THE PRICE OF ONE SWEET CALORIE

Sebastien Buttet
Business Administration Division, Guttman CC, City University of New York, USA

Veronika Dolar
Economics Department, Long Island University, Brookville, NY 11548, USA
E-mail: veronika.dolar@liu.edu

Abstract

We propose a new measure for food prices to further examine the impact of changes in food prices and real income on individuals' eating decisions and weight. We calculate price per calorie for food consumed away from home and food consumed at home as the dollar amount spent by households on each food category divided by the number of calories consumed. We use our newly constructed time series for price per calorie as an input into a neoclassical model of eating decisions and weight. Our goal is to propose a quantitative explanation for the increase in calories consumed away from home as well as changes in weight for men and women 1971 and 2006. We find that prices determine the allocation of calories across food types, while income determines the total number of calories consumed and thus individuals' weight. Based on our results, we share the view that taxes on food will impact what people eat but will have limited effect on reducing the population body-mass index or the obesity prevalence.

Keywords: Obesity, body weight, food prices, household income

1. Introduction

Two decades of intense research in the field of economics of obesity have improved our understanding of the impact of food prices on weight and food choices and two critical results have gained wide acceptance. First, several empirical studies show that changes in aggregate food prices over time have little effect on the population body mass index or obesity prevalence (e.g., Chou, Grossman, & Saffer, 2004; Beydoun, Powell, & Wang, 2008; Anderson & Matsa, 2011). Second, experimental studies show that changes in the price of selected food items drastically affects what people eat. For example, French et al. (2001) find that a fifty percent price reduction on low-fat snacks in vending machines at schools and work places increase the percentage of low-fat snack sales by ninety three percent. These two results about the effect of food prices on weight and food choices are important because of their influence on the public health debate about the effectiveness of fiscal policies for winning the fight against the obesity epidemic. A common view held by policymakers is that taxes applied selectively to different food items work effectively to reduce consumption of a particular type of food or ingredient (e.g., ban of trans-fats) but are unlikely to produce significant changes in body-mass index or obesity prevalence (Powell, Chiqui, & Chaloupka, 2009; Chouinard, Davis, LaFrance, & Perloff, 2012).

In this paper, we further examine the impact of changes over time in food prices and household real income on individuals' food choices and weight using a calibrated static model. Our first objective is to propose a new measure for food prices to further examine the
impact of changes in food prices and real income on individuals’ eating decisions and weight. We calculate *price per calorie* for food consumed away from home and food consumed at home as the dollar amount spent by households on each food category divided by the number of calories consumed. Our second objective is to contribute to the debate about the impact of food prices and household real income on weight and food choices using a different modeling strategy. We ask how much of the increase in calories consumed away from home as well as changes in weight for men and women between 1971 and 2006 can be accounted for by changes in food prices and household real income. Our final, and perhaps the most critical objective, is to use economic theory and available evidence from medical research on obesity to look inside the black box of how people make eating decisions and to improve our understanding of what determines the (low) food price elasticity of weight.

In this paper we assume that there is a one-to-one relationship between agent’s weight and total calories consumed. In addition, weight affects the probability that agents are alive. Given household real disposable income and the relative price of a calorie (at home versus away from home), agents decide how much to eat at each location as well as how much of the non-food good to consume to maximize their expected utility.

Identification of the model is clean. On the one hand, we use available evidence from medical research on nutrition to calibrate the parameters of the weight function and medical research on obesity-related diseases to fit the survival probability function. On the other hand, we choose the remaining preferences parameters to match the mean weight and fraction of calories away from home observed in NHANES 19711, allowing some preference heterogeneity between men and women.

We use the calibrated model to assess the impact of changes in food prices and household real income on food choices and weight between 1971 and 2006. We find that prices determine the allocation of calories across food types, while income determines the total number of calories consumed and thus individuals’ weight. Based on our results, we share the view that taxes on food will impact what people eat but will have limited effect on reducing the population body-mass index or the obesity prevalence.

The remainder of the paper is organized as follows. In Section 2, we describe data about weight and calories consumed at and away from home. In Section 3, we introduce our new method of calculating per calorie food prices and show the household real income between 1971 and 2006. In Section 4 and Section 5, we develop and calibrate our model and we conduct our simulations in Section 6. Finally, we offer concluding remarks in Section 7.

### 2. Nutrition Data

In this section, we use two distinct data sets from the National Health and Nutritional Examination Survey (NHANES) to document changes over time in Body-Mass Index (BMI), weight, and the fraction of calories consumed away from home for men and women for the period between 1971 and 2006 (see Table 1).2 Data about weight comes from the

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1 The data for NHANES I was collected during the period 1971-75 however, for clarity and convenience we will refer to it as NHANES 1971 and refer to it by year 1971. Similar, the data for NHANES 2005-2006 was collected over these two years, however, we will refer to it as NHANES 2006 and refer to it by year 2006 throughout the paper.

