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From the help desk: Comparing areas under receiver operating characteristic curves from two or more probit or logit models

Mario A. Cleves, Ph.D.

Department of Pediatrics
University of Arkansas for Medical Sciences
Little Rock, Arkansas

Abstract. Occasionally, there is a need to compare the predictive accuracy of several fitted logit (logistic) or probit models by comparing the areas under the corresponding receiver operating characteristic (ROC) curves. Although Stata currently does not have a ready routine for comparing two or more ROC areas generated from these models, this article describes how these comparisons can be performed using Stata's roccomp command.

Keywords: st0023, Receiving Operating Characteristic (ROC) curve

1 Background

Stata's roccomp command is one of Stata's general-purpose programs for computing, analyzing, and comparing areas under the ROC curve. See [R] roc for more details on this and other ROC commands. The roccomp command tests the equality of two or more ROC areas obtained from applying two or more test modalities to the same sample or to independent samples. That is, there are two "flavors" of roccomp. The first is used to analyze correlated data, where several test modalities are applied to the same set of observations. The second is used to analyze independent data, where each test modality is applied to a different (disjointed) set of observations. In order to compare areas under ROC curves from different models, we must first determine if each model to be compared was estimated on the same set of observations or on different disjointed sets. This article describes methods for comparing areas from several receiver operating curves produced by logit and probit models under these two data scenarios. Although in most of the examples in this article, we estimate logistic (logit) models, the procedures described are identically applied to probit models.

Before describing the procedure for comparing areas under two or more ROC curves, let's examine the similarity between Stata's lroc command, used to produce ROC curves after logistic regression, and the roctab command. We illustrate this using the auto data distributed with Stata 7.0. We begin by fitting a logistic model with foreign as the dependent variable and price as the only covariate:

foreign	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
price	1.000035	.0000844	0.42	0.676	.9998699	1.000201

```
. lroc, nograph
Logistic model for foreign
number of observations = 74
area under ROC curve = 0.5769
```

After fitting the logistic model, we use lroc to compute the area under the ROC curve (0.5769). We now use predict to obtain the predicted probability of a positive outcome.

```
. predict p
(option p assumed; Pr(foreign))
```

The new variable, p, containing the model-predicted probability of a positive outcome, has been added to our data in memory. Note that we did not specify any options for predict because the predicted probability is the default after logistic regression. A safer way would have been to type

```
. predict p, p
or, even better,
. predict p if e(sample), p
```

Although specifying if e(sample) is not needed in this case because all 74 observations in the data were used during estimation, as we will see later, this is not always the case. Thus, we recommend that if e(sample) always be specified when predicting probabilities for ROC comparison.

Returning to our example, we can now use the roctab command to generate a ROC curve. roctab is used to perform nonparametric ROC analyses. It calculates the area under a single ROC curve, and optionally, it can plot the ROC curve. The simplest syntax for roctab is

```
retraction retractio
```

where *refvar*, the reference variable, is a dichotomous variable indicating the true state of each observation, such as diseased and non-diseased or normal and abnormal, and

variable *classvar* contains the outcome of the classification test. See [R] **roc** or type help roctab for more details and for additional options.

Using the original outcome variable foreign as the reference variable and the predicted probabilities from predict as the classification variable, we obtain

. roctab	foreign	p			
	Obs	ROC Area	Std. Err.	-Asymptoti [95% Conf.	
	74	0.5769	0.0747	0.43053	0.72331

Note that the area under the ROC curve computed by roctab is the same as that previously reported by lroc; thus, the two commands are equivalent, and in fact, they are identical. Note, however, that unlike lroc, roctab also reports the standard error and 95% confidence interval for the area under the curve.

