100	0.000\$13	0.000000	0.034141	0.033953	0.0042
0.001268	0.000390	0.000173	0.003762	0.002498	0.002628	0.000005	0.000472	0.001261	-0.3200
0,001601	0.000533	0,000055	0,004442	-0,123530	0.000248	0.000000	0.020852	0.000172	0.0008
0.001625	0.000543	0.000482	0.004492	0,000172	0.000264	0.004203	0.000000	-0.049995	0,0008
0.001203	0.000352	0.000314	0.003630	-0.218945	0.000000	0.024469	0.004042	0.004929	0.0004
0,001080	0,000309	0,000285	0.003378	0.028191	0.000000	0.000000	-0.000127	0.000061	0.0031
-0.000011	-0.000005	0.000187	0.001071	0.012495	0.016062	0.007142	0.005354	0.005354	0,0404
0,001127	0.000330	0,000195	0.003473	0.000402	0.000440	-0.000186	-0.000011	0.000292	0.0092
0.001535	0.000504	0.000447	0.004307	0,000401	0.000395	0.000050	0.000023	0.000243	0.0005
0.001687	0.000471	0.000415	0.004148	0.000353	0.000339	0.000025	0.000005	0.000223	0.0007
0.001529	0.000502	0.000444	0.004295	0.000396	0.000391	0.000018	0.000021	0.000241	0.0008
0.001528	0.000501	0.000444	0.004294	0.000397	0.000390	0.000048	0.000021	0.000241	0,0008
0.001692	0.000571	0.000652	0.004628	0.000497	0.000508	0.000101	0.000060	0.000282	0.0011
0.001559	0.000814	0.000456	0.004368	0.000414	0.000412	0.000058	0.000028	0.000248	0.0008
0.001025	0.000285	0.000242	0.003264 0.003300	0.000088	0,000028	-0,000115	-0.000097	0.000115	-0.0000
0.002249	-0.002298	-0,001260	-0.005806	-0,000097	0.000041	-0.000109 -0.000142	-0.000093 -0.000123	0.000120	-0.0000 -0.0041
-0.001219	-0.000789	-0.000729	-0.000488	-0.001486	-0.001814	-0.000993	-0.000122	-0.000468	-0.0046
0.001416	0.001133	0,000850	0.001700	0.001398	0.001797	0.000799	0.000599	0.000599	0.0045
					0.001.01	1	0.0000000	0.000000	1

TABLE 5

	Commodities	Canned peas	Canned corn	Canned tomatoes	Dry vegetablee	Frozen vegetables	Other canned fruits and vegetables	Rice
aluma '	<u> </u>	36	37	38	39	40	41	42
Row					-			
1	Beef	0.000221	0,000178	0.000109	0.000103	0.000078	0,000739	0.00020
2	Veal	0.001215	0.000978	0,000608	0.000564	0.000429	0,004063	0.00110
3	Pork	0,000422	9,000340	0.000209	0,000196	0.000149	0.001411	0.00038
4	Lamb and mutton	0.000658	0,000530	0.000326	0.000306	0.000233	0.002200	0,0006
5	Chicken	0.000375	0.000303	0.000186	0.000174	0.000133	0.001254	0.0003
6	Turkey	0.000380	9,000290	0.000178	0.000167	0.000127	0.001205	0.0003
7	Fish	0.001813	D. DOJ 460	0.000894	0.000845	0,000640	0.006063	0.0016
8	Eggs	0.002438	0.001963	0,001202	0.001138	0.000860	0,008151	0.0022
8	Butter	0.000575	0.000463	0.000283	0.000268	0.000203	0.001922	0.0005
10	Lard	0.000223	0,000180	0.000110	0,000104	0.000079	0.000747	0.0002
11 12	Shortening	0.008111	0.006558	0.004040	0.003785	0,002869	0.027178	0.0074
12	Margarine.	0.000717	0.000580	0.000367	0.000335	0.000254	0.002402	0.0006
18 14	Salad dressing	0.000195	0.000158	0.000097	0.000092	0.000069	0.000854	0.0001
15	Freeh milk	0.000193	0,000156	0.000096	0.000090	0.000068	0.000647	0.0001
16	Evaporated milk	0,000354 0,001319	0.000287 0.001066	0.000176	0.000165	0.000125	0.001188	0.0003
17	Ice aream	0.000838	0.000677	0.000657 0.000417	0.000615 0.000391	0.000468	0.004417	0.00120
18	Potatoee	0.000182	0.000147	0.000090	0,000085	0,000298	0.002805	0.00076
ĨŶ.	Sweet potatoes	0.000339	0.000274	0.000168	0.000158	0.000064 0.000119	0.000609	0.0001(
20	Bugar	0.000945	0.000765	0.000471	0.00041	0.000335	0.001135	0.0003/
21	Cora aytup	0,000289	0.000232	0.000144	0.000135	0.000102	0.000967	0.0002
22	Apples	0.000137	D.000110	0.000068	0.000064	0.000048	0.000458	0,00013
23	Bananas.	0.000727	0.000588	0.000362	0,000339	0.000257	0.002437	0.00064
24	Отводев	0.001994	0.001612	0.000993	0.000930	0.000705	0,006879	0.0018
25	Other fresh fruits	0.000705	0.000571	0,000352	0.000329	0.000250	0.002366	0.0000
26	Canned peaches	0.001184	0.000941	0.000580	0.000543	0.000412	0.003900	0.0010
27	Canned pineapples	0.000078	0,000063	0.000039	0.000036	0.000028	0.000261	0.00007
28	Dried fruite	0.000387	0.000313	0.000193	0.00018t	0.000137	0.001298	0.00038
29	Frozen fruits	0.002609	0.002271	0.001400	0.001311	0.000994	0.009411	0.00257
30	Lettuce	-0.125083	0.000000	-0.133699	0.017200	0.015992	0.002027	9.00026
81	Tomatoes	0.000000	0.000000	0.00003	0.000010	0.015953	0.001533	0.00014
32	Веаль	0,000015	0.005987	0.038778	0.000184	0.016243	0.000177	0.00016
33 34	Onions	0.049332	0.000021	0.005979	0.000000	0.016234	0.001057	0.00011
34 35	Carrota	0.000000	-0.094900	0.006870	0.00000	0.015699	0.002192	0 00015
30 36	Other fresh vegetables	0.000113	0.000054	0.000109	0,000642	0.015987	0.000600	0.00012
37	Canned peas	0.185000 0.050001	0.047200	0.033962	0.014684	0.016187	0,003581	0.00022
38	Canned tomatoes.	0.059001 0.056376	-0.265000 0.000000	0.000127	0.059132	0.016202	0.008307	0,00021
39	Dry vegetables	0.024200	0.078600	0.000000	0.000037	0.015398	0.001904	0.00006
40	Frozon vegetables	0.012856	0.010127	0.007597	-0.480000 0.007597	0.015573	0.003115 0.053182	0.00008
ñ	Other canned fruits and	0.012000	0.010147	0.001401	0.007097	-1.009900	0.000154	0.00170
	vegetables	0.000614	0.000430	6.000240	0.000459	0.015902	-0.409000	0.00108
42	Rice.	0.000201	0.000146	0.000144	0.000194	0.003124	0.005681	-0.32000
43	Wheat flour	0.000153	0,000108	0.000119	0.000169	0.003002	0.005352	0.04992
44	Breakfast cereals	0.000195	0.000143	0.000143	0.000109	0.009114	0.005656	0.00537
46	Corn meal	0.000195	0.000142	0.000142	0,000192	0.003112	0.005652	0.00000
45	Bread and other cereals	0.000296	0.000221	0.000195	0.000255	0.003365	0,006345	0.00025
47	Coffee	0.000214	0.000157	0.0001.52	0.000202	0.003160	0.006781	0.00035
48	Soup	-0.000308	-0.000100	-0.000019	0.000028	0.002828	0.003522	0.00002
49	Other beverages	-0.000097	-0.000092	-0.000013	0.000033	0.002356	0.003598	0.00002
50	All food	-0.000471	-0.000330	-0,000762	-0.000914	-0.005427	-0.006875	-0.00050
51	Nonfood	-0.001695	-0.001370	-0.000876	-0.000631	-0,000600	-0.005677	-0.00155
52	Expenditure proportions.	0.001416	0.001133	0.000850	0,000650	0.001700	0.005950	0.00133

(Continued)

Wheat	Breakfast	Сога	Bread and	Cottee	Boup	Other	All		<u> </u>
flour	elaeroo	meal	other cereals		Doup	beverages	food	Nonfood	Income
43	- 44	45	46	47		49	50	51	. <u>6</u> 2
0.000346	0.000983	0.000134	9.003592	0.000652			İ		
0.001905	0.005407	0.000739	0.019758	0.004690	0,000415 0,002283	0.000530	-0.389553	0.099639	0,289914
0.000662	0.001878	0.000267	0.006864	0.001624	0.000793	0.001013	-0.179327	0.203185 0.045868	0.591134
0.001032	0,002928	0.000401	0.010702	0.002539	0.001236	0.001579	-0.767470	0.196303	0.133459 0.571167
0,000688	0.001669	0.000228	0,006102	0.001447	0.000705	0.000000	-0.239835	0.061345	0.178490
0.000565	0.001603	0.000219	0.006880	0.001391	0.000677	0.000866	-0.920213	0.157824	0.768389
0.002839	0.008065	0.001099	0.029472	0.006990	0.003405	0.004348	-0.005411	0.001384	0.004027
0.000900	0.002558	0.001478 0.000348	0.039620	0.009398	0.004577	0.005846	-0.073743	0.016862	0.054881
0.000350	0.000994	0.000135	0.003539	0.002215 0.000881	0.001079	0.001378	-0.427444	0.109331	0.318113
0.012736	0.036177	0.004933	D, 132187	0.031344	0.015271	0,019508	0.067184	-0.017184	-0.059000
0.001126	0.003199	0.000436	0.011687	0.002771	0.001350	0.001725	0.000000	0.009999	0.029094
0.000307	0,000870	0.000118	0.003178	0.000736	0.000368	0.000470	-0.382785	0.097908	0.254877
0.000303	0.000861	0.000118	0.003146	0.000746	0.000384	0.000464	-0.273638	0.009991	0.203847
0.000566 0.002070	0.001581	0.000217	0.008778	0.001370	0.000668	0.000552	0.000000	0.000000	0.000000
0.001315	0.003881	0.000802 0.000509	0.021488	0.005095	0.002482	0.003171	-0.334389	0.085530	0.248859
0.000285	0.000811	0,000111	0.013645 0.002964	0.003236	0.001576	0.032014	-0,445158	0.113662	0.331296
0.000530	0.001500	0.000207	0.005512	0.001308	0.000342	0.000437 0.000813	-0.156716	0.040085	0.116631
0.001465	0.004218	0.000575	0.015412	0.003655	0.001871	0.002275	-0.043167	0.000000	0.000000
0.000453	0.001287	0.000176	0.004703	0.001115	0.000543	0.000094	-0.233411	0.059703	0.173709
0.000314	0.000609	0.000083	0.002225	0.000528	0.000257	0.000329	-0.158015	0.046090	0.139925
0.001142	0.003244	0.000443	0.011853	0.002810	0.001369	0.001749	-0.187133	0.047885	0.139268
0.003131	0.008893	0.061213	0.032493	0,007705	0.003754	0.004795	-0.349973	0.089516	0.260457
0.001828	0.003161 0.005192	0.000430	0.011512	0.002730	0.001330	0.001699	-0.537475	0.137475	0.400000
0.000122	0.000347	0.000047	0.018971 0.001368	0.004499 0.000301	0.002193	0.002800	-0.399212	0.088542	0.340670
0.000608	0.001728	0.000236	0.006313	0.001497	0.000147 0.000729	0.000187 0.000232	-0.524135 -0.389423	0.076861	0.447274
0.004411	0.012530	0.001709	0.045783	0.010856	0.005289	0.006757	-0.888801	0.054173 0.227374	0.315250 0.661427
0.000448	0.001265	0.000173	0.004624	0,001096	0.000534	0.000682	-0.172288	0.025205	0.147023
0.000240	0.000683	0.000093	0.002495	0.000592	0.000288	0.000368	-0.228834	0.056531	0.170393
0.000271	0.000771	0.000105	0.002818	0.000668	0.000326	0.000416	0.000000	0.000000	0.000000
0.000323	0.000578 0.000916	0.000079	0.002114 0.003349	0.000501	0.000244	0.000312	-0.006319	0.001616	0.004703
0.000208	D, D00591	0.600081	0.003349	0.000794 0.000512	0.000387	0.000494	-0.429128	0.109782	0.319366
0.000377	0.001071	0.000146	0.003915	0.000928	0.000249 0.000452	0.000318 0.000578	~0.201553	0.051553	0.150000
0.000367	0.001048	0.000142	0,003810	0.000903	0.000440	0.0006/8	-0.043072 -0.031771	0.011017 0.008126	0.032056 0.023645
0.000119	0.000339	0.000016	0.001237	0.000293	0.000143	0.000183	-0.203221	0.029801	0.023048
0.000153	0.000434	0.000059	0.001587	0.000376	0.000184	0.000234	0.254101	0.637275	0.216916
0.002921	0.008297	0.001131	0.030135	0.007189	0.003502	0,004474	-0.827856	0.211748	0.618108
0.001854	0.005267	0.000718	0.019244	0.004563	0.002223	0.002840	-0.268737	0.068737	0.200000
0.088792	0.026367	0.000002	0.003063	0.001452	0.000707	0.000904	-0.074553	0,019069	0.055484
-0.300000 0.000060	0.000000 -0.220000	0.004466	0.010000	0.003358	0.001636	0.002080	-0.111703	0.028571	0.083132
0.011838	0.900000	0.000000	0.006280	0.002977	0.001450	0.001653	-0.077494	0.019821	0 057673
0.001263	0.002218	0.000237	-0.150000	0.002202 0.001894	0.001073 0.000922	0.001371	-0.077672	0.019867	0.057805
0.001512	0.003649	0.000361	0.006500	-0.252161	0.000922	0.001179	0.000000	0.000000	0.000000
0.000732	0.001506	0.000111	0.000538	0.032660	-0.450000	0.026323	-0.003409	0.016234 0.081238	0.047235 0.236378
0.000758	0.001574	0.000119	0.000743	0.033031	0.020834	-0.438699	-0.309048	0.079048	0.236378
-0.001383	-0.001414	-0.000408	-0.003916	-0.002270	-0.004720	-0.003837	-D. 230846	0.060680	0,176265
-0.002660	-0.007556	-0.001031	-0.027613	-0.006548	-0.003189	-0.004076	-0.235288	-1.017898	1.243165
0.002360	0,006516	0.000889	0.022212	0.005573	0.003538	0.004475	0.227018	0.772082	1,000000

Over —5	-8 to -3	-3 to -1	1 to 1	J to 3	3 to 5	Over 5
Eggs Lard	Veal Butter	Milk Ice aream	Pork Lamb	Beef Sugar	Margarine Salad and cook- ing oil	Beans
8weet potatoes Dried fruits	Evaporated milk Oranges Canned pess	Corn syrup Apples Canned peaches Tomatoes Carrote Canned corn Dried vegetables Wheat flour Corn meal Coffee	Chicken Shortening Potatoes Cauned pineapple Onions Breakfast cereals	Bananas Lettuce Rice Soup	Checce	
TOTAL COMMO	DITIES:					
4	6	12	8	6	3	1

TABLE 6 CLASSIFICATION OF COMMODITIES ACCORDING TO LINEAR TREND

logarithm of the constant term plus 2, if all variables in the first difference analysis are converted to logarithms and if the constant term differs significantly from zero. For example, in the case of cheese, a_i is equal to .017222 and we to kthe antilogarithm of 2.017222 as 104.20. So we could say that time trend alone would increase consumption of cheese by 4.20 per cent annually. For eggs, we have a_1 equal to -0.025019 and, therefore, we found the antilogarithm of 1.974981 as 94.40, which means that time trend alone would decrease the consumption of eggs by 5.60 per cent annually. Though some of the commodities appearing in Appendix table A-6 showed coefficients not significantly different from zero, we took these coefficients also to obtain the percentage effects of time in each year on the consumption of these commodities. Summary table 6 is based on the percentage changes given in Appendix table A-6.

Seasonal effects on time trend

When quarterly rather than annual data are used, considerable seasonal vari-

ation is possible. Therefore, it may not be appropriate to assume that the effect of season is the same for all the seasons. To test the seasonal effects on time trend, we specified two different types of regression equations:

(a) The first type is the same as in (109), except that the first differences correspond to differences in observations from season to season. The constant term in this equation can be interpreted as an indication of the linear effect of seasons, assuming that the trend during different seasons does not vary.

(b) The second type assumed that the time trend varied from season to season. Instead of putting a single constant, we specified four constants corresponding to four seasons (using dummy variables) and all the other variables were retained as in (109). In this case, the coefficients corresponding to each dummy variable can be interpreted as the time trend associated with that particular season. Having estimated both types of equations, we tested the significance of individual coefficients, using *t*-values, and the difference in the two specifications,

using *F*-values. For this study, we have confined this analysis to five commodities—butter, margarine, shortening, salad and cooking oil, and lard. In table 7, column a_i corresponds to the constants obtained when no dummy variable was introduced and s_1 , s_2 , s_3 , and s_4 correspond to the coefficients of the four dummy variables, denoting four quarters of the year. While the linear effect of time was not significantly different from zero in the case of all commodities when season was not considered, these coefficients became significantly different from zero in eight cases when season was introduced. The F-test showed that three out of five commodities showed variations in the constants according to season.

Analysis of the Farm-retail Price Spread

The retail market is only one link in a chain of institutions or agencies affecting the marketing process and the prices at these levels are linked by marketing charges (defined to include costs such as transportation, processing, packaging. and profits). Often public policy decisions may be influenced by the behavior of marketing margins and an economic analysis of factors influencing prices will not be complete without proper consideration of this aspect. In many situations demand theory has overlooked the spread between prices at the retail level and at the farm level, and only a limited number of studies have treated margins explicitly. The lack of understanding of the nature of margins and their behavior on the market seriously limits our understanding of demand theory. This section analyzes the nature of price spreads between the retail and farm levels, and explores the possibilities of obtaining demand elasticities at one level of the marketing system from a knowledge of these measures at another level.

Marketing margins and the elasticity of demand

The Concept of the Farm-retail Price Spread — A farm-retail price spread (marketing margin or marketing charge) "is the difference between the retail price of a product and its farm value—the payment (adjusted for by-product values) to farmers for an equivalent quantity of farm products" (U. S. Department of Agriculture, 1957, p. 1). Generally the spread includes the costs incurred and profits enjoyed by all agencies involved in the transfer of products from farmers to consumers. Often, these charges include the payments for the services such as assembly of raw materials from the farm, processing, storage, transportation, wholesaling, and retailing.

This study divides consumer expenditures on food items into two parts: payments to the farmers as returns for production of raw food products (farmer's share) and payments to the agencies that assemble and process the raw materials and distribute the final product to consumers (farm-retail spread). Both of these together equal the retail price. For measurement purposes, if any two of these factors are known, the third can be deduced. The practice of the U.S. Department of Agriculture is to obtain retail price and farmer's share independently and to deduce the farmretail spread. Three measurements used in obtaining estimates of farmer's share are discussed by Ogren (1956). These measures, together with the retail prices

TABLE 7 SEASONAL EFFECTS ON TIME TREND

-

				Beastral coefficient			Sum of	Domeon of] ₽
Commodity	Equation	1	1	5	Ξ	4	equarte of deviations	freedom	statistic
Buttler	General	1H9H00'					002143	Ř	
	Dummy varjabje	(1899))	116720	- , (134874 (-3.8289)	. 003078 (4. 3172)	087730 (→2.6970)	89119140'	*	0.5411*
Margarine	General	. 106021 					125210.	88	
	Dummy verjable	(2000-)		, 006894 (0. 6047)	. (060021 (4. 8000)	(0291.)	\$00300	*	14, 19900*
Øbortsving.	General	140200' -					061866	38	
	Dimary variable	(100933) — 1	0(3115 (1.0049)	.006273 ()	.010042 (.6706)	,019056 (-1.4300)	04,14,140	8	1.08131
finited and cooking oil	General	002200					.134140	8	
	Dumur variable	(00)	020733 (-1,4428)	006613 (3350)	—. 030437 (1573. —)	.027064 (1.2962)	\$2291t	35	1.7980†
Lard	General	.000668					506211	8	
	Dumny varjable		(0876°-)		(95120) (95438)	(066910 (-3.4882)	600020 .	\$	0.7941

Significant.
 Nonsignificant.

published by the Bureau of Labor Statistics, provide us with data on farmretail spread.

The importance of marketing services varies for different commodities. In general, the farmer's share decreases as the number of intermediate operations increases. Fox (1951, p. 68) points out that marketing margins for food crops show great variation. Grain products undergo much processing between farms and consumers. Meat products move through the marketing system in a short time. Fruits and vegetables, during the producing seasons, may go directly from the processor to the consumer without much processing. In other crops, transportation costs may account for a substantial portion of the marketing spread. In the present study, we could obtain data on marketing margins for 32 commodifies; among them, the farmer's share varied widely. Table 8 shows that the highest percentage of farmer's share is for butter (about 75 per cent) and the lowest for breakfast cereals (about 10 per cent).

Pricing methods.—Because the basis of calculating farm-retail spread is the retail prices paid by the consumers and the payments received by farmers for equivalent quantities of products, an understanding of pricing practices is necessary (see discussions in Oxenfeldt, 1966, Chs. 9 and 10 and Kotler, 1967, Ch. 15). No single method of setting price is applicable to all the products. Oxenfeldt (1966, pp. 289-294) discusses two types of pricing methods—complete and partial methods.

Complete pricing methods. The prices at each level may be set, using any one of the following methods:

(a) Cost-plus pricing and average-cost pricing, calling for the addition of some base cost as a margin to cover profit.

(b) Flexible mark-up method, calling for

	Тав	LE 8		
FARMER'S	SHARE	OF	RETAIL	PRICE

	Farm price/retail price				
Commodity	Quarterly data*	Annual data†			
	per caul				
Meat	1				
Beef	59,44				
Pork					
Lamb					
Chicken	62,46				
Eggs	65.16				
Fats and oils					
Butter		75.90			
Shortening		37.08			
Margarine	28.33				
Salad dressing	20.70				
Milk products					
Milk	44.04				
Evaporated milk		48,12			
Cheese		44.60			
Ice creara	\$7.18	•			
Polators					
White					
Sweet		37, 52			
Sugar	35.99	87.90			
Fruit					
Apples		32.68			
Oranges					
Canned peaches Dried fruit		35.05			
Vegetables					
Lettuce					
Freeh tomatoes	. 84.80 43.4L				
Beans	32.59				
Oniona					
Carrots Canzed peas		14,17			
Canned peas	12.69	18.79			
Caused tomatoes		16.91			
Dried vegetables		44.93			
Other					
Wheat flour	35.35				
Breakfast cereal		10.82			
Corn meal					

* Data for 1955 to 1967 obtained from USDA (1968), various issues).

various issues). † Data for 1947 to 1964 taken from USDA (1965) and data for 1965 and 1966 obtained from USDA (1968b, various issues).

markup to be varied on the basis of several possible considerations, including demand conditions. (c) Trial-and-error or experimental pricing method, calling for trying one or more prices that seem to be appropriate and choosing the one which gives best results.

(d) Research method of pricing which is based on actual market trials through experimental markets.

(e) Intuitive method of pricing which is based on the price setter's intuitive knowledge. It may not involve any systematic techniques.

Partial pricing methods. The prices at each level may be fixed through price maintenance or price followership. Price maintenance implies that a constant price that has been proven effective is retained for a long period. Price followership implies that prices charged by the "followers" will, in some way, be related to the price charged by a "leader."

In addition to complete and partial pricing methods, two other forms of pricing are known as price-line pricing and multi-stage pricing. In price-line pricing, the price charged for a commodity is retained at the same level for a long time but adjustments are made in quality to offset increased cost. Multistage pricing is done in different stages such as selection of market target, choice of brand image, choice of marketing mix, selection of pricing policy, selection of pricing strategy, and choice of specific price.

Hoos (1954, pp. 123-141) classifies the farm-retail spread as systematic and nonsystematic. Systematic methods of setting margins include: (1) fixed absolute margin, (2) fixed percentage margin, and (3) costs-per-pound margin which varies with the store's purchase price. Nonsystematic methods include: (1) following closely the price of near or strong competitors by "shading" under or "padding" over the price set by a "leader" or a "competitor" and (2) shortrun profit maximization.

Types of price spread.—These pricing practices provide guidelines to determine the relationship between price spreads and prices at different levels of the marketing system. In an analysis of this nature, it is possible to incorporate only "systematic" margin policies. In many studies on price spreads (see Dalrymple, 1961, for a review), it is assumed that price spreads are determined in one of the following ways:

Constant percentage spread assumes that the margin is a percentage of prices at the farm level or at the retail level. Although it is not necessary to assume that the percentage remains the same for all levels of volume, in many cases it is assumed to be constant. Let $p^{(r)}$ denote the retail price, $p^{(f)}$ the farm level price, and M the margins. Under constant percentage margins (say, k percentage of retail prices),

$$M = k p^{(r)} \tag{110}$$

Therefore,

$$p^{(r)} = p^{(f)} + kp^{(r)}$$
(111)

or

$$p^{(\prime)} = (1 - k)p^{(\prime)}$$

Absolute spreads add a specified amount to the farm-level price to obtain the retail price. In some cases, the amount to be added may be a function of variables like price and quantity. However, the simplest case is to assume a fixed quantity as the margin (M^0) .

$$p^{(r)} = p^{(f)} + M^0. \tag{112}$$

Price spread and quantity handled may have certain relationship. In this case, it is often assumed that the price spread is a linear function of the quantity handled (q).

$$M = a + bq. \tag{113}$$

Therefore, the relationship between farm price and retail price can be written as

$$p^{(r)} = a + bq + p^{(f)}. \tag{114}$$

Though these three assumptions regarding the behavior of marketing margins may be applicable to certain situations, it seems appropriate to assume that the price spreads are determined as a combination of percentage and absolute margins. Dalrymple (1961, pp. 5-6) points out that wholesalers appear to use a constant percentage markup and retailers appear to make use of an absolute margin so that when we consider the market as a combination of wholesalers and retailers, it may be appropriate to consider margins as a combination of these two approaches. Also, studies by Thomsen (1951, pp. 221-223), Shepherd (1955, pp. 253-254), and Rojko (1957, p. 157) reveal that margin is composed of elements of which about 50 per cent are absolute and 50 per cent are percentages. Waugh (1964, p. 20) reports that, ". . . many studies of this matter (percentage and absolute spread) in the [U.S.] Department of Agriculture suggest that the price spreads are neither constant percentages nor constant absolute amounts, but somewhere in between the two." Here, the margins are specified as a linear function of retail prices.

$$M_j = \alpha_j + \beta_j p_j^{(r)} \tag{115}$$

where

$$j$$
 stands for the j^{th} commodity.

If $p_i^{(r)}$ and $p^{(t)}$ denote the retail- and farm-level prices,

$$p_j^{(r)} = p_j^{(f)} + M_j.$$
 (116)

From (115) and (116)

$$p_j^{(r)} = p_j^{(f)} + \alpha_j + \beta_j p_j^{(r)}.$$

 $= a_i + b_i p_i^{(r)}$

Therefore,

$$p_{j}^{(f)} = -\alpha_{j} + (1 - \beta_{j})p_{j}^{(r)}$$
 (117)

where

$$a_i = -\alpha_i$$
 and

$$(1 - \beta_i) = b_{i*}$$

Using the data reported by U. S. Department of Agriculture, we have fitted an equation of type (117) for 32 commodities and the results are presented in table 9.

The table shows that 19 commodities. had both slope and intercept significantly different from zero: beef, pork, lamb, chicken, eggs, butter, shortening, milk, checse, ice cream, potatoes, sugar, oranges, canned peaches, lettuce, beans, onions, carrots, and breakfast cereals. In 11 commodities the intercepts were not significant but the slopes were: margarine, salad dressing, sweet potatoes, apples, dried fruit, tomatoes, canned peas, canned tomatoes, dry vegetables, wheat flour, and corn meal. The nonsignificance of a_i implies that α_i also is nonsignificant. Therefore, for these commodifies, the hypothesis that margin is a linear function of retail prices is not different from a hypothesis that margin is a fixed proportion of retail prices. Finally, in two commodities-evaporated milk and canned corn-the inter-

	TABLE 9		
RELATIONSHIP BETWEEN FARM	PRICE AS A	FUNCTION OF	F RETAIL PRICE

Commodities grouped as to significance" of:	Data†	Jotercept (-aj)	81ope (b ₁)	<i>R</i> 2
Nope and intercept				
Beef	Q	24,52	. 9188	.75
Pork	Q	-21.58	.9014	.90
Lamb	Q		.8447	.78
Chicken	Q	- 6.12	. 6769	.95
Egg	Q	-14.08	.9214	.93
Butter	Q	18.59	.454L	.44
	A	\$3,55	1.0011	.77
Shortening	Q	7.79	. 2330	.37
	Å	-50,74	.9410	.76
Freeh mitk.	Q	89	.4897	.00
Checee	Q	18.46	1591	.21
	Å	4.96	.3005	.58
Ice cream	Q	- 3.09	.3179	.93
Potatoes.	ě.	- 22,13	6630	.65
Sugar	Č.	9.03	1995	.41
-	Ā	8.90	2145	.70
Oranges	Q	-10.48	\$674	.49
Canned peaches.	Q.	- 3.25	2752	.60
Lattuce	Ă	- 3.17		.79
Beaus	A	- 0.73	.4724	.98
Onions	Ä	- 4.00	.7070	. 180
Carrote	A	- 6.81	,7090	.39
Cereals	Q	7.57	1973	.86
Rope but not intercept				
Margarine	Q	- 1.68	.3457	.35
Salad dreesing	Q	- 0.37	.2173	.24
Sweet potatoes	Q	- 0.19	.3934	. 95
Apples.	Q	1.81	.2298	.23
	A	- 0.33	.3479	.85
Dried fruit	A	- 0,95	.3022	.90
Fresh tomatoes	A	- 0.87	.3769	.72
Canned peas.	Q	D.69	. 1091	.24
	A	- 0.06	.1447	.52
Canned tomatoes	Q	1.49	. 0659	.04
Ļ	Å	.30	,1495	.41
Dried vegetables	A	- 0.37	. 4759	.90
Wheat flour	Q	- 4.32	.4337	.17
Corn mest	Q	0.04	,2681	.77
vercept but not slope				
Evaporated milk	Q	3.60	, 1663	.06
	Å	2.85	. 2629	.18
Canned corp.,	Q	- 2.54	- ,0110	.01
	Ā	2,13	0224	.03

* Significant at the 5 per cent level. † Quarterly data (Q) relate to 1985-1967 period, and annual data (A) to 1947-1968 period.

cepts were significantly different from zero but not the slopes. Nonsignificance of the slope $(b_i = 1 - \beta_i)$ implies that β_i is not significantly different from one. implying that the farm level prices may not change with a change in retail price.

The negative slope for cereals, given in table 9, illustrates one problem in the above analysis. The negative slope may be caused by (a) widening margins and higher retail prices over time due to more elaborate packaging, changes in the products themselves, the exercise of market power, or similar factors; and (b) a general downward trend in the farm prices of cereal grains that may be associated with markets other than domestic use in ccreals. If grain prices were to rise, holding prices of all other marketing costs constant, cereal prices would tend to rise in time, given the expected positive relation between farm and retail price. A limitation of the above analysis is that a detailed study of marketing margins and costs was not undertaken that would allow analysis of the relation of farm and retail prices, holding marketing costs constant.

Effect of margins on derived demand.—In many empirical studies it may be necessary to derive demand parameters at one level of the marketing system from a knowledge of corresponding parameters at another level. When we consider the intermediaries such as processors, wholesalers, and retailers, it is possible to derive demand functions for all these levels. The quantity demanded by processors, quantity consumed, retail price, and farm-level price can be determined simultaneously using a simplified model consisting of the following elements.

(a) Consumer demand.

where

 $q_e =$ quantity consumed, $p^{(r)} =$ retail price, and y = consumer income.

 $f_1(q_c, p^{(r)}, y) = 0$

(b) Marketing group behavior. This consists of the supply and demand for the marketing group and can be reduced to a single equation of the form

$$f_2(q_s, p^{(r)}, p^{(f)}, V_2) = 0 \qquad (119)$$

where

 q_c , $p^{(r)}$, and y are defined as in (118) and V_2 represents all other variables influencing marketing group behavior. (c) Producer supply. Let q_p be the quantity supplied. The producer-supply relationship can be expressed as

$$f_3(q_p, p^{(j)}, V_3) = 0 \qquad (120)$$

where

V₃ represents all other exogenous variables influencing supply.

If equilibrium conditions are assumed, $q_p = q_e = q$. Using (118), (119), and (120), it is possible to eliminate $p^{(r)}$ and a derived demand equation¹³ can be obtained of the form

$$f_i(q, p^{(f)}, y) = 0.$$
 (121)

Thus, using the behavioral equations of various marketing groups, we can obtain derived demand equations for one level from the corresponding demand equation for another level in the marketing system.

Bearing this in mind, let us analyze the implications of the behavioral assumption of margins specified in (115) on elasticities at the farm level and elasticities at the retail level. Here, it is assumed that there are *n* commodities $q_1, q_2 \cdots, q_n$ with retail price $p_1^{(r)}, p_2^{(r)}, \cdots, p_n^{(r)}$. The elasticity at the retail level is defined by

$$e_{ij} = \frac{\partial a_i}{\partial p_j^{(r)}} \cdot \frac{p_j^{(r)}}{q_i}$$
(122)
$$(i, j = 1, 2, \dots, n),$$

Let the corresponding farm-level prices be $p_1^{(f)}, p_2^{(f)}, \dots, p_n^{(f)}$, and the corresponding margins be M_1, M_2, \dots, M_n .

(118)

¹⁸ This is similar to the derived demand relation specified in Hildreth and Jarrett (1955, p. 108). Also see Foote (1958, pp. 100-102). This formulation assumes that farm price and processing price are determined in the same time period, which is not necessarily the case. A more realistic formulation might deal with expected, rather than equilibrium, prices.