2 Body-mass index is a measure of body fat based on height and weight that equally applies to adult men and women. It is calculated as 703 times weight measured in pounds divided by height squared measured in inches squared. Individuals with BMI lower than 18.5 are considered underweight, between 18.5 and 24.9 normal weight, between 25 and 30 overweight, and 30 or greater obese. BMI combined with other information about waist
examination component of NHANES and is measured by trained medical personnel. The fraction of calories consumed away from home, on the other hand, is self-reported by individuals.3

Table 1. Changes in BMI, Weight, Calories, and Fraction of Calories Consumed Away From Home for Men and Women

<table>
<thead>
<tr>
<th></th>
<th>1971</th>
<th>2006</th>
<th>% Change</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Men</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BMI</td>
<td>25.9</td>
<td>29.0</td>
<td>12.0</td>
</tr>
<tr>
<td>Weight (lbs)</td>
<td>175.7</td>
<td>198.2</td>
<td>12.8</td>
</tr>
<tr>
<td>Calories</td>
<td>2433</td>
<td>2543</td>
<td>4.5</td>
</tr>
<tr>
<td>% calories away</td>
<td>29.9</td>
<td>40.5</td>
<td>35.5</td>
</tr>
<tr>
<td><strong>Women</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BMI</td>
<td>25.2</td>
<td>28.8</td>
<td>14.3</td>
</tr>
<tr>
<td>Weight (lbs)</td>
<td>145.8</td>
<td>168.9</td>
<td>15.8</td>
</tr>
<tr>
<td>Calories</td>
<td>1538</td>
<td>1802</td>
<td>17.2</td>
</tr>
<tr>
<td>% calories away</td>
<td>19.5</td>
<td>35.9</td>
<td>84.1</td>
</tr>
</tbody>
</table>

In the last thirty years, men have gained on average 23 pounds and their body-mass index increased from 25.9 (slightly overweight) to 29.0 (borderline obese).4 The increase in average weight and body-mass index is even more pronounced in percentage terms for women who also gained 23 pounds. In addition, men and women changed their eating habits dramatically and ate out more. Total daily calories consumed increased by 110 calories for men and 264 for women, while the fraction of calories away from home increased by 35.5 and 84.1 percentage points for men and women, respectively.

3. Price per Calorie

As already mentioned, in the field of public health numerous controlled experimental studies have been developed that show that changes in the price of selected food items drastically affects what people eat (e.g., Jeffery, French, Raether, & Baxter, 1994; French, 2003; Epstein, Dearing, Paluch, Roemmich, & Cho, 2007). Because the above studies imply great price sensitivity they have clear implications for public health policy. For example, lowering prices on healthy foods and hiking the prices of unhealthy foods can induce people to reduce their intake of calories and body-mass index. Lowering prices on fruits and vegetables, for example, is likely to lead to increased consumption of these foods. Higher prices on unhealthy foods can also induce people to reduce their consumption of these foods. In addition, changes in prices can affect the availability of healthy foods and the prices of unhealthy foods can also affect the availability of healthy foods. For example, higher prices on fruits and vegetables can lead to increased production of these foods, while lower prices on unhealthy foods can lead to decreased production of these foods. This can have important implications for public health policy, as changes in prices can affect the availability of healthy foods and the prices of unhealthy foods can also affect the availability of healthy foods.

3 The question about where do people eat their meal has changed over time. In NHANES 1971, individuals can choose among the following four locations: at home, in school, in restaurants, and other, while in NHANES 2006, the location question is: “Did you eat this food at home?” and the possible answers are yes, no, refused to answer, do not know, and missing information. We get rid of a small fraction of missing values or unknowns. To maintain consistency across the two data sets, we define food eaten at home as any food item for which individuals answered “at home” in NHANES 1971 and “yes” in NHANES 2006. We then calculate the fraction of calories eaten away from home as one minus the fraction of calories eaten at home.

4 Simple t-tests show that differences in mean weight and mean body-mass index over time are statistically significant for both men and women.
to buy more of the former and less of the latter (Brownell & Frieden, 2009; Brownell et al., 2009).

Price sensitivity of demand, however, is only a necessary and obviously not a sufficient condition to reduce food consumption and body weight. For example, take two food items with the same price elasticity of demand but where one is more calorie-dense than the other. Then the same tax will equally decrease quantity demanded (measured in pounds of food for example) of these two food items but will have drastically different impact on body weight; the decrease in the quantity demanded of high caloric food will have a much bigger effect on body weight. This issue can be ameliorated by studying the impact of changes in price per calorie (“Calorie” will be used in lieu of kilocalorie throughout the paper) instead of looking at regular food item prices, since the change in quantity demanded measured in calories more directly translates in changes in body weight.