Why does this work? Each logistic predicted probability is a possible cut-point for classifying subjects. For example, if in the above model we use p=0.5 as a classification cut-point, then we could classify automobiles with p>=0.5 as domestic and those with p<0.5 as foreign, and then construct the following table:

Logistic	Actual Origin			
Classification	Foreign	Domestic		
Foreign Domestic	A C	B D		

where A is the number of foreign cars correctly classified, and similarly, D is the number of domestic cars correctly classified. From the above table, we can compute the sensitivity, A/(A+C), and specificity, D/(B+D), of our classification cut-point. A perfectly discriminate cut-point would classify every automobile correctly; that is, both sensitivity and specificity would equal one.

If instead of selecting p = 0.5 we select p = 0.3, we would obtain different counts for A, B, C, and D, and consequently, different values for sensitivity and specificity. If we use each predicted probability value obtained from our model as a possible cut-point, we would obtain for each probability value an associated sensitivity and specificity. By plotting these sensitivity and specificity values, we generate a ROC curve. This is how both lroc and roctab construct a ROC curve.

The same approach for computing the area under the ROC is followed for a probit model. That is, estimate the model, predict the predicted probabilities, and then use these probabilities in roctab to produce the ROC. We illustrate with the same setup as before:

```
. probit foreign price
               log likelihood = -45.03321
Iteration 0:
Iteration 1:
               log likelihood = -44.94401
Iteration 2: log likelihood = -44.943972
Probit estimates
                                                    Number of obs
                                                                               74
                                                    LR chi2(1)
                                                                             0.18
                                                    Prob > chi2
                                                                           0.6727
Log likelihood = -44.943972
                                                    Pseudo R2
                                                                           0.0020
                             Std. Err.
                                                  P>|z|
                                                             [95% Conf. Interval]
     foreign
                     Coef.
       price
                  .0000222
                              .0000522
                                           0.42
                                                  0.671
                                                            -.0000802
                                                                         .0001245
                 -.6701415
                             .3605534
                                          -1.86
                                                            -1.376813
                                                                         .0365302
       _cons
 predict lp if e(sample), p
. roctab foreign lp
                       ROC
                                               -Asymptotic Normal-
           Obs
                      Area
                               Std. Err.
                                               [95% Conf. Interval]
                    0.5769
                                 0.0747
                                                0.43053
                                                             0.72331
```

Note that, not surprisingly, given the similarity between the probit and logit models, the area under this curve is the same as that previously obtained, at least out to the reported precision.

2 Comparing models estimated using the same set of observations

This entry refers to situations where all models to be compared are being estimated on the same set of observations. In this situation, difficulties can arise if there are missing values in covariates included in some models and not in others. For now, let's put this issue aside and look at the simple case where there are no missing covariate values and all models to be compared use the same observations.

In the previous section, we saw how to obtain the ROC from logit and probit models using roctab. We did this because roccomp computes ROC areas in the same way, except that it repeats the process for each curve to be compared.

We now illustrate how to compute ROC curves from two nested logistic models and compare their areas.

We begin with the same logistic model that we estimated before and save the predicted probabilities in the p1 variable:

(Continued on next page)

```
use http://www.stata-press.com/data/r7/auto, clear
(1978 Automobile Data)
. logistic foreign price
Logit estimates
                                                  Number of obs
                                                                             74
                                                  LR chi2(1)
                                                                           0.17
                                                  Prob > chi2
                                                                         0.6784
Log likelihood = -44.94724
                                                  Pseudo R2
                                                                         0.0019
             Odda Pati
```

foreign	Udds Ratio	Std. Err.	Z	P> z	[95% Conf.	Interval
price	1.000035	.0000844	0.42	0.676	.9998699	1.000201
. predict p1 i	if e(sample),	p				

```
. lroc, nograph
Logistic model for foreign
number of observations =
area under ROC curve =
                          0.5769
```