If it is assumed that the margin is a linear function of retail prices, using (117), it is possible to specify a relationship between farm-level prices and retail prices as

$$(1 - \beta_j)p_j^{(r)} = \alpha_j + p_j^{(f)}.$$
 (123)

Therefore,

$$p_j^{(r)} = \frac{1}{(1-\beta_j)} (\alpha_j + p_j^{(f)}).$$
 (124)

The elasticities obtained from a derived demand equation can be represented as

$$E_{ij} = \frac{\partial a_i}{\partial p_j^{(f)}} \quad \frac{p_j^{(f)}}{q_i} \tag{125}$$

which, in this case, can be treated as the farm-level elasticity. Now $\partial_{q_i}/\partial p_j^{(f)}$ can be expressed as

$$\frac{\partial q_i}{\partial p_j^{(f)}} = \frac{\partial q_i}{\partial p_j^{(r)}} \cdot \frac{\partial p_i^{(r)}}{\partial p_j^{(f)}} \qquad (126)$$

From (124), the value $\partial p_{j}^{(r)}$ can be obtained as

$$\frac{\partial p_j^{(r)}}{\partial p_j^{(f)}} = \frac{1}{(1-\beta_j)} \,. \tag{127}$$

Substituting (126) and (127) in (125),

$$E_{ij} = \frac{1}{(1-\beta_j)} \frac{\partial a_i}{\partial p_j^{(r)}} \cdot \frac{p_j^{(f)}}{q_i} ,$$

$$= \frac{1}{(1-\beta_j)} \cdot \frac{\partial q_i}{\partial p_j^{(r)}} \frac{p_j^{(r)}}{q_i} \cdot \frac{p_j^{(f)}}{p_j^{(r)}} ,$$

$$= \frac{1}{(1-\beta_j)} \cdot e_{ij} \cdot \frac{p_j^{(f)}}{p_j^{(r)}} \text{ and}$$

$$= e_{ij} \cdot \frac{p_j^{(f)}}{(1-\beta_j)p_j^{(r)}}.$$
(128)

Again, we can express (128) in terms of α_i by substituting the value of $(1 - \beta_i)p_i^{(z)}$ from (123) as

$$E_{ij} = e_{ij} \cdot \frac{p_j^{(f)}}{\alpha_j + p_j^{(f)}}.$$
 (129)

The relationship in (129) can be used to derive conditions under which the elasticity at retail is higher than the elasticity at the farm level. Special cases of this result are shown in Hildreth and Jarrett (1955, p. 111) and Foote (1958, p. 105). From (129), we have

$$E_{ij} \leq e_{ij} \text{ if } \alpha_j \geq 0.$$
 (130)

Special cases.—Constant percentage spread. When the price is a constant percentage of retail price, we can write

$$p_{j}^{(f)} = k_{j} p_{j}^{(r)}$$
 (131)

Comparing (131) with (123),

$$\alpha_i = 0 \text{ and } (1 - \beta_i) = k_i. \quad (132)$$

From (129) and (132),

$$E_{ij} = e_{ij}.\tag{133}$$

Therefore, the elasticities at the farm level and at the retail level are the same.

Constant absolute spread. Here, we have

$$M_i = \alpha_i \text{ and } \beta_i = 0.$$
 (134)

From (128) and (134) we can write

$$E_{ij} = e_{ij} \cdot \frac{p_j^{(f)}}{p_j^{(r)}}.$$
 (135)

The elasticity at the farm level is obtained as a product of elasticity at the retail level and the proportion of farm price to retail price. Because in most cases retail prices are higher than the farm price, the elasticity at the farm level is lower than the elasticity at the retail level as discussed, for example, by Waugh (1964, p. 78).

Elasticity of price transmission.—Elasticity of price transmission is the ratio of relative change in retail price to the relative change in the farm-level price. If we denote this elasticity for the j^{th} commodity as η_{j_i}

$$\eta_j = \frac{\partial p_j^{(r)}}{\partial p_j^{(r)}} \cdot \frac{p_j^{(f)}}{p_j^{(r)}}.$$
 (136)

When we assume that the marketing margin is a linear function of retail prices, from (127) we have

$$\frac{\partial p_j^{(r)}}{\partial p_j^{(f)}} = \frac{1}{(1 - \beta_j)}.$$

Substituting this in (136), η_j is obtained as

$$\eta_j = \frac{1}{(1-\beta_j)} \cdot \frac{p_j^{(r)}}{p_j^{(r)}}.$$
 (137)

Using the average prices at the farm and retail levels, we have calculated the elasticity of price transmission for 32 commodities included in the present analysis. In the majority of the cases, the elasticity of price transmission was less than one. Hildreth and Jarrett (1955, p. 111) explain the implications of an elasticity of price transmission of less than one as follows: ". . . if producers' price rises while quantity processed and such other factors as prices of inputs used by processors remain fixed, the relative change in consumer price will not exceed the relative change in producers' price. This would certainly be true if effective competition

existed in processing, and might be expected to be typical of other instances as well."

Derived farm level elasticities

As stated before, clasticities at one level of the marketing system can be derived from a knowledge of the elasticities at another level; the direct and cross elasticities for many commodities can also be obtained at the retail level. This section shows how elasticity at the farm level can be obtained from clasticity at the retail level and the elasticity of price transmission. In (128), it was established that the relationship between retail-level elasticities and farmlevel elasticities follows the pattern,

$$E_{ij} = e_{ij} \frac{p_i^{(f)}}{(1 - \beta_j)p_i^{(r)}}.$$

Also, from (137),

$$\eta_j = \frac{1}{(1-\beta_j)} - \frac{p_j^{(f)}}{p_j^{(r)}}$$

A combination of these two results

$$E_{ij} = e_{ij} \cdot \eta_j \tag{138}$$

shows that the elasticity at the farm level is the product of elasticity at the retail level and the elasticity of price transmission. Since, for most commodities, elasticity at the farm level is lower than the elasticity at the retail level, the elasticity of price transmission should be less than one. Table 10 shows that the elasticity of price transmission was less than one for 24 commodities. In two commodities (corn meal and canned tomatoes) the margin behavior is such that one of the special cases (percentage margin) is applicable and when we have constant percentage spread, the elasticity of price transmission is one. Table 11 presents the elasticities at the farm

TABLE 10 ELASTICITY OF PRICE TRANSMISSION, EXPRESSING THE PERCENTAGE CHANGE IN RETAIL PRICE TO A 1 PER CENT CHANGE IN FARM PRICE

Commodity	Electicity
Meals	
Beef	.646917
Pork.	583224
Lamb	636246
Chicken	774894
Rega	.707173
Pats and alls	
Butter	,706369
Shortening	1.400023
Margarine	.819340
Salad drossing	.952760
Milk producte	
Kilk	. \$37509
Evaporated milk	2,561220
Cheese	2.740936
Ice cream	. 855069
Potatoes	
White	484788
Bweet	.953660
Sugar	1.804544
Pruit	
Fresh apples	. 939406
Freeh orangee	. 686715
Canned peaches	. 632480
Dried Iruita	.893730
Vogetables	
Letiuce	,676210
Freah tomatoes	.923259
Bosna	918910
Onions	, 160910
Carrote	378923
Canned pess.	979548
Canned corn	6,155602
Canned tomatoes.	1.130774
Dried vogstablee	.9441.50
Other	
Wheat flour	.814939
Breakfast cereals	606390
Corn mesi.	1.014740

level obtained as the product of retaillevel elasticities in table 5 and the elasticities of price transmission corresponding to 26 commodities. The commodities are retained as at the retail level and no attempt is made to convert them to the equivalent commodities at the farm level.

Seasonal variation in margin behavior

Seasonal variation of prices of many agricultural products differ widely among commodities and commodity groups. For example, fresh fruits and vegetables grown locally during the summer and fall may move directly from farmers to consumers while in winter transportation costs on fresh crops absorb a substantial portion of the consumer's payments. Gale (1961, p. 5) observes, ". . . seasonal changes (in prices and price spreads) for most fruits and vegetables were relatively large, but those for dairy products were small, Eggs, frving chicken, and meat products tended to fall into an intermediate group in magnitude of seasonal variation. Tomatoes showed the widest seasonal fluctuations in prices and spreads of those products reported on, and fluid milk showed the smallest fluctuations." This study uses a covariance analysis to test the significance of the intercept and slope of the relationship expressing price spreads as a linear function of retail prices in different seasons.

Covariance analysis.—Using the quarterly data for the period 1955–1967, we have specified the following three relationships:

First, all the four seasons are considered together to obtain a single regression equation without incorporating any seasonal factors, or

(a) $p^{(f)} = a + bp^{(r)}$.

Second, all the four seasons are considered together and it is assumed that the intercept is different in the four seasons but the slope remains the same, or

(b)
$$p^{(f)} = d_1 D_1 + d_2 D_2 + d_2 D_2$$

where

 D_1 , D_2 , D_3 , and D_4 correspond to four dummy variables such that

 $+ d_{I}D_{I} + c p^{(r)}$

$$D_i = \begin{cases} 1 \text{ in the } j^{\text{th}} \text{ quarter} \\ 0 \text{ elsewhere.} \end{cases}$$

Third, it is assumed that both slope and intercept are different during the four seasons, or

$$p_{1}^{(f)} = a_{1} + b_{1}p_{1}^{(r)},$$

$$p_{2}^{(f)} = a_{2} + b_{2}p_{2}^{(r)},$$

$$p_{3}^{(f)} = a_{3} + b_{3}p_{3}^{(r)}, \text{ and }$$

$$p_{4}^{(f)} = a_{4} + b_{4}p_{4}^{(r)}$$

where

(¢

 $p_{j}^{(f)}$ and $p_{j}^{(r)}$ represent the farm-level and retail-level prices, respectively, in the jth season (j = 1, 2, 3, 4).

If s_1 , s_2 , and s_3 correspond to the sum of squares of deviations corresponding to these three different specifications. we can calculate *F*-values and test the significance of the differences in these specifications. Only four commodities (chicken, potatoes, apples, and carrots) showed significant variations in margin behavior in both slope and intercept (table 12). In three commodities (pork, shortening, and salad dressing), the intercept did not vary from season to season but the slope did. Two commodities (milk and tomatoes), showed seasonal variation in intercept without any variation in slopes. The remaining 18 commodities included in the covariance analysis showed no change in either slope or intercept over the seasons.

Alternative specifications of margin behavior

In the previous analysis, specification of the marketing margins as a linear function of retail prices was based on the hypothesis that the pricing practices followed by the marketing group was in accordance with this specification. Although, in many cases, this hypothesis gave a reasonable explanation of margin behavior, there is no reason why all commodities should follow the same pattern. Another relationship may give a better result. The approach used in the previous sections to obtain the nature of changes at different levels in the market is still valid under alternate specifications of margin relationship. For example, if we have reason to believe that the price spread is determined as a combination of an absolute spread and a percentage of farm-level price, we can write the margin relationship as

$$m_i = \alpha_i + \beta_i^* p_i^{(f)}$$
. (139)

As before,

$$p_j^{(\prime)} + m_j = p_j^{(r)}.$$
 (140)

That is,

$$p_{j}^{(f)} + \alpha_{j}^{*} + \beta_{j}^{*} p_{j}^{(f)} = p_{j}^{(r)},$$

$$(1 + \beta_{j}) p_{j}^{(f)} = -\alpha_{j}^{*} + p_{j}^{(r)}, \text{ or }$$

$$p_{j}^{(f)} = -\frac{\alpha_{j}^{*}}{(1 + \beta_{j})} + \frac{1}{(1 + \beta_{j})} p_{j}^{(r)}, (141)$$

$$= \alpha_{j}^{*} + b_{j}^{*} p_{j}^{(r)}.$$

Equation (141) is similar to equation (117). All the remaining relationships can be developed similarly. Again, the relationship assumed here is for aggre-

TABLE DEMAND INTERRELATIONSHIPS

	Commodities	Beef	Fork	Lamb	Chicken	Egga	Butter	Margarine	Salad
olumn	:	1	2	& mution 3	1	5	6	7	dressin 8
Row							· ·		
	 10t	A 110105		A					
12	Beef Veat	-0.416485 0.232434	0.046180	0.026907	0.052356	0.000946	0.000233	0.000162	0 0003
2	Pork	0.232434 0.049349	-0.240879	0.012003	0.134494 0.027316	0.005203 0.001808	0 001281 0.000445	0.000892	0 0013
4	fors. Lamb and	0.040340	-0.240819	0 030212	0.021310	v.vuisua	0.000445	0.000310	U 0 00 3
ĩ	mutton .	0 381326	0 519864	-1,670464	0.181006	0.002818	0 000691	0.000483	D, 0008
5	Chicken.	0.127486	0.070429	0.034397	-0.602348	0.001014	0.000395	0.000275	0.000.
ti	Turkey	0 063126	0.038073	0.011325	0.30995R	0.001518	0.000380	0.000265	0.000
7	Fish	0.013527	0 015501	0.001306	0.005254	0.007764	0.001913	0.001331	D, 002.
8	Eggs	0.006585	0.005470	0.001234	0,002577	-0.225079	0.002571	0,001789	0.003
9	Hutter	0.001258	0.000177	0.000710	0.000244	0.005364	-0.460860	0.131504	0 000
10	Lard	0.008693	0.008958	0.001410	0.003489	0.012900	0.001854	0.062326	0.000
11	Shortening.	0.007102	0.007088	0.001285	0.002793	0 010593	0.001587	0.042839	0.162
12 13	Margatine Salad	0.007691 0.002252	0.007766	0.001342	0.003049	0.011470	0.299878	-0.693572	0.110
14	dressing. Fresh nitk	0.004140	0.001604 0.002912	0.000847 0.000938	0.000735	0.007322 0.007577	0.006463	0.014670	-0.661
15	Evaporated milk	0.007610	0 007592	0.001325	0.002997	0.011114	0.000995	0.000199	0,000
18	Cheese.	D. 002657	0.001837	0 000847	0.002991	0.006703	0.000541	0.000528	0.000
17	Ice cream	0.000987	→0.000139	0.000853	0.000107	0.005114	0.000560	0.000125	0.000 0.000
18	Potntoes	D, 005336	0,007040	0.001111	0.002017	0.009253	0 001292	0.000330	0.000
19	Sweet							0.000000	0.400
	potatoes	0.005217	0.002893	0.000790	0.001389	0.011568	0.001695	0.000528	0.001
20	Sugar.	0.007046	0 007014	0.001279	0.002768	0.010874	0 001579	0.000425	0, D00:
21	Corn syrup.	0.002257	0.003626	0.000997	0 001507	0.008151	0.001097	0.000247	0.000
22	Apples	0.004866	0.004437	0.001062	0.001509	0,008813	0 001199	0.000302	0.000
23	Валипан	0 001970	0.004438	0.001064	0.001812		0 001211	0 000303	0.000
24 25	Oranges Other fresh	0.002267	0.001243	0.000790	0.000632	0.005853	0.000747	0 000107	0.000:
26	fruit Canned	0 000102 0 000796	-0.001783 -0.000365	0.000547 0.000692	-0.000503 0.000026	0.003802	0.000326 0.000528	-0.000119 -0.000023	0.000
27	peaches Canned pinespples	-0.001357	-0.002926	0.000452	-0.000927	0.003929	0.000167	-0.100023	0.000 -0.000
28	Dried Iraits	0.001293	0.000237	0.000715	0.000250	0.005428	0.000614	0.000018	0.000
29	Frozen fruits	0.005688	0.008022	0.000027	-0 002829	-0.001194	-0.000562		-0.000
30	Lettuce	0.004713	0.004265	0.001050	0.001746	0.003642	0.001185	0.000291	0,000
31	Tomatoes	0,004247	0,003716	0.001005	0.001511	0.008212	0,001108	0.000252	0.000
32	Beans	0.007690	0.007733	0.001345	0.003059	0.011468	0.001685	0.000705	0.0010
33	Onione .	0.007619	0.007665	0.001334	0.003016	0.011472	0 001678	0.000522	0,0010
34 35	Carrots Other fresh	0.001233	0 000136	0 000707	0 000208	0.005366	0.000684	-0,000274	0.000
	vegetables	0.001660	0.004193	0.001015	0.001721	0.008609	0.001178	0.001245	KK00.0
36 37	Canned pess	0.007053 0.007214	0.007023	0.001281 0.001295	0.002773 0.002839	0.010597	0.001582	0,000604	0.000%
38 38	Canned corn Canned to- matoes	0.007214 0.004169	0.007207	0.001293	0.002839	0.011018	0.001607	0.000652	0,000
39	Dry vegeta- bles.	0 003308	0.003021	0,000990 0,000911	0,001308	0.007336	0.000051	0.000247 0.000020	0.0004
40	Frozen vege- tables.	-0.001776	-0.006946	0.000118	-0.002424	-0.000/346	0.00040B	-0.000469	~0.000
41	Other cunned fruits and							0.000100	
	vegetables	0.003618	0.093000	0 0D0949	0,001270	0.007650	0.001005	0,000205	0.0004
42	Rice	0.008563	0.006450	0.001232	0.002558		0 001497	0.000438	0.0008
43 44	Wheat flour Breakfast	0.006012	0.005798	0.001178	0.002315 :		0.001405	0.000394	0.0005
45	cerculs	0.006527	0.006400	0.001329	0.002513		0 001491	0.000435	0.0008
45 46	Corn meal . Bread and . other	0.006523	0.004304	0,001230	0.002543	0.010366	0.001489	0 000434	0.0008
	cercals	0,007694	0,007780	0,001343	0,003054	0.011484	0.001688	0.000528	0,0010
47	Coffee	0.006739	0.006637	0.001250	0.002636	0.010681	0,001627 ;	0.000452	0.0009
48	Soup	0.002910	0.002132	0,000873	0.000953	0.006818	0.000864	0.000146	0.0003
49	Other bever-	1				1			
	ages.	0.003039	0.002283	0.000885	0.001007	0.007066	0.009905	0.000156	0.0003
50	All food	-0.027184	-0.014608	-0.003791	-0.007053	-0.002780	-0.003962	-0.000206	-0.0038
51	Nonfood	·-0.014043	0.016462	0,000533	0.006611	-0.007270	-0.001790	-0.001249	-0.0020

11

AT THE FARM LEVEL

g		11	Potatoes		1	peaches	featily	Lettuce	Tomatoe
	-	··	12		_			17	18
A			[ļ	ł				-l –
0.002608			0.000062	2 0 000305	0.00027/	0 00005	7 0.00007	8 0.000126	
0.014344 0.004983		0.001041	0.000339		0.001483		0 00042		0.00021
	0.000770 	0.000362	0.00011	\$ 0.600562	0,000518				0.00118
0.007768	0.001201	0.000564	0.000284	I 0.00090X	0 000803	0.00026			
0 001427	0.000681	0.000321	0.000105						I 0.000G4
0.004253	0 000658	0.090309	0.000101				0 00012		0.00036
0.021400	0 003304	0 001555	0.000509						0.00035
0 028768	0.004142	0.002091	0.000684						0.00176
0.000781 0.002837	D. D01017	0.000493	1 0 000161	0.000794	0.000702				0.00237
0.095953	0.000107	0 000191	0.000063		0.000273	0.000088			0.00055
0.006164	0.014839	0.006970	0.002265		0 010610				0.00021
0.005164	0.001312	0.000616	0.000200	0.000991	0.000956				0.00791
0.092307	0 000357	0.000165	0 000054	0.090270	0.000260				1
-0 323952	0.000353	0.000166			0.000258				0.00019
0.201272	0.000649	0.000304	0.000100	A @08400					0.00018:
0.001172	0 001725	0 001123	0.000368	0.000490	0.000473	0 000140			0.00034
~0 000858	-0 451141	0.000719	0.000234	0.001823	0.001757		0.000466		0.00128
0.004423	0.003023	-0.1495K2	0.057158	0.000153	0 001116	0.000332	0.000296	0.000181	0.00061
A 4999094			0.001100	0.100202	0.000242	0 000072	0.000064	0.000105	0 00017:
0 007320	0.003835	0.203690	-0.496308	0 000469	0.000451	0.000134	0.000120	0.000195	0.00000
0.006503 0.003020 ;	0.003613	0 000388	0.000076	0.00(308	0.001260	0 000375	0.000333	0.000544	0.000330
0.003850	0.002628	0.099067	0.000010	0.000399	0.000385	0.000114	0.000102	0.000166	0.000923
0.003869	$0.002864 \\ 0.002868$	0.000120	0.000026	-0.676372	0.175674	0 001541	0.000133	0.000078	0 000282
0 000838	0.002025	0.000121	0.000026	0.200655	0.000316	0.019000	D.060878	0.000419	0.000133
	0,002024	-0.000069	-0 000033	0.151492	-0 455418	0.007350	0.000042	0 001146	0.001946
-0.002547	0 001055	-0.000287	-9.600102	0.001258	0.001923	0 001756	0 001485	0.000406	0 000690
-0 001059	0.001466	·-0,000E94	-0.000072	0 003421	0.021173	-0 480153	0.057352	0.000669	0.001137
0.001793	0,000725	-0.000361	-0.000125	0.115358				1 1	
-0 0004ng ji	0.001644	-0.000154	-0.000060	0 000000	0.000000	0.098571	0.000000	0.000045	0.000076
-D 008976	-0.000764	-0.000697	-0.000230	0.002622	0.000060 0.003603	0.067648	-0 585668	0.000222	0.000378
0.003675	0.002813	0.000109	0 000023	0.000171	0.003454	0.003795	0.003276	0.001615	0.002742
0.003103	0.002651	0.000253	0.000010	0.000(12	0.003291	0.000308	0.000307	-0.095616	0 043107
0.007290	0.003837	0.000400 (0.000091	0.000540	0 001190	0.001070	0.000253	0.024592	-0.355085
0.007165	0.003803	0.000333	0 000003	0.000530	0.004459	0.001062	0.000155	0.037386	0.000283
0.000469	0.001694	-0 000155	-0.000059	-0,000254	0.002360	0.000523	0.000450 0.000304	0.000135	0.000751 0.019264
0.003606	0.002793	0.000104	0.000021	D, 000468	0.00%/24	A 4000000			0.011214
0.006504	0.003514	0.000289	0.000078	0.000460	0.003434 0.004264	0.000302	0 000423	0 001689	0.002426
0.008712	0.003672	0.000302	0.000083	0.000480	0.004324	0.001013	0.000058	- 0.083532	0.000226
0.003024	0.000600.0				0.000024	0,001028	0.000431	0.000116	0.000244
	0.002630	0.000066	0.000001	0.000104	0 003271	0.000761	0.000261	-0.145053	0.000000
0.001967	0.002330	0.000000	-0.000011	-0.000004	0.002964	0.090653	0.000237	0.019063	0.000000
-0.007866	-0.000449	-0.000626	-0.000208	-0 00:053	0.000154	-0.000028	-0 000107	0.005449	0.014829
	I			1	I	I			
0.002375	0.002445	0.000026	-0.000004	0.000038	D 00:000		I		
0.005935	0.003453	0.000252	0.000067	0.000401	0.003082	0.000713	0.000174	0.000272	0.000406
0.005248	0.003259	0.000208	0.000053	0.000332	0.003099	0.000971 0.000922	0.000399	0.000271	0.000265
0.005875	0.003435	0.000249	0.000066						0.000313
0.005586	0 003432	0.000249	0.000066 0.000066	0,000395 0,000395	0.004084 0.004083	0.000367 ¹	0.000397 0.000397	0.000268	0.000361
					W. 001060	0.000966	0.000397	0 000268	0.000360
0.007295	0.003836	0.000339	0.009094	0.000540	0.00		.	i	
0.005132 j	0.003507	0.000265	0.000072	0.000540	0,004490	0.001070	0.000493	0.000336	0.000469
0.001182			-0.000022	-0.000422	0.004157	0.000986	0.00040B	0.000250	0.000380
	1			0.000004	0.002827	0.000945	0 000216	0.000058	0.000026
0.001633			-0.000018	-0.000038	0.002871	0.000660	0.000223	0.0000c4	0.000000
			-0.00068	~0.001939	-0.003762		-0.001126	0.000066 -0.000683 (-	0.000038
v.u.u.u	-0 003100 -	-0.001456	- D. 000473			-0.000740	0.000140		-0.001675

TABLE 11 (Continued)

	Commodities	Веаля	Onions	Carrots	Canned	Canned	Dry	Wheat	Corn
Column		19	20	31	peas 22	tomatoes 23	vegetables 24	flour 25	meal 26
Row	,			-		· · - -• ·• •		·	· · · ·
1	Beef	0 000119	0.000045	0,000023	0.000216	0.000109	0,000097	0.000282	0.000134
2	Veal	0.000854	0.000245	0.000127	0.001190	0.000602	0.000533	0.001553	0.000739
3	, Pork	0.000237	0.000085	0.000044	0.000413	0 000209	0.000135	0.000539	0.000257
4	Lamb and								
	mution .	0.000355	0 000132	D. 000069	0.000645	0.000326	0.009259	0.000811	0.000401
5	Chieken .	0.000202	0.000076	0.000039	0.000367	0.000186	0.000161	0.000479	0.000228
6 7	Turkey Fish	0,000191 0.000972	0 000072	0,000035	0.000353	0.000178 0.000894	0.000156	0.000460 0.002314	0.000219
ŝ	Eggs	0.001308	0.000493	0.000255	0.002398	0.001202	0.001073	0,003191	0.001478
9	Butter	0.000308	0 000116	0 000060	0 000563	0.000253	0.000253	D.000733	0 000346
10	Lard	0.000119	0.000015	0 0/0023	0.000218	0.000110	0.000098	0.000285	0.000135
11	Shortening	0.004369	0.001635	0.000590	0.007945	0.004010	0.003574	D.DLD379	0.001933
12	Margarine.	0.000386	0.000145	0.000076	0.000702	0.000357	0.000316	0.000918	0.000136
13	Salad dressing	0.000106	0.000040	0.000022	0.000191	0,000097	0,000087	0.000250	0 000119
[4	Fresh milk	0.000104	0,000039	0,000021	0.000189	0 000036	0 000085	0.000217	0.000118
15	Evaporated	•.••••	0.0000						
		0.000191	0.000071	0.000039	0,000347	0.000176	0.000158	0.000453	0 000217
16	Cheese	0 000710	0,000266	0 000145	0.001292	0 000657	0 000581	0.001687	0.000503
17	Ice cream	0.000451	0.000169	0.000092	0.000821	0.000417 0.000090	0.000369 0.000369	0,001072 0,000232	0.000509
18 19	Pointoes Sweet	8,000098	0.000037	0.000020	0,000178	0,000090	0 00008D	0.000232	0.000111
14	potstoes	0.000183	0.060069	0.000037	0.000332	0.000168	0.000149	0.000432	0,600207
20	Sugar.	0.000509	0,000191 (0.000104	0 000927	0.000471	0.000416	0.001210	0.000575
21	Corn syrup.	0 000155	0.000059	0.000032	0.000263	0.000144	0.000127	0 000369	0.000176
22	Apples	0 000074	0.000028	0.000015	0.000134	0.000066	0.000060	0.000174	0.000083
23	Bananus.	0.000392	0.000147	0 0000090	0,000712	0,000362	0.000320	0.000931	0.000443
24 25	Oranges Other fresh	0 001074	0 000402	0 000219	0.001953	0.000993	0.000878	0.002552	D.001213
20	fruit	0.000380	0.000142	0,000078	0 000692	0 000352	0.000311	0.000904	0.000430
26	Canned								
	peaches	0.000627	0.000285	0.000128	0.001140	0.000580	0.000513	0.001490	0.000708
27	Canned						\		
	pineappies	0,000042	0,000016	0.000009	0.000076	0.000039	0.000031	0.000099	0.000017
28 29	Dried fruits Frozen Iruits	0.000209 0.001513	0.000078 0.000556	0.000042 0.000308	0.000379 0.002752	0.000193 0.001400	0 000171	0.000195 0.003595	0.000236
30	Letruce	D 028928	O CHINODO	0 003305	-0.122524	-0.133009	0.016239	0.000363	0,000173
31	Tomatoes	0.000000	0.000079	0.002669	0.030000	0.000003	0 000035	0.000196	0.000093
32	Beans	-0.234322	0.000001	0.001151	0,000044	0.038778	0.000174	0.000221	0.000105
33	Onions .	0 000000	-0 115228	0,012806	0.048323	0.005979	0.000000	0.000166	0.000079
34 35	Carrots	0.003469	0.015736	i ~0.166363	0.000000	0,006570	1 0.000000	0.000263	0.000125
5 3	Other fresh vegetables	0.000005	0.000218	0.000478	0.000111	0.000109	0,000606	0.000170	0.000081
36	Canned peas	0.000000	0.009611	0.000065	-0.181216	0,033962	0.013864	0,000307	0.000146
37	Canned corn	0.003662	0,000000	-0 018944	0.057794	0.000127	0 055829	0.000299	0,000142
38	Canned to-								
	matoes	0 022485	0.001963	0.001565	0,055223	-0,176000	0.000035	0.000097	0.000040
39	Dry vegeta- bles	0.000000	0 000059	0.000023	0.023705	0.000000	-0,453192	0.000125	0.000051
40	Frozen vege-	0.00000	0.000039	0.00028	0.040100	0.000000	-0,40,0152	0.000040	0.00007
	tables	-0.006563	-0.002468	0 002029	0,012397	0,007597	0.007178	0.002380	0.001131
4 1	Other					•			
	canned	i							
	fruits and	A 44014F	A 40000-			0.0000.00	0,000433	0.001511	0.000718
42	vegetables Rice	0.000125	0.000005	0.000111 0.000092	0.000601	0.000249	0.000153	0.072360	0,000002
-13	Wheat flour.	0 000023	0.000002		0.000150	0.000119		-0.244482	0.001166
41	Breakfast	1				1	1	•	
	cereals	0.000044	0.000010	0,000091	0,000192	0.000143	0.000181	0 000049	0,000000
45	Corn mea!	0.000011	0.000010	0.000091	0 000192	0.000142	0.000185	0.009647	-0.220000
40	Bread and	1	1						
	other cereals	0,000093	0.000028	0.000107	0.090281	0.000195	0,000241	0.001029	0.000237
47	Coffee.	0.000053	0.000013	0.000004	0,000210	0.000152		0.001232	0 000361
48	Soup.	-0.000106	-0 000045	0.000044	-0.000106	-0.000019		0.000597	0.000111
49	Other bever-				•		1	i	
	uges.	-0.000100	-0.000043	0.000045	-0.000065	-0,000013		0.000615	0.000119
50	All food .	0.000130	-0.000056	-0.000395	0.000461 -0.001660	-0.000763		-0.001127 -0.002168	-0.000408 -0.001031
51	Nonfood	-0.000912	···0.000341	-0.000177	-0.000560	-0.000876	-0,000/60	-0.005105	-0.001031

.

gate spreads. If we are interested to study the breakdown of aggregate spreads to different elements in the marketing system, we can specify appro-

priate behavioral assumptions for price spreads at each of these stages and carry out an analysis similar to that for the aggregate spread.

Income-Consumption Relationships

This section illustrates different anproaches to income-consumption relationships, using the 1955 and 1965 household food-consumption data obtained from the USDA (1956, 1968). In particular, it analyzes the effects of income, bousehold size, and region in determining the consumption pattern. and explains the changes in demand coefficients as a result of using quantity consumed or expenditures on different items as the dependent variable.

Estimation of income elasticities

Choice of data - Often the effect of income changes on consumption is measured by the elasticity of demand with respect to income (income elasticity) defined as the ratio of relative change in the quantity consumed to the relative change in income, holding other factors influencing demand at a constant level. Thus, the income elasticity for the i^{th} commodity is given by

$$e_{iy} = rac{\partial q_j}{\partial y} \cdot rac{y}{q_i}$$

where

 $q_i = f(p_1, p_2, \cdots, p_n, y)$ $q_i = \text{consumption of } i^{\text{th}} \text{ commodity},$ $p_i = \text{price of } i^{th} \text{ commodity, and}$ y = income.

Both time-series data from market statistics and cross-section data from

household food consumption surveys are used to obtain income elasticities. For time-series data, we specify a form of the demand function in terms of prices and income and obtain the coefficients through a regression equation. From this demand function, the income elasticity can be obtained as a partial derivative w.r.t. income when a double logarithmic form is used. For cross-section data, prices remain approximately the same for all consumers and, therefore, we can specify the demand relationship omitting prices.¹⁹ However, it is possible to

TABLE 12 SEASONAL VARIATION IN THE RELATION BETWEEN FARM-LEVEL PRICE AND RETAIL-LEVEL PRICE

Commodities with variation in slope and/or intercept	Commodifies without variation in alops or intercept
Intercept and slope	Beef
Chicken;	Lamb
Potatoes"	Eggs
Apples"	Butter
Carrota‡	Margarine
	Evaporated mith
Intercept only	Cheese
Milkt	Ice cream
Tomatoes*	Sugar
	Oranges
Slope only	Canned peaches
Pork†	Lettuce
Shortening*	Onions
Salad dressing*	Canned peas
	Canned corn
	Canned tomatoes
	Wheat flour
	Breakfast cereal

* Significant at 5 per cent level. † Significant 10 per cent level. ‡ Significant at 5 per cent for intercept, 10 per cent for alone.

¹⁹ Strictly speaking, in the cross-section data, apart from income, we can expect influences of variables like household size, education, social status, and similar other variables. Often classification of data according to all these factors may be difficult. (See Clark et al. (1954) and Rockwell (1959).

demand elasticities obtained from these two methods. In a static analysis, we assume that the consumer makes a change in consumption, if there is any, as soon as there is a change in income. A lag may exist in consumption adjustments as a result of income changes. Generally, the items included in family budgets have different durability and the purchases may represent a long-term consumption pattern. On the other hand, a short-term expansion in income may lead the consumer to acquire goods for immediate consumption. Wold and Jureen (1964, pp. 227-228) point out that, for the majority of consumers, the income level is fairly stable. For a group of families included in the cross-section data, the changes in income over time are, on the whole, small and infrequent compared with existing income differences between the families in the group. Therefore, "the families have usually adapted themselves to the income level at which they have been recorded, so that the budget data primarily reflect the demand pattern in the sense of long run income changes. In other words, the income elasticities derived from family budget data can most immediately be interpreted as long run elasticities." From the point of view of practical applications of demand analysis, these long-term elasticities are more relevant for many policy decisions than the shortterm elasticities obtained from timeseries data.²⁰ This is one reason why we chose income elasticities obtained from budget studies over those from timeseries data. Other reasons were:

give two different interpretations for the

(1) Time-series data on prices and income are highly correlated which makes it difficult to obtain structural income elasticities from time-series data. (2) Estimates of income elasticities may differ, depending on whether we use quantity or expenditure as the measure of demand. Comparing the estimates obtained from these two measures of demand, we can draw certain conclusions regarding the quality consciousness of consumers. It is often difficult to obtain consistent time-series data on these two measures of demand because of limitations in collecting and reporting data while, in a budget study, it is easy to incorporate these two measures.

(3) Demand elasticity may shift over time. When using time-series analysis, often we assume fixed coefficients if we do not include some shift variables. It is difficult to estimate the coefficients, using an assumption of varying parameters. If we have data for different cross sections, it may be possible to estimate one set of coefficients for each cross section and, then, taking these coefficients, we can estimate the trends in the coefficients if they follow a systematic patterns.

(4) To compare the elasticity measures for different commodities, the data must be comparable in other respects. If we are using time-series data to obtain income elasticities for different commodities, it is difficult to assure consistency in a number of other factors. Therefore, to obtain meaningful comparisons of income elasticities that can be used to assess the changes of different commodities due to an income change, it is desirable to keep a number of other variables constant. This is effectively handled in cross-section analysis because it provides a measure of the reaction of consumers' demand to changes in income without complications of changes in distribution of income, family size, and other social, economic, and demo-

²⁰ Wold and Jureen (1964, pp. 228-230) point out that irreversibility of demand functions and continued introduction of new products tend to make the income elasticities of family budget data smaller than the income elasticities obtained from time-series data.

graphic factors which are present in the time-series data.