In addition, a problem with experimental studies is that they only include a very limited amount of items and focus on the consumption changes only at one point in time (e.g. at lunch or at school). As a result, one cannot observe how a person behaves outside the parameters of the experiment. For example, if individuals substitute away from highly priced or taxed foods at the vending machine towards other lower-priced but potentially highly caloric foods there will be no significant change in body weight (in fact, weight might actually increase). A soda tax might induce people to switch to other high-caloric drinks such as orange juice or chocolate milk at home, with no impact on their weight. In this case including only few food items ignores the possibility for substitution. This can be somewhat improved by including all possible food items, which is impossible or by allowing for more broadly defined food groups such as food at home and food away from home.

Economists have been trying to add to this line of work by using larger observational data to analyze the relationship between food prices and weight but with mixed success. For example, several empirical studies show that changes in aggregate food prices over time have little effect on the population body-mass index (BMI) or obesity prevalence for adults (Beydoun et al., 2008; Goldman, Lakdawalla, & Zheng, 2011) and almost no effect on children and adolescents (Sturm, Powell, Chriqui, & Chaloupka, 2010, Powell & Chaloupka, 2011). As concluded by Lakdawalla and Zheng (2011) the current literature on how food prices affect body weight suffers from substantial empirical challenges of causal inference that have not yet been satisfactorily overcome.

One such challenge comes from the measurement of food prices themselves. In order to identify the effect of food prices on body weight researches have use two familiar data sources: Bureau of Labor Statistics (BLS) and Council of Community and Economic Research (C2ER), formerly known as American Chamber of Commerce Researchers Association (ACCRA). The common problem with using these data sets is that they use only around 20 to 60 food items. Given the fact that about 320,000 foods and beverage products are available in the United States, and that an average supermarket carries 30,000 to 40,000 of them, this seems very limited (Nestle, 2006).

In this section, we introduce a new method to measure much broader average prices that adjusts for changes in calories consumed over time. Using household expenditures share data for different food categories we calculate the price per calorie as household expenditures on food divided by calories consumed. The logic behind construction of price per calorie in this paper is quite simple. Divide the amount of money spent on a certain food item by the number of calories consumed for this food. A similar strategy is used elsewhere where they take the price per unit of food item and divide it by the calories per unit of food (Grossman, Tekin, & Wada, 2013; Goldman et al., 2011;Christian and Rashad 2009). The difference with our approach is that instead of focusing on a specific food item, we can take broad food categories and calculate price per calorie for that category.
We calculate price per calorie for food consumed away from home, \( p_{a,t} \), and food consumed at home, \( p_{h,t} \), as the dollar amount spent by households on each food category divided by the number of calories consumed:

\[
p_{a,t} = \frac{\alpha_{a,t} I_t}{\text{Calories}_{a,t}}, \quad p_{h,t} = \frac{\alpha_{h,t} I_t}{\text{Calories}_{h,t}}
\]  

(1)

We calculate the dollar amount spent by households on food as household real disposable income, \( I_t \), multiplied by the expenditure share on food consumed away from home \( \alpha_{a,t} \) or at home \( \alpha_{h,t} \). Information about the expenditure share on food away from home and food at home is obtained from household expenditures data published by the US Department of Agriculture (USDA). The expenditure for food away from home is equal to 3.5 and 4.1 percent, respectively, for the periods 1971 and 2006. The expenditure for food away from home is equal to 9.9 and 5.7 percent, respectively, for the same time periods. Information about nominal disposable income comes from the Bureau of Economic Analysis (BEA) and we use the consumer price index (CPI) published by BLS to calculate the real disposable income expressed in 2006 dollars. Between 1971 and 2006, household real disposable income increased by 24 percent, while the per calorie price of food consumed away from home declined by seventeen percent (see Table 2).

<table>
<thead>
<tr>
<th>Table 2. Changes in per Calorie Food Prices and Real Income</th>
</tr>
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<tbody>
<tr>
<td>Price per thousand calories for food away from home</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>Price per thousand calories for food at home</td>
</tr>
<tr>
<td>Relative Price (away/home)</td>
</tr>
<tr>
<td>Mean Real Income in $2006</td>
</tr>
</tbody>
</table>

Two reasons commonly advanced for the weight gain of Americans are the increase in calories consumed away from home and larger portion size at restaurants. Between 1977 and 1995 the consumption of food prepared away from home increased from eighteen percent to thirty-three percent of total calories (Guthrie, Lin, & Frazao, 2002). Furthermore, in 1977, thirty-one percent of all food spending was on food away from home; by 1995, that share rose to thirty-nine percent (Putnam & Allshouse, 1999). In addition, the food portions are larger today than they were in the past (Young & Nestle, 2002). According to Young and Nestle (2002) “in the mid-1950s, McDonald’s offered only 1 size of French fries; that size is now considered “Small” and is one third the weight of the largest size available in 2001” (p.248).