We now add the variable mpg (miles per gallon) as an independent variable in the model and save the predicted probabilities from this second model in variable p2:

```
. logistic foreign price mpg
Logit estimates
                                                    Number of obs
                                                                                74
                                                    LR chi2(2)
                                                                            17.14
                                                    Prob > chi2
                                                                           0.0002
Log likelihood = -36.462189
                                                    Pseudo R2
                                                                           0.1903
     foreign
                Odds Ratio
                             Std. Err.
                                                  P>|z|
                                                             [95% Conf. Interval]
                                             z
       price
                  1.000266
                             .0001166
                                           2.28
                                                  0.022
                                                             1.000038
                                                                         1.000495
                  1.263436
                             .0848332
                                                  0.000
                                                             1.107642
                                                                         1.441143
```

3.48

```
. predict p2 if e(sample), p
. lroc, nograph
Logistic model for foreign
number of observations =
area under ROC curve =
                           0.8112
```

mpg

Note that in both models, the complete data and the same 74 observations were used. We asked Stata to compute the area under the ROC curve after estimating each model. Although this is not necessary, we did it so that we can compare these areas with those reported by roccomp. In variable p1, we have the predicted probabilities from the first model, and in p2, the predicted probabilities from the second model. To compare the areas under the two corresponding ROCs, we use roccomp.

As mentioned in roccomp's help file, roccomp expects the data to be in wide form when comparing areas estimated from the same sample, and that is exactly how we have our data. Here is a partial list:

```
. list foreign p1 p2 in 1/5
                    p1
     foreign
 1. Foreign
                .291237
                          .9669088
 2. Foreign
              .2853879
                         .8528188
              .2797308
                          .8244022
 Foreign
 4. Domestic
               .3731745
                          .8166367
 5. Domestic
               .2842094
                          .8144851
```

Each observation in the data contains the outcome variable, foreign, and the two variables p1 and p2 containing the predicted probabilities generated from each of our two logistic models. If we were to compare three models, we would expect each observation to have, in addition to the outcome variable, three new variables containing the predicted probabilities from the three models, and so on.

The syntax for roccomp, without options, for comparing ROC areas estimated from the same sample is

```
roccomp refvar classvar classvar [classvars]
```

where, as in roctab, the reference variable, refvar, is a dichotomous variable indicating the true state of each observation, and the classvar variables contain the outcome of each of the classification tests applied to the observation. See [R] roc or type help roccomp for more details and additional options.

Using the original outcome variable foreign as the reference variable and the predicted probabilities p1 and p2 as the classification variables, we obtain

```
. roccomp foreign p1 p2
```

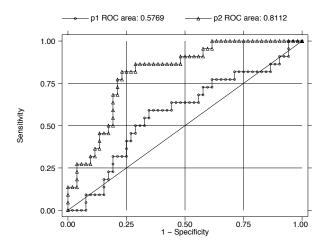
		ROC			-Asymptotic Normal-		
	Obs	Area	Std. Err.	[95% Conf.	Interval]		
p1	74	0.5769	0.0747	0.43053	0.72331		
p2	74	0.8112	0.0514	0.71040	0.91198		
Ho: area(n1)	= area(n2)						

```
Ho: area(p1) = area(p2)
chi2(1) = 6.03 Prob>chi2 = 0.0141
```

First, note that the areas that roccomp reports for the two curves are the same as those computed by lroc above. We are therefore confident that we are comparing the correct areas from the two models. roccomp computed a significance probability of 0.0141, suggesting that the two models are different in their predictive ability. We can visually examine this difference by specifying the graph option of roccomp:

```
. roccomp foreign p1 p2, graph s(oT)
```

(Continued on next page)



When comparing areas under ROC curves from models estimated on the same sample, it is important that we be cognizant of the actual estimation sample that each model is using. Stata makes this evaluation easy by identifying the used observations by flagging them with e(sample). We want to make sure that predict only generates predicted probabilities for the sample used in the estimation so that the ROC curves compared are the correct ones based on the estimated models. That is why we previously recommended that if e(sample) always be specified when using predict in the current context. Difficulties in comparing ROC curves can arise when there are missing covariate values that drop observations from some models and not from others.