We also chose to use cross-section data because detailed data on consumption and income were available from at least two nationwide surveys (in 1955 and 1965) on food consumption. The 1965 survey had a broad objective and, at the time of this analysis, only data relating to the spring quarter were available. Therefore, the present analysis is restricted to these data.

Choice of function.—To calculate the income elasticities, the first job is to specify a functional relationship of consumption and income. Various functional forms may be appropriate as for time-series analysis. Assuming that the effect of all other variables are negligible, a linear relationship between demand and income can be specified as

$$q = a + by. \tag{142}$$

In particular, when the variables q and y are in logarithms, the coefficient b is the income elasticity. If the data show the presence of a unit serial correlation coefficient, first differences of the variables will get rid of this serial correlation. In this case, it is convenient to use a regression equation of the form

where

- $\Delta q = a + b \Delta y \qquad (143)$
- Δq and Δy represent the first differences of the variables.²¹

Again, the income elasticities are obtained directly if the variables are specified in logarithms as

$$\Delta (\log q) = a + b \Delta (\log y). \quad (144)$$

Ordinary versus weighted regression.—Published data on food consumption from the cross-section surveys are reported by income groups. The effects of induced heteroskedasticity can be eliminated by using a weighted regression. In the present study, we have calculated the income elasticity for different commodities, using both ordinary and weighted regression procedures. We have used the per-capita quantity consumed and per-capita income²² for obtaining a regression equation of the form

$$\log q = a + b \log y. \tag{145}$$

On the whole, the estimates of income elasticity obtained from both ordinary and weighted regressions were not very different, but in many cases where the elasticities were positive, coefficients from weighted regressions were slightly higher than those from ordinary regressions, a result in conformity with that of Iyengar (1964). Table 13 gives the estimates obtained from these two methods. Further analysis of these data, with household size an added variable, indicates somewhat different estimates, as is discussed later.

Consumption differentials.—To show the relationship between the consumption differences in the upper and lowerincome groups and the income elasticity, a bivariate classification of commodities was constructed as table 14. The income elasticities used are the same as in column 2 of table 13. The quantity index is obtained by expressing the average per-capita consumption as a percentage of the per-capita consumption of persons in the lowest income-group (0-1,000

^a In time-series data, we define $\Delta q_i = (q_i - q_{i-1})$ while, using cross-section data, we have to take the differences between successive observations (samples) during the same period. If the succorrelation coefficient is other than unity, other methods of estimation are more appropriate.

²⁶ The per-capita income is obtained by dividing the family income by the number of persons in the family. The family income represents the family's 1964 money income after deduction of state and federal income taxes. See Appendix A for a description of the data and their sources.

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TABLE 13

COMPARISON OF INCOME ELASTICITIES OBTAINED FROM ORDINARY AND WEIGHTED REGRESSIONS BASED ON HOUSEHOLD FOOD CONSUMPTION SURVEY DATA, SPRING, 1965

Beef	(Terawa - 3/4		Income elasticity	
Veal .531 .591 .690 Pork .606 .006 .601 Pork .603 .006 .601 Chicken Chicken Chicken Chicken	Commonly	Ordinary regression	Weighted regression	Deviations
Pork 006 .099 .001 Lamb and mutton .591 .571 620 Kank 060 033 623 Fish 060 038 623 Fish 060 038 623 Fage 072 076 064 Butter	Beaf	.270	. 290	.020
Pork 606 .009 .001 Lamb and mutton .591 .571 .603 Lamb and mutton .991 .571 .603 Fish .060 .033 .603 Fish	Ves]	. 551	. 591	
Lamb and mutton .941 571 -020 Chicken -034 -037 -020 Chicken -034 -037 -038 Chicken -038 -038 -038 Curkey -788 779 -038 -021 Dutter -072 -078 -004 -004 Jutter -260 .318 -019 -1437 -1437 Sated -005 -622 -006 -037 -006 -037 Argania -029 -0068 -037 -010 -043 -0137 Marganiae -029 -0068 -037 -016 -044 -044 -044 Stald dressing -284 225 -0016 -022 -016 -022 Stale dressing -015 -068 -068 -068 -068 -068 Stale dressing -514 610 674 641 -064 -083 States 016 622 012 -002 021 -002 021 -002 021	Pork	808	. 609	
Chicken - 034 - 037 - 033 Fish - 060 - 038 - 034 Stat - 072 - 078 - 033 Segs - 072 - 078 - 034 State - 259 . 318 0.033 Statuter - 029 - 008 - 037 Statud dressing .	Lamb and mutton.	. 591		
Tish. 060 -038 -064 Turkey. 788 789 .624 Jurkey. 250 318 .004 Jurkey. 250 318 .004 Jurkey. .250 318 .004 Jurker. .250 318 .004 Jurker. .250 .318 .004 Jargarine. .022 005 037 Jargarine. 006 022 018 Jargarine. 006 022 018 Jargarine. 006 022 010 Jurkey.		- 034		
Durkey. 789 789 621 Sage	Fish	060		+
Sags - 072 - 076 - 004 Jutter 250 318 0.49 Ard -1.297 -1.437 - 140 Shoreniag 029 - 008 - 037 Aargarine - 006 - 022 - 018 Aargarine - 006 - 022 - 018 Jargarine - 284 285 001 Svap. milk - 610 - 674 - 064 Josee - 227 240 022 O'statees - 016 - 068 - 0068 Vest. - 016 - 674 - 064 Jorn syrup - 705 - 537 - 003 O'statees - 0169 - 190 - 021 Jorn syrup - 706 - 756 - 050 Jorn syrup - 706 - 756 - 050 Samanas 133 140 - 012 Anned peaches - 012 - 002 - 014 Anned peaches - 012 - 002 - 014 Samanas - 033 - 043 - 012 Tozen fruit	furkey	. 768		
Jutter. 259 318 049 ard. -1.237 -1.337 140 Shorteniaz. 029 008 037 Jarad dreesing .234 .285 .001 Stargarine				
Lard. -1.297 -1.337 + 140 Shortenias .029 008 037 Margarine 005 022 018 Safad dreening .284 .285 .001 Svap. milk .367 .377 .010 Svap. milk				
biortening 029 -008 -037 Jargarine -006 -022 -018 Jargarine 284 285 001 Yeah ruik 367 377 010 Syap, milk -006 -674 -064 Diesee 227 249 029 Oce cream 323 331 008 Vataces -006 -008 -008 weet potatoes -016 008 -008 weet potatoes -504 -587 -083 Jorn syrup -706 -756 -080 pples -142 140 -002 preanges 227 260 033 Janned peaches 012 -0002 -014 Janned peaches -012 -002 -014 Jorin syrup -161 -170 009 Tozen fruit -021 -002 -014 Janned peac -013 -043 -012 Tozen fruit -024 060 -014 Jonions 005 <t< td=""><td></td><td></td><td></td><td></td></t<>				
Margarine 005 022 018 salad dressing .284 .285 .001 Treah milk .367 .377 .010 Svap, milk 610 674 .006 Dyap, milk 610 674 .006 Svap, milk 610 674 .006 Co cream .323 .331 .008 Svatces .016 .006 .009 Svatces .016 .006 .009 Svatces		+-		
atal dressing .284 .285 .001 reah milk .367 .377 .010 Svap, milk				
Treah milk 367 377 010 Svap, milk - 610 - 674 - 004 Cheese 227 249 022 0331 006 Sotatoes 006 . . 006 . . 006 . 002 . . 006 . . 006 . 008 . . 008 . . 008 . . 008 . . 008 . . 008 . . 008 . . . 003 .	•			
Evap. milk 610 674 064 Costceam .323 .331 .006 Costceam .323 .331 .008 Svettes		1		
Cheese 227 249 102 coc cream 323 331 006 Potatoes 016 008 -008 Potatoes -504 -587 -083 iugar. -169 -190 -021 Dorn syrup -706 -756 -083 plass 227 260 033 mansas 135 139 004 Panges 227 260 033 amasas .012 -002 -014 Canned picesples .012 .002 -014 Canned picesples .012 .003 -003 Creat Truit .031 -043 -012 Creat Truit .031 -043 -014 Canned peas .045 .003 -003 Canned corn <t< td=""><td></td><td></td><td></td><td></td></t<>				
Construction 323 331 008 Potatoes 016 006 -008 -008 Sweet potatoes - 504 - 537 -083 Sweet potatoes - 165 - 190 -021 Torn syrup - 706 - 756 -033 Inner syrup - 706 - 756 -033 Inner syrup - 706 - 756 -033 Sanasas 012 - 002 -014 Panges 227 260 033 333 Sanand peaches 012 - 002 -014 Anned piuespples 408 417 -039 - 012 Pry fruit - 031 - 043 - 012 Prosen tornatces 161 .170 .009 .009 .003 .008 Serots .065 - .003 - .008				
Potatoes				
iweet potatoes	•			
iugar. 169 190 021 Corn syrup. 706 756 050 piples. .132 .140 002 Dranges. .227 .2600 .033 Sanass. .135 .139 .004 Canned piesches .012 062 014 Canned piespies .008 .447 .039 Cry fruit. 031 043 012 Crosen truit .039 .004 .037 Crosen truit .033 014 .039 Crosen truit .031 043 012 Crosen truit .033 003 014 Crosen truit .033 003 003 Crosen truit .0424 .0661 .033 Crosen truit .035 .003 014 Crosen truit .0424 .0466 .022 Canned peas .043 .032 011 Canned peas .043 .032 .011 Canned peas .054 .029				
John syrup	-			
142 140 - 002 Pranges. 227 260 033 Jannages.				
tranges				
Jamanas. .135 .139 .004 Janned pesches .012 062 014 Janned piuespies .003 .417 .039 Dry fruit. 031 043 012 Jrosen fruit .064 .061 .037 Tossen fruit .043 013 043 012 Tossen beans .161 .170 .009 .003 003 Tresh beans				
hanned peaches .012 002 014 hanned piueapples .003 .447 .039 Dry fruit 031 043 .012 frozen fruit .024 .061 .039 frozen fruit .024 .061 .039 frozen fruit .024 .061 .039 frozen fruit .024 .061 .037 frosh brances .164 .170 .009 fresh beans 481 495 014 baines .033 .008 .003 .008 cartots .015 .032 .011 lanned peas .043 .032 .011 lanned tomatoes .043 .032 .011 lanned tomatoes .054 .029 .025 lanned tomatoes .056 .173 .008 Dry vegetables				
Janned pluexpples .408 .417 .039 Dry fruit				
Dry fruit - 0.031 - 0.043 - 0.012 Crozen fruit	-			
Tozen Iruit				
Tesh tornatces .161 .176 .009 Tresh beans 481 495 014 Daions .005 003 008 Carrots .312 .319 .006 Carned peas .043 .032 011 Canned corn .054 .029 025 Canned tomatoes				
Trash beans				
Dnions .005 003 006 Arrots .313 .319 .006 Arrots .313 .319 .006 Latuce .424 .446 .022 Daned peas .043 .032 011 Janed corn .034 .029 025 Daned tomatoes .165 .173 .008 Dry vegtables 616 .039 .029 Prozen vegtables 611 685 .054 Drocen vegetables 651 .651 .054 Drocen vegetables 605 .651 .064 Drocen vegetables				
Chirrota .312 .319 .006 Lettuce .424 .446 .022 Canned peas .043 .032 011 Lanned peas .043 .029 025 Canned tomatoes .066 .173 .008 Dry vegetables .666 .173 .008 Proven vegetables				
.ettuce .424 .446 .022 Janned peas .043 .032 011 Janned corn .054 .029 025 Janned tomatoes .165 .173 .008 Dry vegetables 818 914 096 Trosen vegetables 631 685 054 Utes 651 654 .002 Durn meal			+	
Sanned peas. .043 .032 011 Janned corn .054 .029 025 Janned tomatoes. .165 .173 .008 Dry vegetables. .616 .039 Prozen vegetables. .631 .616 Vibest flour Vibest flour Vibest flour				
Canned corn .034 .029 025 Sanned cornatoes. .165 .173 .008 Dry vegetables.				
Jannad tomatoes. .165 .173 .008 Dry vegetables. 818 914 996 Prozen vegetables. .677 .616 .639 Vosen vegetables. 631 685 054 tice. 605 651 046 breakfast cereste. .056 .058 .002 Durn meal. 1.059 -1.143 084 coffee				
Dry vegetables - .616 .039 Prozen vegetables - .617 .616 .039 Whest flour - .631 - .685 - .054 Ute - .605 - .651 - .646 Breakfast cerests .056 .058 .002 .002 Jon meal - .047 .047 .064 Loup .216 .236 .020				
Prozen vegetables .677 .616 .039 Wheat flour 631 685 054 Lice 605 651 046 Break float cereals .056 .058 .002 Jura meal 047 .047 .064 Coffee .216 .236 .020				
Wheat flour - .631 - .685 - .054 Lice - .605 - .651 - .046 Break fast cereste .056 .058 .002 .002 Durn meal. - .047 .047 .084 Joup. .216 .236 .020	Man verstables			
1001 005 651 0045 Sreakfast cereate .056 .058 .002 Urn meal 1.059 -1.143 084 foffee 047 .047 .094 .000 .216 .236 .020			11111	
Breakfast cereate .056 .058 .002 Forn meal -1.059 -1.143 084 foffee				
Jorn meal. -1.059 -1.143 084 Joffee 047 047 .094 Outp .216 .236 .020				
offee,				
oup				
11 fact	wap	.210	. 236	. 020
ul 1004	ll food	.277	.304	.027

Deviations are calculated by taking the difference between weighted regressions and ordinary regressions.

dollars). Thus, a quantity index of less than 100 means that the per-capita consumption in the lowest-income group is higher than average consumption levels. The results in table 14 are useful to persons engaged in marketing farm commodifies because it provides a framework to determine the nature of emphasis to be placed on different income groups while designing a program for promoting the sale of a particular commodity.

TABLE	14
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BIVARIATE CLASSIFICATION OF COMMODITIES ACCORDING TO INCOME ELASTICITY AND CONSUMPTION INDEX*

Consump-			Ind	ome Elasticity			
tion Index	Negative	01	.12	.23	.34	>.4	Total
0-50	Lard, evap. milk, corn syrup, fresh beans, dry vegetables, wheat flour, rice, corn meat (8)						(8)
50–100 .	Chicken, fish, eggs, sweet polatoes, sugar, margarine, dry fruits (7)						(7)
100-150 ,		Pork, shorten- ing, oniona, canned peas, canned corn, breakfast corcals, coffee, pots- toes, canned peaches	Apples, bana- nss, canaed tomatoes (3)	Butter, cheese, oranges (3)			
150-200		(9)	Fresh tomatoes (1)	Beef, salad dressing, soup (3)	Ico cream, carrote (2)	Canned pine- apple (1)	(15)
200-250			:		Fresh milk (i)		(1)
250-300						Lettuce, vesl, froten vege- tables (3)	(3)
>300						Lamb. turkey. frozen fruita (3)	(3)
rotal	(15)	(9)	(1)	(6)	(3)	(7)	(44)

The consumption index is derived by expressing the average quantity consumed as a percentage of the quantity consumed by the lowest income group.

Quantity versus quality elasticity.— While discussing the income elasticity, we have deliberately defined income elasticity as the ratio of relative change in the quantity consumed and the rela-

tive change in income. It is possible to define demand in terms of expenditures on a particular commodity or in terms of quantities of the commodity consumed. When we use these different variables as the dependent variable in the demand equation, we get two different estimates of income elasticities, namely, "the elasticity of expenditures with respect to income" and the "elasticity of quantities consumed with respect to income." The difference between these two types of elasticities can be interpreted as a measure of the quality consciousness of the consumers, because the quality of a product and its price can be assumed to be directly correlated. Quality here merely assumes that the consumer has at least a subjective reason to rank different varieties as superior and inferior.

Let x denote the expenditure on a commodity which is the product of the quantity consumed (q) and its price (p).

$$x = pq. \tag{146}$$

The elasticity of expenditures with respect to income (hereafter referred to as expenditure elasticity) is defined as

$$e_{xy} = \frac{\partial x}{\partial y} \cdot \frac{y}{x}.$$
 (147)

From (146) and (147),

$$e_{xy} = \frac{\partial(pq)}{\partial y} \frac{y}{pq} \qquad (148)$$

 But

$$\frac{\partial (pq)}{\partial y} = p \frac{\partial q}{\partial y} + q \frac{\partial p}{\partial y}$$

Substituting in (148)

$$e_{xy} = \left(p \frac{\partial q}{\partial y} + q \frac{\partial p}{\partial y}\right) \frac{y}{pq}$$

$$= \frac{\partial q}{\partial y} \frac{y}{q} + \frac{\partial p}{\partial y} \frac{y}{p}.$$
(149)

The first term on the right-hand side of (149), by definition, is the elasticity of quantity consumed with respect to income (quantity elasticity). The second term gives the relative change of price with respect to the relative change in income. As we have assumed that the quality of a commodity and its prices are directly correlated, the higher the price, the higher the quality and therefore, the relative changes in prices can be interpreted as relative changes in qualities.23 Thus, the second term on the right-hand side of (149) can be taken as the ratio between the relative change in quality and relative change in income, which can be referred to as the quality elasticity. So we have split the expenditure elasticity as the sum of two termsone representing quantity elasticity and the other representing quality elasticity (See Gerra 1959, p. 149). The quality elasticity can be taken as a measure of consumers' desire for improved quality, given the present average or standard quality. In general, it is expected that the quality elasticity is positive, because higher-income groups tend to consume more expensive or fancy grades and varieties. Also, upgrading of diets, with increases in income, is reflected in the fact that changes in quantities consumed

¹³ We have excluded the possibility that consumption of food commodities is influenced by snob appeal or scarcity. Although we recognize that, in reality, higher prices need not necessarily reflect higher quality, we assume that, for the market as a whole, higher average prices imply higher average quality. Scitovsky (1945, p. 100) supports this view as, "Economists are wont to minimize the importance of this factor (price) fearing the havoc it may wreak with the whole theory of choice. But 'mass observation' of one's friends and [their] wives shows that more often than not pople judge quality by price. The word 'cheap' usually means inferior quality nowadays; and in the United States 'expensive' is in the process of losing its original meaning and becoming a synonym for superior quality."

may not be so large as changes in expenditures on food items. In the present analysis, the majority of the commodities met this expectation, though some of them did not (see table 15).

Commodity	Commodity Expenditure Elasticity		Quantity Elastici	
eef	.380	.270	.110	
eal	.698	. 551	.147	
ork	.130	.008	,122	
amb and mutton	.576	. 591	015	
bicken.	.056	··· .034	.090	
ʻish ,	.140	- 060	,200	
urkey	. 869	.768	.101	
ска страници	— .016	072	.056	
utter.	274	.269	. 605	
ard	-1.236	-1.297	.061	
hortening	- 040	029	069	
Iargarine	.051	006	.057	
alad dressing	.401	284	.117	
resh milk	.349	.367	018	
Vep. milk	640	610	030	
beese	.241	227	.014	
ce cream	.335	.323	.012	
otatoes	.036	.016	.020	
weet potatoes	293	504	.211	
•	178	169	009	
идат	569	706	,137	
	.207	.142	.065	
pplea	.192	. 227	085	
Pangea		. 125	.005	
алалад	.140	. 188	.003	
anned peaches	.009			
anned pineapples	.475	. 408	,067 — ,005	
Dry fruits	037	031		
resh tomatoes	.278	.161	.117	
resh beans	431	481	,050	
)nions	,023	.005	.017	
arrole		.313	045	
ettuce		.424	076	
anned peas	.110	.043	.067	
anned corn	.065	.054	.011	
soned tomatoes		165	014	
Ory vegetables		818	177	
rozen vegetables	. 619	.577	.042	
Vheat flour	611	631	.020	
tice	319	605	.286	
Breakfast cereals	.195	. 056	. 139	
Cora meal	÷10.1	-1.059	.046	
Coffee		.047	036	
юцр	.228	.216	.012	

TABLE 15 COMPARISON OF QUANTITY AND QUALITY ELASTICITIES BASED ON HOUSEHOLD FOOD CONSUMPTION SURVEY DATA, SPRING, 1965*

* Based on ordinary regression.

The two assumptions, that prices reflect quality, and that income and quality of the goods consumed are positively correlated, lead to the conclusion that persons in the higher-income group pay more than those in lower-income groups for the same quantity. To see whether this is true, we took the 1965 consumption data in terms of quantities and expenditures and assumed that their ratio represents the price. Taking this estimate of price, we obtained indices of prices paid by different groups with the lowest group price as the base. We found

TABLE 16

CLASSIFICATION OF COMMODITIES ACCORDING TO QUALITY ELASTICITY AND DIFFERENCE IN PRICES PAID BY UPPER AND LOWER INCOME GROUPS

Differential		Qua	lity Elasticity		
Price Index*	Negative	005	0.05110	>.10	Total
Negative	I.amb. shortening, fresh milk, evap. milk, sugar, or- aoges, dry feuits, carrots, lettuce, canned tomatoes, coffeo (11)	Lee crean), corn meal (2)			(13)
0-15	Canned peaches (1)	Butter, theose, po- tatoes, bananas, fresh leans, eanned corn, wheat flour, soup (8)	Eggs, margarine (2)	Turkey, onions, corthayrup (3)	(14)
15-30		Frozen vegetables (1)	Apples, canted peas (2)	Pork (1)	(4)
30-50			Chicken, canned pincapple (2)	Beef, yeal, salad dressing, fresh to- matoes, breakfast cereata	
				(5)	(7)
>50			Lard (I)	Fish. sweet potstoes, dry vegetables, rice (4)	(5)
Total	(12)	(11)	(7)	(13)	(43)†

* See the text for the definition of differential price index. † Frozen fruits excluded.

large variations among these indices for different commodities. Table 16 compares the quality clasticities obtained from table 15 and the calculated price indices.

The price index in table 16 represents the difference between the prices paid by the upper income group and the lower income group expressed as a percentage of the prices paid by the lower income group. Thus, a negative price differential implies that the price paid by the higher income group is less than the price paid by the lower income group. Incidently, most of the commodities with negative quality elasticity are those

with a negative price differential. Although there is an explanation for the negative quality clasticity from this behavior, it may not be proper to conclude that high income groups pay lower unit prices for these commodities because of lower quality. It is possible that quality may be only one factor influencing prices—the prices paid by consumers may be a function of many other factors like quantity purchased, nature of demand for the commodity, the availability of substitute products, and family economies of scale. For example, if distributors offer quantity discounts, persons in the higher income group can buy

in-bulk quantities to obtain a lower unit cost compared to persons in the lower income group who can afford to buy only small quantities. In other words, it is not possible to ascertain whether the price variation from one income group to the next is due to such influences as differences in quality of the products purchased, extensive buying habits, or heavy purchases from farms to avoid regular marketing channels. Since the effects of these different factors are not the same for all commodities, it would be useful to analyze each case separately to explain the factors influencing the negative price differential. However, because such detailed analysis would require data collected specifically for this purpose, we have excluded it from the present study.

Effect of household size

So far, the analysis is based on the assumption that income is the only variable influencing consumption in a cross-section analysis. Although a number of other factors may also influence the level of consumption, the data available for this analysis contained only information on quantity consumed, expenditures, income, and household size. In studies using earlier cross-section data, it was found that there were economies of scale in food use in large households. Analyzing 1955 consumption survey data for individual households, Rockwell (1959, p. v) observes, "total household consumption of food increases with increases in the number of persons in the household, but consumption per person declines as household

size increases." Therefore, we included the household size variable to test whether the 1965 survey data show a similar result. We used both expenditure and quantity as dependent variables and obtained a regression equation of the type

$$\log q = a + b \log y + c \log s,$$

and
$$\log x - a' + b' \log y + c' \log s$$
(150)

where

- q = per capita quantity consumed,
- x = per capita expenditure,
- y = per capita income, and
- s = household size. (measured in terms of adult equivalent units, with one unit equal to 21 meals eaten at home.)

For comparison, the results obtained from the two different forms of regression equations are tabulated for quantity and expenditure data in Appendix tables A-1 and A-2.

Significance of the coefficients.— Table 17 presents a summary of the results from Appendix tables A-1 and A-2. A negative coefficient indicates that here exist economies of scale in food use associated with household size while a positive sign indicates the opposite tendency.²⁴ As expected, total food consumption per capita has a negative coefficient associated with household size although the coefficient itself is not significantly different from zero. When using quantity as the dependent variable, 24 coefficients were positive and 20

²⁴ Such economies can be attributed to a number of factors: (a) holding household income constant, income *per person* decreases as family size increases with a higher number of children in such family units with different consumption patterns. For example, in table 17, milk has a positive coefficient associated with family size whereas coffee has a negative coefficient; this pattern probably is associated with family composition; (b) there may be savings in expenditures per person associated with buying large quantities at lower unit prices; and (c) there may be a reduction in leftover food on a per-capita basis for large family units.

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TABLE 17

EFFECT OF HOUSEHOLD SIZE ON CONSUMER PURCHASES, QUANTITY, AND EXPENDITURES

Commenting	Sign of coefficient	associated with household exper	d size with dependent ve aditure	riable as quantity or
Commodity group	Both positive	Quantity (+) Expenditure (-)	Quantity (-) Expenditure (+)	Both negative
Mcata	Beef Veal	: Turkey	Pork	Lamb and mutter Chicken Fish
Egga		Egga		
Fate and oils	Lard Shortening Salad dressing	Margarine		Butter .
Milk	Fresh milk Evaporated milk Ice cream			Cheese
Polatoes	White potatoes Sweet potatoes			
Sugar and syrup	Sugar			Corn syrup
Fruit,	Frozen (ruit (quantity only)	Oranges Canned peaches		Apples Bananas Canned pineapple Dried fruit
Vegetables	Carrots Canned peas Canned corn	(Janned tomatoes Dried vegetables		Fresh tomatoes Fresh beans Onions Lettuce Fresh vegetables
Other	Wheat flour Soup		ļ	Rice Breakfast ceresia Corn meai Coffee
All food				All food (expenditure only)

coefficients were negative. Only five coefficients were significant at the 5 per cent level and another six coefficients were significant at the 10 per cent level (see table 18).

Existence of economies in consumption was more revealing in the case of consumption expenditures of different food items—26 coefficients were negative with 6 of them being significant. Only three positive coefficients were significant. Effects on quality elasticity. A comparison of tables 16, A-1, and A-2 shows that, as a result of the introduction of household size in the regression equation, the sign of quality elasticity has changed from negative to positive for seven commodities (lamb, fresh milk, sugar, corn syrup, oranges, canned peaches, and canned tomatoes.) However, six commodities (shortening, evaporated milk, dried fruit, carrots, lettuce, and coffee) did not change the negative

	Quantity	y as dependent variabl	Expenditure	Expenditure as dependent variable		
Sign of coefficients	Level of	Level of significance		Level of a	gnificance	<u> </u>
	5%	10%	Total	5%	10%	- Toia
Positive	Salad dressing Frozen fruit Canned corn	Veal Shortening Freeb milk Potatoes	. 7	Salad dressing	Shortening Canned corn	3
Vegative	Dried fruit Coffee	Lamb Breakfaat eereal	4	Lamb Canned pineapple Dried fruit Coffee	Chicken Apples	6
TOTAL	5	6	11	5	4	9

TABLE 18 COMMODITIES WITH SIGNIFICANT COEFFICIENTS ASSOCIATED WITH HOUSEHOLD SIZE

quality clasticity reported in table 16. and corn meal, which had a small positive quality, has changed its sign to negative. Thus, when household size also is included as a variable in the regression equation, the number of commodities with negative quality clasticity is reduced from 13 to 7. Incidentally, this suggests that the presence of negative quality elasticity, in the case of these commodities, can be explained in terms of some other variables excluded from the demand equations. Isolation of such additional variables influencing the demand for these commodities may require an exhaustive analysis of individual commodity demand.

Comparison of 1955 and 1965 consumption

When data from different cross sections are compared, it is necessary to take into account any differences in the population characteristics, sampling procedures, and other structural changes that have occurred during the interval between the cross sections. In the United States, nationwide surveys on food consumption of families were conducted in

1936 (U. S. Bureau of Labor Statistics, 1940, and USDA, 1941a and 1941b), 1942 (USDA, 1944), 1948 (Clark, et al., 1954), 1955 (USDA, 1956), and 1965 (USDA, 1968). There are a number of conceptual and methodological problems, discussed in detail by Clark, et al., 1954, and Bush, 1961, such as differences in the universe covered, sampling design, and the type of information gathered associated with comparing the data from these cross sections. In particular, it is difficult to adjust the data from 1936. 1942, and 1948 to a comparable form with those of 1955 and 1965. There are a number of factors like the season, universe, and size of sample that are in common with the 1955 and 1965 spring cross-section surveys. Therefore, we have used only these two cross-section data for comparison purposes.

Changes in the level of consumption.—Using the per-capita consumption of different commodities during this period (Appendix table A-3), table 19 shows the direction of change in consumption of different commodities for the aggregate of all households and by low, medium, and high income groups.

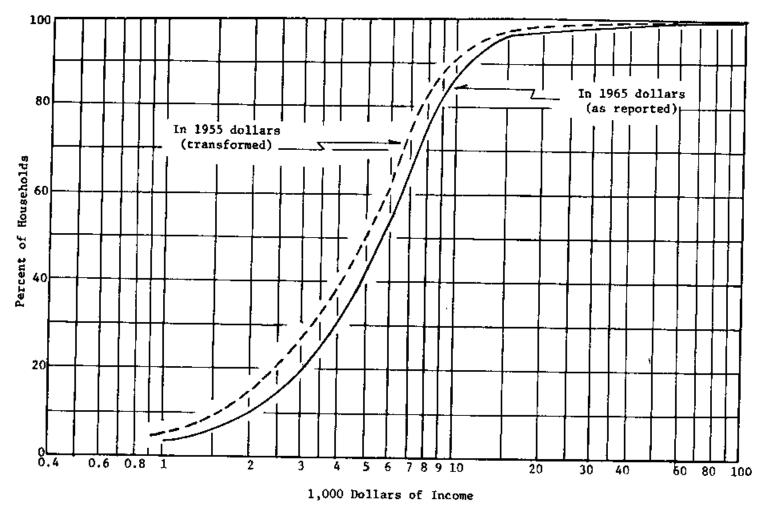


Fig. 1. Classification of shifts in regression coefficients.

TABLE 19 CHANGE IN PER CAPITA CONSUMPTION, 1955 TO 1965

Commodities with consumption over all households*				
Increasing	Decreasing			
All income groups: (11) Beef, chicken, fash Margasine Apples Canned corn, canned to- matoes, frozen vegetables Rice, cereals, soup	All income groups: (16) Veal, lamb, turkey, egga Butter, shortening Milk, evaporated milk, potatoes Oranges, canned pine- apple, frozen fruit Tonnatoes, onions, car- rots Wheat flour			
Two income groups only: (3) Canned peaches (L, M) Choese (L, H) loe cream (L, H)	Two income groups only: (6) Lard (L, H) Sugar (L, H), coffee (M, H) Beans (L, H), canned peas (L, M) Sweet potatoes (M, H)			
One income group only: (3) Bananas (L) Salad dressing (H) Lettuce (H)	One income group only: (3) Pork (L) Dried vegetables (H), dried fruit (H) Corn meal (L), corn eyrup (H)			
Total commodities (17)	Total commodities (27)			

 \bullet Income groups are designated low (L), modium (M), and bigh (H), and all households.

Of the 44 commodities, consumption increased in all income groups for 11 and decreased for 16.²⁶ For the remaining 17 commodities, increases or decreases were shown for at least one income group. Summarizing by income group, the low income group had 20 increases and 24 decreases, the medium income group had 20 increases and 24 decreases, the high income group had 18 increases and 26 decreases, and all households had 17 increases and 27 decreases in per-capita consumption in 1965 as compared with 1955.

We can further analyze these changes by considering the relative changes given in table A-3, summarized in table 20. The shifts in consumption behavior were

not uniform; wide fluctuations existed in the extent of variations in the consumption of different commodities. All income groups reduced the per-capita consumption of three commodities-veal, butter, and frozen fruit—by more than 40 per cent. If we consider that an arbitrary 5 per cent change may be due to reporting errors in the data, 19 commodities showed a reduction in consumption by more than 5 per cent and 17 commodities showed an increase by more than 5 per cent in the low income group. In the medium and high income groups, 21 and 24 commodities, respectively, showed a reduction of more than 5 per cent while 15 and 13 commodities, respectively, showed an increase of more than 5 per cent.

Shifts in slope and constant coefficients.—To compare the nature of shifts in regression coefficients, we obtained both ordinary and weighted regression equations of the type

$$\log q = a + b \log y$$

for the two periods. Looking at the size of the coefficients, we classified the commodities into four different groups shown graphically in figure 1.

Group I (increase in the intercept and decrease in the slope). The diagram shows that the gap between the regression lines corresponding to 1955 and 1965 decreases as income increases up to y^* . Whether these two lines will meet at a finite horizon will depend upon the relative size of changes. Lower income groups experienced a relatively higher percentage increase in consumption than higher income groups. In fact, beyond the point of intersection, people in the higher income group reduced their consumption of the commodity under consideration.

²⁶ This is consistent with the time-series data on consumption reported in Hiemstra (1968) except for the commodities, apples, shortening, and onions.