The price per calorie has two significant advantages over traditional food prices. First, it provides a simple method for aggregating food items in different categories. Second, it is intuitively appealing as it controls for changes in portion sizes. Note that the relative price of food away from home is always greater that one, implying that eating out is more costly than eating at home, even after adjusting for differences in the number of calories. In addition, we looked at changes in food prices published by the Bureau of Labor Statistics. Similarly to Christian and Rashad (2009) we find that the price of food consumed away from home increased by 40 percent from 1971 to 2006. The increase in food prices away from home is clearly at odds with the observed increase in the fraction of calories eaten away from home. However, the trend in the increased consumption of food away from home can be easily explained if one includes the price per calorie of food away from home.
4. A Simple Optimization Model Of Eating Decision And Weight

We propose a static model where agents decide how much and where to eat (out or at home) as well as non-food consumption. We let $a$ and $h$ be the number of calories consumed away and at home, respectively, and $c^{nf}$ represents non-food consumption. Calories away and at home are aggregated using a constant elasticity of substitution (CES) function to obtain food consumption:

$$c^f = (\eta a^\rho + (1 - \eta) h^\rho)^{\frac{1}{\rho}}$$  \hspace{1cm} (2)

with $\eta \in (0,1)$ and $\rho \in (-\infty, 1]$. Food away and at home are perfect substitutes, Cobb-Douglas, or perfect complements when the parameter $\rho$ is equal to one, zero, or minus infinity, respectively. The parameter $\eta$ reflects consumer’s preference for eating at home or eating out.

Preferences of the representative agent are Cobb-Douglas and are given by:

$$U(c^f, c^{nf}) = (c^f)^\alpha (c^{nf})^{1-\alpha}$$  \hspace{1cm} (3)

with $\alpha \in (0,1)$.

Agents make ex-ante eating decisions understanding that weight affects the probability $\pi(W)$ of being alive. We assume that the function $\pi$ is an inverted U-shape function of BMI which implies that agents who are either over- or underweight have a greater chance to die. Finally, agents receive utility $U \leq 0$ when they die. The expected utility is equal to:

$$\pi(W)U(c^f, c^{nf}) + (1 - \pi(W))U$$  \hspace{1cm} (4)

Note that it is never optimal for people to eat so much that they would die with certainty since $U(c^f, c^{nf})$ is positive and $U \leq 0$.

The relationship between weight and calorie consumption is given by the simple linear relationship:

$$W = \mu + \theta(a + h)^5$$  \hspace{1cm} (5)

with $\theta > 0$.

Finally, the budget constraint of the representative agent is given by:

$$c^{nf} + p_h h + p_a a = l$$  \hspace{1cm} (6)

\footnote{Body weight quite obviously depends on physical exercise as well. Equation (5) in principle does not exclude weight being dependent on other factors. All other factors that determine weight such as height, gender, and physical effort are potentially captured with parameter $\mu$. The assumption that we are making is that all these other factors are constant for all individuals and vary only by gender. Since we are looking at an average American man and woman in the US we assume that his/her height remained unchanged between 1971 – 2006, a fact supported by the data. In addition, we also keep the level of exercise, physical effort, and energy expenditure constant. This assumption is based on the paper by Cutler, Glaeser, & Shapiro (2003)In this paper they examine two components of energy expenditure: voluntary exercise, and involuntary energy expenditure associated with employment and conclude that their results suggest that increased caloric intake explains the rise in obesity, not reduced caloric expenditure.}
where we normalized the price of non-food to one, \( p_h \) and \( p_a \) are the real price of food at and away from home, respectively, and agents are endowed with real income \( I \).

For any prices and income, \( \{ p_h, p_a, I \} \), the representative agent chooses optimal calories from food away and at home as well as non-food consumption, \( \{ a, h, c^n, c^f \} \), to maximize the expected utility in equation (4) subject to the budget constraint (6), the weight function (5), the food aggregation equation (2), and non-negativity constraints for calorie and non-food consumption.

We substitute the weight relationship into the objective function: the weight function, the survival probability function, and the deep preference function in equation (4). The consumption of food away from home, \( a \), and food at home, \( h \), appear as follows in the objective function:

\[
\pi(\mu + \theta(a + h))(\eta a^\rho + (1 - \eta)h^\rho)^\frac{a}{\rho}(1 - p_h h - p_a a)^{1 - a} + (1 - \pi(\mu + \theta(a + h))) \frac{U}{\pi'}(\mu + \theta(a + h))
\]  

(7)

We take first-order conditions with respect to food away from home, \( a \), and food at home, \( h \).