Recall that Stata will drop from the estimation any observation in which at least one of the specified model covariate values is missing. Therefore, if we have a dataset in which the variable age is never missing and we estimate, for example, a logistic model using age as the only covariate, then every observation in the dataset will be included in the estimation. If, on the other hand, the dataset contains the variable sex missing in 5% of observations, then a logistic model with age and sex as covariates would drop 5% of the observations due to the missing value for sex in these observations. Additionally, roccomp will drop any observations in which at least one of the predicted probability values is missing. If we use roccomp to compare the two ROC areas from these two nested models, although roccomp will correctly compare the curves based on the nonmissing data, the comparison may not be the one that we think we are making.

To illustrate this using the auto data, assume that rep78 is a continuous variable that can be included directly in our models. In reality, rep78 is a categorical variable and would need to be "dummied-up" for model inclusion. In our data, the rep78 variable is missing in five observations.

0.4018

```
. use http://www.stata-press.com/data/r7/auto, clear (1978 Automobile Data)
```

. logistic foreign price mpg

Logit estimates Number of obs = 74LR chi2(2) = 17.14Prob > chi2 = 0.0002Log likelihood = -36.462189 Pseudo R2 = 0.1903

foreign	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
price mpg	1.000266 1.263436	.0001166		0.022	1.000038 1.107642	1.000495 1.441143

```
. predict p1 if e(sample), p
```

. lroc, nograph

Logistic model for foreign

 $\begin{array}{lll} \text{number of observations} = & 74 \\ \text{area under ROC curve} & = & 0.8112 \end{array}$

. logistic foreign price mpg rep78

Pseudo R2

Log likelihood = -25.362394

foreign	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
price mpg	1.000141 1.18063	.0001379 .0966693	1.03	0.305 0.043	.9998712 1.005583	1.000412 1.386148
rep78	5.321595	2.656575	3.35	0.001	2.000398	14.15687

```
. predict p2 if e(sample), p
(5 missing values generated)
```

. lroc, nograph

Logistic model for foreign

number of observations = 69
area under ROC curve = 0.9147

Note that all 74 observations were used in the first logistic model, whereas the second model with rep78 was estimated using only 69 observations. That is because, as mentioned, rep78 is missing in five observations. Let's now examine what roccomp does with these data.

. roccomp foreign p1 p2

	Obs	RUC Area	Std. Err.	-Asymptotic [95% Conf.	
p1	69	0.8264	0.0515	0.72535	0.92742
p2	69	0.9147	0.0352	0.84562	

Ho: area(p1) = area(p2) chi2(1) = 3.86 Prob>chi2 = 0.0495

First, note that the number of observations for p1 and p2 are both 69. Although the first model, on which p1 was predicted, was estimated using all 74 observations, when comparing the ROC curves, five observations were dropped due to missing p2 values. However, the number of observations is not the only difference, and more importantly, the ROC area for the first model is not 0.8112 as lroc reported but is now 0.8264 based on the 69 observations that remained.

Because roccomp performs the correct comparison based on the data that remain after dropping missing values, we may be misled into thinking that all is fine, but it is not. Note that p1 was predicted based on a model that had 74 observations. Had we dropped the five observations with missing rep78 before we began, we would obtain different values for p1 and, consequently, a different ROC area from the one computed by either 1roc or roccomp above.

```
use http://www.stata-press.com/data/r7/auto, clear
(1978 Automobile Data)
. drop if rep78==.
(5 observations deleted)
. quiet logistic foreign price mpg
. predict p1 if e(sample), p
. lroc, nograph
Logistic model for foreign
number of observations =
area under ROC curve =
                           0.8284
. quiet logistic foreign price mpg rep78
. predict p2 if e(sample), p
. lroc, nograph
Logistic model for foreign
number of observations =
                                69
area under ROC curve =
                            0.9147
. roccomp foreign p1 p2
                              ROC
                                                       -Asymptotic Normal-
                   Obs
                              Area
                                       Std. Err.
                                                       [95% Conf. Interval]
                                                                    0.92862
                            0.8284
                                                        0.72813
                     69
                                         0.0511
p1
p2
                     69
                            0.9147
                                         0.0352
                                                        0.84562
                                                                    0.98374
Ho: area(p1) = area(p2)
                              Prob>chi2 =
                                            0.0617
```

Although the difference is not large in this example, it can be, and often is, quite substantial for other larger datasets or models.