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TABLE 20 COMPARISON OF CHANGES IN PER CAPITA CONSUMPTION OF DIFFERENT COMMODITIES DURING SPRING 1955 AND 1955

Income			Percentage (Change in 1985 ov	er 1955		
Group	<-40	-40 to -20	-20 to -6	-5 to 5	5 to 20	20 to 40	>40
dollars			·	per cent	· •		
<3000	Veal, but- ter, fro- zen fruits (3)	Lamb, turkey, lard, shorten- ing, fresh milk, oranges, canned pine- apple, wheat flour, corn meal (9)	Salad dressing, potatoes, sug- ar, toniatoes, bcans, car- rots, lattuce (7)	Eggs, potk, evap. milk, sweet pota- tocs, apples, onions, canned peas, canned tomatoes (8)	Fish, chocse, ice cream, corn syrup, bananss, canned corn, dry vego- tables, coffee (8)	Beef, chieken, margarine, dry fruite, break fast cerculs (3)	Canned peachea, frozen vegeta- bles, rice, soup (4)
3000 to 4999	Veal, Ismb. butter, oranges, canned pine- apples, frozen fruits (6)	Milk, carrols (?)	Turkey, short- ening, evap. milk, ice cream, pota- toes, sweet potatoes, ba- nanas, toma- toes, onions, lettuce, canned pess, wheat flour, coffee (13)	Pork, eggs, salad dress- ing, cheese, sugar, apples, bests, frosen vegetables (8)	Beef, fish, lard, corn syrup, canned toma- toes, soup (6)	Margarine, canned peaches, canned corn, dry vegetables, breakfast cereals (5)	Chicken, dry fruits, rice, eorn meal (4)
>5000	Lamb, vesl, turkey, butter, sweet polatoes, oranges, frozen fruits, dry vegeta- bles (8)	Lard, shorten- ing, evap. milk, caned pineapples, carrots (5)	Eggs, milk, po- tators, sugar, corn syrup, dry fruits, tomatoes, beans, obions, wheat flour, coffee (11)	Pork, cheese, ice cream, ba- nanas, canned peaches, canned peas, frozen vegetables (7)	Salad dressing, apples, let- tuce, canned tomatoes, soup (ö)	Beef, chick- en, fish, margarine, canned corn (5)	Rice, brask- fast cereals, corn ; meal (3)
All Kouse- bolds	Lard, dry fruits, frozen fruits, dry Vege- tables (4)	Veal, lamb, but- ter, ahorten- ing, evap. milk, beans, sweet pota- toce, oranges, wheat flour, cora meal, canned pine- apples (11)	Turkey, egge, inilk, pota- toes, sugar. corn syrup, onions, car- rots, canaed poss (P)	Pork, banapas, tomatoes, coffee (4)	Fieb, aslad dressing, choose, ice cream, ap- ples, croned peaches, let- tuce, canned corn, canned tomatoes, breakfast cereals (10)	Beef, chick- en, mar- garine, fro- seo vegeta- tables, soup (5)	Rice (I)

Group II (decrease in the intercept and increase in the slope). Here, the change is exactly opposite to group I. The diagram shows a similar pattern except that the lines corresponding to the two years are interchanged. Here, the lower income group experienced a reduction in the quantities consumed while the upper income groups might have experienced an increase in consumption. Again, the boundary between increase and decrease in consumption (the point of intersection) depends upon the slopes and intercepts of different commodities in these two periods.

Group III (increase in both intercept and slope). In this case, both upper and lower income groups increased consumption and the percentage of increase may be higher for the upper income group compared to the lower income group.

Group IV (decrease in both intercept and slope). This group's behavior is opposite to that of group IHI. Here, both upper and lower income groups have reduced consumption. The 1965 regression lines lie everywhere below the 1955 regression line.

Group I: Change in intercept positive change in slope negative		Group II: Change in intercept neg- ative change in slope positive		Group III: Change in intercept po tive change in slope positive		
Regn	ession	Regre	seion.	Reg	ression	
Weighted	Nonweighted	Weighted	Nonweighted	Weighted	Nonweighted	
Beef	Beef	Veat	Veal	Cheese	Fish	
Chickon	Chicken	Pork	Pork	Onions	Cheese	
Eggs	Eggs	Fish	Lamb	Breakfast	Oniona	
Lard	Lard	Turkey	Turkey	cereals	Breakfast	
Margarine	Margarine	Butter	Butter	Corn meal	cereals	
Evap. milk	Evap. milk	Salad dressing	Shortening	(4)	(4)	
Sweet potstoes	Sweet potatoes	Fresh milk	Salad dressing			
Sugar	Sugar	Loe cream	Freah milk	Come IV. Char	ge in intercept neg	
Cora syrup	Сога зугар	Potatoes	Ice cream		ge in intercept neg	
Oranges	Bananas	Apples	Potatoes	change in .	slope negative	
Bananas	Canned peaches	Canned pineap-	Apples	ļ <u></u>	··	
Canned peaches	Dry fruita	ples	Canoed pinesp-	. Res	reasion	
Dry fruits	Fresh beans	Fresh tomatoes	ples	·		
Fresh beans	Canned peas	Fresh lettuce	Frozen fruits	Weighted	Nonweighted	
Canned corn	Dry vegetables	Canned peas	Fresh tomatoes	weighteed	Tionweillinen	
Dry vegetablea	Frozen vegetables	Canned tomatoes	Lettuce			
Frozen vegetables	Rice	(15)	Canned tomatoes	Lamb	Oranges	
Wheat flour	Coffee		Corn meal	Shortening	Carrots	
Rice	Soup		(17)	Frozen (ruits	Wheat flour	
Coffee	(19)			Carrota	(3)	
Soup				(4)		
(21)						

 Table 21

 CLASSIFICATION OF COMMODITIES ACCORDING TO CHANGES IN

 REGRESSION COEFFICIENTS FROM 1955 TO 1965

Table 21 gives the classification of commodities into these four groups.

Testing the equality of coefficients.— Table 21 gives only a qualitative estimate of the nature of the changes in regression coefficients. To make a statistically sound statement on the variability of regression coefficients obtained from these two cross sections, it is necessary to apply certain testing procedures. Here are two such procedures: (1) To test the equality of coefficients obtained from two cross sections, we can pool the data from them and obtain a covariance analysis to test the significance of the difference in income elasticities during these two periods.

(2) The second approach is similar to that of Middelhock (1968) to test the stability of input-output coefficients over two different periods. If $\ddot{\alpha}_1$ and $\ddot{\alpha}_2$ are two estimates, with standard deviations ϑ_{α_1}

and ϑ_{α_1} obtained from two cross sections of size n_1 and n_2 , the difference between these estimates is significant if $|\hat{\alpha}_1 - \hat{\alpha}_2| < t_1\vartheta_{\alpha_1} + t_2\vartheta_{\alpha_2}$, where t_1 and t_2 corresspond to the *t*-values α_1 and α_2 , respectively, at the desired level of tolerance.

We used the second approach to test the equality of income elasticities obtained from 1955 and 1965 survey data. At the 5 per cent level, only four commodities (beef, eggs, fresh milk, and canned peaches) showed significant deviations in the income elasticities. At the 10 per cent level, three more commodities, (sweet potatoes, lettuce, and soup) are added. Beef, eggs, sweet potatocs, and soup decreased in income elasticity, the others showed an increase.

The income elasticity of all foods remained relatively stable during this period. There is close similarity between the coefficients of regression equations, using expenditures from 1955 and 1965 cross-section surveys when the dependent variable is the per-capita expenditure on total food. The regression equations obtained for these two periods were

 1955:
 $\log x = .132 + .266 \log y;$ $R^2 = .92 \text{ and}$

 (1.49)
 (9.09)

 1965:
 $\log x = .132 + .277 \log y;$ $R^2 = .88,$

 (3.66)
 (3.43)

where

- x = per-capita consumption expenditure on all food items,
- y = per-capita income (the figures in the parentheses are *t*-values).

A comparison with some of the previous cross-section estimates shows that the income elasticity has been falling over the last three decades and has become relatively stable. For example, using earlier cross-section data, Burk²⁵ (1951) estimated the income elasticities in 1935–1936, 1941 (two), 1944, and 1947 as .49, .49, .58, .33, and .31, respectively. From these five estimates and the two estimates obtained in this study for 1955 and 1965, it appears that the income elasticity for all food expenditures has stabilized in between .25 and .30.

Effect of a change in income distribution.—The comparison of income elasticities obtained from 1955 and 1965 cross-section data is proper only if the structure of the populations was comparable in these two periods. A closer look at the samples used in both surveys reveals that there was an improvement in the distribution of families in different income groups. In the 1955 sample, only 32 per cent belonged to the group with

¹⁸ Burk (1951) reports the following regression equations: 1935-1936 $\log x_1 = ...88 + ...49 \log y_1; R^2 = ...99$ $\log x_1 = ...93 + ...49 \log y_1; R^2 = ...99$ $\log x_2 =64 + ...58 \log y_2; R^2 = ...99$ $\log x_2 = 1...47 + ...33 \log y_2; R^2 = ...95$ $\log x_2 = 1...61 + ...31 \log y_2; R^2 = ...96$

where

 $x_i =$ average expenditure per capita for food and alcoholic beverages, total population;

- y_i = average per capita disposable income, current dollars, total population;
- $x_2 = food$ expenditure per capita, urban families; and
- y_2 = disposable income per capita, urban families, current dollars.

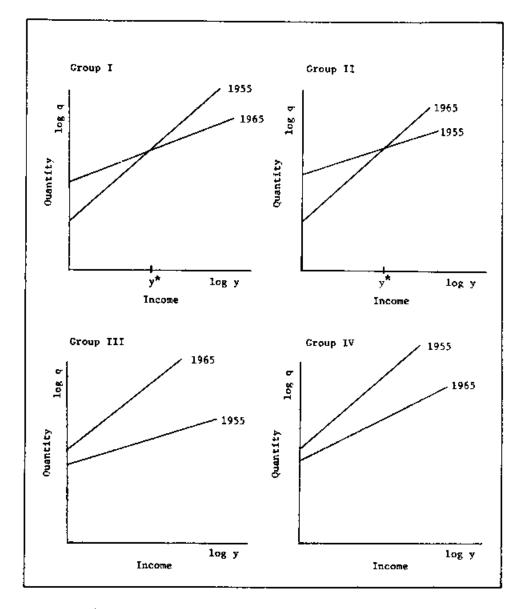


Fig. 2. Cumulative frequency distribution of families by income level in 1965 and transformation to 1955 dollars.

household income greater than \$5,000, in the 1965 sample, 58 per cent. If the samples during these two periods were representative, this increase might have been the result of two factors-a general increase in the price level and a general improvement in the income status of families. To make meaningful comparisons of data from these two samples, we isolated the price effect from the increases in general income. In other words, we adjusted the 1965 income-size distribution to a distribution among income classes, in terms of 1955 dollars, without a change in relative distribution of income. To achieve this, we used an approach suggested by Burk (1961, p. 56). The procedure is illustrated in figure 2 and involves the following steps:

(1) Take the distribution of samples in 1965 and plot the percentage cumulative frequencies on the ordinary vertical axis of a semilogarithmic paper against the upper class limit of each income class taken along the logarithmic horizontal axis.

(2) To adjust the distribution from the 1965 price level, move the curve obtained above to the left by the ratio of consumer price index in 1955 to that in 1965 (86.586 per cent).

(3) Read off the cumulative frequencies for the adjusted curve at the class limits and calculate the frequencies for each class by subtraction. The adjusted frequencies are shown as in table 22. Comparing the distribution of samples in 1955 and in 1965 adjusted at 1955 price levels, it appears that the movement was mainly from the middle income group to the high income group with only minor changes in the low income group.

Implications of the redistribution of sample size on aggregation.—Here, we shall demonstrate the implications of the redistribution of sample proportions on income elasticities obtained as an aggre-

TABLE 22

THE TRANSFORMATION OF 1965 SAMPLES TO 1955 PRICE LEVELS

Income group	1955 Survey (sctual)	1965 Survey (actual)	1965 Survey (adjusted to 1955 price levels)	
dollars	per cent			
< 3,000	. 29.3	22.2	27	
3,000 4,999	37 8	19.6	25	
> 5,000	. 32.3	58.0	48	

TABLE 23

TOTAL FOOD EXPENDITURES IN 1955 AND 1965

	Weekły per- i	capita total fo	od expenditur
Income group	1955 (actual)	1965 (actual)	1965 (at 1955 price level)
		dollars	
< 3,000	6.31	7.50	6.49
3 ,0001 ,999	8,20	(18,65) 8,90 (8,53)	(2 85) 7.70
> 5,000 .	10.95	(8.35) 11.90 (8.67)	(6, 10) 10, 30 (5, 94)

Norg: The figures in the parentheses represent percentage changes over the expediture levels in 1955.

gate of subgroups within a cross section with reference to total food expenditures. Comparing the total food expenditures in 1955 and 1965, the low income group has registered the highest percentage increase in food consumption expenditures—about 18 per cent -compared to about 8 per cent in other groups (see table 23).

To estimate the aggregate elasticity for all groups with known income elasticities (E_i) , the aggregate elasticity Ecan be written as

$$E = \frac{\Sigma k_i E_i}{\Sigma k_i} \tag{151}$$

where

- $k_i = n_i e_i$
- $n_i =$ number of observations in group i. and
- $e_i = \text{per-capita food expenditure in}$ group i (in the present case, i = 1, 2, 3).

Since k_i for a given group is defined as the product of the number of observations and the per-capita food expenditure, the effect of a unilateral reduction in the sample size in a group is to reduce k_i , while the effect of a unilateral increase in per-capita expenditure is to increase k_i . Therefore, the changes in the value

Income group	1955*	1965 (actual)†	1965 (distribution and expenses at 1955 lovel)‡	1965 (distribution at 1965 levels and ex- penses at 1965 price)
		dollars		·
< 3,000	198.04	165.50	175,23	202.60
	(22.08)	(16.12)	(20.32)	(20.32)
3,000-4,999	309.96	176.22	192 50	222.50
	(36.39)	(17.06)	(22.33)	(22.33)
>5.000	353.68	690, 20	495.40	571.20
	(41 53)	(66.82)	(\$7.35)	(57.35)
TOTAL.	851.68	1,032.92	862.13	996.20
(2ki)	(100,00)	(100.00)	(100.00)	(100,00)

TABLE 24							
WEIGHTS ASSOCIATED WITH	INCOME GROUP						
(VALUES OF k _i FOR 1955	AND 1965)						

* Column 2 in table 22 multiplied by column 2 in table 23. † Column 3 in table 22 multiplied by column 3 in table 23. † Column 4 in table 22 multiplied by column 4 in table 23. † Column 4 in table 23 multiplied by column 8 in table 23.

Norn: The figures in the parentheses represent percentages of total weight.

of k_i for each year is determined as an outcome of these two opposite effects. The values of k_i for each group in 1955 and 1965 are presented in table 24.

The combined effects of the redistribution of the samples and the changes in per capita expenditures during the period, 1955–1965, is to reduce the value of k_i for low and medium groups and to increase it for the high income group. In the case where the lower income group has higher income elasticities, the changes in k, described above reduce the weight given to higher income elasticities (and increase the weight given to lower income clasticities), resulting in an aggregate income elasticity which is lower in the latter period than in the original period so long as the income

elasticities within different groups remain unchanged during the period. Therefore, when comparing the income elasticities obtained as the aggregates of subgroups in two cross-section surveys, the effects of the following factors are important:

(1) Distribution of samples into subgroups in both cross sections after removing the effects of price changes.

(2) Changes in per-capita consumption among subgroups belonging to the two cross sections.

(3) Changes in income elasticities in each subgroup during the interval between the survey.

In comparing any of the above factors the effect of changes in other factors must be removed. Further, it is possible

$\frac{\text{TABLE 25}}{\text{REGIONAL CONSUMPTION INDEX (U. S. AVERAGE = 100)}}$

Quantity Index Region	0-50	50-75	75-95	95-105	105 125	125-150	>150
North- enst (R1)	Corn syrup, dry vege- tables, wheat flour, corn meal (4)	Lard, sbort- cning, beans (3)	Pork, ezgs, murga- rine, aslad dress- idg, evap. milk, sweet polatoes, augar, canned peaches, canned pineapples. dry fruits, frozen fruits, forzen fruits, tomatoes, canned corn {13}	Beef, chicken, fish, milk, cheesa, ice eream, potatoes apples banane carnots, lettuca, canned peas, breakfast cereals, coffee (14)	Oranges, onions, rice, soup (4)	Butter, canned toma- toes, frozen vegeta- blen (3)	Veal, lamb, tur- key (3)
West (Rz)	Lard, beans, corn meal (3)	Ves), sweet pota- toes, corn syrup (3)	Pork, fish, butter, shortening, ice cream, potatoes, sugar, canned peas, dry vegetables, wheat flour, rice (11)	Chicken, eggs, milk, evap. milk, bans nss, toma- tocs, onions, coffee (8)	Beef, turkey, marga- rine, salad dross- ing, cheese, apples, oranges, cauned peaches, troxen fruits, canned corn, canned to- matoer, breakfast cereals, soup (13)	Canned pinesp- ples, carrots, lattuce, frozen vegeta- bles (4)	Lamb. dry fruits, (2)
North Central (R ₄)	Lamb, lard, evap, milk, rice, corn meal (8)	Veal, sweet pots- toes, corn sytup, dry vego- tables (4)	Chicken, turkey. fish, shortening aslad dressing, milk, tomatoes, beans, onions, canned comatoes, frozen vegetables, wheat flour (12)	Eggs, margarine, sugar, dry fruits, canned peas (5)	Beef, pork, cheese, ice creatn, pota- toee, apples, or- abges, banansa, canned pincapple, frozen fruits, car- rots, lettune, canned corn, breakfast cereals, coffee, soup (17)		Butter (1)
South (R4)	Lamb (I)	Veal, tur- key, butter, cheese, or- anges car- rots, soup (7)	Beef, mitk, ice cream, potatoes, apples, canned peaches, canned pineapples, dry fruits, frozen fruits, frozen canned corn, canned corn,	Bananas, oniens (2)	Pork, chicken, eggs, matgarins, salad dressing, eugar, fresh tomatces, canned peas (8)	Piah (1)	Lard, short- eaing, evap. milk, sweet toes, corn syrup, beans, dry voge- tables, wheat flour, rice, corn meal (10)

to obtain the same income elasticity from two sets of cross-section data as a result of compensating adjustments in the above factors.

Regional variations

When we discuss the U. S. food consumption pattern, it would be useful to see the extent of variation among regions. Unfortunately, detailed data on consumption levels by regions are not available for extended periods. The 1965 consumption survey data is tabulated for four regions—Northeast, West, North Central, and South. From the average consumption and size of the household

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Commodity	Outside the interval 50-150	Outside the interval 75-125	Outside the interval 95-105	Range
ei			✓	26.22
al	V	· · ·		148.15
ork	*			20,25
unb	v	\checkmark		161.61
nieken	,	•	· · ·	17.35
irkey	~	V	l V l	118.21
sh	v	, v		49.60
ga		v		21 60
11ter	~	~		201.06
rd	v v	, v	l v i	159 98
artening	, v	l Č	v v	103,29
	v	Ý	v v	27.60
urgarine			v l	26.52
lad dressing				20.02
esh mjik		, I	V	100.97
aporated milk	\checkmark		✓	
19688		~	√	50 64
cream			✓	18.64
latoes			V	31.19
eet potatoes	\checkmark	✓	✓	88 32
gar			✓	39.24
meyrup	\checkmark	\checkmark	·	160.88
ples		1	! ✓	26 57
Inges		✓	✓	46 87
nanas			✓	8.23
nned peaches.			✓	35 GL
nned pineapples.		✓		52.40
y fruita	\checkmark	v v	1 1	77.89
ozen fruita				37,08
matoes				35.67
ans	~			146.56
uons	*		V	26 64
urots		✓	V	72.08
ltucc			v	53.86
anned peas		*	v l	20.47
nned corn			· · ·	30 48
anned tomatoes			l V l	61.71
ry vegetables.	\checkmark	l V		124.73
ozen vegetables	v	l V	V 1	44.59
	,		· · ·	114.54
eat flour	V,	×	✓	115.16
Ce	\checkmark	✓	V	31.80
eakiast cereals		, , , , , , , , , , , , , , , , , , ,	V	240.08
orni meal	 ✓ 	✓		
offce			✓	16.98
ар сор		✓	✓	49.60
			· · · ····	

TABLE 26 VARIABILITY IN REGIONAL CONSUMPTION INDICES

Norp: A \sqrt{mark} indicates that consumption index in at least one region fell outside the specified interval.

given in the regional data, the average per-capita consumption of the commodities were derived for each region. Using the per-capita consumption obtained in this manner and the per-capita consumption for the United States as a whole, we derived a consumption index for each region by expressing the per-capita consumption in regions as a percentage of the per-capita consumption for the United States (Appendix table A-4, summarized in table 25).

Table 25 shows that the importance given to different food items in the four regions differs considerably. The consumption pattern in the Northeast is closest, and that of the southern regions farthest from the U.S. average (see table

TABLE 27 REGIONAL INDICES OF PRICES PAID (U. S. AVERAGE = 100)

Price Judex Regione	0-50	50-75	75-95	95~105	105-125	125-150	>150
(R.)	Tur- key (1)		Canned pineapples, dry fruits, canned oorn, frozen vege- tables, corn meal (5)	Lamb, botter, salad dressing, ovap. milk, potatoes, sugar, corn syrup, apples, or- anges, beans, torna- tocs, onions, carrots, lettuce, cannod pese, soup (16)	Heef, veal, pork, chicken, fish, enga, lard, shortening, milk, margarine, cheese, ice cream, swnet polatoes, ba- nanas, camed peach- es, canned tomatoes, breakfast cereals, dry vrgetables, wheat flour, rice, coffee (21)	Frozen vege- (ables (1)	
West . (Ri)			Veal, lamb, carrots, lettuce, canned to- matoes, frozen vegetablea (8)	Beef, pork, chicken, eggs, shortening, margarine, milk, obcesc, ice cream, po- tatnes, sugar, corn eyrup, canned pine- spples, dry fruits, tomators, froits, canned corn, wheat Bour, breakfast cere- als, coffee, soup (23)	Turkey, fish, lard, sal- ad drearing, evap. milk, apples, or- anges, bananas, canned peaches, canned peaches, (i0)	Butter, dry tables, rice (3)	Sweet pota- toca, corn meal (2)
North Central (Ra)		Soup (1)	Beef, vcal, turkey, egge, lard, choese, apples, bananas, canned peaches, canned pineapplee, canned pcas, canned corn, dry vegetables, coffee (14)	Pork, chicken, fish, butter, shortening, margarine, evap, milk, ite eream, po- tatoes, sugar, or- anges, dry fruits, to- matoes, wheat flour, breakfast cereals (15)	Lamb, salad dressing, fresh milk, cora ayr- up, beans, onions, carrots, lettuce, canned tornstoes, rice, corn meal (11)	Sweet pota- toes, frozen fruits (2)	Frozen vege- table: (1)
douth (R4)		Beans, dry vegc- ta- bles (2)	Beef, veal, pork, chicken, fish, ice cream, salad dreas- ing, corn syrup, apples, oranges, banana, dry fruit, tomatoes, canned peas, rice (15)	Lamb, turkey, eggs, butter, lard, short- ening, margatine, sweet potatoes, sug- ar, canned peaches, canned pineapples, onions, breakfast cereals, corn meal, coffee, soup (16)	Fresh milk, evap. milk, checse, pota- toes, canned carn, frozen vegetables, wheat flour {7}	Carrots, let- tuce, canned torna- toes (3)	Frozen fruite (1)

26). Of the 44 commodities considered in the analysis, 15 had a consumption index falling outside the range (50-150)in at least one region, 24 fell outside the range (75-125), and all the 44 commodities had at least one index falling outside the range (95-105). Thus, even after we make allowances for a 5 per cent deviation from the U.S. average consumption pattern due to variations in reporting data, all the commodities showed some regional variations in their consumption pattern. The range of consumption index (difference between the highest and lowest regional index) varied from 8.23 for bananas to 240.08 for corn meal. Thirteen commodities (veal, lamb, turkey, butter, lard, shortening, evaporated milk, corn syrup, beans, dry vegetables, wheat flour, rice, and corn meal) had a range of more than 100.

The presence of such wide variations in the quantity consumed in different regions could be explained in terms of (1) differences in prices, (2) differences in income-consumption relationship, and (3) other regional factors. We attempted to analyze the influence of prices and income in regional consumption behavior.

Differences in prices paid.—The expenditure and quantity data published in the survey reports were used to find the prices paid by consumers in different regions, and these were expressed as a percentage of average U. S. figures to obtain the index of prices paid. Using these indices (Appendix table A-5) we have prepared table 27 corresponding to table 25 for quantity indices. The spread or price indices in different regions is not so wide as the spread of quantity indices.

Although the cross-section data do not provide information to study the effects of price changes on quantity consumed, it denotes one point on the demand curve for each commodity. For each commodity, the quantity index in Appendix table A-4 and the price index in Appendix table A-5 provide four observations -one for each region-on price-quantity relationships. These points can be located on a two-dimensional space and, if the demand curve is assumed to be downward sloping, there will be an inverse relationship between the price index and the quantity index. Since it was assumed that the average U.S. quantities and prices form a basis of comparison, this point will be represented by (100, 100). We can locate the points corresponding to the price-consumption relationship in the four regions with reference to the basis, and if the demand relationship follows the conventional

shape, a positive deviation of price index from 100 will be associated with a negative deviation of quantity index and vice versa. Therefore, if the deviations of price index and quantity index from 100 are opposite in sign, it can be concluded that a high or low consumption index in a particular region is effected as a result of low or high price in that region. Also, if the deviations of price and quantity indices follow the same sign, it could mean either that the demand curve is not downward sloping or that the regional difference in consumption is not influenced by some factors other than prices. In table 28, deviations of price indices and quantity indices in different regions are expressed in terms of their signs -a positive sign denoting an index greater than 100 and a negative sign denoting an index less than 100.

Assuming that the demand curves for all these commodities are downward sloping, a positive sign can be expected to be associated with a negative sign if the consumption difference is influenced by price differences alone. However, this was not true for 16 commodities in the Northeast, 14 commodities in the West, 17 commodities in the North Central, and 13 commodities in the South.

Table 29 shows that the regional difference in consumption can be explained, at least partly, in terms of prices for seven commodities—pork, shortening, margarine, sweet potatoes, corn syrup, beans, and frozen vegetables. Consumption in all other commodities was influenced by factors other than prices in at least one region. Therefore, it is not possible to reject a hypothesis that certain regional factors influence consumption of various commodities in different regions.

To analyze the second aspect (variations in income-consumption relation-

				-					
Commodity	Nor	theast	H	iest	North	North Central		South	
	Р	Q	Р	Q	Р	Q	P	Q	
leef.	+	_	_	+		+		_	
eal	÷	+	_	1	÷ _	<u>'</u>	_		
ork	+	1 -	+			+-	L _	+	
estado	÷	+	l <u>-</u>	+	+		+	1 1	
hicken	÷	4	+	! <u>'</u>	<u> </u>	! _	<u> </u>		
urkey.	_	i 🕂	+	+ 1			+	<u> </u>	
ista.	÷			L _	_			+	
gg8	+			+	! _				
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ard	+	- T	ļ +		<u> </u>	-1-	+		
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and the second	+			<u> </u>	+	- 1	_	+	
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alad dressing	+	i —	+	+	+	- 1		+-	
	+	+	+	-	+	-	+	_	
vaporated milk	+	-	+	+		-	+	+	
heese	Ŧ	+	-	4	-	+	+	-	
е слевли	+	+	-	-	! -	+	-	-	
ntatoes	—	+	-	-	- 1	+	+	-	
weet potatoes	+		+	l –	+	-	-	+	
ugar	+	. –	-	- 1	-	-	-	+	
orn syrup	+	-	+	·	· ⊢	! _	- 1	+	
pples	-	+	+	[+	+	· +		· _	
JANG@A,	+	L +	+	+	+	+	- 1	-	
AAAAAS	+	-	+	_	_	+	_	-	
anned peaches	÷	-	+	+	-	i ÷	~	_	
anned pincapples	_	_	+	.		÷	_	_	
ry fruita	-	-	L		+	· <u> </u>	_	_	
rozen fruita	+	- 1	_	i i	' +	+	+	_	
omatoes	+		+	<u>'</u>	. =	F -	- -	+	
¢&III3	÷	-		_	+	_		+	
ліопа	_			_	+	~		+ +	
arrots	_		-	+		- -	÷	- -	
etiuce	+	+	-	+		- +	+ +	_	
aoned peas	- -	4	_	+					
snaed corn	_		+		~		-	÷	
		-	-	+	- +	Ŧ	+	-	
	+	[[−] +-]	-	+		-	+	-	
ry vegetables.s.	+		+	-	~		-	÷	
ozen vegetablea	-	+	-	. +	+	-	+	-	
heat flour	+	1 7	+	-	F —	-	+	+	
ice	+	+	+	-	+	-	-	+	
reakiast cereals	+	-	+	÷	-	+	-	_	
orn meal	-	-	+	-	+	-	-	+	
offee	+	+	-	-	-	+	-+-	-	
oup	-	! +	-	+	+	+	+		

TABLE 28 DEVIATIONS OF PRICE AND QUANTITY INDICES FROM BASE IN DIFFERENT REGIONS

Nor:: P stands for prices and Q for quantities. A \rightarrow indicates that the index is greater than 100 (so that the deviation is positive) and a = indicates that the index is less than 100.

ship over the regions), we have used a where covariance analysis.

Covariance analysis for testing regional variation.—Using the consumption data from four regions, we specified three types of regression equations as follows: where

$$q_{ij} = \text{consumption of } i^{\text{th}} \text{ commodity}$$

in the j^{th} region and
 $y_i = \text{income in the } j^{\text{th}}$ region.

Here, for a given commodity, the data from the four regions are pooled to obtain a single regression equation. With

90

Model 1

 $\log q_{ij} = a_i + b_i \log y_j \qquad (152)$

11 income groups, we have 44 observations to fit the regression equation in (152).

Model 2

 $\log q_{ij} = b_i \log y_j + c_j \log d_j \tag{153}$

where

the variables q_{ij} and y_i are as in the previous model and d_i is a dummy variable associated with the j^{th} region such that $\log d_i = 1$ in region j0 elsewhere.

An alternative way to express equation (153) is to specify three dummy variables associated with three regions and to retain the constant in the regression equation. The difference between model 1 and model 2 is that the latter incorporates different intercepts for different regions while the former assumes the same intercepts for all the regions.

Model 3

 $\log q_{ij} = a_{ij} + b_{ij} \log y_j \tag{154}$

where

the variables are defined as above.

While models 1 and 2 used all the 44 observations of a commodity to obtain a single regression equation, model 3 provides four regression equations corresponding to four regions. Therefore model 3 incorporates variations in both the intercepts and slopes of regression equations for a commodity in different regions.

Thus, model 1 assumed that the intercept and slope of the demand equation remained the same over the four regions; model 2 assumed that the intercept was different in different regions, but the slopes remained the same; and model 3

TABLE 29 COMMODITIES WITH REGIONAL PRICE-CONSUMPTION RELATIONSHIP NOT CONSISTENT WITH EXPECTION

Northeast		North Central	South
Yeal	Veal	Veal	Veal
Lamb			Beef
Chicken		Chicken	
	Tutkey	Turkey	
Fish		Fish	1
		Eggs	
Butter			
		Lard	Lard
	Salad dress-		
	ing		
Fresh milk		!	
	Evaporated	1	Evaporated
	milk		milk
Cheese			
Icc Cream	Ice Cream		Ice Cream
	Potatoes	i	Peo co cam
	Sugar	Sugar	
	Apples	Apples	Apples
Oranges	Orangea	Oranges	Orangea
			Bananas
	Canned		Canned
	Traches		peaches
Canned	Саллед		Canner
pineapples	piacapples		pineapples
Dry fruits	pricappies		Dry fruits
		Frozen fruita	Long trutts
		Tomatoes	
	Oniona	1 (111010)20	
	es capacita	Carrota	
Lettuce		Lettuce	
		Canned peas	
Canned corn		Canaca peas	
	'	Dry vege-	
	I .	tables	
	!	Wheat flour	Whent four
Rice		Wheat none	n DEAL ROUL
	Brenkfast		Breakfast
	ccreals		Cereals
Corn meal	octeana		vereats
Coffee	Coffee		
		Soup	
LG	14	57	13

assumed that both intercept and slope varied over the regions. Let s_1 , s_{2_1} and s_3 be the sum of squares of residuals associated with models 1, 2, and 3, respectively, and n_1 , n_2 , n_3 , respectively, be the degrees of freedom. Because the number of restrictions are least in the case of the third model, s_3 will be the smallest. Similarly, it can be shown that $s_1 > s_2 > s_3$. For testing the hypothesis that variations exist in intercepts alone, we use the sum of squares from the first and second models and define an F-ratio given by²⁷

$$F_{(n_1-n_2),n_2} = \frac{(S_1 - S_2)/(n_1 - n_2)}{S_2/n_2}$$

$$= \frac{(S_1 - S_2)n_2}{(n_1 - n_2)S_2}.$$
(155)

If the calculated F is higher than the table value of F at the desired level of significance, we reject the hypothesis of zero variability in the intercepts over the different regions and conclude that there exists significant variation at least in two of the intercepts in different regions.

Similarly, for testing the significance of variation in slopes alone, we can use the second and third models and define an F-test given by

$$F_{(n_1-n_2),n_1} = \frac{(S_2 - S_3)/(n_2 - n_3)}{S_3/n_3}.$$
 (156)

As before, if the F-values obtained in (156) are higher than the tabled value of F, we reject the hypothesis of nondifferences in the slopes (in this case, income elasticities) of the regression equations in the four regions. In other words, a rejection of the hypothesis that income elasticities are not different in the four regions makes it necessary to use different income elasticity measures for different regions.

Combining the two tests, if a particular commodity shows significance in both cases, variations exist in both intercept and slope. Also, it is possible to repeat the whole analysis, using expenditures on commodities in different regions instead of quantities consumed. In the present analysis, we have used both

quantities and expenditures as dependent variables to test the regional variations. In most cases, the intercepts showed significant regional differences. Only three commodities (bananas, canned peas, and breakfast cereals) provided nonsignificant differences in intercepts when quantity was the dependent variable, while the intercepts were nonsignificant for five commodities (bananas, canned peas, sweet potatoes, canned peaches, and frozen fruits) when expenditure was the dependent variable. When using quantity as the dependent variable, the income elasticities were significantly different for 31 commodities (25 at the 5 per cent level of significance and 6 at the 10 per cent level) and nonsignificant for 13 commodities. However, the number of commodities with nonsignificant regional differences in income elasticities rose to 20 when expenditure was used as the dependent variable. It may be possible to attribute this change to the influence of prices, that is, a significant regional difference in income elasticities, with quantity as the dependent variable, might have been offset by price differences within the regions to show a nonsignificant regional difference in income elasticities, with expenditure as the dependent variable. These factors are revealed in table 30 where we have adopted a cross classification according to the significance of the slopes and intercepts of income-consumption relationships in different regions.

When quantities were the dependent variables, 28 commodities showed significant regional variations in both intercept and slope, 13 commodities showed significant variation in intercept but nonsignificant variation in slope, and the remaining 3 commodities showed

²⁷ When we are interested in testing the significance of a few dummy variables, a *t*-test on individual coefficients will suffice. However, here an F-test is used to test the significance of the coefficients simultaneously.