\[
[a]: \theta \pi'(W)(U(c^f, c^{nf}) - U) + \pi(W)U(c^f, c^{nf})\left(\frac{a\eta a^{\rho - 1}}{\eta a^\rho + (1 - \eta)h^\rho} - \frac{p_a(1 - \alpha)}{l - p_a a - p_h h}\right) = 0
\]

\[
[h]: \theta \pi'(W)(U(c^f, c^{nf}) - U) + \pi(W)U(c^f, c^{nf})\left(\frac{a(1 - \eta)h^{\rho - 1}}{\eta a^\rho + (1 - \eta)h^\rho} - \frac{p_h(1 - \alpha)}{l - p_a a - p_h h}\right) = 0
\]

(8)

Note that consumer’s utility might not be strictly concave because the survival probability depends on consumer’s weight. As a result, it is not clear whether first-order conditions are sufficient for optimality. Although we do not offer a formal proof, we check in our computer simulations that the allocations that satisfy the first-order conditions in equation (8) are also utility-maximizing (locally).

We rearrange the first-order conditions in equation (8). The optimal level of food away from home, \( a \), and food at home, \( h \), are obtained by solving the following system of equations (9):

\[
\frac{\eta a^{\rho - 1} - (1 - \eta)h^{\rho - 1}}{\eta a^\rho + (1 - \eta)h^\rho} = \frac{1 - a}{\alpha} \frac{p_a - p_h}{l - p_a a - p_h h}
\]

\[
\frac{a\eta a^{\rho - 1}}{\eta a^\rho + (1 - \eta)h^\rho} - \frac{p_a(1 - \alpha)}{l - p_a a - p_h h} = \theta \frac{\pi'(\mu + \eta(a + h))}{\pi(\mu + \eta(a + h))}(1 - \frac{U}{\pi'(c^f, c^{nf})})
\]

(9)

In the reminder of the paper, we explain our method to calibrate the three key parts of our model: the weight function, the survival probability function, and the deep preference parameters. We then use the calibrated model to conduct a lab experiment where we assess the impact of food price and real income on weight and the fraction of calories away from home.

5. Calibration

We use medical research on obesity to calibrate the weight law of motion and the survival probability function. We then chose the remaining preference parameters to match
the average weight and calories away from home for men and women observed in the NHANES 1971 sample.

5.1. Weight Function

The weight function in equation (5) contains two distinct important parameters. First, the constant $\theta$ converts calorie intake into weight. According to the dietary guidelines from the US Department of Agriculture, people gain ten pounds per year if they eat an extra one hundred calories every day above and beyond the recommended daily calorie intake. As a result, we fix $\theta = \frac{10}{100 \times 365} = 2.7397 \times 10^{-4}$.

Second, we use the average observed weight and calorie consumption by men and women in NHANES 1971 to fix $\mu^m$ and $\mu^f$. The weight and total calories data comes from Table 1.

$$\mu^m = W^{m,1971} - \theta \text{cal}^{m,1971} = 175.7 - 2.7397 \times 10^{-4} \times 2433 \times 365 = -67.6$$
$$\mu^f = W^{f,1971} - \theta \text{cal}^{f,1971} = 145.8 - 2.7397 \times 10^{-4} \times 1538 \times 365 = -8.0$$

5.2. Survival Probability Function

We posit that the survival probability function $\pi(W_t)$ is given by the following functional form:

$$\pi(W_t) = \frac{1}{1 + \kappa(W_t - W^*)^2} \quad (10)$$

with $\kappa > 0$ and $W^* > 0$ represents the agent’s “best” weight where the survival probability is maximized and equal to one. Note that the survival probability increases with the agent’s weight when $W_t \leq W^*$ but decreases once the agent’s weight is greater than $W^*$.

First, we set the best weight $W^m = 170$ for men and $W^f = 145$ for women which corresponds to a body-mass index of 25 for both sexes.

Second, the parameter $\kappa$ is identified by the increased mortality risk due to obesity alone. For two different weight $W_1$ and $W_2$, the increased mortality is equal to:

$$\frac{1 - \pi(W_1)}{1 - \pi(W_2)} = \frac{(W_1 - W^*)^2}{(W_2 - W^*)^2} \times \frac{1 + \kappa(W_2 - W^*)^2}{1 + \kappa(W_1 - W^*)^2} \quad (11)$$

Allison, Fontaine, Manson, & Stevens (1999) report the hazard ratios of death based on six large prospective cohort studies where subjects are placed into two distinct groups: the control group is comprised of individuals whose BMI is between twenty-three and twenty-five; the treated group consists of individuals with BMI higher than twenty-five.