3 Models estimated using different sets of observations

On occasion, we may want to compare the same model estimated on different sets of similar observations. For example, we may want to compare the ROC curve produced from a model applied to our data to the ROC curve produced by the same model applied

to a colleague's data. Or, for example, in a given study, we may want to compare the ROC curve produced from a model using only males to the same model applied to only females. Thus, we may have two or more models estimated on separate datasets, or two or more models estimated on subsets of the same dataset.

We describe the procedure by comparing ROC curves computed from models applied to subsets of data. We again use the auto data distributed with Stata 7.0. We want to compare the area under the ROC curve from a logistic model regressing price and mpg on foreign using only autos with a Repair Record of 3 or less to a similar model fitted to autos with Repair Records of 4 or 5. We begin by creating a dummy or indicator variable, rep78_dummy, identifying the two groups that we wish to compare. Note that of the original 74 observations, 5 have a missing repair record and are not included in the analysis.

```
. use http://www.stata-press.com/data/r7/auto, clear
(1978 Automobile Data)
. gen rep78_dummy=1 if rep78<=3
(34 missing values generated)
. replace rep78_dummy=2 if rep78==4 | rep78==5
(29 real changes made)</pre>
```

We now fit a logistic model to each subset of data and obtain the corresponding predicted probabilities.

```
. logistic foreign price mpg if rep78_dummy==1

Logit estimates

Number of obs = 40

LR chi2(2) = 3.06

Prob > chi2 = 0.2164

Log likelihood = -9.1246556

Pseudo R2 = 0.1437

foreign Odds Ratio Std. Err. z P>|z| [95% Conf. Interval]
```

```
foreign Odds Ratio Std. Err. z P>|z| [95% Conf. Interval]

price .9999979 .0002927 -0.01 0.994 .9994243 1.000572
mpg 1.307117 .2337931 1.50 0.134 .9205915 1.85593
```

```
predict p1 if e(sample), p
(34 missing values generated)
. lroc, nograph
Logistic model for foreign
number of observations =
area under ROC curve = 0.8378
. logistic foreign price mpg if rep78_dummy==2
Logit estimates
                                                  Number of obs
                                                                            29
                                                  LR chi2(2)
                                                                          8.27
                                                  Prob > chi2
                                                                        0.0160
Log likelihood = -15.112878
                                                  Pseudo R2
                                                                        0.2148
```

foreign	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
price	1.000596	.0003265	1.83	0.068	.9999563	1.001236
mpg	1.232908	.1115754	2.31	0.021	1.032521	1.472185

```
. predict p2 if e(sample), p
(45 missing values generated)
. lroc, nograph
Logistic model for foreign
number of observations = 29
area under ROC curve = 0.7929
```

The procedure, so far, is similar to that of the previous section, with the exception that we have included a conditional if statement in order to estimate the model on the proper data subset. It is very important in this situation to specify e(sample) with predict. If we fail to specify e(sample), predict will generate predicted probabilities for all observations in memory. Let's examine our data in memory by listing a few observations.

```
. list foreign p1 p2 rep78_dummy in 1/5
                   p1 p2 rep78_d~y
     foreign
 1. Foreign
                       .9806504
                   .
 2. Foreign
3. Foreign
4 Foreign
                       .9593273
                        .9444055
                        .899147
                        .8676886
 5. Domestic
. sort rep78_dummy
. list foreign p1 p2 rep78_dummy in 1/5
                  p1
     foreign
                             p2 rep78_d~y
 1. Domestic .0067503
 2. Domestic .0915387
             .1472585
 3. Domestic
 4. Foreign
 5. Domestic
             .0557233
```

We see that for observations with rep78_dummy==2, the values for p1 are always missing and the values for p2 are filled in, and for observations with rep78_dummy==1, the opposite is true. This is because we predicted p1 based on a model fitted for observations with rep78_dummy==1, and p2 was predicted based on a model fitted for observations with rep78_dummy==2. This is exactly as it should be. Only those observations included in the estimation sample should contain the predicted probabilities.