TABLE 30

CLASSIFICATION OF COMMODITIES ACCORDING TO REGIONAL VARIATIONS IN INTERCEPTS AND SLOPES OF INCOME CONSUMPTION

Intercept and slope significant*		Intercept signifi signif		Intercept n cant slope s		Intercept and slope nonsignifi- cant	
Quantity dependent	Expenditure dependent	Quantity dependent	Expenditure dependent	Quantity dependent	Expendi- ture dependent	Quan- tity depen- dent	Expendi- ture dependent
Beef	Beef		Chicken				
Vea!	Veat :			Вапалаз	Bananas		
Pork	Pork		Turkey				
Lamb	Lamb			Cannod	Canned		
Chi chura		Fish	Fish	pess	peas		
Chicken Turkey		Butter	Butter				
Eggs	Eggs	Dutter	Dutter				
TTARP		Lard	Lard				
Shortening	Shortening						
			Salad dressing				
Margarine	Margarine	Mitk	Milk				
Salad dressing							
Cheese	Cheese	Evaporated	Evaporated				
		milk	milk				
Ісе стеаль	Ice cream	Sweet potatoes					Sweet
Tee clean	ite tream	theee polatoea					potatoes
Potatoes	Potatoes		Corn syrup				
Sugar	Sugar						
		Orangea	Orangea				
Corn syrup							
Apples	Apples	Canned peaches					Canned peaches
Canned pinesp- ples			Canned pinesp- plcs		I		
•							
Dry fruits Freah tomatoes	lomatoes	Frozen frujta	Dry fruits				Frozen fruits
Beans	Beans	Onjons	Onions				
Carrots	Carrots		Frozen vegeta-			ļ	
			bles		i		
7	Testure	Wheat flour	Whest flour				
Lettuce Canned corn	Lettuce Canned corn	Wheat nour Rice	Wheat hour Rice				
Canned tomatoes	Canned tornatoes	Corn meal	Corn meal			-	
Dry vegetables	Dry vegetables						
Frozen vegetables	Breakfast cercals			Breakfast			
				cereala			
Coffee	Coffee						
Soup	Soup						
	· · · · ·	(13)	(17)	(3)	(2)	(0)	(3)

* Significant category includes significance at 5% and 10% levels.

nonsignificant variation in intercept but significant variation in slope. There was no commodity with both intercept and slope showing nonsignificant regional variation. However, there were some modifications when expenditure was the dependent variable. Here, 22 commodities had significant regional variation in both slope and intercept, 17 had significant variations in intercept but nonsignificant variation in slope, 2 commodities had nonsignificant variation in intercept but significant variation in slope, and the remaining 3 commodities had nonsignificant variation in both intercept and slope.

Seasonal variations

Seasonality in food consumption originates from factors like crop production, climatic factors, and similar other reasons. Though modern processing, transportation, and refrigeration facilities have reduced the incidence of seasonality

in food consumption, many food items, especially fruits and vegetables, still show seasonal consumption patterns. Since the 1965 consumption survey was spread over the four seasons, it was originally planned to analyze the incomeconsumption pattern during the four seasons, using an approach similar to the one used for analyzing regional variations. Later on, it was revealed that these data will be available only after some time and, therefore, it was not possible to incorporate this aspect in the present analysis. For the same reason, it became necessary to exclude a discussion on the interaction of regions and seasons.

Demand Projections for 1980

This section reviews alternative approaches to demand projections and also projects consumption by commodity to 1980 on the assumption of constant real prices, time trends, and a particular increase in real income. To facilitate exposition, the commodities are discussed under ten groups—meat, eggs, fats and oils, dairy products, potatoes, sugar, fruits, vegetables, cereal and bakery products, and other commodities.

Alternative approaches to demand projections

Presented are possible uses of the demand interrelationship matrix for projecting future levels of demand.

Long-run changes in per-capita consumption of different food commodities occur as a result of individual and joint effects of many factors such as changes in relative prices and income, changes in tastes and preferences, introduction of new products, changes in occupation and urbanization, and changes in the age composition of the population. In the short run, it is convenient to assume that socioeconomic factors other than prices

and income remain constant. Therefore short-run changes in per-capita consumption will be influenced by price and income changes. Price changes result. mainly from supply conditions such as production cycles, seasonal variations, weather conditions, and technological changes. It may be possible to obtain forecasts of these variables for short-run periods. These forecasts of supply conditions can be used to project the price levels in the immediate future and, thus, changes in consumption levels for the immediate future can be projected. However, projections for longer periods of time cannot be handled in the same manner, because we may not assume that all the other factors remain the same. The following discussion indicates several alternative possibilities as to the use of the demand interrelationships for projecting consumption levels to 1980.

Projections with constand demand matrix plus time trend.—The demand interrelationship matrix was developed under conditions of static equilibrium. The only dynamic element introduced into the analysis is the measurement of the time trend of consumption for certain commodities obtained from the constant coefficient of the first difference of logarithmic estimating equation. One approach to projecting consumption in a future period is to use the demand matrix plus the time trend.

If the demand matrix is denoted by M, we have

$$Q = M \cdot P_{(n \times 1) \quad (n \times n+1)} \cdot P_{(n+1 \times 1)} \quad (157)$$

where

- Q = vector of quantities, expressed in logs;
- M =matrix of price and income elasticities; and
- P = vector of prices and income, expressed in logs.

When estimates of P are available for a future period, an estimate of Q can be

obtained from (157) under the assumption of constant demand elasticities. Let this estimate for the i^{th} commodity be \hat{q}_i . Also, let the annual time trend for the i^{th} commodity be S_i , expressed as a percentage change per year. If the projection is for K periods ahead of the present period, the time trend alone will introduce a multiplier of $(1 + S_i)^{\kappa}$. This multiplier, together with the projected static level (\hat{q}_i) , provides the following equation for consumption for K periods as:

$$\hat{q}_{iK} = \hat{q}_i (1 + S_i)^K. \tag{158}$$

Projections with changing demand matrix.—Another method of incorporating dynamic elements into the projection framework is by assuming a varying demand interrelationship matrix. Here, it is possible to assume that the elements in the matrix M vary over time in a certain manner. For example, consider the demand equations

$$\Delta \log q_i = \sum_{j=1}^n e_{ij} \Delta \log p_j + e_{ij} \Delta \log \bar{y} \quad (i, j = 1, 2, \dots, n)$$
(159)

where

- q_i = quantity of the *i*th commodity demanded,
- $p_i = \text{price of } j^{\text{th}} \text{ commodity, and}$
- $\bar{y} = a$ measure of real income.

Let y denote the income at current

prices. Then the expenditure proportion on the ith commodity is given by

$$W_i = \frac{p_i q_i}{y}.$$
 (160)

Multiplying (159) by (160) we obtain:

$$W_{i} \Delta \log q_{i} = \sum_{j=1}^{n} W_{i} e_{ij} \Delta \log p_{j} + W_{i} e_{ij} \Delta \log \bar{y}$$
$$= \sum_{j=1}^{n} \tau_{ij} \Delta \log p_{j} + \tau_{iy} \Delta \log \bar{y}$$
(161)

where

$$\P_{ij} = W_{i}e_{ij} \text{ and } \\
\P_{iv} = W_{i}e_{iv}.$$

If a regression equation of the type (161)

is fitted, using time-series data on quantities, prices, income, and expenditure proportions, it is implied that \P_{ij} and \P_{ij} remain the same over the years whereas, in (159), it was assumed that

O	1		Direct Elasti	icities (ϵ_B) in	
Commodity	Value of ¶n	1955	1960	1963	1970-
Jeef	-4.09595	-0.68268	-0.60235	-0.63015	-0.63999
ea]		-3 72325	-3.19136	-2.79244	-2,48217
ork	3.18393	-0 44844	-0.40820	-0 43026	-0.42452
amb and mutton	-1.07680	-1.79467	-1.79467	-2.15360	-2.15360
hicken	1,37835	-0 41768	-0.65134	-0 57431	-0 59928
ard	0.07850	-0.19628	-0.26667	-0 26667	-0.26667
oe cresin	0.68074	-0.60067	-0.66074	- 0.66074	-0.66074
otatoes	-0.34812	-0 26779	-0 21758	-0,24566	-0 26779
mnges	1.22042	-0.87173	0.71789	-0.64233	-0.61021
offee	-0.93738	-0 22862	-0.33477	-0.36052	-0.37494

TABLE 31 ELASTICITIES IN DIFFERENT YEARS

Hypothetical.

 e_{ij} and e_{iy} remain the same over the years. But \P_{ij} and \P_{iy} are obtained from e_{ij} and e_{iy} by multiplying with W_i . Since the budget proportion W_i varies over time, as a result of changes in the prices and consumption pattern, e_{ij} and e_{iy} also vary over time. Thus, if expenditure proportions are known for different years, it is possible to obtain an estimate of the demand matrix M for the different periods. For projection of future consumption levels, two different approaches could be used.

Estimation of changing demand coefficients. Using the values corresponding to each element of M, obtain a time trend for the coefficient and use this trend to project the value of the coefficient for a future period. That is, if M_{ij} corresponds to the (ij)th element of the interrelationship matrix for the period $t(i, j = 1, 2, \cdots, n; t = 1, 2, \cdots, s),$ the s values of M_{ij} could be used to establish a trend equation for M_{ij} and this could be used to obtain M_{ij}^{*+k} where K is the desired number of years for which projection is required. Having obtained the value of M_{ii}^{s+K} for all i and j, equation (157) can be used to project the value of Q if the price and income levels are known. For practical reasons. it is impossible to isolate trend values from price effects from every element of M_{ij} .

Estimation of expenditure proportions. Instead of obtaining a projection for $M_{ij}^{i+\kappa}$ directly, it is possible to estimate the expenditure proportions and to derive the value of $M_{ij}^{i+\kappa}$. From the estimation procedure used, \P_{ij} is assumed to be the same for all time periods or

$$\P_{ii} = W_i^{(t)} M_{ii}^{(t)}$$

Therefore,

$$M_{ij}^{(i)} = \frac{f_{ij}}{W_i^{(i)}},$$
 (162)

To illustrate this procedure, \P_{ii} was calculated for a few commodities using a regression equation similar to (161).

Table 31 shows the value of \P_{ii} and the direct price elasticities (e_{ii}) for 1955, 1960, and 1963. These are obtained by dividing \P_{ii} with the expenditure proportions corresponding to these commodities during 1955, 1960, and 1963, respectively. The last column (5) gives a projected value of the direct elasticities, assuming hypothetical values of the expenditure proportions in 1970. The same procedure could be used to obtain projected values of $M_{ij}^{i+\kappa}$ for all i and j and, once these values are known, as before, equation (158) can be used to project the consumption levels for K periods ahead.

To use (157) for projection of prices, it can be rewritten as

$$P = M^{-1}Q. (163)$$

When the objective of the study is to predict prices, it is more appropriate to fit demand equations with prices as dependent variables and to obtain a price flexibility matrix corresponding to M^{-1} . Most of the restrictions in deriving the demand interrelationships in terms of elasticities can be derived in terms of price flexibilities (see, for example, Houck, 1966). However, the inverse of the elasticity matrix, M, can be taken as a rough approximation to the price flexibility matrix and can be used for projecting future prices if the quantities consumed and income are known. For agricultural commodities, however, price prediction equations generally require specification of alternative outlets (fresh, processed), stock changes, and exports.

The above discussion indicates that projections of per-capita consumption levels in 1980 could be obtained either by using a projected demand interrelationship matrix for 1980 or by using projected expenditure proportions for 1980. Both these methods require that prices and income levels are available for 1980. In the absence of projections of future price levels, we have obtained projections of demand assuming constant retail prices, increasing income levels, and a time trend factor.

Demand projections by commodity group

These demand projections are based on (a) a particular assumption as to increased real income by 1980, (b) the income

elasticities used in the demand matrix. and (c) the time-trend coefficients obtained from time-series analyses of individual commodities. In particular, percapita consumption levels for individual commodities are projected for 1980, assuming constant real prices (1962-1966 average); real income per capita will increase from \$2,298 (the 1962-1966 average) to \$3,261 in 1980 as reported by Daly and Egbert (1966); and the estimated time trend, where statistically significant, will continue to 1980. The average annual per-capita consumption during 1962-1966 was taken as the base period. The cumulative effect of the time trend on this base consumption level was obtained as a product of the base consumption level and the multiplier $(1 + S_i)^K$ where S_i is the annual percentage change in consumption due to trend and K is the number of years to 1980. For many commodities, the time trend was not statistically signficant and projections are based only on the income elasticity. Results are presented by commodity group, given estimates of consumption and expenditures per capita for 1962-1966 and 1980.

Meat, poultry, and fish,-These commodities accounted for about one-third of the 1962-1966 average food expenditures. Detailed analyses of time-series data were made for only five itemsbeef, veal, pork, lamb and mutton, and chicken. Other items, such as turkey, fish, and edible meat offals are included for completeness but time-trend coefficients are not available for these commodities. Data on per-capita consumption are shown in table 32 for the base period (1962-1966) and for 1980, and are in terms of retail weight. For purposes of comparison, estimates by Daly and Egbert (1966) were converted to retail weight and also are given in the table.

	Cons	muniption per ca	pite				
Commodity	Estimated 1950 based on:		Retail price, 1962-1966	Expenditures per capits (1962-1966 dollars)			
	1982-1966	Income elasticity	Daly- Egbert	1002-1000	1962-1906	1980	
	1901	ində (retail weig	ht)	cents	doll	a76	
deat	-						
Beef	72.08	60.64	86.6*	74.10	53.41	59 90	
Veal	4.20	3.04		87.65	3.68	2.66	
Pork	57.76	60,82	53.9	75,60	43.67	45.98	
Lamb and mutton	3,90	4.37	∣ 3 .1 [60.00	2.34	2,62	
Edible offals	10.241	11.18	i	61.90	6.34	6.91	
Total meat	148,18	160.23			109.44	118.07	
oultry							
Chicken	32 18	39,22		40, 50	13.16	16.04	
Turkey	7.28	9 62		54.10	3 94	5,20	
Total poultry	39 46	48.84	45.5		17.10	21.24	
fish				İ			
Fresh and frozen	5 88			70.20	4.13		
Canned	4.28			75.25	3.22		
Cured	. 60			73.40	.37		
Total fish	10.66	10.45			7,72	7.72	
ГОТЛL	198.30	219,75			134.26	147.03	

TABLE 32 MEAT, POULTRY, AND FISH: CONSUMPTION, PRICES, AND EXPENDITURES, 1962-1966 AVERAGE AND PROJECTED 1980

Includes yeal.

† Increase estimated at 9 per cent corresponding to projected increase in beef plus pork consumption.

The income elasticities for beef, veal, lamb and mutton, and turkeys are weighted regression coefficients based on the 1965 survey data. Those for pork, chicken, and fish are based on the 1955 survey data, with estimates from the 1965 data negative in sign and not statistically significant for chicken and fish. Income elasticity coefficients and annual time-trend factors are summarized in table 33. Because none of the time-trend variables were statistically significant, projections are based on the income elasticity coefficient.

Data on expenditures per capita, given in table 32, are in terms of constant (1962-1966) dollars. Expenditures are projected to increase by 9.5 per cent in real terms. The level of beef consumption in recent years would suggest that the projected 1980 level may be too low. (See Appendix A figures A-1 to A-14 for postwar trends in actual prices and consumption per capita.)

Eggs account for about 3 per cent of consumer food expenditures. The income elasticity is close to zero. The estimate, based on the 1965 survey data (using weighted regression), was -.076 but the log difference equation result of .055 was used in this study (see table 33). There was a statistically significant negative time trend of more than 5 per cent per year but consumption appears to have leveled off at about 40 pounds per capita. Thus, the estimates of consumption and expenditures for 1980 are based on the income effect only. The estimate is considered as an upper limit and is somewhat higher than that reported by Daly

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TABLE 33 RETAIL INCOME ELASTICITIES AND TIME TRENDS FOR MAJOR FOOD COMMODITIE8+

Item	Income elasticity	Annual time trend:	Item	Income electicity	Annual time trend‡
		per cent			per cent
Meat, poultry, and fish	000		Canned		
Beef	.290	2.90	Peaches	.341	-2.55**
Veal	. 591	-4,82	Pineapple	.447	0.84
Pork	.133	-0.02	Other	. 200	
Lamb and mutton	.571	-0.83	Dried prunes	.315	8,60**
Chicken	.178	0,90	Frozen	. 661	
Turkey	.768		1		
Fieb	.004		Vegetables Fresh		
Egas	.055	5.60*	Lettuce.	. 147	J.10
			Tomatoes.	.170	-1.54
Fats and oils			Beaus (anap and lima)	0.0	5.71*
Butter.	.316	-3.22**	Onione	005	0.0
Lard	050	-5.09**	Carrots	.319	-2.42**
Shortening	029	-0.16	Other.	150	
Margarine	00	3 70	Otue1	. 200	
Mayonnaise and sajad	0.0	D .10	Canned		
dorsailog	.285	3.20		.032	-4.90
Greening	. 400	C	Paas,	.023	
Dairy products			Corn		-1,12*
	A		Tomatoes and products.	.173	
Milk	.204	-1.42	Other	.200	,
Evaporated milk	0.0	3.69*	Dry edible beans	.217	-1,30
Cheese	.249	4.20**	Frozen vegstables	.610	
Ice cream	.331	-2,74	Cereals and bakery products		
Potatoes			Rice (milled).	.055	1.30
Potatoes (freeh)	.117	-0.71	Wheat flour (white and	1-11	
Sweet potatoes (fresh)	0.0	-6.46*	whole wheat)	083	-1.25
			Breakfast cereals.	. 958	-0.11
Sugar and successers			Corn meal and hominy	058	-1.86**
Sugar	.032	1.80	Bread and other products.	0.0	
Corn syrup	.174	-2.12	showd and other products.	0.0	
com syrup.		-4.14	Beverages and soup		
Pruit			Coffee	.017	
Fresh				.057	2.70
	.140	1.00	Soup		
Apples.		-1.02	Other beverages	.230	
Bananas	.140	2.00			
Orstages	,260	-3.02	H I		
Other	. 400				

† Income elasticities are hased on cross-section data and time trends on time-sectics adalysis (see Appendix table A-I). I Figures without subscript indicate coefficient not statistically significant.

Significant at the 5 per cent level.

** Significant at the 10 per cent level.

and Egbert (1966) as shown in table 34. Fats and oils account for about 4 per cent of consumer food expenditures. Income elasticities, derived mainly from the 1965 survey data, are relatively low except for butter (.318) and mayonnaise and salad dressing (.285). The trend coefficients were negative and statistically significant for butter and lard (see table 33). Projections for 1980 for butter and lard are based on income and trend effects which result in consumption levels below those for 1962-1966,

The consumption of margarine is pro-

jected at current levels if 1962-1966 average price relationships hold. This estimate may be low, however, if the current trend in prices and consumer preferences continues. The consumption estimate for all fats and oils of 47 pounds per capita is below that of Daly and Egbert (1966) of 49.5 pounds, as shown in table 35.

Dairy products (excluding butter) account for about 15 per cent of consumer food expendtures. In this study, only major dairy products were analyzed, including fluid whole milk, American

cents

35.0

 TABLE 34

 EGGS: CONSUMPTION, PRICE, AND EXPENDITURES 1962–1966 AVERAGE AND 1980

 Consumption per capita (1960 estimate based on : 1962 - 1966
 Retail price 1962 - 1966

 Income elasticity
 Retail price 1962 - 1966

 Income elasticity
 Retail price 1962 - 1966

38.85*

* SOURCE: Daly-Egbert (1986) estimate of consumption is 86 per cent of the 1957-1959 level.

pounds (retail weight)

41,27

cheese, evaporated whole milk, and ice cream.

40 34

The income clasticity for milk obtained from 1965 survey data is .20 which compares favorably with that reported by Rojko (1957). Further, Rojko reports the percentage effect of time per year as -1.32 as compared with -1.42in this study. Although our coefficient is not statistically significant, a negative time trend appears consistent with observed trends and with Rojko's study. Thus, the combined income and trend effects are used in projecting consumption to 1980 (as indicated in table 36).

For American cheese, Rojko reports a positive trend of 4.27 per cent which

compares with 4.20 in this study. However, our income elasticity from crosssection data of .249 differs markedly from Rojko's time-series estimate of -.99, an estimate that was not statistically significant. For projections to 1980, the estimated level, based on the income elasticity and significant time-trend effect, was 12.04 pounds and only 6.78 pounds based on income effect alone. These estimates were averaged to obtain the 1980 consumption level given in table 36.

dollars

14.44

14 12

Estimated consumption of evaporated milk is based on a statistically significant negative time trend obtained from timeseries analysis. The income elasticity

TABLE 35	
FATS AND OILS: CONSUMPTION, PRICE, AND EXPENDITE	URES, 1962-1966

	-	· ·						 _	-
AV	ER	$\mathbf{A}G$	\mathbf{E}	AN	D	198	30		

		Consumption per capita					
Commodity	1960 estimate based on:			Retail price	Expenditures per capita (1962-1966 dollars)		
	1962–196 6	Income Income Income elasticity and trend		Daly- Egbert	1962-1966	1962 - 1966	1980
	pounds (retail weight)				cents dollars		
Butter	6.62		4.93		77.65	5.14	3.83
.erd	8.35		3.04		20.15	1.28	.61
hortening	14,10	14.27	[· .	29.40	4.15	4.20
largarine	9.80	9. 8 0			26.85	2.83	2.83
Other	13.40*	15.00			38.35	5,14	5.75
TOTAL	50,28	47.	બ	49.5		18.54	17.22

* Includes all other fats and cile of which mayonnaise and salad dressing equal 3.9 pounds.

Eggs

	Const	Consumption per capita			E		
Commodity		1980 estimate based on :		Retail price 1962–1966	Expenditures por capita (1962-1966 dollars)		
1	1962-1966	Income an(i tren(i	Daly Egbert		1962-1966	1950	
· · · · · · · · · · · · · · · · · · ·	році	nde (retail weight	:)	cents	doll	Gra	
Fluid milk and cream				l !]		
Fluid whole milk (A)	271.40	242 18		11,9	(32.30)		
Other	40 96	36.55*					
TOTAL fluid milk equivalent	(303.6)			11.9	36.13	32,24	
Cheese		1					
Americaa (B)	6.14	9.41†		84.10	5, 16	7.91	
Other	7.88	12.08;		36.459	2.87	4.40	
Evaporated and condensed				' I			
Evaporated whole milk (C)	8.90	5.06		17.5	1.66	. 89	
Other	7 12	4.095		22.4	1,59	.92	
Ice cream (D)	18.14	17.55**		35.9	6.51	6.30	
Dry milk products							
Nonfat dry milk	5.86	{ }					
Other	1,06						
	6 92	7.00If		49.011	3 39	3.43	
Total							
Product weight	367.46				57.21	56,09	
Sum of items A, B, C, D	301.68	274.20			[
Milk equivalent: fat content basis	625		570				

TABLE 36 DAIRY PRODUCTS EXCLUDING BUTTER: CONSUMPTION, PRICES, AND EXPENDITURES, 1962-1966 AND 1980

· Percentage increase assumed equal to that for milk.

Average of estimates based on income (5,78) and income and trend (12,04), Percentage increase assumed equal to that for American cheese.

Listimate for cottage cheese

Percentage increase assumed equal to that for evaporated milk.

Estimate for contensed milk.
 * Average of estimates based on income (20.60) and income and trend (14.44).
 † Estimated at about 1962-1966 level.
 ‡ Estimate for nonfat dry milk.

(shown in table 36) was set at zero although the cross-section data for 1965 provided a negative income clasticity of -.674. It is expected that consumption will continue to decline in the future.

Estimated consumption of ice cream. based on an income coefficient, was 20.66 pounds and that for income and a statistically significant time trend was 14.44 pounds. These estimates were averaged in making projections for 1980.

Potatoes.—Per capita consumption of potatoes and sweet potatoes showed a

declining trend during the postwar period (see Appendix figure A-5). The decline in fresh potatoes were somewhat offset by increases in the consumption of processed potato products, especially chips (included with fresh) and frozen french fries. Retail prices for fresh potatoes and sweet potatoes increased over the period, contributing to the downtrend in consumption.

The income elasticity coefficients are from 1955 survey data. The elasticity coefficients, based on the 1965 survey

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	<u> </u>	_	1980	<u> </u>			<u> </u>
Commodity		Consumption	n per capita				
		1980 estimate based on :			Retail price 1982–1965	Expenditures per capita (1952-1966 dollars)	
	19621986	lncome elasticity	Income and trend	Daly- Eghert		1962-1966	1980
		pounde (rela	il weight)	•	Cents	dol	lars
Potatoes							
Fresh	92.40	96.92	87.59		7.60	7.21	6, 83
Canaed	. 42	2					
Frozen	5.36		9 00 •		30.05	1.61	2.70
TOTAL, product			1 - 1			—	
weight	98.18		96.59			8,62	9.53
fresh equivalent.	106.20			106		0.04	¥.34
Sweet potatoes							
Freeh	4.40	4.40	1.54		15.30	.67	. 24
Canned .	1.16		1.18		22 00	.26	.28
							. 80
TOTAL, product			i]		
weight	5.56		2.70			.93	. 50
fresh equivalent	5.72				ł		
TOTAL, product weight	103.74		99.29			9.75	10.03

TABLE 37 POTATOES: CONSUMPTION, PRICES, AND EXPENDITURES, 1962-1966 AND

* Rough estimate based on trends in consumption.

data, were .008 for potatoes and -.587for sweet potatoes. For projections to 1980, the combined effect of income and time trend is used for fresh potatoes and sweet potatoes (table 37). The estimates for potato products are rough estimates

based on recent trends in consumption

Sweeteners (excluding noncalorics).---Sugar is the major item in this group that accounts for more than 3 per cent of consumer food expenditures. Consumption per capita has remained rela-

TABLE 38

SUGAR AND SWEETENERS: CONSUMPTION, PRICES, AND EXPENDITURES, 1962-1966 AND 1980

	Con	sumption per ca	pita		Emeralitaria per seria (1995		
Commodity		1980 estimate based on:		Retail price 1962-1966	Expenditures per capita (1962 1966 dollars)		
	1962-1966	Income elasticity	Daly-Egbert		1962-1966	1980	
		unde (retail weig	ht)	centa	dollars		
Sugar, refined. Corn syrup Other sweeten-	96.32* 13.00	98.12 13,95	97.2†	13.50 21.25	12.10 2.75	12.27 3.96	
ењ ТОТАЦ	0.64 116,46	8.641		27,005	1,80 16, 55	1.80 17,03	

Includes 5.3 pounds in processed fruits and vegetables.
 † Converted to refined from raw as reported by Daly-Egbert (1966), using factor 783.5.
 † Assumed equal to 1962-1966 average.
 † Price of other sweeteners (1967-1959) adjusted to 1982-1968 level (Hiemstra 1968).

		Consumption	per capita					
Item	1980 estimate based on			l on:	Retail price 1962-1968	Expenditures per capita (1962-1965 dollars)		
	1962-1960	Income elasticity	Income and trend	Daly- Egbert		1962-1966	1980	
		pounde (retail weight)			cento	dollars		
'resh								
Apples	17.20	16,21			17.35	2.98	3,16	
Bananas .	16,96	17,95	:		15.90	2.70	2.85	
Orangee	14.46	15.04	:		18.10	3.62	2.90	
Other	29.16	29,16			22.05	6.43	6,43	
TOTAL .	77.78	81.36				14.73	15.34	
Canned fruit								
Peaches	6.42		5.26		18.55	ւսց	.98	
Pincapples	3.08	3.66			27.20	.84	1.00	
Other	13,46	13.455			20.00	2.69	2.69	
TOTAL .	22.96	22.39				4,72	4.67	
)ther items								
Canned juice	11.66	11.68*			18.401	2,15	2.15	
Chilled fruit and juice	199	t, 99*			26 801	. 53	. 53	
Chilled citrus segments	.37	.37*			22,101	.049	.08	
Frozen fruit	3.70	4,72			58.20	2.08	2.65	
Frozen citrus jujce	4,62	5.90			69,40	3.21	4.09	
TOTAL	22.34	24 64				8,05	9.50	
Dried fruits								
Prunes	.60		.23		42.43	, 26	.10	
Other	2.36	2.029			39 50‡	.93	.80	
TOTAL	2,96	2.25				1,19	.90	
OTAL, Retail						28.69	30,41	
Product weight	128.04	130.64						
Fresh equivalent				206				

TABLE 39 FRUITS: CONSUMPTION, PRICE, AND EXPENDITURES, 1962-1966 AND 1980

Assumed coust to 1962-1966 level

Based on income elasticity of ~.002 from 1965 survey data weighted regression analysis.
 Weighted average price for 1967-1959 (Hiemstra, 1968, p. 51).
 Based on income elasticity of ~.043 from 1965 survey data weighted regression analysis.

tively constant at about 97 pounds per capita. The income elasticity for sugar (and also for corn syrup) is based on 1965 survey data with the coefficient obtained by a log difference equation. The annual time trend obtained from the time-series data analysis was not statistically significant. Projections, therefore, are based on the income clasticity coefficient and the projected increase in per capita disposable income (table 38). The same approach was used for corn syrup. The exclusion of noncaloric sweeteners, the demand for which has been increasing, is an important limitation on the possible accuracy of these projections.

Fruits include a large number of commodities, but statistical analyses were made on only a few of the important

		TABLE 40		
VEGETABLES:	CONSUMPTION,	PRICE, AND	EXPENDITURES,	1962-1966 AND
		1980		

		Consumption	per capita			D		
Commodity	1980 estimate based on:				Retail price 1962-1966	Expenditures per capita (1962-1966 dollara)		
	1062-1966	Income elasticity	Income and trend	Daly- Egoert	1972.1910	1962-1966	1980	
		pounds (reta	il weight)	-	Cents .	dolle		
Vegetables Fresh								
Lettuce	19.04	20 21			16 40	3,12	3.31	
Tomatoes	10.44	11.19			32,90	3,43	3.68	
Beans, snap and linu	2.30	1.67			24.40	, 56	.41	
Oniona	10,92	10,94			12.00	1.31	1.31	
Carrots	5.54		7.31		15,25	1.01	1.15	
Other	42 44	45.10			18.00	7,64	8,12	
TOTAL	91,78	96.42		ļ		17.07	17.98	
Canned								
Реяз	4.12		2.00		18.70	.77	.38	
Corn	5.48	5.53			19.50	1.07	1.08	
Tomatoes, whole	4.50	4.97			13.90	.63	69	
Tomato products	14.10	15.10*			26 90	3.79	4.06	
Other	17.86	19.34			26.95	4.81	5.21	
TOTAL	46.06	46.94				11.07	11.42	
Frozen	8.18	10.27			36.50	2,99	3,75	
TOTAL, Product Weight.								
Retsil.	146 62	153.63				31,13	33,15	
Freeh Equivalent, Retail	194.06			209†		01.10	00.70	
Dry beans.	7,16	2.30			24,4	.17	.18	
TOTAL						31.40	33.28	

Estimated at .25 as compared to .17 for canned whole tomatoes.
 † Converted from farm to retail using factor of 98.2.

fruits. About 8 per cent of consumer food expenditures are for fruits in fresh, canned, dried, and frozen form. The existence of many commodities and multi-outlets prohibited a detailed analysis of each item with the adopted approach to demand analysis. The fresh fruits studied include apples, bananas, oranges, and all others. The demand for prones was selected as an important dried fruit and frozen fruit was taken as an aggregate.

All items showed positive income coefficients based on weighted regressions of the 1965 survey data except for canned peaches (-.002) and dried fruit (-.043) for which alternative estimates were used.

Projected consumption levels for included items are based on income elasticity estimates except where trend coefficients also were statistically significant (canned peaches and pruncs). Other items were assumed equal to 1962–1966 per capita consumption levels (table 39).

Vegetables account for more than 8 per cent of consumer food expenditures.

7. t8

ID8.2D

7.88

9.76

	196	52-1966 AND	1980		
Commodity	Co	maumption per c	Expenditures per capita		
		1980 estimate based on :			
	1962-1966	Income electicity	Income and	A verage 1963 and 1968*	1980†
		pounda	<u> </u>	dolla	518

7.35

93 35

7.94

7.62

TABLE 41
CEREAL AND BAKERY PRODUCTS: CONSUMPTION AND EXPENDITURES,
1962-1966 AND 1980

* Based on the relative importance of expenditures on cereals and bakery products in the BLS consumer surveys of	
1963 and 1966 (Hiemstra, 1968, p. 172) of 2.48 per cent of total expenditures. This percentage was applied to the average	
of disposable income in 1963 and 1966 of \$2,380. The distribution of expenditures by item is based on data from the 1965	
aurvey	

[†]With constant prices, the change in expenditures is proportional to the change in per-capita consumption.

As with fruit, vegetables are sold in many varieties and forms but only a limited number of commodities were analyzed separately. Fresh vegetables include lettuce, tomatoes, snap and lima beans, onions, carrots, and "all other fresh vegetables." Canned vegetables include peas, corn, canned whole tomatoes and tomato products (product weight), and "all other canned vegetables." Dry

Rice, milled.

Corn meal and hominy

TOTAL..

.. .

Wheat flour, white and whole wheat.....

Bread and other products....

.

edible beans and frozen vegetables are considered also.

2 24

4.16

11.45

1.56

39.02

58.53

Income elasticities show considerable variation, with frozen vegetables estimated at .610 as compared with negligible income effect, for example, for canned peas. Several vegetable items have statistically significant negative time trends—such as canned peas, fresh beans, and carrots (table 40).

TABLE	42
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BEVERAGES	AND SOUP:	CONSUMPTION	AND	EXPENDITURES,	1962-1966
		AND 1986			

	Co	nsumption per cay)ita	: Expenditures per capita		
Commodity	1960 estimate based on:		Average	1		
	1962~1966	Income elasticity	Daly- Egbert	j 1983 and 1966	1980*	
	pounde			dollars		
Coffee, green bean equivalent	15.24	15.54	16.00	9.62	10.01	
Soup	16,16	17,76		7.89	8 67	
Other beverages				6.24	8.00	
TOTAL				23.95	26.681	

* With constant prices, the change in expenditures is proportional to the change in per-capita consumption, † Based on relative importance of expenditures on nonalcoholic beverages in the ELS consumer surveys of 1988 and 1985 (Heimstra, 1985, p. 172) of 1.045 per cent of total expenditures. This percentage was applied to the average of disposable income per capita in 1983 and 1985 of \$2,380. The distribution of expenditures by item is based on data from the 1985 survey.

2.40

3.59

1,22

39.02

57,77

11.54

TABLE 43

PER CAPITA FOOD EXPENDITURES, 1962-1964 AND PROJECTED 1980, ASSUMING COMMODITY PRICES REMAIN AT 1962–1964 LEVELS

	Food expenditures per capita						
Commudity group		1980					
	1962-1966	Estimated	Changes from 1962-1966	Percentage of all food expen- ditures			
	ào	la78	per	cent			
Meat, poultry, fish	134.26	147.03	: + 9.5	33.0			
Eggs	14,12	14.44	+ 2.2	3.2			
Fats and oils (including butter)	18.54	17,22	- 7.1	3.9			
Dairy products (excluding butter)	57.21	56.09	-20	12.6			
Polatoes	9.75	10.03	+2.9	2.2			
Sweeteners (excluding non-caloric).	16.55	17.03	+ 2.9	3.8			
Fruits	28 69	80.41	+ 6.0	5.8			
Vegetables	31.40	33.28	+ 6.6	7.5			
Cereal and bakery products	59.53	57 77	- 1.3	13.0			
Beverages and soup	23 95	26.68	+11.4	6.0			
TOTAL included items	392.73	409.85	+ 4.4	92.0			
Excluded food expenditures	34.27*	35.75†	+ 4.4	80			
Expenditures		·					
Food	427	446	+ 4.4	100			
Nonfood	1,686	2, 572	·1·52, 6				
TOTAL	2, 113	3,018 \$	+ 12.6				
Disposable personal income	2,298	3,281 ¶	 ; +1.01				

Includes underestimation of expenditures for meals away from home since consumption is evaluated at retail prices
 Also, the following expenditures (1957-1969) are not included: malons (\$2.07), baby food (\$1.55), peanuts (\$2.24), treenuts
 and coconuta (\$2,30), and frozen desserts (\$2.46).
 † Estimated at 104.4 per cent of 1962-1964 level, equal to the increase for included iteros.
 2 Estimated at 92 per cent of disposable personal income, equal to that for 1962-1964.
 † Expressed in 1964 dollars, as given by Daly-Fgbert (1966).