The death likelihood increases by a factor of 1.08 for overweight individuals (when BMI is between 25 and 28) and by a factor of 1.43 for obese people (when BMI is between 30 and 35). Choosing the middle point for each interval, a BMI of 26.5 corresponds to a weight of 181 pounds for a male of average height, while a BMI of 32.5 corresponds of a weight of 221 pounds. As a result, the parameter $\kappa^m$ is obtained by solving the following equation:

$$\frac{121 \times 1 + 2601 \kappa^m}{2601 \times 1 + 121 \kappa^m} = \frac{1.08}{1.43} \quad (12)$$

It is equal to $\kappa^m = 2.39 \times 10^{-2}$
Similarly, choosing the middle point for each interval, a BMI of 26.5 corresponds to a weight of 153 pounds for a female of average height, while a BMI of 32.5 corresponds to a weight of 188 pounds. As a result, the parameter \( \kappa_w \) is obtained by solving the following equation:

\[
\frac{64}{1849} \times \frac{1 + 1849 \kappa_w}{1 + 64 \kappa_w} = 1.08 \overline{1.43}
\]

It is equal to \( \kappa_w = 4.6 \times 10^{-2} \).

5.3. Preferences

We are now left with calibrating four preferences parameters, \((\alpha, \eta, \rho, \bar{U})\). First, since the utility function \( U(c_f, c_{nf}) \) is positive, we fix \( \bar{U} = 0 \) so that death resulting from excess eating is never an optimal choice.

Second, we use the research of Reed, Lavedahl, & Hallahan (2005) which estimates the elasticity of substitution between food away from home and food consumed at home. They find that both types of foods are substitutes and a result, we fix \( \rho = 0.75 \).

Finally, we use the two first-order conditions in equation (9) to determine \((\alpha, \eta)\) to match the observed average weight and fraction of calories consumed away from home for men and women in the NHANES 1971 sample.

**Proposition 1** The calibrated parameter values of \((\alpha, \eta)\) are given by:

\[
\eta = \frac{BG + FB - GED}{G(A + B) - A(E - F) + FB + GE(C - D)}
\]

\[
\alpha = \frac{EG(C\eta + D(1 - \eta))}{(E - F)A\eta + FB(1 - \eta)}
\]

where \( A = (a^{1971})^{\rho - 1}, B = (h^{1971})^{\rho - 1}, C = (a^{1971})^{\rho}, D = (h^{1971})^{\rho - 1}, \)

\[
E = \frac{p_{a}^{1971} - p_{h}^{1971}}{1 - p_{a}^{1971} a^{1971} - p_{h}^{1971} h^{1971}}
\]

\[
F = \frac{p_{a}^{1971}}{1 - p_{a}^{1971} a^{1971} - p_{h}^{1971} h^{1971}}
\]

\[
G = -\frac{2\kappa\theta(W^{1971} - W^*)}{1 + \kappa(W^{1971} - W^*)^2}
\]

*Proof: See the Appendix.*

For the period 1971, men's average weight, total calories, and fraction of calorie consumed away from home was equal 175.7 pounds, 2433 calories, and 29.9 percent, respectively (see Table 1). This implies that calories at home and away from home are equal to \( h^{m,1971} = 1705.5 \) and \( a^{m,1971} = 727.5 \), respectively. Per calorie prices of food away from home and food at home are equal to \( p_{a}^{1971} = 5.56 \times 10^{-3} \) and \( p_{h}^{1971} = 3.36 \times 10^{-3} \). Using the information about real income\(^6\) from Table 2, non-food daily consumption is equal

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\(^6\) In principle, we would like to use separate income for men and women; however, the NHANES data set we are using for information about weight and calories consumed has a very limited information on income. Income appears in 4 broad categories, which is simply
to: \( c^{nf,1971} = I^{1971} - p_a^{1971} a^{m,1971} - p_h^{1971} h^{m,1971} = $153.9 \). Note that food expenditures is equal to roughly five percent of income. By plugging all these numbers into equation (9) we find that \( \eta^m = 0.49 \) and \( \alpha^m = 0.15 \).

Similarly, we determine the coefficient \( \alpha^w \) and \( \eta^w \) to match the observed average weight and fraction of calories consumed away from home for women in the NHANES 1971 sample. For the period 1971, women's average weight, total calories, and fraction of calorie consumed away from home was equal 145.8 pounds, 1538 calories, and 19.5 percent, respectively (see Table 1). This implies that calories at home and away from home is equal to \( h^f,1971 = 1238.1 \) and \( a^f,1971 = 299.9 \), respectively. Using the information about food prices and income from Table 2, non-food consumption is equal to \( c^{nf} = 157.8 \). By plugging all these numbers into equation (7) we find that \( \eta^w = 0.45 \) and \( \alpha^w = 0.12 \).

Note that men and women differ considerably in their preferences for food versus non-food goods and food at home versus food away from home. The food share, \( \alpha \), and the preference parameter for food away from home, \( \eta \), are greater for men compared to women. The heterogeneity across gender is not counter-intuitive since men tend to eat more than women and they also eat more away from home. In the next section, we use the calibrated model to assess the impact of changes in relative food prices and real income on eating habits and weight of Americans between 1971 and 2006.