If we attempt to use roccomp as before, we will get an error because all observations will be dropped due either to missing p1 or missing p2.

```
. roccomp foreign p1 p2
Outcome does not vary
r(198);
```

As stated in the help file, roccomp expects the data to be in long form for areas estimated from independent samples. In this case, the simplest syntax for roccomp, without options, for comparing ROC areas estimated from independent samples is

```
roccomp refvar classvar, by (varname)
```

Note that we can only specify one classification variable and must specify the by() option. So, we must create a single classification variable based on our predicted probabilities, and then use roccomp specifying by(rep78_dummy).

```
. gen newp=p1 if p1~=.
(34 missing values generated)
. replace newp=p2 if p2~=.
(29 real changes made)
```

. roccomp foreign newp, by(rep78_dummy)

rep78_dummy	0bs	ROC s Area Std. Err.		-Asymptoti [95% Conf.	c Normal— Interval]
1 2	40	0.8378	0.0796	0.68184	0.99384
	29	0.7929	0.0982	0.60039	0.98547

```
Ho: area(1) = area(2)
chi2(1) = 0.13 Prob>chi2 = 0.7224
```

We can verify that the ROC areas reported by roccomp are the same as those previously obtained by lroc for the two models.

Although in the previous examples we have only compared two ROC areas, roccomp has no limit on the number of areas that it can compare. For example, we can compare the areas under the ROC curves for rep78==3, rep78==4, and rep78==5.

```
. use http://www.stata-press.com/data/r7/auto, clear
(1978 Automobile Data)
. quiet logistic foreign price mpg if rep78==3
. predict p3 if e(sample), p
(44 missing values generated)
. quiet logistic foreign price mpg if rep78==4
. predict p4 if e(sample), p
(56 missing values generated)
. quiet logistic foreign price mpg if rep78==5
. predict p5 if e(sample), p
(63 missing values generated)
. quiet gen newp=p3 if p3~=.
. quiet replace newp=p4 if p4~=.
. quiet replace newp=p5 if p5~=.
. roccomp foreign newp, by(rep78)
```

rep78	Obs	ROC Obs Area Std. Err.		-Asymptotic Normal- [95% Conf. Interval]	
3	30	0.8642	0.0723	0.72247	1.00000
4	18	0.8765	0.0905	0.69914	1.00000
5	11	0.7778	0.1470	0.48969	1.00000

```
Ho: area(3) = area(4) = area(5)
chi2(2) = 0.35 Prob>chi2 = 0.8407
```

Not a very interesting example, but it illustrates well the procedure for comparing several ROC curves, each computed on a subset of observations.

Finally, a similar procedure works to compare ROC curves from models estimated on different datasets. Simply, estimate the model on each dataset separately, estimate the predicted probabilities and save them in a variable with same name in both datasets,

create a dummy variable that identifies the datasets, append the datasets, and then use roccomp with the by() option. For example, assume that we have two auto datasets, auto1.dta and auto2.dta. Then, the commands needed to compare the ROC curves are

```
. use auto1.dta, clear
. logistic foreign price mpg
. predict p if e(sample), p
. gen dataset=1
. save temp,replace
. use auto2.dta, clear
. logistic foreign price mpg
. predict p if e(sample), p
. gen dataset=2
. append using temp
. roccomp foreign p, by(dataset)
```

About the Author

Mario Cleves is an Associate Professor in the Department of Pediatrics at the University of Arkansas for Medical Sciences.