Consumption levels in 1980, assuming constant prices at 1962-1966 levels, are projected to increase for most vegetable products--especially for frozen vegetable items. Decreases are expected in consumption per capita of dried, edible beans and items such as canned peas. where frozen products will replace market demand for the product. Expenditures in 1980 are projected to increase by 6.48 per cent.

Cereals and bakery products account for about 15 per cent of consumer food expenditures. This group posed difficulties for analysis because certain items such as wheat flour are purchased as

such by the consumer but also is used in processed products such as bread and bakery products. We analyzed four items -milled rice, white and whole wheat flour, breakfast cereals (taking the price of corn flakes as representative of all items), and corn meal and hominy (using corn meal prices). Bread and other bakery products were included by using the direct elasticity of -.150 for cereals and bakery products used in Brandow (1961).

The income elasticity related to crosssection data for wheat flour purchased as such. The time-trend coefficients, obtained from time-series analyses of each commodity using log first difference equations, are negative except for milled rice. Although not statistically significant, these time-trend coefficients plus income elasticities are used to adjust base period expenditure levels to 1980 expenditures. This appeared reasonable because of consumption trends in recent years. These estimates are given in table 41.

Beverages and soup.—Only two commodities, coffee and soup, were analyzed based on survey and time-series data. Another item, "other nonalcoholic beverages," was included since expenditures are important as based on the U.S. Bureau of Labor Statistics consumer expenditure surveys of 1963 and 1966 (see table 42). In projecting expenditures to 1980, the income elasticity coefficient alone was used for coffee and soup, although the time-trend coefficients were statistically significant. This judgment factor was based on inspection of recent trends for these commodities (see Appendix figure A-15).

The summary of per-capita expenditures for 1980 is given in table 43. The distribution of expenditures changes slightly with the major dollar increase in expenditures (in 1962–1966 dollars) for meat. In 1962–1966, food expenditures accounted for 18.6 per cent of disposable personal income. This proportion is expected to decline to 13.5 per cent in 1980, assuming real income per capita increases 42.8 per cent and real food expenditures per capita increase by only 4.4 per cent.

Conclusions and Implications

Conclusions

The major conclusions, based on the results of this study, are listed below in the order in which they are discussed in the text.

(1) It is possible to obtain a demand interrelationship matrix incorporating the ideas of neutral want association and want independence.

(2) For most commodities included in this study, the behavior of marketing margins appeared to be a linear function of the retail prices. One advantage of this specification is that it includes both the constant absolute spread and the constant percentage spread as special cases.

(3) Both the intercept and slope in the relationship expressing price spread as a linear function of retail price did not show significant variations over seasons for most commodities. Only four commodities showed seasonal variations in both intercepts and slopes.

(4) In general, higher income groups tended to consume high-quality products as far as quality can be measured in terms of prices. In the cases where quality elasticity was negative, the prices paid by the upper income group was less than the prices paid by the lower income group. This may indicate that quality is only one of the factors that influence average prices paid; other factors are ability to obtain quantity discounts, facilities to shop from low priced areas, and direct bulk purchases from farms.

(5) With per-capita quantity consumed as the dependent variable, economies of food use were revealed for four commodities and diseconomies of scale were revealed for seven commodities. However, when per-capita expenditure was the dependent variable, the number of commodities with economies and diseconomies was six and three, respectively. Economies in food use were more predominant in per-capita expenditures than in per-capita quantities.

(6) For most commodities, income elasticities did not change significantly between 1955 and 1965. Though there were some readjustments in the quantities consumed by persons in different income groups over this period, a redistribution of population in the income groups offset some of this effect and the net result was that only seven commodities showed significantly different income elasticities for these two years.

(7) For most of the commodities, a relationship, linear in logarithms, between consumption and income showed significant regional variation in the intercept over the four regions. When quantities were the dependent variable, 31 commodities showed significant regional variations in income clasticities, while the corresponding number was reduced to 24 when expenditure was the dependent variable. The existence of such wide variations in the coefficients of income-consumption relationship over the different regions makes it necessary to place emphasis on regional estimates rather than an approximation to national estimates when a study is intended to analyze regional demand characteristics. (8) Projections of per-capita consumption levels and expenditures are developed for all major food items. The assumption of constant prices at the 1962-1966 level allowed estimation of consumption and expenditures in 1980. If further research on supply response at farm, processing, and retail were available, the constant price assumption could be relaxed to allow more realistic price consumption and expenditure estimates.

Implications of the Results

Implications on methodology.—The implications on the methodology of de-

mand analysis presented here are not based on theoretical considerations alone, rather, they provide empirical support to some of the existing theoretical analysis.

(1) It was concluded that grouping of households according to income groups does not constitute serious loss of preciion on the estimates. As Malinvaud (1966, pp. 242-46) points out, the loss of precision will be small if the exogenous variables are homogeneous within a group and if there are at least ten groups. The results indicate that the classification of households, according to family income, into twelve income groups in the 1965 household food consumption survey is appropriate. For such cross-section studies, if the objective is only to obtain the income-consumption relationship, it is enough to retain data according to income groups.

(2) Although it can be argued that income elasticities obtained from timeseries data may be more appropriate for projection purposes for most of the commodifies included in this analysis, income and prices were highly correlated and, therefore, estimates of income elasticities obtained from the time-series data seemed to be inappropriate. Also, the income elasticities obtained from time-series data reflect short-run clasticities. Cross-section data provide estimates of income elasticities that are generally considered more accurate than those obtained from time-series data. This indicates that it may be appropriate to use a combination of cross-section and time-series data for estimating demand interrelationships. In other words, estimates of income elasticities can be obtained from cross-section data and it can be used as an extraneous estimate for time-scries analysis.

(3) Comparison of income elasticities obtained from different cross-section sur-

veys requires that the effects of changes in general price levels and the effects of a redistribution of income over the cross sections should be removed before shifts in income elasticities can be analyzed. The estimated income elasticities will be influenced by the level of prices and relative proportion of individuals in different income classes. In this analysis, a graphic approach was used to convert the 1965 distribution of samples into the 1955 price levels and an illustration was provided to show the implications of redistribution of income on aggregate income elasticity.

(4) Analysis of covariance was used to test the variations in income elasticities over the regions and to test the seasonal variations in margin relationships. Aggregate income elasticitics can be obtained as a weighted sum of income elasticities for different regions. However, given an aggregate income elasticity, if there is reason to believe that regional variations exist in income elasticities, there is no method to disaggregate for regional elasticities. In such circumstances, for regional demand analysis, it may be necessary to obtain regional estimates instead of approximating it from the aggregate estimate. In this case, disaggregation of an aggregate income elasticity into regional elasticities is a more important and serious problem than the generally recognized aggregation problems.

(5) Use of the first differences of the variables sometimes may improve the reliability of the coefficients appearing in the demand functions. In the present study, the demand functions were specified as linear in logarithms of the variables and linear in the first differences of the logarithms of the variables. In a number of cases, the first difference specification gave demand equations satisfying a priori expectations of signs

and significant coefficients. In most cases, a higher R^2 was obtained when the variables were in logarithms rather than in log differences. However, the higher R^2 , in the case of some equations with logarithms of original variables, could be partially explained by the high intercorrelation among some variables appearing in the equations. Also, in some cases, when the logarithms of the original variables were used, the Durbin-Watson statistic showed either the presence of serial correlation or it fell in an inconclusive range. When the first difference of the logarithms of the original variables were used in the regression equations, both the intercorrelations and serial correlations were reduced. Thus, specification of the regression equations with the first differences of the logarithms of the original variables improved the statistical properties of the estimates. This result is in conformity with Parks' (1968) empirical comparison of alternative functional forms of demand where he concluded that the specification with variables in the first differences of logarithms (referred to as the Rotterdam model of Theil and Barten) gave the best statistical properties among the models compared.

(6) Frisch's procedure for calculating all the direct and cross elasticities implies that the utility function is additive in a cardinal sense. Although this assumption may hold for commodity groups, it may not be true for all the individual items of food. Therefore, when the goal is to obtain a demand interrelationship matrix of the type discussed in this study, Frisch's approach alone is not satisfactory. It was demonstrated here that concepts of ordinal separability can be utilized to identify separable groups and, among the separable groups, an assumption of strong separability permits the use of Frisch's

approach. Still, the approach used here does not handle the simultaneous nature of demand relationships since the procedure used in the present study is based on a single equation approach. The solution of demand equations incorporating the simultaneous nature of demand characteristics and the theoretical restrictions on demand parameters may often lead to the solution of a nonlinear system of equations. When the number of commodities included in the study is large, as in the present case, the iterative procedures used for the solution of the nonlinear system will often become cumbersome though not impossible. In such cases, often it may become necessary to determine a trade-off between including more commodity details and estimating demand parameters through simultaneous relationships.

Implications on demand parameters.— In addition to the factors pointed out in the text, here are some aspects of the results which can be generalized:

(1) Although the income elasticity for total food is small, wide variations exist among different food items. For commodities such as lard, margarine, evaporated milk, sweet potatoes, beans, and bread, the income elastiticities were very close to zero, while frozen fruits and frozen vegetables had income elasticities of more than 0.6. The classification of income elasticities, according to their magnitude, presented in table 14 may be useful for marketing managers in terms of planning their marketing strategy although more detailed analyses may be needed. Similarly, the regional characteristics of income consumption relationship will help marketing managers to determine the nature of emphasis to be placed upon different regions in the overall marketing program. Also, for those commodities showing economies or diseconomies in consumption pattern,

changes in family structure also will be an important consideration.

(2) An estimate of demand interrelationships is required for many policy decisions, especially in the areas of supply control and demand adjustments. Our demand interrelationship matrix is for the United States as a whole and, as such, it is applicable only as an aggregate relationship. Variations among regions and problems of disaggregation make it difficult to derive similar demand interrelationships for different regions directly from the estimates for the United States as a whole. Therefore, when policy decisions are restricted to a state or to a region, it may be necessary to obtain separate regional estimates of demand interrelationships. Another aspect to be kept in mind is that the process of synthesis adopted in obtaining the individual coefficients appearing in the interrelationship matrix is such that the estimates cannot be considered as precise. Also, it is not possible to obtain a measure of accuracy associated with many coefficients. However, these limitations may not reduce the usefulness of the results as they are intended to be only approximate relationships. The assumptions used in obtaining a static demand interrelationship as in table 4 could be modified to incorporate dynamic elements and these modified estimates could be used for projecting the demand interrelationships in a future period.

(3) The nonrejection of the hypothesis that farm retail spreads can be expressed as a linear function of retail prices opens a number of interesting aspects. Demand theory has often emphasized only retail markets and, therefore, most theories are based on retail prices and quantities consumed by the final consumers. The retail market is only one link in the pipeline joining producers and con-

sumers, and a theory of markets will be complete only if all the different links are considered. In particular, it would he convenient if the demand characteristics at one level of the market could be estimated from a knowledge of corresnonding characteristics at another level of the market. It was in this connection that the farm level elasticities were derived from retail level clasticities using the elasticity of price transmission. Since margin data were not available for all the commodities included in the present study, farm level elasticities were derived for only a few commodities. However, with margin data for all commodities, it is possible to obtain a complete demand interrelationship matrix at the farm level similar to table 4

Suggestions for further research

This study has drawn heavily from other demand studies and it is hoped to serve as a basis for further studies. Considering the large number of commodities included in the present analysis, it was possible only to analyze some broad characteristics of demand which are applicable to all commodities. However, individual commodities may often possess certain special characteristics of demand which cannot be brought into the framework of a general study of this nature. Limitations of data and other facilities restricted the scope of this study to certain aspects of demand analysis. Here are some of the factors omitted from the present study which offer great potential for further research. (1) While defining the quality elasticity. it was assumed that it represented the difference between expenditure elasticity and quantity elasticity. The implications of the assumption that quality factors account for the difference in these two kinds of elasticities are discussed in the text. Since the estimates of quality elasticity are derived estimates, the reliability of these estimates will depend upon the reliability of expenditure elasticity and quantity elasticity. Existence of omitted variables will affect both expenditure and quantity elasticity. For example, inclusion of household size in the regression equations has explained some of the negative quality elasticity. If data were available, it would be possible to identify other significant variables. Thus, it may be useful to study the effect of other variables influencing demand relationships on quality elasticity.

Apart from the problem of refining the estimates of quality elasticity from cross-section data, it may be important to study consumer behavior in terms of reactions to quality changes for individual products. Food processing firms and marketing organizations often face the problem of determining the characteristics of their final products. To make effective decisions on the ultimate quality of the product offered in the market. it is important to observe how consumers in different income and social classes react to products with different qualities. It is, therefore, necessary to handle each product separately. For a given commodity, different varieties (qualities) can be identified and specific studies can be undertaken to isolate the salient features influencing huver decisions. Most existing time-series data are not suited for this type of detailed analysis and, therefore, it is necessary to devise special surveys of buying habits and consumer reactions towards quality. Also, it is important to obtain proper measures of quality which can be quantified.

(2) The effects of income, household size, and region on quantities consumed were analyzed in detail. It was also pointed out that some other variables such as season, age distribution, and education also influence consumption. Although it may be difficult to obtain data on all these factors, some of them can be obtained. For example, the 1965 consumption survey obtained data for the four seasons and the complete set of data may be available in the next few years. These data will provide an excellent source of materials for analyzing the seasonal variations in demand and the interactions of seasons and regions on consumption behavior. Isolation of similar other factors will contribute towards better understanding of consumption behavior.

(3) Another area of theoretical and empirical relevance is the application of separability concepts in obtaining demand interrelationships. Our analysis combined cardinal separability and ordinal separability. The major problem in using ordinal separability assumption alone in estimating a simultaneous system of demand equations is that when the number of commodities is large, the resulting nonlinear system is difficult to solve. Also, it is important to obtain suitable criteria to group the commodities into separable groups. Thus, identification of proper separable groups and estimation criteria are two promising areas of applied statistical research. Comparison of results obtained from such different methods to determine their relative accuracy may be a related topic.

(4) Ample opportunities exist for research in the area of price spreads. Our analysis was based on one particular behavioral relationship between farm level prices and retail prices. It is possible to extend this analysis to include a number of other intermediaries specifying their behavioral characteristics. Also, it may be possible to try other forms of behavioral relationships and to compare these forms with the results obtained from this study. Possible generalizations from these behavioral relationships would be a valuable addition to the present understanding of behavior of different marketing groups and the mechanism of setting prices in the market.

APPENDIX A Source of Data

Cross-section data

In the present study, we have made extensive use of data from the household consumption surveys in 1955 and 1965. These two surveys were conducted in a systematic manner and they have many aspects in common.

The 1955 survey. (USDA, 1956) provides data on food consumption by all households during the spring of 1955. The objective of the survey was listed as "to obtain current information on patterns of food consumption, expenditures, dietary levels, and household food practices. The households were grouped (1) by region—Northcast, North Central, South, and West, . . . ; (2) by urbanization—rural farm, rural nonfarm, and urban within each region; and (3) by several family income classes within region-urbanization categories." A description of the survey, procedures for working with the data, and examples of use of the data in economic analysis are available in Burk and Lanahan (1958).

The sample included 6,060 households, selected from a housekeeping population of about 153 million civilians. (Out of a total of 162 million, 9 million people were excluded because they lived in a household not having at least one person who ate ten or more meals from the household during the survey week or because they lived in rooming houses, hotels, or institutions.) The 6,060 sample households were classified into two groups: the first, containing 4,605 households, was selected on a percentage-probability basis and served as the basic survey group; the second group of 1,455 farm households were taken as a supplementary sample to assure reliable data on farm-consumption patterns.

Data collection.—The survey was conducted by a private marketing research firm under the direction of statisticians and economists from the U. S. Department of Agriculture. Actual data collection was done in personal interviews by trained interviewers.

Period of observation.—Earlier studies had indicated that the spring season was the most representative period for the consumption of many food items. Therefore, the interviews were conducted in the April-June period and the data collected related to food consumption in the week preceding the interview.

Types of information.—The questionnaires used in the survey were designed to cover information about family membership and household composition, money income in 1954, use of individual food items at home in the seven days preceding the interview, and expenditures for meals and snacks away from home by members of the family. A number of reports have been published, using the basic data collected. Reports 1 to 5 contain information on income, household size, expenditures on food items, quantity consumed, and percentage of households consuming the particular item. These five reports correspond to five areas-the entire United States, and the Northeast, North Central, South,

and West; for each region, details are available according to urbanization and income classes, Reports 6 to 10 contain information on (a) less detailed tables on the quantities of foods used than contained in reports 1 to 5, (b) on nutritive value of foods used, and (e) distribution of persons into age and sex groupings. Report 11 provides data on home canning and freezing, Report 12 provides data on home production in 1954. and Report 13 is on home-baking practices. In the present study, we were mainly interested in the structure of the consumption of food commodities and, therefore, we have used the quantities of individual foods used from all sources. Since the present study has emphasized demand interrelationships and shifts in consumption patterns, we considered per-capita quantities of foods to be more appropriate to calculate income elasticities and other measures than expenditure data. However, we have used expenditure data when we were considering the quality aspects.

The 1965 survey was similar to that in 1955. As the report (USDA, 1968, p. 3) points out, "The chief difference between the 1965-66 nationwide survey and the earlier surveys is that the 1965-66 survey is the only one which covered all the four seasons of the year."

The sample for the 1965 survey consisted of 15,101 households of one or more members. As before, it was selected from all households excluding (a) about 5 per cent of the population who were not housekeeping; (b) about 1.5 per cent who were living in group quarters such as rooming houses, hospitals, and prisons; and (c) about 3 to 4 per cent of the population who lived in households in which no member ate at least ten meals from the home supplies. Half the sample (7,532) was collected in the spring of 1965 and the other half was distributed equally among the other seasons (summer and fall, 1965 and winter, 1966). "The sample design provided for a national self-weighting basic sample plus a supplementary farm sample which overweights the number of farm households in the approximate proportion of 5:1." (USDA, 1968, p. 204)

The households to be interviewed were selected in accordance with a multistage area sample design with added control by season. For the basic sample, 144 first-stage units of expected size of 10.000 households were selected at random. Within each first-stage unit, secondstage units of 30 expected housing units were selected at random. Each of the second-stage units was visited and a list of housing units was prepared. By systematic selection, housing units were chosen for interview in the spring in sufficient numbers to yield an average of three households per second-stage unit after allowing for vacancies and other omissions. The lists were updated in summer, fall, and winter, and a sufficient number of households were chosen to yield an average of one schedule per second-stage unit in each of these seasons. Selection of housing units from the second-stage units was independent for each season and no substitutes were provided for households unable or unwilling to participate in the survey.

The data collection was by means of personal interview with members of the household conducted by experienced interviewers who were specially trained for this survey. A detailed list of food items was used to help the respondents to recall the items consumed during the seven days preceding the interview.

Period of observation.—Interviews for collecting data were conducted in all regions during the period, April 3, 1965 to April 2, 1966. Since no substitutions were made in the samples, interviewers were instructed to call as many as three times if necessary to make the original contact in rural areas, four times in the urban areas, and six times in 281 secondstage sample units in 15 large cities where collection difficulties were anticipated.

Types of information.—As before, the data contained the kinds, quantities, and costs of food items used at home during the seven days preceding the interview. Expenditures for meals and snacks away from home paid by the family members were also outlined. In addition to family income, data were collected on age, education, and employment of the homemaker. Food consumption was measured at the level at which the foods came into the kitchen and, therefore, the data correspond to economic rather than physical consumption. Although the survey covered all the four seasons, at the time of the present study, only five reports relating to spring, 1965 were released. These five reports gave data on household size and consumption of different food items in terms of quantities and values for the United States and the four regions-Northeast, North Central, South, and West.

Comparison with the 1955 survey.— One of the objectives of the 1965 survey was to obtain comparable data with those obtained in the 1955 survey. Therefore, the survey methods had a number of similarities. Here, we shall point out some differences that might affect comparability (this is taken from Report 1 [USDA, 1968, pp. 202-04]).

Modification of schedule. (a) To facilitate machine computation, the design of the 1965 schedule was different from that of 1955.

(b) In 1955, a figure for income was derived from a set of questions asked by the interviewer. For the 1965 survey, a "global" figure for income was obtained by asking the respondent to estimate 1964 money income after first asking about specific sources of income.

(c) Separate information on donated food issued to low-income families was not obtained in 1955. In 1965, this was obtained separately.

(d) The 1955 questionnaire contained a section on home baking. This was not included in the 1965 questionnaire. On the other hand, the 1965 survey obtained data on the food intake of individuals a section which was not included in the 1955 survey.

Treatment of households of single individuals. The 1955 data by income were for households of two or more persons. In addition, data on one-person households were shown separately on each table. In 1965, the income classification included all households regardless of size.

Exclusion of money value of food used by boarders and help. In 1955, the money value of food used at home was adjusted to exclude the value of food used by boarders and farm help. In 1965, this adjustment was not made because the effect had been found to be slight.

Difference in the handling of homemade mixtures. Homemade mixtures on hand at the beginning of the seven-day period and used during the survey week in 1965 are included in prepared form whereas, in 1955, such mixtures were included as individual ingredients.

Change in grouping of food items. "Half and half" and "baby cereals" were treated differently in the two cross sections.

Time-series data

Length of time interval.—Published data on consumption and prices are generally on an annual basis. If demand conditions are fairly homogeneous during the year, it is enough to use annual

data to estimate the demand equations. If demand conditions vary widely within a year, it is necessary to use data with shorter intervals. Quarterly data on consumption and prices are available for a few commodities. The choice between annual and quarterly data depends upon the homogeneity in the demand relationship and the purpose for which the model is built. Hiemstra (1967, p. 9) points out that "use of annual data appears most useful for the immediate future, that is, for the next two or three years. Shortterm outlook up to and including one year ahead, probably should be based on quarterly data to account for near term variations such as the effects of stock changes." In the present study, we have used both quarterly and annual data to estimate demand equations and a choice of coefficients was made based on the properties of the estimates.

Years considered.-It is generally believed that, for most commodities, the consumption pattern before and after World War II has changed. If we have to handle data from different structures in one regression equation, special devices such as the inclusion of dummy variables have to be adopted. During the immediate period following the war years, enough time-series data were not available to use only the postwar years. Now enough data have been accumulated since the War to permit analysis of the postwar period alone and, therefore, we have used data starting from 1946.

Consumption data.—Often consumption of food items is expressed in terms of three different measures—(1) weight of food items consumed, (2) expenditure on different food items, and (3) nutritive value of food items expressed in terms of calorics, proteins, fats, and other vitamins and minerals. When we are interested in the demand for an individual

commodity, the most appropriate measure of demand would be the quantity of the commodity being used. However, when we deal with aggregates of individual commodities, it is difficult to aggregate different commodities if they are expressed in terms of physical units and, therefore, we have to convert them into comparable units. In this situation, it becomes convenient to measure demand in terms of expenditure or nutritive values. Also, when consumption is measured in terms of quantities, aggregation can be made using index measures of consumption of individual foods. While comparing the trend in the consumption of commodities, it is possible to obtain different directions of trend from measures of consumption in terms of quantities and expenditures on account of the influence of price movements. So long as the demand curve is downward sloping, a decrease in the price will cause an increase in quantity consumed, resulting in its upward trend, Whether or not the trend in expenditure also shows the same direction depends upon the elasticity of the commodity. Using the elasticity theorems (Baumol. 1965, p. 179), "if a demand curve has elasticity less than unity (it is inelastic). a rise in price will increase consumer expenditure and vice versa." Also, "if the curve has an elasticity greater than unity (it is elastic), a fall in price will increase consumer expenditure and vice versa." In the present analysis, our choice of the quantities measured in terms of physical units as the measure of demand was based on the following considerations: (1) in most cases, we were interested in the demand for a single commodity and, as such, aggregation problems were not important; (2) for many policy decisions regarding supply adjustments in agriculture, we are interested in the nature of changes

in quantities demanded rather than reallocation of family food budget according to the changes in prices of different commodities; (3) demand theory specifies quantity consumed as a function of prices and other variables; and (4) since the expenditure on a commodity is the product of its price and quantity consumed, inclusion of both expenditure and prices in the same equation may create some statistical problems of estimation.

Quantity data is available at different levels of the marketing system. Quantity produced and quantity consumed domestically are available in separate tabulations. In our study, we were only interested in domestic consumption and, therefore, we have used data corresponding to domestic food consumption alone. Most of the per-capita consumption figures used in this study are taken from Hiemstra (1968).

Trends in commodity consumption.---Trends in per-capita food consumption is available in Hiemstra (1968, pp. 7-15) and only a brief discussion is given here, Consumption of beef and poultry have increased considerably during the postwar period while pork and yeal consumption have declined. Lamb consumption has remained fairly stable. Per-capita consumption of eggs and total dairy products have declined; those of processed fruits and vegetables have increased at the expense of fresh fruits and vegetables. Consumption of total fats and oils have remained fairly stable and the consumption of total cereal products has dropped. Increases in consumption of instant coffee has offset the decline in the consumption of regular coffee. These trends are shown in figures A-1 to A-14, Figure A-15 gives trends in actual percapita food expenditures (undeflated) and expenditures expressed as a percentage of personal disposable income.

Appendix figures A-1 to A-14 illustrate 1946–1968 prices for selected commodities, and their per-capita consumption with projection to 1980.

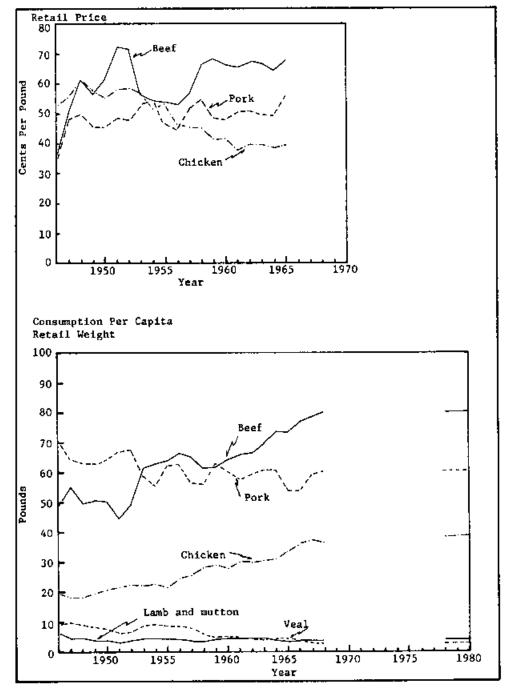


Fig. A-1. Meat and chicken.

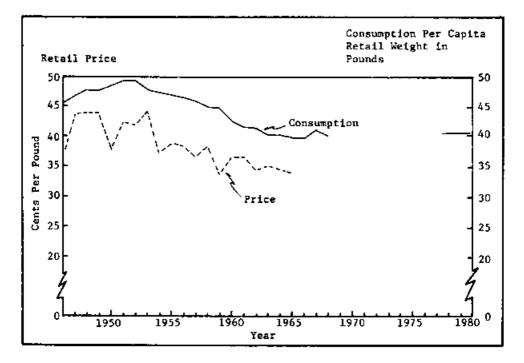


Fig. A-2. Eggs.

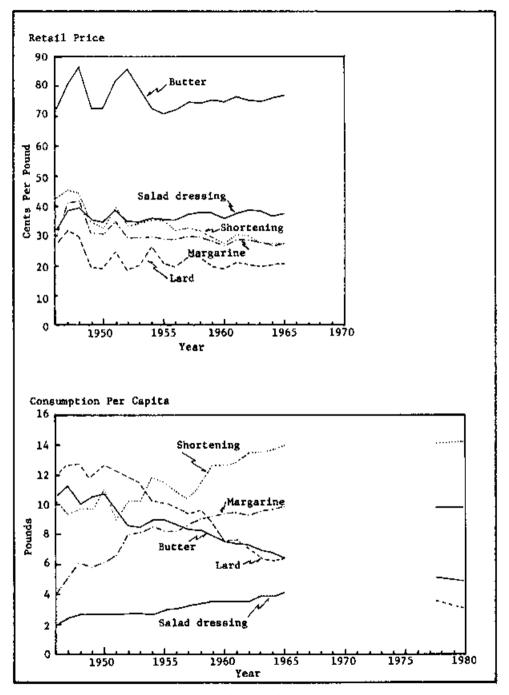


Fig. A-3. Fats and oils.

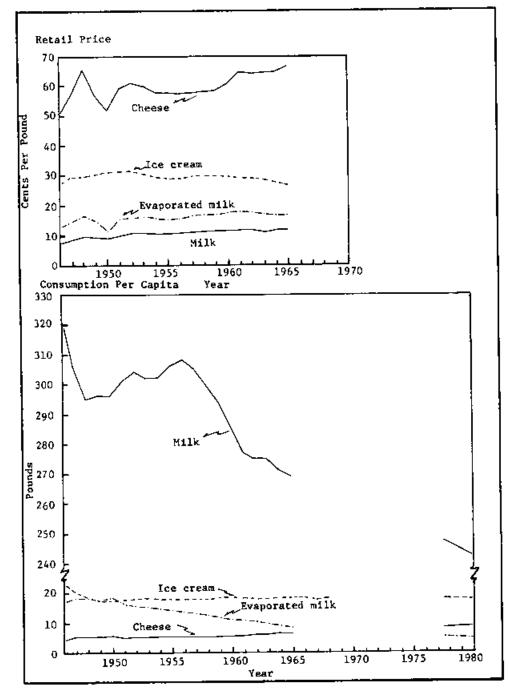


Fig. A-4. Dairy products, excluding butter.

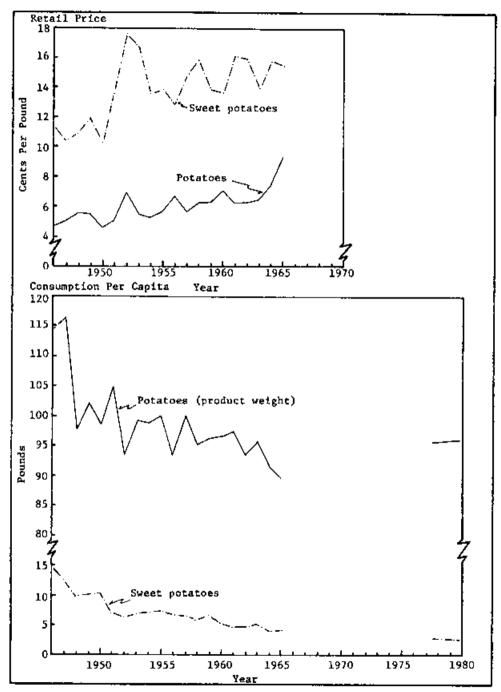


Fig. A-5. Potatoes.

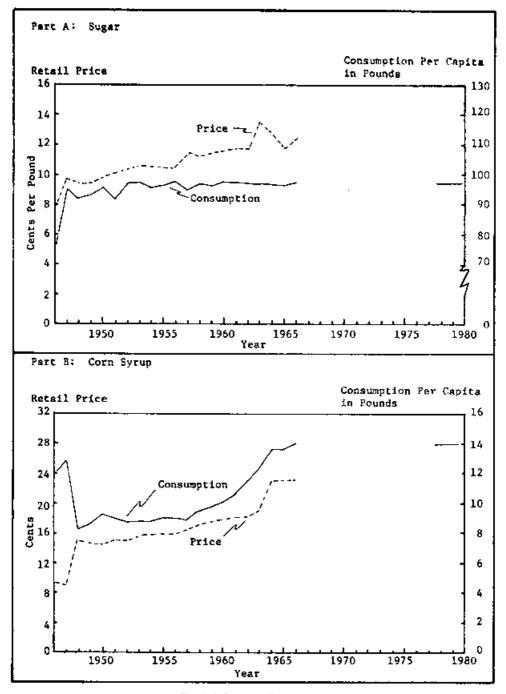


Fig. A-6. Sugar and corn syrup.

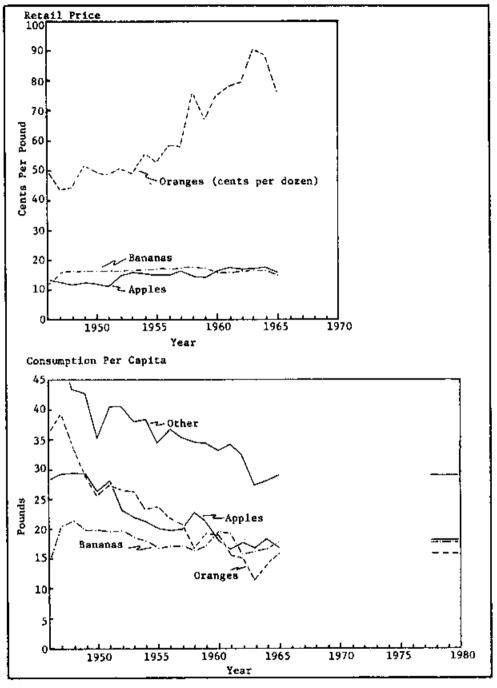


Fig. A-7. Fresh fruit.

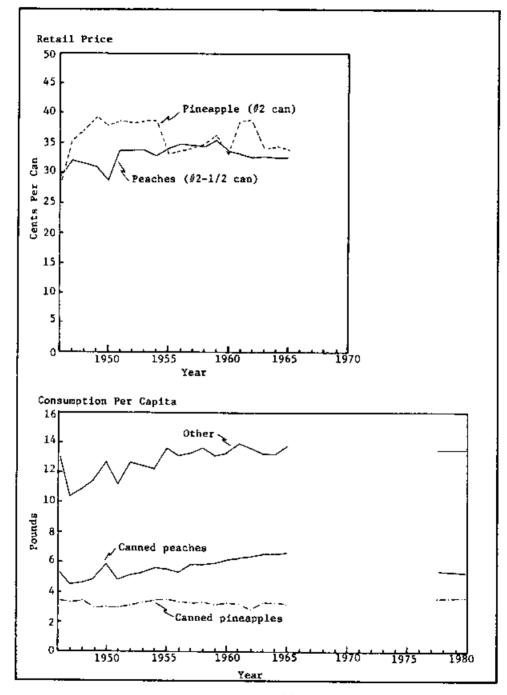


Fig. A-8. Canned fruit.