6. Simulations

We perform the following experiments. First, we change the price per calorie of food away from home from its 1971 value, \( p_a^{1971} = 5.56 \times 10^{-3} \), to its 2006 value, \( p_a^{2006} = 4.04 \times 10^{-3} \) leaving all other parameters of the model constant. From the first-order conditions in equation (7), we calculate the new values for food away from home and food at home. We then calculate for men and women, respectively, as well as the resulting BMI. We report results of the first experiment in the first column of Table 3. For men, the fraction of calories away from home increases by 12 percentage points from 30 percent (calibrated value from Table 1) to 42 percent. For women, the fraction of calories consumed away from home increases by 8 percentage points from 19 percent (calibrated value) to 27 percent. The impact on agent's weight is small. Men gain 1.5 pounds while and women gain only 0.2 pounds as their weight increases to 178 and 146 pounds, respectively.

The second experiment consists of changing the price per calorie of food at home from its 1971 value, \( p_h^{1971} = 3.36 \times 10^{-3} \), to its 2006 value, \( p_h^{2006} = 3.03 \times 10^{-3} \) leaving all other parameters constant. We calculate the new value for food away from home and food at home as well as weight and body-mass index as explained above. We report the result in the second column of Table 3. For men, the fraction of calories away from home decreases by 4 percentage points from 30 percent to 26 percent. For women, the fraction of calories away from home decreases by 5 percentage points from 19 percent to 14 percent. Again, the decline in food prices has little impact on agent's weight.

too limited to use for our exercise. As a result we use the same mean real income obtain from the Bureau of Economic Analysis for both men and women. As a result, women and men face the same, but looser budget constraint.

\(^7\) For men, results slightly overshoots the data as the observed fraction of calories consumed away from home in 2006 is equal 41 percent. For women, results do not fully account for the observed change in the data as the fraction of calories consumed away from home by women in 2006 is equal to 36 percent.
Table 3. Average BMI, Weight, and Fraction of Calories Consumed Away Predicted by the Model

<table>
<thead>
<tr>
<th></th>
<th>Data 1971</th>
<th>Data 2006</th>
<th>$p_a$</th>
<th>$p_h$</th>
<th>Income</th>
<th>All</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Men</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BMI</td>
<td>25.9</td>
<td>29.0</td>
<td>26</td>
<td>26</td>
<td>28</td>
<td>29</td>
</tr>
<tr>
<td>Weight (lbs)</td>
<td>175.7</td>
<td>198.2</td>
<td>178</td>
<td>175</td>
<td>194</td>
<td>197</td>
</tr>
<tr>
<td>Calories</td>
<td>2433</td>
<td>2543</td>
<td>2453</td>
<td>2425</td>
<td>2620</td>
<td>2644</td>
</tr>
<tr>
<td>% calories away</td>
<td>29.9</td>
<td>40.5</td>
<td>42</td>
<td>26</td>
<td>34</td>
<td>36</td>
</tr>
<tr>
<td><strong>Women</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BMI</td>
<td>25.2</td>
<td>28.8</td>
<td>25</td>
<td>25</td>
<td>29</td>
<td>30</td>
</tr>
<tr>
<td>Weight (lbs)</td>
<td>145.8</td>
<td>168.9</td>
<td>146</td>
<td>144</td>
<td>166</td>
<td>170</td>
</tr>
<tr>
<td>Calories</td>
<td>1538</td>
<td>1802</td>
<td>1539</td>
<td>1519</td>
<td>1738</td>
<td>1782</td>
</tr>
<tr>
<td>% calories away</td>
<td>19.5</td>
<td>35.9</td>
<td>27</td>
<td>14</td>
<td>21</td>
<td>24</td>
</tr>
</tbody>
</table>

The third experiment consists of changing household real disposable income from its 1971 value $I^{1971} = $59,742 to its 2006 value $I^{2006} = $74,089 (see Table 2) leaving all other parameters constant. We report the results in the fifth column of Table 3. Changes in income account for a large fraction of the observed change in individual's weight. The weight of men and women increases to 194 and 166 pounds, respectively. Changes in income also induce a reallocation effect. As agents become richer, the fraction of calories consumed away from home increase from 30 percent to 36 percent for men and from 19 percent to 24 percent for women.

Finally, the fourth experiment consists of changing food prices and income all at once. For men, the model predicts that a weight equal to 197 pounds and the fraction of calories away from home is equal to 36 percent. For women, the model predicts that a weight equal to 170 pounds and the fraction of calories away from home is equal to 24 percent.