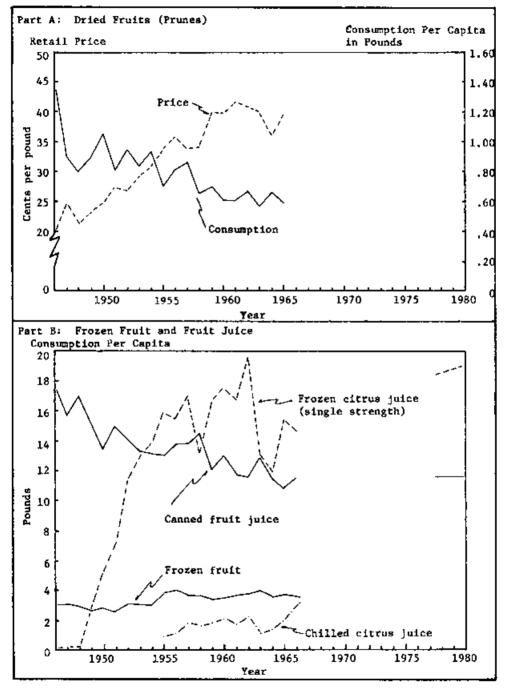


Fig. A-9, Dried fruit (prunes), frozen fruit, and fruit juices.

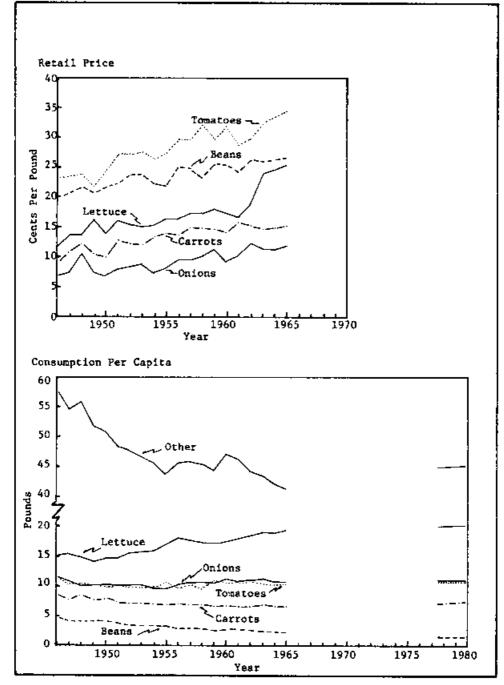


Fig. A-10. Fresh vegetables.

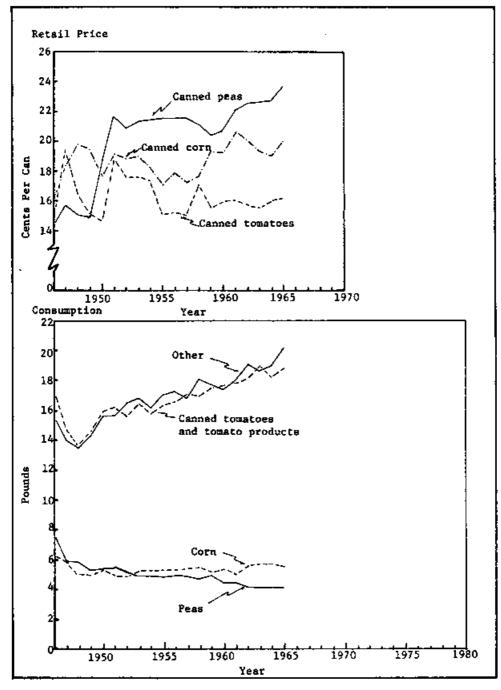


Fig. A-11. Canned vegetables.

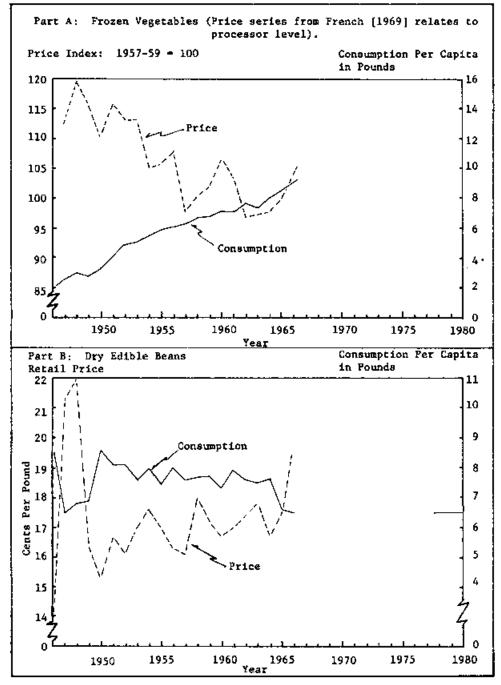


Fig. A-12. Frozen vegetables and dry edible beans.

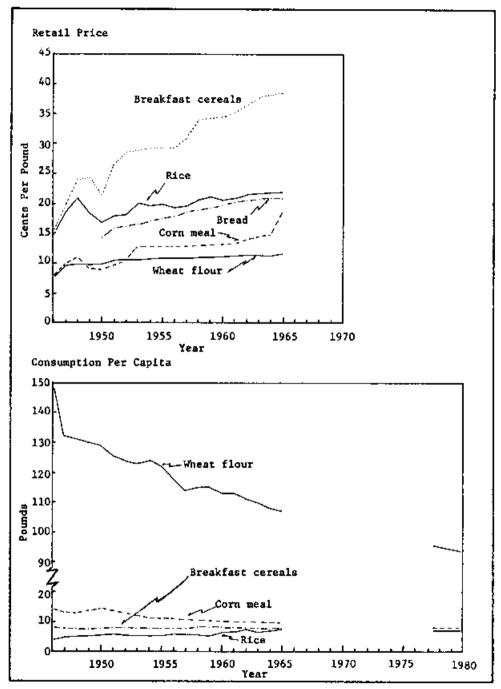


Fig. A-13. Selected cereal and bakery products.

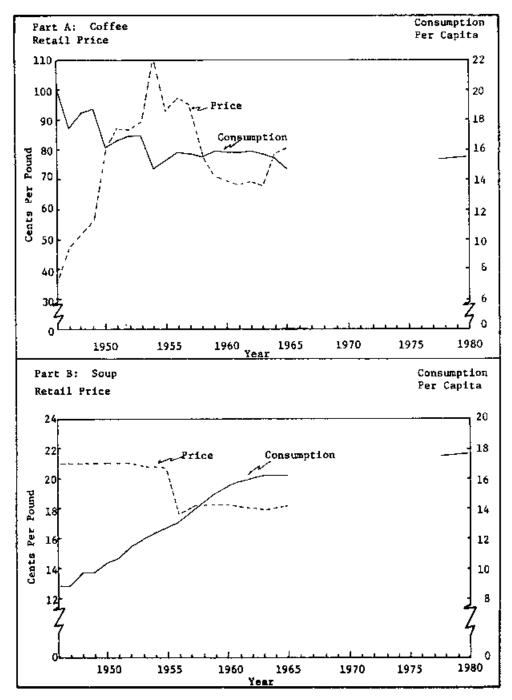


Fig. A-14. Coffee and soup.

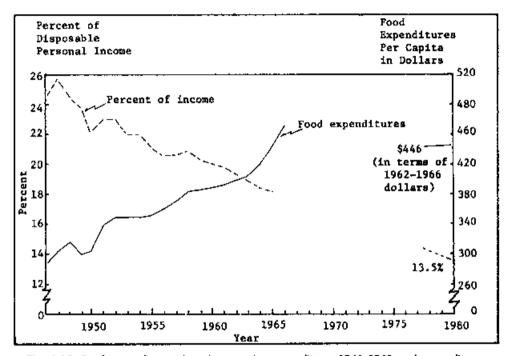


Fig. A-15. Food expenditures: Actual per-capita expenditures 1946–1968 and expenditures as percentage of personal disposable income. (Source: U. S. Department of Commerce as reported by Hiemstra, 1968, p. 181.)

Prices.—We have used retail prices (annual and quarterly) for obtaining the demand relationships, and prices at the farm level (annual and quarterly) for obtaining the relationship between retail prices and farm level prices. Annual data on retail prices were derived from various reports of the U. S. Bureau of Labor Statistics (1963), and annual data on farm level prices from the USDA report on farm-retail spreads (USDA, 1965). Quarterly data on both retail prices and farm-level prices were derived from various issues of marketing and transportation situation (USDA, 1955).

Trends in retail prices. -In general, prices of most commodities have increased. However, there was substantial reduction in the price of poultry. Also, prices of ice cream and bananas have declined. Prices of coffee, margarine, and eggs remained fairly stable. The highest increase of retail prices was experienced by fresh fruits and vegetables. The trends in prices for major commodities are shown in figures A-1 to A-14. These prices are in actual rather than deflated values.

Defiation of prices.—Time-series data on prices represent the actual prices in each year. The price level in a given year is influenced by supply and demand factors along with changes in general price levels. Different approaches have been suggested to remove the effects of inflation and defiation in the economy from the prices reported:

(1) A general approach to remove the effect of changes in price level is to deflate the observed data using the consumer price index. (For problems associated with deflation, see Foote (1958) and Shepherd (1963, pp. 121-31).

(2) A second approach is to include the general price level as a separate variable in the regression equation. Kuh and Meyer (1955) suggest different criteria

to determine whether the data should be deflated or the deflator should be included as a separate variable in the analysis.

(3) Waugh (1964, p. 11) suggests that when the analysis concerns only two variables (the quantity consumed and some kind of deflated prices), "it may often be convenient to deflate by dividing prices by consumer income."

As Shepherd (1963) points out, no standard technique of deflation is applicable to all problems. Considering the merits of all the above three approaches, while using time-series data, we have followed the practice of deflating prices and income by the consumer price index.

Price-quantity relationships are static in nature since we have assumed that the various coefficients remain the same over the different years. Stochastic elements in the coefficients and other dynamic factors can be incorporated only with a number of estimation problems and the large number of commodities included in our analysis prevented us from introducing any dynamic considerations. We could only isolate the shown effects of linear trends.

Marketing margins

For the purpose of this study, we have defined marketing margin as the difference between the prices paid by consumers and the prices received by the producers. Thus, the data correspond to aggregate price spreads in the sense producers. Thus, the data correspond to aggregate price spreads in the sense that they include processing charges, handling charges, and profits earned by different marketing agencies.

A statistical note on grouped-data regressions

Consider a general linear model in which the dependent variable y is a func-

tion of k predetermined variables X_i and an error term u. There are n observations. In matrix notation, the model is expressed as:

$$Y = X\beta + u. \tag{164}$$

The assumptions required for estimation are the well-known conditions, Ω , that:

E(u) = 0 $E(uu') = \sigma^2 I_n$ (165) X is a set of fixed numbers X has rank k < n.

The estimate of β is given by $\hat{\beta}$ =

 $(X'X)^{-1}X'y.$

In the case of two variables, the regression equation can be written as

$$y_t = \alpha + \beta X_t + U_t \tag{166}$$

and the estimate of β is given by

$$\hat{\beta} = \frac{\sum_{i=1}^{n} (X_i - \bar{X})(y_i - \bar{y})}{\sum_{i=1}^{n} (X_i - \bar{X})^2}$$
(167)

Often, in cross-section analysis, the size of the sample is large, and it is difficult to calculate the sum of squares and sum of cross products of the deviations in (167) for all observations. Also, most of the published data give the averages of a number of observations after grouping the observations according to certain characteristics. Therefore, it is important to examine whether the grouping of the observations introduces any bias in the estimates.

Grouped data.²⁸—Now assume that the n observations are grouped into k

groups with n_1, n_2, \dots, n_k observations in each group $(n_1 + n_2 + \dots + n_k = n)$. Also, let X_{ij} and y_{ij} be defined as

 $X_{ij} = i^{\text{th}}$ observation of X belonging to j^{th} group and $y_{ij} = i^{\text{th}}$ observation of y belonging to j^{th} group.

The group averages of X and y are given by

$$\bar{X}_{j} = \frac{\sum_{i=1}^{n_{i}} X_{ij}}{\prod_{i \neq j}}$$

$$(j = 1, 2, \dots, k). \quad (168)$$

$$\bar{y}_{j} = \frac{\sum_{i=1}^{n_{j}} y_{ij}}{n_{j}}$$

When a regression equation of the type (166) is specified for the group means as variables, we have

$$\bar{y}_i = \alpha + \beta \bar{X}_i + V_j. \tag{169}$$

If (166) satisfies the Ω assumptions given in (165), V_i will equal

$$E(V_i) = 0 \text{ and}$$

$$V(V_j) = \frac{\sigma^2}{n_j}$$
(170)

Using the least-square estimation procedure, from (169) an estimate of β can be obtained as

$$b = \frac{\sum_{j=1}^{k} (\bar{X}_{j} - \bar{\bar{X}}_{j})(\bar{y}_{j} - \bar{\bar{y}}_{j})}{\sum_{j=1}^{k} (\bar{X}_{j} - \bar{\bar{X}}_{j})^{2}} \qquad (171)$$

^{*} This section is partly based on Malinvaud (1966, pp. 242-46).

where

$$ar{ ilde{X}}_j = rac{1}{k} \sum_j ar{X}_j$$
 and
 $ar{ ilde{y}}_j = rac{1}{\kappa} \sum ar{y}_j.$

The expected value of b will be the same as β and, hence, b is an unbiased linear estimator of β . However, the variance of the estimates will be different in both cases (i.e., using original data and grouped data). The extent that grouping causes loss of precision will depend upon the variability within groups. It is possible to group the observations in such a manner that the loss in precision is brought to a minimum. For example, the loss in precision is zero when all the y values within a given group are the same. However, this may be difficult to achieve in practice and, therefore, the next best thing is to obtain groups such that values of y within a group are close together. If the sample is designed to have the same number of observations in each group, the observation of y can be arranged in an ascending or descending order and then make the first (n/k)observations to fall in the first group, the next (n/k) observations to fall in the second group, \cdots , and the last (n/k)observations to fall in the last (k^{th}) group. If it is not necessary to have an equal number of observations in each group, and if the total number of desired groups is given, it is possible to form class intervals of u and to obtain a frequency distribution of observations belonging to each group to derive at group averages.

From (170), it can be seen that we have introduced heteroskedasticity as a consequence of grouping the data. Though the original data were assumed to have homoskedasticity, grouping has induced heteroskedasticity. To estimate the parameters under such induced heteroskedasticity, it is possible to use Aitken's generalized least-squares method. Since the variances are changed by a multiple of the number of observations in each group, this procedure reduces to a weighted regression (Draper and Smith, 1966, pp. 77-81).

Weighted regression.—In the use of Aitken's generalized least squares, the estimates of $\hat{\beta}$ from a model $Y = X\beta +$ U where E(U) = 0 and $E(UU^{\dagger}) = \sigma^{2}\Sigma$ is given by

$$\hat{\beta} = (X'\Sigma^{-1}X)^{-1}X'\Sigma^{-1}Y.$$

In the case of grouped data, using (170)

Therefore,

Since Σ^{-1} is known, the estimates can be obtained as

$$\hat{\beta} = (X'\Sigma^{-1}X)^{-1}X'\Sigma^{-1}Y,$$

In particular, if there are only two variables having a relationship of the type (166), the estimate of β is given by

$$\hat{\beta} = \left[\frac{\sum_{j} n_{j}(\bar{X}_{j} - \overline{X}_{j})(\bar{y}_{j} - \overline{y}_{j})}{\sum_{j} n_{j}(\bar{X}_{j} - \overline{X}_{j})^{2}}\right] (173)$$

which is of the same form as (171) except

that each term inside the sum is weighted according to the number of observations from which the group average was formed.

The tables A-1 to A-6 on the pages following present certain statistical results of interest.

Statistical Tables

TABLE A-1

COMPARISON OF REGRESSION COEFFICIENTS OBTAINED FROM TWO SPECIFICATIONS WHEN QUANTITY IS THE DEPENDENT VARIABLE

.	$\log q = a + b \log y$			$\log q = a' + b' \log y + c' \log s$				
Commodity	4	ъ	R ²	a'	۶.	c'	R [±]	
leef	656 (~7.04)	.270 (9.10)	.90	626 (-6,09)	.225 (3.45)	,219 (.78)	.91	
eal	(-1.04) -8.103 (-14.29)	(9,10) .551 (7,96)	. 86	(-0.09) -2.959 (-14.47)	(3,43) .326 (2,52)	1.066 (1.96)	. 92	
ork	273	(7.86) .008 (.41)	. 02	311 (-3.18)	(0.52)	(1,60) 277 (-1.70)	. 28	
amb and mutton	(-4.46) -3.210 (-11.94)	(591 (6.80)	. 84	-3.18) -3.412 (14.17)	.894 (5,85)	-J. 468 (-2.24)	. 90	
hicken	(~13.94) .009 (18)	(9.60) 034 (-2.19)	.35	009 (17)	(3, 33) 007 (-, 21)	132 (90)	.43	
`ieh	247 (-1.64)	(-1.24)	.15	(-342) (-2,32)	,082	687 (1.73)	.38	
urkey	-3.613 (-7,93)	,788	.74	~3.805 (~6.92)	.757 (2,17)	,006 (.04)	.74	
kga	027 (48)	072 (-4.01)	.04	- 026 (41)	073	.003	. 64	
utler	1,776 (\$.33)	.269 (3.96)	.64	-1.779 (-7.29)	.273 (1.76)	,018 (,03)	. 64	
ard	2.824 (4.65)	-1,297 (→6,70)	.83	2.949 (4 31)	-1.488 (-3.42)	,912 (.49)	. 84	
hortening	-1.068 (-3.71)	.029 (.31)	.01	871 (-3.29)	298 (-1.77)	1.581 (2,20)	.38	
fargarize	598 (-6.67)	008 (21)	.01	- 578 (-3,75)	044 (70)	. 186 (.69)	.05	
alad dressing	-1.709 (-18,27)	.284 (8.47)	. 69	-1.601 (-25.05)	. 122 (3.01)	.781 (4.50)	.97	
rosh milk	780 (-9.55)	.367 (13,96)	, 96	— ,723 (—9.36)	.281 (5.74)	.418 (1,99)	97	
vaporated milk.	1.166 (3.16)	- .610 (-5.77)	. 70	1.207 (3.21)	673 (-2.82)	.308 (.30)	.79	
heese	-1.183 (-9.04)	. 227 (5.44)	,76	-1.227 (-8.57)	.294 (3.23)	— . 326 (— . 83)	.79	
08 Gream	-1.498 (-23.15)	.323 (15.65)	. 96	-1.496 (-20.23)	,320 (6.62)	.012 (.06)	. 96	
otatoes	.104 (1.19)	.016 (.69)	.04	.103 (1.96)	072 (+1.36)	.427 (1.89)	.34	
weet potatoes,	.074 (.18)	,504 (3.82)	.82	.207 (.45)	704 (-2,43)	,964 (.78)	.65	
ugar	.385 (3 17)	109 (-4,37)	. 65	. 156 (3.78)	276 (-3.59)	.518 (1.57)	.76	
ora syrup	. 834 (2.15)		. 78	.734 (1,70)	556 (-2.02)	728 (62)	.79	
pples	827 (~8.79)	.142 (4.73)	.71	845 (-7,95)	.169 (2,51)	131 (45)	.72	
raogea	-1.092 (-6.71)	, 227 (4.34)	.68	-1.022 (-5.84)	.122 (1.09)	. 508 (1.07)	.72	
ADADAS	793 (-9.04)	.136 (4.85)	. 72	798 (-7,97)	,144 (2.26)	039 (14) .127		
anned peaches	— .911 (—8,59)	.012 (.35)	.01	893 (-7.44)	(19)	(.39)	.03	

Sanned pineapples	-2.724	.408	.67	-2.876	.636	-1,103	.75
	(-9.05)	(4.24)		(-9,15)	(3 19)	(-1,20)	
Dry fruits	-1.424	031	.01	-1.659	.366	-1.923	. 63
	(-4.69)	(32)		(-7.01)	(2.39)	(-2.91)	
rozen fruita	3.883	.624	. 62	-3, 597	.195	2 079	. 9
	(-12, 50)	(6,31)		(-15.63)	(1.33)	(8.82)	
resh tomatoes	-1.004	. 161	.67	-1.078	.273	543	.7
	(-8,49)	(4.27)		(-9.36)	(3,74)	(174)	
rcah beans	652	481	.91	.589	- 386	- 464	.9
	(4,19)	- (9,70)		(3,51)	(-3, 63)	(-1,02)	
nions	734	.005	.063	- 750	.028	115	α
	(-7, 53)	(,15)		(-6.79)	(.41)	(~ .38)	
arrota.	-1.826	.313	.88	-1.809	288	.124	.8
	(-13,89)	(7,48)		(-12 (1))	(3 03)	(.31)	
ettuce	-1.772	.424	91	-1.798	. 454	195	.9
	(-13.05)	(0.50)	ļ +.	(-11,75)	(4,78)	(47)	
apped poss	-1.047	.043	.09	-1.005	020	.306	. J.
	(7,30)	(.94)		(-6.32)	(20)	(.70)	· ·
anned corn	997	.654	.07	624	- 205	1,256	.5
	(-4.73)	(.80)		(-4.65)	(-1.53)	(2,61)	
anned tomatoes.	-1.396	.165	.83	-1.369	.124	. 197	.8
stined tomatoes.	(-17.84)	(6.60)	.00	(-15, 97)	(2.28)	(.84)	
ry vegetables	1.560	818	.77	1,690	864	224	.7
ALA ACTERIAL TEA	(3,35)	(-5,51)		(2,99)	(-2,56)	(.15)	
rozen vegetables.	-2.601	.577	.91	-2,639	.684	- 276	.9
tosen vegetanies.	(-13.36)	(9,29)	.81	(-12,01)	(4,54)	(46)	
heat flour	1.641	631	.87	J.641	631	.003	8
mart nogr	(8.44)	(-7.76)	-04	(5.63)	(-3.41)	(.00)	.0
liœ	.999	605	.80	1.028	648	209	.8
	(3,14)	(-5,96)	.00	(2.83)	(-2.81)	(20)	.0
reakiast cereals.	661	.058	.48	704	.119	309	.6
HERRINGC OFFERING	(-)0,88)	(2,87)	.90	(-12,82)	(3,32)	(-2.01)	
orn meal	2,521	-1.059	.87	2.453	~ .958	488	. 6
orn meal			.04	(5,08)	(-3.13)	(37)	. 0
offee	(5.92)	(-7.81)	.35	862	.144	- 466	7
onee	798	.047	.30	(-17.80)	(4,66)		6
	(11.76)	(2.19)	-			(-3 54)	7
oup	-1.287 (-9.36)	.216 (4.93)	.73	(-1.208) (-8.72)	,098 (1.11)	(1.52)	6

TABLE A-1-Continued

TABLE A-2 COMPARISON OF REGRESSION COEFFICIENTS OBTAINED FROM TWO SPECIFICATIONS WHEN EXPENDITURE IS THE DEPENDENT VARIABLE

	ોલાદ્ર ઽ = ઘ + βોલાદ્ર પ્ર			$\log x = a' + \beta \log y + r' \log s$				
Commodity		β	Rī	at	β ¹	 r'	Rı	
cef	-1,153	.380	.01	••1.152	.379	.009	91	
	(-9.07)	(9.39)		(-7.93)	(4.11)	(.02)		
eal	→3 .615	. 698	.90	-3.502	, 529	,816	.91	
	(-14,76)	(\$ 94)		(-13.52)	(3.22)	(1 16)		
ork	568	081. (20.7)	. 93	559	.116	.066	.87	
amb and mutton	(-10.66) -3.256	(7-63) .576	.79	(-9.27) 3.505	(3-03) .950	(.40) 1.813	88	
ano ano mutton	(-10,51)	(5.83)	. (9	(-13.27)	(5.67)	(-253)	,00	
hicken.	.710	.056	.47	754	.123	- 322 .	.65	
	(-11,32)	(2,82)		(-12.96)	(3.33)	(-2.04)		
iah	-1.108	. 140	.46	-1.188	. 261	587	. 65	
.	(-8.96)	(2.75)		(-7 20)	(2 49)	(-1 31)		
urkey	-4.424	. 669	. 85	-4 476	.947	379	85	
	(-11,62)	(7.16) ↔ .016	.12	((3.45) - ,002	(.15	
ggs	.543 (12,11)	(-1,1)	مدر.	(-10.93)	(05)	(- 49)		
utter.	-1,934	.274	. 63	-1.948	.294	099	. 63	
	(-8.81)	(3.91)		(-7,77)	(1 \$5)	(15)		
ard	1.953	-1.236	.78	2 007	1.317	.390	.78	
	(2, 85)	(-5.65)		(2.57)	(-2.65)	(.18)		
hortening	-1.443		. 02	-1.245	- 338	1,444	40	
	(-5.46)	(47)	47	(5.27) 1.326	(-2.25) .052	(2.25)	.41	
argarine	-1,325 (-20,55)	.051 (2,48)	14.	(-17.98)	(1,10)	(01)	. 47	
slad dressing	-2.529	. 401	.95	-2 451	2.85	.562	.92	
	(-27, 62)	(13,73)		(32.77)	(6.00)	(2.77)		
resh milk	- 1 351	.349	.96	-1.313	.293	.271	.97	
	(- 17,78)	(14.42)		(-16,55)	(5.63)	(1.26)		
vaporated milk	. 486	640	.81	.511	677	.181	.81	
	(1.50)	(-6.20)		(1.36)	(-2.69)	(18)	. 81	
heese	1.498 (11.41)	. 241	. 79	-1.547 (-10.85)	.315 (3.48)	359 (98)		
e onean i .	-1 956	(5,75) .335	.91	(-10.85) -1.947	.321	,066	.9	
Ac careacan ,	(17.80)	(9,56)		(-15.53)	(4.04)	(.19)		
otatoes	941	036	. 18	907	015	.246	.2	
	(-11.86)	(1.42)		(-10.69)	(28)	(1,07)		
weet potatoes	-1.325	293	.23	-1.288	350	.273	.24	
	(-2.36)	(-1.65)		(-2.02)	(~ .87)	(.16)	-	
ugar	- 512	178	.72		- 274	.473	78	
orn syrup	(4.42) 281	(-4.82) 569	,79	(3,60) 380	(-3.68) 420	(1.45)	, .B4	
orn syrup	(.90)	(-5.74)		(-1.1)	(-1,93)	(78)		
pples	-1.841	.207	.85	-1 908	.308	490	.90	
	(-20.03)	(7 07)		(-22.87)	(5.83)	(-2,16)		
ranges .	-1883	,192	. 51	1.884	.194	009	.5	
	(9.63)	(3.03)		(-8 43)	(1.37)	(02)		
adanas	-1.679	.140	,70	-1.703	.177	(.7	
anned peaches	(-17.40) -1.607	(4.56) .009	.003	(15,78) -1,680	(2 58)	(60) 631	13	
anned perches	(-9.26)	(.16)		(-9.03)	(0.0)	(-1,05)		
anned pineapples;	-3.482	.475	, 78	-3.686	,782	-1.485	.6	
	(-13, 22)	(5.66)	-	(-15,96)	(5 34)	(+2.37)		
bry fruits	1.809	037	.02	-2.059	. 889	-1.821	.5	
	(0.16)	(40)		(-8.67)	(2.25)	(-2.82)		
resh tomatoes	-1,947	.278	.83	-1.984	.333 (3.53)	278 (66)	8.	
resh beans	(-14.55) 098	(6 52) — .431	j , 66	(-13.32)	308	(66)	l s	
Iosa Denns .	(5 9)	(-8,13)		(75)	(-3.12)	(61)	ľ	
nions	1.681	.022	,04	-1.688	. 032	- 047	.0	
	(-15.50)	(.64)		(-13.62)	(.40)	(~ .14)		
arrots	-2.519	.268	. 88	-2.5t5	.261	.034	.8	
	(-23.98)	(8.01)		(-20.96)	(8.43)	(.10)		
ettuce	-2.207	.348	.85	-2.274	. 450	494	.8	
an and many	(14,46) 1,012	(7.15)	24	(-14,02)	(4.38)	(-1.12)	.3	
anned peas	-1.942	190 . 190 (2018)	.32	-1.910 (~10.21)	.062 (52)	(.45)	i	
	(11.72)	(2,08)	l				بد ا	
anned corn	-1,742	. 065	.10	-1.594	157	1.077	.43	

Canned tomatoes.	-2,015	. 151	. 75	-2.035	. 181	144	.78
	(-21.93)	(5.17)		(-19,69)	(2.76)	(51)	
Dry vegetables	.322	641	.77	. 258	544	468	.77
	(. 87)	(5.4L) j		(.61)	(-2.04)	(41)	
Frozen vegetables	~3.191	.619	.90	-3,288	.766	710	.92
	(15.06)	(9,17)		(-14.69)	(5.40)	(-1.17)	
Wheat flour	. 601	611	. 88	.804	615	021	.88
	(2.53)	(-8.07)		(2.22)	(-3.57)	(.03)	
Rice	538	319	. 81	- 585	247	348	. 82
	(-3,30)	(-6.13)		(-3.24)	(-2,15)	(71)	
Breakfast coreais.	-1.489	. 195	.87	-1.523	,246	250	. 88
	(-18,70)	(7 68)		(-17, 92)	(4.57)	(-1.08)	
Corn mesl	1,399	-1.013	.87	1.398	-1,012	007	.87
	(8.43)	(-7.60)		(3.50)	(-3.43)	(01)	
Coffee	— .701 I	.011	. 04	765	. 106	460	.78
	(-11.64)	(.59)		(22.42)	(4.92)	(-4,98)	
Soup	1.933	.228	. 77	-1.870	.132	.464	. 81
	(-15.04)	(5.57)		(~13.96)	(1.56)	(1.28)	-
All food	,132	. 277	.88	.111.	. 309	- 163	. 88
	(3.68)	(3.43)		(.91)	(4,01)	(46)	

TABLE A-2-Continued

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TABLE A-3

COMPARISON OF WEEKLY PER-CAPITA CONSUMPTION IN 1955 AND 1965 (QUANTITY)

				Income G	roup				
Commodity	<3009			3000 — 4989			>5000		
	1955	1965	Change	1955	1965	Change	1955	1965	Change
	pounds		per cent	pounds		per cent	pounda		per cen
Beef	. 84.93	1.1501	35.42	1.2115	1,4879	18,69	1,4469	1.8301	26.46
Vesl	. 0383	.0220	-42.56	.0758	.0413	-45.51	. 0995	.0576	-12.1
		1.0925	- 1.23	1.0918	1.1157	2.28	1.0728		
Pork	1.1061							1.0775	0.4
amb and mutton.	.0360	,0297	-21.84	.0678	.0365	-47.64	. 1313	.0605	-53.9
hicken	. 5011	.8232	36.95	.5878	.8256	45,40	,6471	.7754	21.7
Sish	.3564	4053	13.09	.3125	.3369	7.81	.2029	.3659	20.8
[u7key	.0225	0175	-22.22	.0519	.0488	- 5.97	. 1059	. 0589	-44.3
Jggs	6026	. 6023	05	5835	. 5805	57	. 6971	. 5348	-10,4
Butter	. 1819	.0895	-60,80	.1662	.0901	-45.79	.2462	. 1445	-41.3
Lard	3252	.2200	-82.35	.1024	.1198	16.99	.0425	.0284	33 . 1
Shortening	. 1244	. 0952	-23.47	.1480	.1284	-13.88	.1275	.0970	-23 2
fargarine	.1762	.2436	38.25	.2075	.2570	23.86	. 1813	.2364	30.3
alad dressing	.1205	,1(03	8.48	.1596	. 1521	- 4.70	.1648	.1758	6.5
resh milk	2.5164	1.6963	-36.56	3.0426	2,2042	27, 56	3,0995	2,6832	- 6.9
Svap. milk	. \$534	.3375	- 4,50	.3112	. 2721	-12.56	.1686	.1209	-28.2
Theese	2278	.2720	19.40	.2911	.2776	- 4.64	. \$873	.3967	2.4
ce cream	2057	2403	16.26	.3244	. 2953	- 8,97	3766	.3904	3.6
otatoes.	1.6885	1.3647	-19.18	1.7768	J. 5651	-11.90	1.5476	1.4225	- 8.0
weet potatoes	.0509	.0529	3,93	0479	0444	- 7.31	.0399	.0232	-41.8
lugar	9509	6294	-12.78	8032	.8363	4.12	,6870	6425	- 0.4
otn syrup	.0873	.0930	6.53	.0532	.0592	11.28	.0259	0270	- 6.5
oples	. 3695	.3685	2.50	.3697	3736	1.11	4311	4541	6 3
ranges	. 5085	.3277	-35.56	6968	.3734	-16.41	.6394	4627	-42.49
ananas	.3143	3749	19.28	,4495	.4193	- 6,72	.4638	4600	8
lanned peaches	.0725	1290	77.03	.1117	1359	21.66	.1400	.1357	- 3.0
anned pineapples	. 0392	0261	-33.42	0586	. 0251	-57.17	.0765	.0479	-37.39
Dry fruit	. 0265	.0201	31,70	.0160	.0266	60.25	.0325	.0303	-6.7
rozen fruit	.0107	.0063	-41.12	.0293	.0200	-59.73	.0445	.0167	-62.4
resh tomatoea	.3026	.2795	- 7.90	.3298	2667	-18.53	.3532	.3547	- 7.6
	.3020	.2190	-10.81	.1513	.1567	1.56	.1204	.1071	-11.0
resh beans	. 2082		- 1,14	. 2167	.2009	-7.29	.2147	.1885	-12,20
nions		.1910	-11.55			-27.52	.2147	.1679	-12, 20 -25, 30
arrots	, 1195	.1057		. 1955	.1417				
eltuce	.2189	.2311	- 7.16	.3338	.3085	~ 7.58	.4350	.4673	7.2
anned peas	.1158	1139	- 1.64	.1367	,127D	- 6.42	. 1256	. 1259	.2
anned corn	,1111	. 1308	17.73	. 1410	.1832	29.92	.1219	. 1488	21.9
anned tomstoes.	. 1054	. 1103	1.65	.1184	.1314	10.98	.1255	.1435	14.8
bry vogetables	2005	. 2383	18.65	. 1237	1888	36.30	.1091	.0581	-46.7
rozen vegetablea	.0497	.0919	84.91	.1277	. 1328	3.99	.2248	.2282	1.5
Wheat flour	1.5064	.9168	-39.17	.6463	. 5986	~ 7.38	.3925	.3186	-18.83
tice	.1568	. 2413	53,89	.0705	. 1731	146.63	.0530	.0900	69.8
reakfast cereals	, 2287	,3090	35.11	.2474	.3118	25.94	.2303	.8391	47.2
orn meal	.6669	. 5171	-22.46	. 1609	2574	59,98	, 9532	.0840	57,89
Coffee	2047	,2160	6.50	.2261	.2127	- 5.93	. 2499	. 2314	- 7.40
oup	1911.	.1930	62.05	.2247	.2479	10.32	. 2510	.2753	9.68
ood ernenditures	0.3138	7.5013	18.81	8,1940	8,9042	8,67	10,9527	11,6965	8,62

TABLE A-4 REGIONAL CONSUMPTION INDEX (U. S. AVERAGE = 100).