The lessons learned from the model for eating decisions and weight can be summarized as follows. Changes in food prices have an "allocation" effect and have little impact on total calories consumed and weight. As the price of one food category changes, households substitute from one food category to another. Changes in income, on the other hand, have a large impact on weight. Between 1971 and 2006, much of the increase in weight and BMI can be accounted for by increase in household real disposable income. 8

Our results corroborate the existing knowledge on obesity in the following way. On the one hand, economists who use empirical models found that the impact of food prices on weight is small (e.g., Chou, Grossman, & Saffer, 2004; Beydoun, Powell, & Wang, 2008; Anderson & Matsa, 2011). Using a fully specified calibrated dynamic model, we also find that changes in food prices over time account for almost none of the weight gain by Americans in the last thirty years. On the other hand, researchers in the field of public health (e.g., French et al. 2001) design small-scale experiments to show that even small changes in food prices can have strong local effect on individual's food choices. For example, the above-mentioned authors examined the effect of lower prices on sales of lower fat vending machine snacks in 12 work sites and 12 secondary schools. According to a study, price reductions of

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8 Dolar (2009) shows that the positive relationship between body-mass index and household income holds for men in several cross-sections of NHANES. For women, however, body-mass index is negatively related to household income suggesting that some other force not captured in our model is at work. We leave the task of reconciling the pattern differences for body-mass index and household income in cross-section and time-series data for men and women for future research.
ten percent, twenty five percent, and fifty percent on low-fat snacks in vending machines increase the percentage of low-fat snack sales by nine, thirty nine, and ninety three percent, respectively. Using our calibrated dynamic model, we also find that change in food prices affect where people eat (at home or out).

7. Concluding Remarks

In this paper, we further analyzed the impact of changes in food prices and household income on people's eating decisions and weight using a static model with rational agents. After careful calibration of the model using evidence from medical research on obesity, we found that food prices determine the allocation of calories across food types, while household income determine the total number of calories consumed and thus individual's weight. Between 1971 and 2006, changes in food prices alone account for almost none of the change in weight of Americans men and women. On the other hand, changes in household income account for almost all of the increase in men's and women's weight. Because of the limited effect of food price alone on the BMI, we support the view that taxes on food will impact what people eat but will have limited effect on reducing the population BMI or the obesity prevalence.

We see two important avenues for academic research on obesity as well as policy recommendation. First, educating people about the benefits of eating healthy, exercising regularly, and the negative health consequences of being obese seem to be promising policies to win the fight against obesity epidemic. Economic research is needed to measure the impact of these education programs on individual's weight and BMI.

Second, we derived our results for the impact of food prices on weight and food choices in an environment where agents are fully rational. An alternative view point is that there is nothing optimal in being obese and that individuals experience commitment problems when making food decisions. It is an open and interesting question to revisit the impact of food prices and household income in a set-up where agents have time-inconsistent preferences à la Laibson (1997). We leave these two tasks for future research.

8. Appendix – Proof Of Proposition 1

Proposition 1 The calibrated parameter values of $(\alpha, \eta)$ are given by:

$$\eta = \frac{BG + FB - GED}{G(A + B) - A(E - F) + FB + GE(C - D)}$$

$$\alpha = \frac{EG(C \eta + D(1 - \eta))}{(E - F)A \eta + FB(1 - \eta)}$$

where $A = (a^{1971})^{\rho - 1}, B = (h^{1971})^{\rho - 1}, C = (a^{1971})^{\rho}, D = (h^{1971})^{\rho - 1}$,

$$E = \frac{p^a_{1971} - p^h_{1971}}{p^a_{1971} - p^h_{1971} h^{1971}}$$

$$F = \frac{p^a_{1971} - p^h_{1971} h^{1971}}{p^a_{1971} - p^h_{1971} h^{1971}}$$

$$G = -\frac{2k\theta(W^{1971} - W^*)}{1 + \kappa(W^{1971} - W^*)^2}$$

Proof: Using the notation from the Proposition, the first-order conditions in equation (9) can be written as: 

12
\[
\frac{A\eta - B(1-\eta)}{C\eta + D(1-\eta)} = \frac{1-\alpha}{\alpha} E
\]

(15)

\[
\frac{\alpha A\eta}{C\eta + D(1-\eta)} - F(1-\alpha) = G
\]

Solving for \(\alpha\) as a function of \(\eta\) by a process of elimination, we get that:

\[
\alpha = \frac{EG(C\eta + D(1-\eta))}{(E-F)A\eta + FB(1-\eta)}
\]

(16)

Substitute the previous equation into equation (15), we get the following expression for \(\eta\):

\[
\eta = \frac{BG + FB - GED}{G(A + B) - A(E - F) + FB + GE(C - D)}
\]

Once the value of \(\eta\) is found, use equation (16) to uncover the value for the parameter \(\alpha\).

References


French, S. A., Jeffery, R. W., Story, M., Breitlow, K. K., Baxter, J. S., Hannan, P., & Snyder,
The Price of One Sweet Calorie