Commodity		Рет-сн	pita consum	Consumption index					
	R	Rt	R;	R.	U , S,	R	R	Rı	R.
Beef	1.6310	1.8626	1.8106	1.4298	1.6504	98,52	112,85	109.70	86,63
Vcal	.0975	0255	.0364	0304	. D486	200.51	52.46	79.01	62.55
Pork	9847	9552	1.1745	1.1768	1.0942	\$9.99	87.29	107.33	107.5
Lamb and mutton	1097	0990	. 0236	.0213	.0547	200,54	180 98	43.14	38.90
Chicken	8045	. 7603	,7307	. \$559	, 7963	101.08	95.47	91.76	109.13
Turkey	.0584	. 0607	.0443	.0274	. 0516	171.31	117.63	85.85	53.10
Fish	.3810	.3162	.2810	.4634	. 3677	103.61	85.99	76.42	126 00
Eggs	4878	. 5814	. 5502	6097	, 5592	\$7.23	103.96	98.39	109.00
Butter	.1737	. 1118	.1627	. 0640	. 1276	136.12	87.61	254.21	50,13
Lard	.6396	0287	.0503	.1524	.0790	50.12	36-32	32,93	192 91
Shortening .	.0518	0830	.0976	.1585	, 1033	50.14	80.34	94.48	153.43
Margarine	.2012	2683	.2366	.2652	. 2431	82.76	110.36	97.32	109.00
Salad dressing	.1403	1757	.1479	.1829	. 1610	\$7.0B	109.13	91.86	113 60
Fresh milk	2.7347	2,6421	2,4911	2,2621	2,7051	101.09	97 07	92.08	83.62
Evap, milk	.1646	. 1948	0887	.2957	1884	\$7.35	103.39	47 08	156 93
Cheese	3628	4376	.4053	.2591	.3525	102,92	124,14	114,97	73 50
loc cream	3628	3258	3786	3140	.3466	104.70	91.02	109.26	90.62
Potatoes	1.4755	1.2044	1.6506	1.3048	1.4316	103.07	84.12	115.81	91-14
Sweet potstoes	.0274	. 0223	.0236	.0518	0334	\$2.03	66,76	70.65	155 08
Sugar.	6036	5910	, 6804	8689	7082	85 23	83.45	96.07	122.69
Corn syrup	0152	.0319	0268	.0884	.0455	33.40	70.10	58.46	191 28
Freah apples	4329	4568	.4704	3506	4194	103.21	108 91	112 16	83.59
Oranges	5000	5207	.4644	.3170	.434G	115 04	119.81	106.85	72,94
Запапаз	4359	4281	.4644	.4298	. 4407	98.91	97.14	105,37	97.52
Canned peaches	1097	1505	1536	.1250	1337	82.04	117.05	115.03	93 49
Canned pinesppics.	0335	0511	.0443	0304	0395	84.81	129.36	112.15	76.96
Dry fruit	.0243	.0479	0295	.0243	.0303	80.19	158.08	97.35	60,19
Frozen fruit	0121	0159	.0177	.0121	0151	80,13	105 29	117.21	80.13
Fresh tomatoes	3109	3226	.2781	.3963	.3313	93.84	97.37	83.94	119.61
Fresh beans	0701	0511	1094	. 2560	.1398	50.14	36.55	78.25	163, 11
Oniona	2225	1853	.1715	. 1920	.1914	116.24	96 SL	89.60	100.31
Carrota	1615	2236	1604	,1097	.1560	102.21	141.51	114.17	69.43
Lettuce	4055	5207	.4171	.3079	.3951	103.39	131.78	105.56	77,92
Canned peas	1250	1080	1213	.1341	1246	100.32	87.15	97.35	107.62
Canned corn.	1341	1597	1804	1341	,1519	85.25	105.13	118.76	88.28
Canned tomatoes	1890	.1533	1065	.1067	.1337	141.36	114.65	79.65	79,80
Dry vegetables	.0518	.0926	.0828	1920	1124	46.08	\$2.38	73.66	170 8
Frozen vegetables	2378	2364	1536	1585	. [864	126.22	125.47	81.63	84.12
Wheat flour	.2164	3865	.4142	.7560	4711	45.93	82.04	87.92	60,47
Rice	1524	.1150	.0502	.2042	1837	113.98	86.01	37 54	152.72
Breakfast cereal	3201	.3769	3550	2743	,3221	99,37	117.01	110.21	85.1
Corn meal.	.0335	0607	,0532	4786	.1854	18.06	32.74	28,69	258.14
Coffee	2285	.2236	2455	2073	2249	101,64	89.42	109.15	92.13
Soup	3079	2971	.2869	1798	.2583	119.20	115.02	111.07	69,60
Total food exp.		11.4345	10.3668	9.5518	10.6413	112,65	107.45	97 42	89.76

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Table A-5 REGIONAL INDICES OF PRICES PAID (U. S. AVERAGE = 100)

		Aven	age prices	paid	Index of prices paid				
Commodity	R,	R2	R.	R ₄	U. S.	R,	R1	R	8.
	. 8430	.7189	.6912	.6844	.7292	115 60	98.31	94 78	93.85
/ea	1.0000	.7500	.8462	. 8000	.9375	108.68	93.75	90.26	65.33
ork	7276	6655	.6448	. 5933	.0472	112,42	102.82	99,62	91.87
amb and mutton.	8611	7419	.8750	. 8571	.8333	103 33	89.03	105.00	102.65
hicken	.4129	3666	3684	3404	.3740	121.29	103.36	98.50	91.01
Furkey.		5760	4606	.5556	.5294	39.11	109 18	88 13	104 94
		7070	.6000	.5132	. 6033	115.38	117.18	99.45	65.06
Гіяћ Сден	5375	4396	4247	4550	.4619	116.30	95.17	91.94	98.50
Castler	7368	1.0000	6909	7143	7142	103,16	140,01	96,73	100,01
Sutter	2308	.2222	.1765	2000	1923	120 02	115.54	91.78	104.00
Shortenitur.	2941	2692	.2727	2692	.2847	111.10	101.70	103.02	101.70
Margarine		2857	2875	2759	2875	105,35	99,37	100.00	95,96
Salad dressing	3696	.3818	3800	.3333	3584	103 12	106.52	106.02	92.99
resh milk		2382	2518	2520	2348	114.66	101.44	107.24	107.32
Svan milk.	.1667	1803	.1667	1753	1612	103.41	111.84	103 41	108.74
Cheese.	.0050	.5109	4891	5647	5344	113.21	95,69	91.52	105.66
ce cream	4454	3725	3672	3495	3859	115.41	96.52	95,15	90.56
Potatoes.	0992	1034	1022	1098	1040	95,38	99.42	98.20	105 57
	.2222	.2857	2500	.1765	1818	122.22	157.15	137.51	97.00
Sweet potatoes.	1312	.1189	1174	.1155	1206	100.91	99.00	97.75	96 41
	.1300	2000	. 2222	.1724	2000	100.00	100.00	110.10	86.2
Corn syrup	.1549	.1748	1509	1475	1594	97.17	109.55	94.65	92.7
Fresh apples	.1260	.1411	1274	.1058	1258	101.74	112.16		84.1
Dranges.	1469	1493	1274	1277	1379	106.62	105.26	92.35	92.6
Запалаа.	2222	2245	.1923	.1951	2045	105,55	109.77	94.03	
Canned peaches	2727	.3125	.1023	.3000	3076	86.65	101.59		97.5
Cauned pineapples					.4000	93.75	101.59		93.7
Dry fruita	.3750	.4000	.4000	.3750		125.00	100.00	125.00	125.0
Frozen fruite	.5000	.4000	5000	,5000	.4000				
Fresh tomatoes	.3039	,2970	.2765	. 2807	.2830	107.38	104.94	97.70	81.5
Fresh beans	2609	.2500	.2703	.1309	2391	109.11	104.55	113.04	54.7
Опіопв.,	.1233	.1207	1379	.1269	1260	97,16	05,11	108,66	100.0
Carrota	1509	,1429	. 1639	.2232	.1538	98,11	92.11	106.58	144.4
Lettupa Canned peas	2164	. 1963	.2199	.2673	2076	104.23	94.55	105.92	128.7
Canned peas	.2195	.2353	1951	.2045	.2195	100.00	107.19	88,88	
Canned corn	2045	. 2200	. 1803	. 2500	. 2200	92.95	100.00	81.95	113.6
Canned tomatoes.	.2258	. 2063	.2222	.2571	.2045	110.41	81.01	108.65	125 7.
Dry vegetables		.2414	.1786	. 1111	.1891	124.43	127.65	91.44	5 8.7
Prozen vegetables		0270	.0576	.0384	.0322	79.50	83.85	178.86	119.2
Wheat flour		. 1074	.1000	.1088	,1032	109.20	104.06	96.89	105.4
Rice		. 3056	,2353	. 1791	.2045	107.57	149.43	115.06	87.5
Breakfast cereal		. 4322	.4083	.4000	.4150	107.85	104.14	96.38	96.3
Corn meal		.1579	.1111	.0955	. 0983	92.47	160.63	113,02	97.1
Coffee	1.0267	. 9143	,9036	.9705	. 9594	167,01	95.29	94.18	101.1
Boup	2475	.2473	1546	.2542	.2470	100.20	100.12	62,59	102.9

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TABLE A-6										
LINEAR EFFECT	OF	TIME ON	CONSUMPTION							

Commodity	Constant*	d \$	Signifi- cancet	Constant + 2	Antilog.	Change
						per cent
Beef	.0!2741 (1.5709)	12	NS	2.012741	102,90	+2.90
Veal	- 021436	12	NS	1.978564	95.18	-4.82
Pork	(-1.4888) 000755	12	NS	1,090245	99.82	-0.02
Lamb and mutton	(0747) 003587	12	NS	1.996413	99.17	-0.83
Chicken	(2062) .004106	12	NS	2,004108	100.90	0.90
Bags	(.7213) 	11	s•	1.974981	84.40	-5.60
Butter (Model 1)	(2.3354) 013227	14	NS	1.986773	96.78	-3.22
Butter (Model 2)	(-1 5598) 021589	12	s٠	1.978411	98, 15	-4.85
(with oils)	(-2.5228) 022715	15	S.	1.977285	94.91	5.09
Shortening	(-2.7515) 000650	12	NS	1,999341	99.85	-0.15
Margarine	(0381) .015690	12	NS	2.015690	103,70	3.70
Balad dreaming	(1.2696) .013932	12	NS .	2,013932	103,20	
tilt.	(1.7766)					3,20
	006169 (14	NS	1.993891	98.56	-1.42
Sveporated milk	016339 (-3 3554)	14	8*	1.98366L	96.31	-3.69
2heens	.017222 (1.8207)	12	S	2,017222	104.20	4.20
oe cream	012465 (2.5840)	12	6*	1.987535	97.26	-2.74
Potatoes	003074 (14	NS	1.996926	99.29	-0.71
weet potstoes	028986 (-2.6893)	14	s.	1.971014	93. 54	-0.40
iugar	.007765 (.9795)	12	NS !	2.007765	101.80	1,80
Огл вутир	009261	12	NS	1.990739	97,88	-2.12
	(6469) 004455	12	NS	1.995848	98.98	1.02
Sananas	(→ .6005) .008464	12	NS	2,008464	102.00	2.00
)ranges	(.953) —.013339	12	NS	1.986661	96.9S	-3.02
Canned peaches	(-1.0410) 011277	12	s	1.988773	97.45 I	2.55
Canned pineapples	(-1.6170) 003676	12	NS	L, 996324	99,16	0.84
Dry fruits	(4670) 039020	12	s	1.960980	91.40	-8.60
attuce	(-1,0752) ,004750	9	215	2.004750	101,10	1.10
omatoes	(1.1108) 	9	NS	I,993079	98.41	-1.59
icans	(-1.3422) 025564	9		1.974436	94.20	
nions	(-2.6969) .000165	9	. N9	2.000165	100.00	5.72 0
arrola	(.0310) 011666	9	s	1.988334	-	
anned peas.	(-1.9236)	9	s•		97.58	-2.42
	021774 (-3.6389)	-		J.978226	95.10	
anned corn	004901 (8200)	ş	NS	1.995099	98.68	-1,12
ry vegetables	006079 (9	NS	1,994301	98.70	-1.30
Vbeat flour	006452 (2, 8859)	13	8•	L.995548	98.75	-1.25

		1	1	1	1	1
lice	.005452 (.3866)	13	NS	2,005452	1.01 .30	1.30
reakfast cereals.	000466	13	NS	1.999534	\$9.89	-0.11
orn meal	(2121) 008138	13	s	1.991862	96, 14	-1.86
offee	(-2.0977) 009409	12	8	1, 990591	97.88	+2,14
oup	(-1.8676) .011282	12	8*	2.011282	102.70	2.70
ا , , i		12	s.	2.011282	102.70	

TABLE A6-Continued

* Figures in the parentheses correspond to 't' values. 1 NS = non-significant, S = significant at 10 per cent level, $S^* = \text{significant}$ at 5 per cent level.

APPENDIX B

Mathematical Proofs

Here, we shall introduce a proof for some of the results presented in this monograph. We shall first derive the conditions on demand functions in the classical theory, followed by the modifications introduced by Frisch and by Barten.

Classical model

Conditions for a maximum.—The first order conditions for a maximum for the n commodity case are given by

$$U_j - \lambda p_j = 0$$

(j = 1, ..., n)
$$y - q_j p_j = 0$$
 (174)

where

 U_j is the marginal utility of commodity j, p and q are vectors of commodity prices and quantities, y is consumer income, and λ is the marginal utility of income.

The second order conditions for a constrained maximum are that the Hessian matrix bordered with prices has principal minors alternating in sign starting with negative (that is, the bordered matrix is negative definite). The Hessian matrix is designated as A with typical elements $U_{ii} = \partial^2 U / \partial q_i \partial q_i$. This is a symmetric matrix.

Effect of changes in prices and income.-The goal of demand analysis is to determine the effect on quantities consumed of changes in prices and income. Small departures from equilibrium may be evaluated by differentiating the first order conditions given in (174). The total differential is given in matrix form as follows:

$$\begin{bmatrix} A & | -p \\ -p' & | 0 \\ -p' & | 0 \end{bmatrix} \begin{bmatrix} Q_p & | q_p \\ -p' & | \lambda_p & | \lambda_p \end{bmatrix} = \begin{bmatrix} \lambda I & | 0 \\ -p' & | -1 \end{bmatrix}$$
(175)

where

 Q_p is a matrix of price slopes where a typical element is $\partial q_i / \partial p_i$, q_y is a vector

of income slopes such as $\partial q/\partial y$, and I is an identity matrix. A typical element in the A matrix is $U_{ij} = \partial^2 U/\partial q_i \partial q_j$.

This system is solved for price and income slopes by obtaining the inverse of the bordered A matrix or

$$\begin{bmatrix} Q_{p} & | & q_{p} \\ | & | & | \\ \ddots & - & - & - & - \\ \lambda_{p} & | & \lambda_{p} \end{bmatrix} = \begin{bmatrix} A & | & -p \\ - & -p' & | & 0 \end{bmatrix}^{-1} \begin{bmatrix} \lambda I & | & 0 \\ | & | & | \\ - & - & - & - & - \\ q' & | & -1 \end{bmatrix}$$
(176)
$$\begin{bmatrix} Q_{p} & | & q_{p} \\ \lambda_{p} & | & \lambda_{p} \end{bmatrix} = \begin{bmatrix} B & | & b \\ b' & | & b^{0} \end{bmatrix} \begin{bmatrix} \lambda I & | & 0 \\ q' & | & -1 \end{bmatrix}$$
(177)

where the inverted bordered A matrix is designated as a bordered B matrix.

We may evaluate an income change from (176) for a typical element as

$$\frac{\partial q_i}{\partial y} = -b_i. \tag{178}$$

Similarly, for a price change, we have

$$\frac{\partial q_i}{\partial p_j} = B_{ij}\lambda + b_i q_j. \tag{179}$$

Substituting (178) in (179), we have the Slutsky equation in which the first term is the substitution effect and the second is the income effect or

$$\frac{\partial q_i}{\partial p_j} = B_{ij}\lambda - q_j \frac{\partial q_i}{\partial y}.$$
(180)

The symmetry of the substitution effect may be proven as follows. The bordered A matrix is symmetric or

$$A_{ij} = A_{ji}. \tag{181}$$

Any element in the bordered B matrix, obtained by inverting the bordered A matrix, also is symmetric or

$$\lambda B_{ij} = \lambda \beta_{ji} \text{ or } \tag{182}$$

$$K_{ij} = K_{ji} \tag{183}$$

where

$$K_{ij} = \frac{\partial q_i}{\partial p_i} + q_j \frac{\partial q_i}{\partial y}$$
 or (184)

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$$\frac{\partial q_i}{\partial p_j} + q_j \frac{\partial q_i}{\partial y} = \frac{\partial q_j}{\partial p_i} + q_j \frac{\partial q_j}{\partial y}.$$
(185)

Converting (185) into elasticities, the relation between any two cross-price elasticities is given by

$$e_{ij} = e_{ji} \frac{W_j}{W_i} + w_j (e_{jy} - e_{iy}).$$
(186)

The own substitution effect always is negative as can be seen directly. The marginal utility of income, λ_i is always positive. Consider the term, $K_{ii} = B_{ii}\lambda$. The value of B_{ii} is obtained by dividing the cofactor of the bordered Hessian matrix (A_{rr}) by the determinant D. The sign of cofactor A_{rr} must be opposite to that of D since D is of order n + 1 and the cofactor is of order n.

The Engel aggregation may be seen from the condition that the inverse of a matrix multiplied by a matrix equals an identity matrix or $A^{-1}A = I$ or

$$\begin{bmatrix} B & | & b \\ B & | & b \\ | & | & | \\ - & - & - & - & - \\ b' & | & 0 \end{bmatrix} \begin{bmatrix} A & | & -p \\ | & | & | \\ - & - & - & - & - \\ -p' & | & 0 \end{bmatrix} = \begin{bmatrix} I & | & 0 \\ I & | & 0 \\ | & | & - & - & - \\ 0 & | & I \end{bmatrix}$$
(187)

Engel aggregation states the price-weighted sum of income slopes equals one or

$$b'(-p) = 1$$
 or
 $\Sigma p_i \frac{\partial q_i}{\partial y} = 1$

where

b' is the vector of income slopes.

The Cournot aggregation states that the price-weighted sum of a given column of price slopes equals the negative of the budget proportion or

$$B(-p) = 0 \quad \text{or}$$

$$\Sigma \ p_i K_{ij} = 0$$
(188)

where

the elements of the B matrix are compensated price slopes.

Using the Slutsky condition (184)

$$K_{ij} = \frac{\partial q_i}{\partial p_j} + q_j \frac{\partial q_j}{\partial y}, \qquad (189)$$

we may express equation (188) as

$$\Sigma p_i \frac{\partial q_i}{\partial p_j} + \Sigma p_i \frac{\partial q_i}{\partial y} \cdot q_j = 0.$$
 (190)

The second term is the Engel aggregation or

$$\Sigma p_i \frac{\partial q_i}{\partial y} = 1.$$

so we rewrite (190) as

$$\Sigma p_i \frac{\partial q_i}{\partial p_j} = -q_j. \tag{191}$$

Frisch model

Frisch starts with the first order conditions of utility maximization specified in equations (174).

$$U_{i}(q_{1}, q_{2}, \cdots, q_{n}) - \lambda p_{j} = 0 \qquad (j = 1, 2, \cdots, n)$$
(192)
$$U_{i} = \frac{\partial U}{\partial q_{i}} \qquad \text{and}$$

$$y = p_1 q_1 - \cdots - p_n q_n = 0. \tag{193}$$

The demand functions can be represented as

$$q_i = q_i(p_1, p_2, \cdots, p_n, y).$$
 (194)

As before, the demand elasticities w.r.t. price (e_{ij}) and income elasticities (e_{ij}) are defined as

$$e_{ij} = \frac{\partial q_i}{\partial p_j} \cdot \frac{p_j}{q_i} \quad \text{and} \quad (195)$$

$$e_{iy} = \frac{\partial q_i}{\partial y} \cdot \frac{y}{q_i} \quad (i, j = 1, 2, \dots, n).$$

The proportion of expenditure on the i^{th} commodity is denoted by

$$w_i = \frac{p_i q_i}{y}.$$
 (196)

The marginal utility of money, λ , is defined as the common ratio

$$\lambda = \frac{U_1}{P_1} = \frac{U_2}{P_2} = \cdots = \frac{U_n}{p_n}.$$
 (197)

where

Since utility, by definition, is a function of quantities consumed, we have

$$U_{i} = U_{i}(q_{1}, q_{2}, \cdots, q_{n}), \qquad (198)$$

and the inverse function can be written as

$$q_i = q_i(U_1, U_2, \cdots, U_n)$$
 $(i = 1, 2, \cdots, n).$ (199)

Now Frisch defines utility accelerators, want elasticities, and money flexibility as

$$F_{ij} = \frac{\partial U_i(a_1 \cdots a_n)}{\partial q_j} \cdot \frac{q_j}{U_i} \quad \text{(utility accelerator)}, \quad (200)$$

$$\sigma_{ij} = \frac{\partial q_i (U_1 \cdots U_n)}{\partial U_j} \cdot \frac{U_j}{q_i} \quad \text{(want elasticity), and} \quad (201)$$

$$\phi = \frac{\partial \lambda}{\partial y} \cdot \frac{y}{\lambda} \qquad \text{(money flexibility)}, \tag{202}$$

From (175), we have

$$\begin{bmatrix} A & -p \end{bmatrix} \begin{bmatrix} Q_p & y \\ \lambda_p & \lambda_y \end{bmatrix} = \begin{bmatrix} \lambda I & 0 \end{bmatrix}, \quad (203)$$

or

$$\begin{bmatrix} U_{11} \cdot \cdot \cdot U_{1n} - p_1 \\ \cdot \\ \cdot \\ U_{1n} \cdot \cdot \cdot U_{nn} - p_n \end{bmatrix} \begin{pmatrix} \frac{\partial q_1}{\partial p_1} \cdot \cdot \cdot \frac{\partial q_1}{\partial p_n} \frac{\partial q_1}{\partial y} \\ \frac{\partial q_n}{\partial p_1} \cdot \cdot \frac{\partial q_n}{\partial p_n} \frac{\partial q_n}{\partial y} \\ \frac{\partial \lambda}{\partial p_1} \cdot \cdot \frac{\partial \lambda}{\partial p_n} \frac{\partial \lambda}{\partial y} \end{bmatrix} = \begin{bmatrix} \lambda & 0 & 0 & 0 & 0 \\ 0 & \lambda & 0 & \cdot & 0 \\ \cdot & \cdot & \cdot \\ 0 & \cdot & \cdot & 0 \\ 0 & \cdot & \lambda & 0 \end{bmatrix}.$$
(204)

Writing the first equation in full,

$$U_{11}\frac{\partial q_1}{\partial p_1} + \cdots + U_{1n}\frac{\partial q_n}{\partial p_1} - p_1\frac{\partial y}{\partial p_1} = \lambda$$

 \mathbf{or}

$$\frac{\partial U_1}{\partial q_1} \cdot \frac{\partial q_1}{\partial p_1} + \dots + \frac{\partial U_1}{\partial q_n} \cdot \frac{\partial q_n}{\partial p_1} = p_1 \frac{\partial \lambda}{\partial p_1} + \lambda, \text{ or}$$

$$\frac{\partial U_1}{\partial q_1} \cdot \frac{q_1}{U_1} \cdot \frac{U_1}{q_1} \cdot \frac{\partial q_1}{\partial p_1} + \dots + \frac{\partial U_1}{\partial q_n} \cdot \frac{q_n}{U_1} \cdot \frac{U_1}{q_n} \cdot \frac{\partial q_n}{\partial p_1} = p_1 \frac{\partial \lambda}{\partial p_1} + \lambda$$
(205)

ı.

Using (195), (197), and (200), (205) can be expressed in terms of price elasticities and utility accelerators as

$$F_{11}e_{11} + \dots + F_{in}e_{in} = 1 + \lambda. \tag{206}$$

Similarly, expressing all the other equations in (204) in terms of price elasticities, income elasticities, and utility accelerators, (204) can be rewritten as

$$\begin{bmatrix} F_{11} \cdots F_{in} \\ \vdots \\ F_{n1} \cdots F_{nn} \end{bmatrix} \begin{bmatrix} e_{11} \cdots e_{1n}e_{1y} \\ e_{n1} \cdots e_{nn}e_{ny} \end{bmatrix} = \begin{bmatrix} 1 + \lambda_1 \quad \lambda_2 \quad \cdots \quad \lambda_n \quad \phi \\ \lambda_1 \quad 1 + \lambda_2 \quad \cdots \quad \lambda_n \quad \phi \\ \lambda_1 \quad \cdots \quad \cdots \quad 1 + \lambda_n \quad \phi \end{bmatrix}$$
(207)

where

$$\lambda_i = \frac{\partial \lambda}{\partial p_i} \frac{p_i}{\lambda}$$

From (207)

Now Frisch shows that

$$[F_{ij}]_{nm} x [\sigma_{ij}]_{nm} = I$$

therefore

$$[\sigma_{ij}]_{nxn} = [F_{ij}]_{nxn}^{-1}$$
(209)

From (208) and (209)

$$\begin{bmatrix} e_{11} \cdot \cdot \cdot e_{1n}e_{1y} \\ \cdot \\ \cdot \\ e_{n1} \cdot \cdot e_{nn}e_{ny} \end{bmatrix} = \begin{bmatrix} \sigma_{11} \cdot \cdot \cdot \sigma_{1n} \\ \cdot \\ \cdot \\ \sigma_{n1} \cdot \cdot \sigma_{nn} \end{bmatrix} \begin{bmatrix} 1 + \lambda_1 \quad \lambda_2 \quad \cdot \cdot \lambda_n \quad \phi \\ \lambda_1 \quad 1 + \lambda_2 \cdot \cdot \cdot \lambda_n \quad \phi \\ \lambda_1 \quad \lambda_2 \quad \cdot \cdot 1 + \lambda_n \phi \end{bmatrix}$$

Therefore,

$$e_{iy} = \phi \sum_{j} \sigma_{ij}$$
 and (210)

$$e_{ij} = \lambda_j \Sigma_j \sigma_{ij} + \sigma_{ij}, \qquad (211)$$

Further, Frisch shows that

$$w_i\sigma_{ij} = w_j\sigma_{ji}$$

Summing over j

$$w_{i} \sum_{j} \sigma_{ij} = \sum_{j} w_{j} \sigma_{ji} \text{ or}$$

$$\sum_{j} \sigma_{ij} = \frac{1}{w_{i}} \sum_{j} w_{j} \sigma_{ji}.$$
(212)

From (210) and (212),

$$e_{iy} = \frac{\phi}{w_i} \sum_j w_j \sigma_{ji} \text{ and}$$

$$w_j e_{iy} = \phi \sum_j w_j \sigma_{ji}.$$
(213)

Summing (213) over i,

$$\sum_{i} w_{i} e_{iy} = \phi \sum_{i} \sum_{j} w_{j} \sigma_{ji}.$$
(214)

Using the Engel aggregation,

$$\sum_{i} w_{i} e_{iy} = 1.$$

therefore, (214) can be written as

$$\varphi = \frac{1}{\sum_{i} \sum_{j} w_{j} \sigma_{ji}} = \frac{1}{\sum_{i} (w_{i} \sum_{j} \sigma_{ij})}.$$
 (215)

From (211) and (212), we have

$$e_{ij} = \frac{\lambda_j}{w_i} \sum_j w_j \sigma_{ji} + \frac{w_j}{w_i} \sigma_{ji}.$$

From the Cournot aggregation, we have

$$\sum_{i} w_{i}e_{ij} = -w_{j}. \tag{216}$$

From (211) and (216),

$$\sum_{i} w_{i}(\lambda_{j} \sum_{j} \sigma_{ij} + \sigma_{ij}) = -w_{j} \text{ and}$$

$$\lambda_{j} \sum_{i} (w_{i} \sum_{j} \sigma_{ij}) + \sum_{i} \sigma_{ij}w_{i} = -w_{j}.$$
(217)

From (215) and (217),

$$\lambda_{j} \frac{1}{\phi} + \sum_{i} w_{i} \sigma_{ij} = -w_{j} \text{ and}$$

$$\lambda_{j} = -(w_{j} + \sum_{i} w_{i} \sigma_{ij})\phi.$$
(218)

Frisch also shows that

$$e_{iy} = \phi \sum_{j} \sigma_{ij}$$

$$= \phi \frac{1}{w_{i}} \sum_{j} w_{j}\sigma_{ji} \quad [\text{using (212)}]$$

$$w_{i}e_{iy} = \phi \sum_{j} w_{j}\sigma_{ji}.$$
(219)

Interchanging i and j,

$$w_i e_{iy} = \phi \sum_i w_i \sigma_{ij}.$$
 (220)

From (218) and (220),

$$\lambda_{i} = -w_{i}\phi - w_{i}e_{i\nu} \text{ and}$$

= $-w_{i}(\phi + e_{i\nu}).$ (221)

Using (211) and (218)

$$e_{ij} = -(w_j + \sum_i w_i \sigma_{ij}) \phi \sum_j \sigma_{ij} + \sigma_{ij}$$

= $\sigma_{ij} - w_j \phi \sum_j \sigma_{ij} - \phi \sum_i w_i \sigma_{ij} \sum_j \sigma_{ij}$, and
= $\sigma_{ij} - w_j e_{iy} - w_j e_{jy} \frac{e_{iy}}{\phi}$ [from (219) and (220)].

Therefore,

$$e_{ij} = \sigma_{ij} - w_j e_{ij} \left(1 + \frac{e_{jj}}{\phi} \right). \tag{222}$$

In particular, when i = j,

$$e_{ii} = \sigma_{ii} - w_i e_{iv} \left(1 + \frac{e_{iv}}{\phi} \right) . \qquad (223)$$

A good *i* is defined as want independent of good *j* if $U_{ij} = 0$. Since σ_{ij} is the $(ij)^{\text{th}}$ element of the inverse of matrix (U_{ij}) , it follows that $\sigma_{ij} = 0$ for want independent commodities. Therefore, (222) can be written as

$$e_{ij} = -w_j e_{ij} \left(1 + \frac{e_{ij}}{\phi} \right) . \tag{224}$$

Also, if a good i is want independent of all other goods,

$$\sigma_{ii} = \frac{e_{iy}}{\phi}$$

and, therefore, from (223),

$$e_{ii} = \frac{e_{iy}}{\phi} - w_i e_{iy} - w_i e_{iy} \frac{e_{iy}}{\phi},$$

$$e_{ii} = -e_{iy} \left(w_i - \frac{1 - w_i e_{iy}}{\phi} \right).$$
(225)

Solving for ϕ , from (225),

$$\phi = \frac{e_{iy}(1 - w_i e_{iy})}{e_{ii} + w_i e_{iy}}.$$
(226)

Having obtained a value of ϕ from (226), (224) can be used to obtain any cross elasticity e_{ij} without making any assumption beyond $\sigma_{ij} = 0$ for that particular (*ij*) combination. To obtain a reliable estimate of ϕ , we need only the direct price elasticity of a single good and income elasticities of all goods. Thus, knowing all income elasticities, expenditure weights and the direct price elasticity of a single commodity, all the remaining parameters can be obtained.

The assumption of want independence imposes complete additivity of the utility function as noted by Barten (1964, 1967). Barten also shows the σ_{ij} 's are not invariant for a transformation of the utility function. Because of these properties, the procedure for computing the complete set of elasticities, using this approach, restricts us to a certain class of utility indicators. Barten suggests an approach which incorporates a weaker assumption on the utility function—the assumption of complete additivity is replaced by an assumption of an almost additive utility indicator.

The Barten approach

Barten also begins his analysis with the classical model where a given consumer maximizes his utility subject to a budget restraint. He expresses (175) as

$$\begin{bmatrix} (U_{ij}) & p' \\ & \\ p & 0 \end{bmatrix} \begin{bmatrix} q_{\nu} & Q_{p} \\ & \\ -\lambda_{\nu} & -\lambda_{p} \end{bmatrix} = \begin{bmatrix} 0' & \lambda I \\ & \\ 1 & -q \end{bmatrix}.$$
 (227)

From (227),

$$\begin{bmatrix} q_{\nu} & Q_{p} \\ -\lambda_{\nu} & -\lambda_{p} \end{bmatrix} = \begin{bmatrix} (U_{ij}) & p^{1} \\ p & 0 \end{bmatrix}^{-1} \begin{bmatrix} 0^{1} & \lambda I \\ 1 & -q \end{bmatrix}$$
$$= \frac{1}{p(U_{ij})^{-1}p^{1}} \begin{bmatrix} p(U_{ij})^{-1}p^{1}(U_{ij})^{-1} & -(U_{ij})^{-1}p'p(U_{ij})^{-1} & (U_{ij})^{-1}p' \\ p(U_{ij})^{-1} & -1 \end{bmatrix} \begin{bmatrix} 0^{1} & \lambda I \\ 1 & -q \end{bmatrix}$$
$$= \lambda_{u} \begin{bmatrix} (U_{ij})^{-1}p^{1} & \frac{\lambda}{\lambda_{v}} (U_{ij})^{-1} - \frac{\lambda}{\lambda_{v}} (U_{ij})^{-1}p^{1}p(U_{ij})^{-1} - (U_{ij})^{-1}p^{1}p \\ -1 & p\lambda(U_{ij})^{-1} + q \end{bmatrix}$$

Therefore,

$$q_{\mathbf{v}} = \lambda_{\mathbf{v}} (U_{ij})^{-1} p^1 \quad \text{and} \tag{228}$$

$$Q_{p} = \lambda (U_{ij})^{-1} - \left(\frac{\lambda}{\lambda_{y}}\right) q_{y} q_{y}^{\mathrm{I}} - q_{y} q. \qquad (229)$$

Converting (229) into elasticities, a typical element can be written in the form,

 $e_{ij} = \frac{p_j}{q_i} U_{ij}^{-1} - \frac{1}{\phi} e_{iy} e_{jy} w_j - e_{iy} w_j$

where

$$U_{ij}^{-1}$$
 is the $(ij)^{th}$ element of $(U_{ij})^{-1}$.

This can also be written as

$$e_{ij} = \frac{p_j}{q_i} U_{ij}^{-1} - w_j e_{ij} \left(1 + \frac{e_{ijj}}{\phi} \right).$$
(230)

Equation (230) is identical with (222) except for the first term on the right-hand side. Earlier, it was pointed out that σ_{ij} in (222) was not invariant under transformations but that $(U_{ij})^{-1}$ is invariant under transformations. Thus, from a theoretical point of view, Barten's formulation incorporates less restrictive assumptions than Frisch's formulation.

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